

# Tracing & Hypothesis

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## *Bug 5: Odds of game are incorrect*

### 1 Tracing

As mentioned above, the inclusion of SPADE may change the win ratio.

First, considered that there are  $n$  faces in the game. There are  $n^3$  possible combinations of 3 dices. The player will lose if the pick is not the same as any of the dices, which means the losing pick lays within the domain of  $(n - 1)^3$ . The winning ratio is calculated as:

$$\text{winning ratio} = 1 - \frac{(n - 1)^3}{n^3}$$

So if there are 6 DiceValues, the winning ratio will be approximately 0.42:

$$\text{winning ratio} = 1 - \frac{(6 - 1)^3}{6^3} = 1 - \frac{125}{216} = 0.4212$$

If there are 5 DiceValues (excluding SPADE), the winning ratio will raise up to 0.48 or 0.49 as in the bug example below.

$$\text{winning ratio} = 1 - \frac{(5 - 1)^3}{5^3} = 1 - \frac{64}{125} = 0.488$$

### 2 Hypothesis

The root of this bug is the same as bug 4 above - no SPADE in the game. So by adding the SPADE, the winning will be resolved.