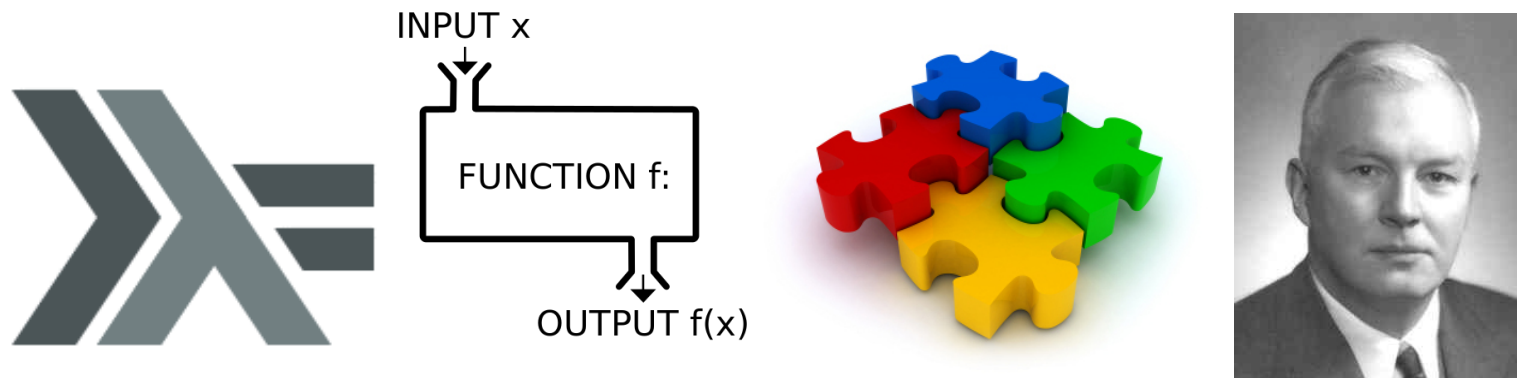


Functional Programming



Functions II

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Learning Targets

You

- know the concept of currying
- understand how partial application relates to currying
- are able to apply lambda expressions
- know how to define and use operators
- can compose functions

Content

- **Currying / Partial Application**
- **Lambda Expressions**
- **Function Composition**
- **Operators**



Functions with Multiple Parameters

- **Every function in Haskell takes only one parameter**

```
add :: Int -> Int -> Int
add a b = a + b
```

- **The function type arrow '->' associates to the right**

```
add :: (Int -> (Int -> Int))
```

```
add :: ((Int -> Int) -> Int)
```

- The function `add` takes a single `Int` parameter and returns a function which accepts another `Int` parameter and which finally returns a result of type `Int`

- **Function application associates to the left**

```
add 1 2 == ((add 1) 2)
```

```
(add (1 2))
```

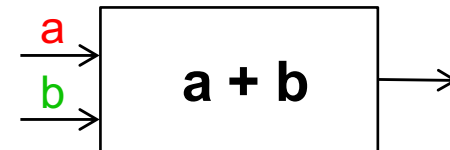
- **These two rules allow for concise function application syntax**



Partial Application

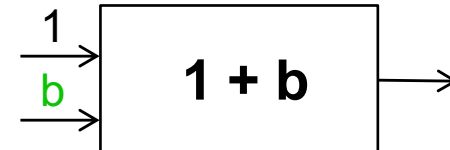
- Applying add to zero arguments

```
Prelude> :t add  
add :: Int -> Int -> Int
```



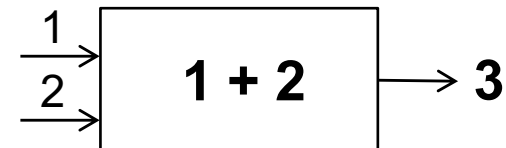
- Applying add to the first argument

```
Prelude> :t add 1  
add 1 :: Int -> Int
```



- Applying add to both arguments

```
Prelude> :t (add 1) 2  
(add 1) 2 :: Int
```



- Functions are values and can be bound to a name

```
inc :: Int -> Int  
inc = add 1
```

Worksheet: Currying



Lambda Expressions

- **The following function definition does two things**

```
inc x = x + 1
```

- It constructs a function: The function which adds one to its argument
 - It binds the name 'inc' to this function
- **These two things are conceptually independent of each other**
- **Many reasons to bind names to values (functions are values btw.)**
 - The value is referred to more than once
 - The value is recursively used in its own declaration
 - The value needs a type signature

Lambda Expressions

- **But not everything needs a name**

```
inc x = x + one  
one = 1
```

- There is no good reason for naming the value 1

- **What about functions which are used only once**

```
incAll :: [Int] -> [Int]  
incAll xs = map inc xs  
  
inc :: Int -> Int  
inc x = x + 1
```

- There is no good reason for naming the increment function

- **We want the functionality without the name**

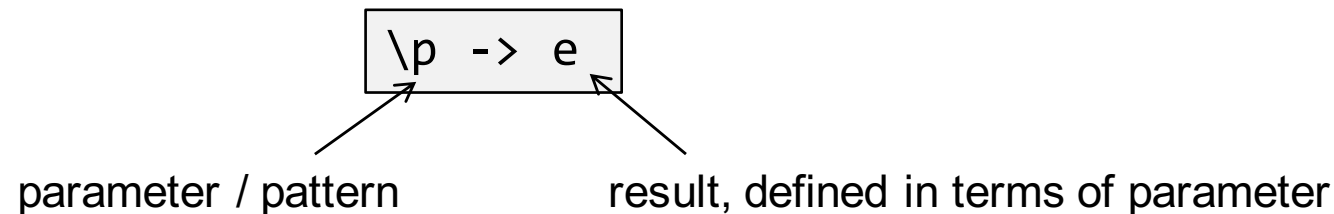
```
incAll :: [Int] -> [Int]  
incAll xs = map (\x -> x + 1) xs
```


Lambda Expressions

- Functions can be defined anonymously

$$\lambda x \rightarrow x + 1$$

- This is called a **lambda expression**
- General form



- Translation

$$\lambda p_1 \dots p_n \rightarrow e \quad == \quad \lambda x_1 \rightarrow \dots \rightarrow \lambda x_n =$$

$$\begin{aligned} &\text{case } (x_1, \dots, x_n) \\ &\text{of } (p_1, \dots, p_n) \rightarrow e \end{aligned}$$

Lambda Expressions and Currying

- **All four functions have the same type**

```
prod1, prod2, prod3, prod4 :: Int -> Int -> Int -> Int
```

```
prod1 x y z = x * y * z
```

```
prod2 x y   = \z -> x * y * z
```

```
prod3 x     = \y -> \z -> x * y * z
```

```
prod4       = \x -> \y -> \z -> x * y * z
```

- Actually the definitions of prod1, prod2 and prod3 all get translated to prod4 by the compiler.

Lambda Expressions in Java 8

```
LambdaTest.java x
package lambda;

import java.util.Arrays;
import java.util.List;

public class LambdaTest {

    public static void main(String[] args) {
        List<String> list = Arrays.asList("abcd", "ef", "abc");

        list.stream().filter(s -> s.length() >= 3)
                .map(s -> s.toUpperCase())
                .forEach(s -> System.out.println(s));
    }
}
```

<http://jdk8.java.net/lambda/>

News zu **lambda**



Code statt Wiesn: München lernt **Lambda**-Ausdrücke kennen

JAXenter - vor 18 Stunden

Lambda-Expressions begeistern die deutsche Entwickler-Gemeinde.

Worksheet: Lambda Expressions



HOFs : Higher-Order Functions

- A function can return another function as its result

`add :: Int -> Int -> Int` == `add :: Int -> (Int -> Int)`

- A function can also take another function as its argument

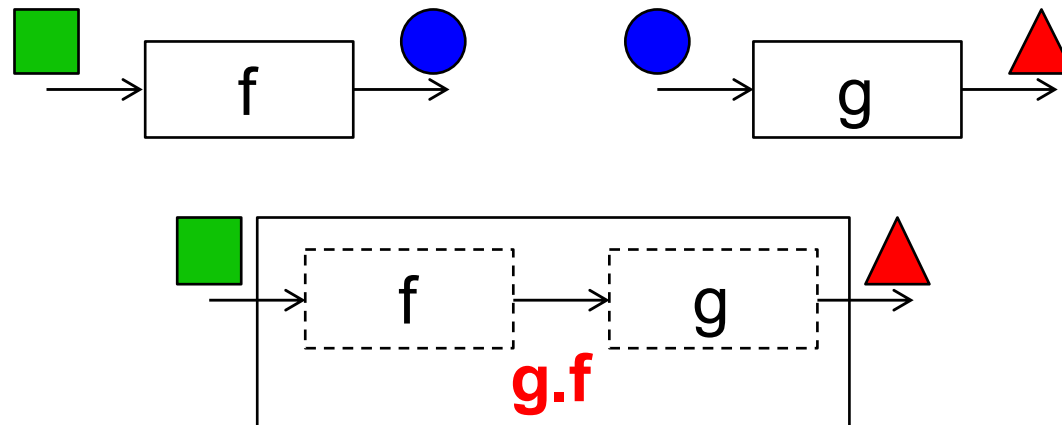
`filter :: (a -> Bool) -> [a] -> [a]`

- First parameter is a function from `a -> Bool`

- **Functions are just values! They can be**
 - input and output to functions
 - put into and retrieved from data structures
- **Functions that have functions as input and/or output are called**
higher-order functions

Function Composition: Pipelines of functions

- Functions can be combined into pipelines if the types line up

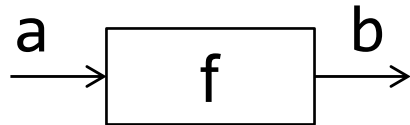


- Function composition of two functions takes the output of one function as the input of a second one.
- The argument order origins from mathematics $g(f(x))$
 - First apply f to x and then apply g to the result: g followed by f

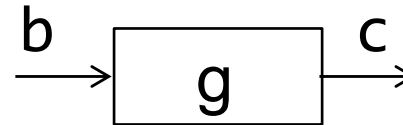
Function Composition: Pipelines of functions

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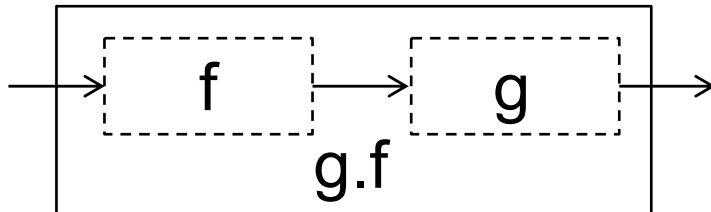
$f :: a \rightarrow b$



$g :: b \rightarrow c$



$(.) :: (b \rightarrow c) \rightarrow (a \rightarrow b) \rightarrow a \rightarrow c$
 $g . f = \backslash x \rightarrow g (f x)$



`map (\xs -> negate (sum (tail xs))) [[1,2,3],[4,5,6],[7,8]]`

`map (negate . sum . tail) [[1,2,3],[4,5,6],[7,8]]`

Operators

- **Function names start with a lower case letter ['a'..'z']**
 - Function names are written in front of their arguments (prefix)

```
add :: Int -> Int -> Int  
add a b = a + b
```

```
add 1 2 ~> 3
```

- **Operator symbols are formed from one or more symbol characters !#\$%&*+./<=>?@\^|_~ [Haskell 2010 Report §2.4](#)**
 - Operator symbols are written between its arguments (infix)

```
(!+!) :: Int -> Int -> Int  
a !+! b = a + b
```

```
1 !+! 2 ~> 3
```


Operators

- An Operator can be used as a function by wrapping it with parentheses (op)

```
Prelude> :t (+)
(+) :: Num a => a -> a -> a
Prelude> (+) 1 2
3
```

- A function can be used as an operator by quoting it with backticks `fun` (not to be confused with ')

```
Prelude> :t div
div :: Integral a => a -> a -> a
Prelude> 9 `div` 2
4
```

- The **syntax** changes but the **semantics** (meaning) remains the same

Sections

- **Infix operators can be partially applied as well.**
 - This is called a section
 - The parentheses are mandatory


`(2+)` is interpreted as `\y -> 2+y`
`(+3)` is interpreted as `\x -> x+3`

- **If the operator is applied to no argument at all haskell essentially treats an infix operator as an equivalent functional value.**

`(+) = \x y -> x+y`

Operator Precedence

- Operators have a defined precedence

`1 + 2 * 3 == 1 + (2 * 3)` 

not: `(1 + 2) * 3` 

- This can be defined using a fixity declaration
 - Declares a precedence level from 0 to 9 (with 9 being the strongest)
 - Normal function application is assumed to have a precedence level of 10
 - Specifies the operator to be
 - left-associative: `infixl`
 - right-associative: `infixr`
 - non-associative: `infix`

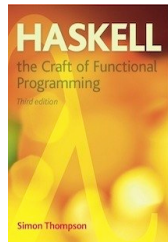
```
Prelude> :info (+)
class Num a where
  (+) :: a -> a -> a
  ...
infixl 6 +
```

```
Prelude> :info (*)
class Num a where
  (*) :: a -> a -> a
  ...
infixl 7 *
```

Further Reading



Chapter 3
Pages 21,22,36,68



Chapter 11
Pages 231 - 252



Chapter 5
Pages 59 – 72 82 - 85