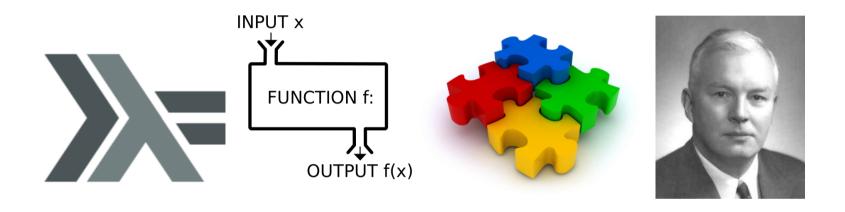
Functional Programming



Recursion

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Learning Targets

You know what recursion is

- You know the concept of recursion
- You can rewrite loops using recursion
- You can effectively use pattern matching to program recursive functions

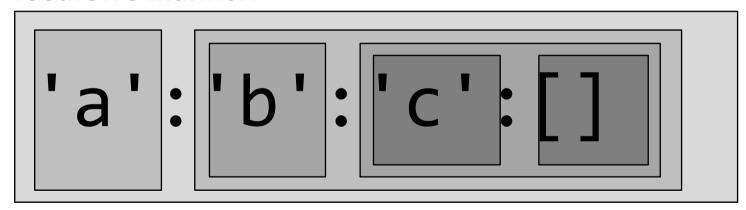


What is recursion?

 Recursion is the process of repeating items in a self-similar way.
 E.g. russian dolls



 The most important datastructure in Haskell is defined in a recursive manner:



A list consists of a head element that is prepended to a list



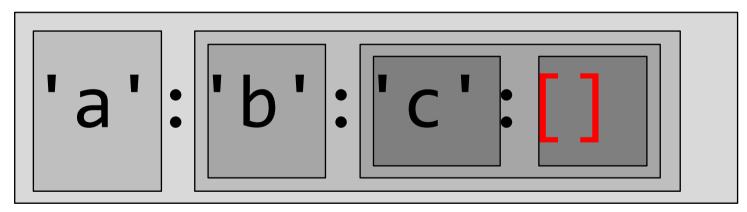
Infinite Recursion?

A list consists of a head element that is prepended to a list.

Wait a moment, what kind of definition is this? This does not stop!

Correct: this is a definition for a infinite list.

Therefore we need an additional condition in our definition to make lists finite:



A list consists of a head element that is prepended to a list **AND** at the end of a finite list is always the empty list [].

```
[3143, 5797, 6551, 8915]

[5797, 6551, 8915]

[6551, 8915]

[8915]
```



What is recursion

We saw that functions can be defined in terms of other functions

```
flipper :: Picture -> Picture
flipper p = beside (flipH p) (flipV p)
```

flipper is defined in terms of beside, flipH and flipV

Recursion occurs when a function is defined in terms of itself!

```
factorial 0 = 1
factorial n = n * factorial (n-1)
```

 factorial maps 0 to 1, and any other positive integer to the product of itself and the factorial of its predecessor.



For example:

factorial 0 = 1
factorial n = n * factorial (n-1)

```
factorial 3
3 * factorial 2
 * (2 * factorial 1)
 * (2 * (1 * factorial 0))
  * (2
         1)
6
```



Worksheet Recursion



Controlling Recursion

Progress in recursion can be made in many ways.

```
countFromTo :: Int -> Int -> [Int]
countFromTo from to
   | from < to = from : (countFromTo (from+1) to)
   | from > to = from : (countFromTo (from-1) to)
   | otherwise = [to]
```

 Oftentimes a function wants to make some preliminary bookkeeping before doing the (recursive) work:

```
gcd :: (Integral a) => a -> a -> a
gcd 0 0 = error "gcd 0 0 is undefined"
gcd x y = gcd' (abs x) (abs y)
  where gcd' a 0 = a
    gcd' a b = gcd' b (a `rem` b)
```

Then a helper function like gcd' can be used!



Mutual Recursion

- Two (or even more) functions can also be defined in terms of each other.
- Example:
 - Definition

Evaluation (simplified)



Tail Recursion

- A function is tail recursive, if the recursive call is done at the very end of the function
- Tail recursion can be optimized by compilers

Instead of writing:

One writes:

```
sum :: Num a => [a] -> a -- tail recursive
sum l = sum' 0 l
where sum' acc [] = acc
    sum' acc (i:is) = sum' (i+acc) is -- tail call
```



Loops and Recursion

- Every loop in Java can also be written as a recursive function and vice versa!
 - Loops are usually controlled by a variable that changes its value from iteration to iteration. This change can be reflected in the recursions progress.
 - The loop's condition is the negation of the base case
 - The loop's body is the recursion step

```
int sum(int n) {
  int sum = 0;
  while (n > 0) {
    sum += n;
    n--;
  }
  return sum;
}
```

```
sum :: Int -> Int
sum 0 = 0
sum n = n + sum (n-1)
```



Ressources

- Chapter 6 in Programming in Haskell, Graham Hutton
- Chapter 7.4 and 7.5 in Haskell, The Craft of Functional Programming, Simon Thompson
- Chapter 4 in Learn You a Haskell for Great Good!, Miran Lipovača
 - Online: http://learnyouahaskell.com/recursion



If you still don't know what recursion is, read this sentence.