### Paper Title

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Here should come the abstract.

Keywords: keyword 1; keyword 2; keyword 3;

### 1. Introduction

Analysis of protein-protein interactions has a growing potential of providing a better understanding about collective protein function and cellular machinery. Such interactions can be modeled as a protein interaction network; that is a weighted graph where each node represents a protein and each edge represents an interaction between a pair of proteins, with a weight representing the level of confidence that this interaction truly exists. Such a structure allows easier extraction of hidden information due to the analogy with well-known graph problems.

An important aspect of the analysis of protein interaction networks is detecting signaling pathways. A signaling pathway is a series of proteins in which each protein signals its successor to transmit some biological information through their interaction. Signaling pathways can be viewed as simple paths in protein interaction networks.<sup>1</sup> Given a confidence value for each interaction, we can assign an overall confidence value for the existence of a pathway simply by multiplying the confidence values of its constituting interactions. An optimal pathway is one with the highest confidence value. To work in an additive framework, edge weights can be assigned logarithmic values of the original interaction confidence.

**Problem** Consider a set V of nodes denoting proteins, and a probability value p(u,v) denoting interaction confidence for each  $u,v \in V$ . A set of undirected weighted edges E can be obtained by adding an edge for each pair (u,v) with p(u,v) > 0, and assigning it a weight  $w(p,v) = -\log[p(u,v)]$ . Now consider the undirected weighted graph G = (V,E,w) representing the protein interaction network, and a set of start nodes  $S \in V$ . For each  $v \in V$ , we want to find a minimum-weight simple path of length m, starting at any node  $s \in S$  and ending at v. The traveling-salesman problem is polynomial-time reducible to this problem; therefore it is NP-hard.<sup>2</sup>

Scott et al. presented a method for detecting pathways<sup>2</sup> using a generic technique devised by Alon et al. called *color-coding*.<sup>3</sup> The basic idea of this method is to randomly assign each

node in the graph one of m different colors, and search for an optimal pathway in the restricted domain of colorful pathways. A pathway is considered colorful if and only if all of its nodes are different in color from each other. This process is repeated for several iterations until reaching a given level of confidence that the unknown optimal pathway was among the colorful ones at some instance. This confidence level builds up with each iteration by calculating a probability value that an optimal path is indeed colorful in this iteration. This success probability value depends solely on the pathway length m and doesnt capitalize on available information like the network topology and color assignment.

Gülsoy et al. presented an enhanced color-coding technique called k-hop coloring.<sup>4</sup> In essence, k-hop coloring makes use of knowing the network topology and the node colors to assign the network a maximal value k such that the network is k-hop colorable. A colored network is k-hop colorable if the shortest path between any pair of same-color nodes is more than k hops in length. This additional piece of information allows for higher success probability in each iteration, with a higher k value resulting in a higher success probability. However, an obvious limitation is that the subnetworks with higher level of connectivity diminishe the k value assigned to the whole network. For example, a network containing a clique of size k cannot be colored with k value assigned to the whole network of example, a network containing a clique of size k

Contribution Our motivation comes from the need for a deeper understanding of the relation between network topology, random color assignment and success probability. We study the possibility of assigning k values to nodes on an individual basis instead of a single k value for the whole network. We also study how this reflects on the resulting success probability for each iteration. We examine the idea that a pathway whose nodes are assigned different k values should result in a higher success probability than if we only consider the minimum of these k values for all nodes. We present a new method for detecting signaling pathways in protein interaction networks using an enhanced k-hop coloring technique based on these findings.

We provide validation experiments to test the biological significance of our results. We use  $weight\ p$ -value and  $functional\ enrichment$  as validation measures. We also compare the performance of our method against the one presented by Scott et al.<sup>2</sup> with respect to how fast our method reaches a given confidence level as opposed to theirs.

The rest of the paper is organized as follows. Section 2 discusses the background and related work. Section 3 explains how to obtain a tighter bound on success probability and describes our enhanced k-hop coloring method. Section 4 shows the experiments performed and their results. Section 5 is the conclusion of the paper.

## 2. Background

### 3. Methods

#### 3.1. Term Definition and Problem Formulation

Here we define the terms we commonly use like: coloring instance, k-value configuration, ..etc. Then we accurately define the problem of finding signaling pathways in PPI networks.

## 3.2. Success Probability: a Tighter Bound

Here we should explain the calculation of success probability, how the number of possible colorings for the optimal path is its key factor, and how obtaining a tighter (smaller) bound on it results in a tighter bound on success probability, and hence a better result. We then explain our notion of k-value configuration and how we calculate this bound from it. We explain the lattice structure and the subset relation between k-value configurations.

# 3.3. Method: Enhanced k-hop Coloring

Here we detail our method. We start by asserting that we have no knowledge about the optimal path, but we use the local optimal as a replacement and experimentally test the correctness of this approach. Then we explain the algorithm in detail.

## 4. Experiments

### 4.1. Datasets

Here we list the datasets used in experiments. I think we can use the MINT datasets for multiple organisms.

## 4.2. Validation Experiments

Here we list the validation experiments we did and their results. I think we should do some validation experiments similar to those done in Sharan's paper, using weight p-value and functional enrichment as validitiy measures.

### 4.2.1. Validation using Weight p-value

For each dataset we use, we should obtain the 99 percent confidence optimal pathway and compare it with optimal pathways obtained we obtain from random networks. We generate random networks by shuffling edges of the original network. The weight p-value is the percentage of cases where the algorithm produces a more optimal pathway when run on one of these random networks.

#### 4.2.2. Validation using Functional Enrichment

For each dataset, we we obtain the 99 percent confidence optimal pathway and test its functional enrichment. For each GO term appearing on the dataset proteins, we count the total number of proteins annotated by it and the number of proteins in the resulting pathway annotated by it. We use these numbers, along with the total number of proteins and the number of proteins in the pathway, as parameters for a hypergeometric test (I still have to develop further understanding about the details of this test). The maximum enrichment value for any of the tested GO terms gives us the final functional enrichment p-value.

# 4.3. Comparison with Sharan

This is just a temporary title for this subsection, I'm not very sure what to name it.

We measure the time and number of iterations needed by our method to obtain 70%, 90% and 99% confidence pathways of lengths 6, 7, 8 and 9 nodes. We compare these numbers against the ones by Sharan's method for the same cases.

We run our method for 500 iterations and measure the incremental success probabilty against iteration number. We do this experiment many times take the average curve. We do the same experiment using Sharan's method and obtain a second curve. We also measure the average practical success probability, which is the observed probability that the DP algorithm finds the optimal solution in a certain iteration or before it. We compare the three curves targetting two conclusions: (1) our method is experimentally solid because our calculated success probabilities are lower than the observed ones; and (2) our method outperforms Sharan's method.

### 5. Conclusion

Here goes the conclusion.

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