



Final Exam
EXAMINATION
Summer 2013

DURATION: 3 HOURS

No. of Students: 72

Department Name & Course Number: **Physics 1004A**

Course Instructor(s) Dr. Andrew Robinson

AUTHORIZED MEMORANDA

Pen, pencil, calculator

Students MUST count the number of pages in this examination question paper before beginning to write, and report any discrepancy to a proctor. This question paper has 12 pages including the cover page.

This examination question paper may not be taken from the examination room.

In addition to this question paper, students require: an examination booklet no
a Scantron sheet no

Please print your name and student number in the boxes below:

Family Name	First Name	Student Number
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This exam is out of 60 marks and consists of two parts:

Section A: 10 multiple choice questions, each worth one mark. Please circle the correct answer on the paper.

Section B: Answer 5 out of the 6 questions and tick the check boxes provided to indicate your choice of the questions to be marked. Each question is worth 10 marks. Write your answers under the questions. You may use the other side of the sheet if you require more space. Useful formulae are provided on the last three pages of the examination paper. These three sheets may be removed from the paper.

	Section A	
<input type="checkbox"/>	B1	
<input type="checkbox"/>	B2	
<input type="checkbox"/>	B3	
<input type="checkbox"/>	B4	
<input type="checkbox"/>	B5	
<input type="checkbox"/>	B6	
	Total	

Section A

Answer all questions. Each question is worth 1 mark. Please circle your answer in the box.

A1

A negatively-charged object is released from rest in a region containing a uniform magnetic field. Which one of the following statements concerning the subsequent motion of the object is **correct**?

- (A) The object will remain motionless.
- (B) The object will experience a constant acceleration and move in the direction of the magnetic field.
- (C) The object will experience a constant acceleration and move in the direction opposite that of the magnetic field.
- (D) The object will move at constant speed in a circle defined by the right hand rule.

A2

A wave is described by the equation:

$$y(x, t) = (0.45 \text{ m})\sin[(8\pi \text{ rad/s})t + (\pi \text{ rad/m})x]$$

Find the frequency of the wave.

(A) 1.0 Hz	(B) 2.0 Hz	(C) 4.0 Hz	(D) 8.0 Hz
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A3

Calculate the **magnitude** of the magnetic force on an electron which is moving at $1.00 \times 10^6 \text{ m/s}$ at an angle of 60.0° to a magnetic field of 1.00 mT .

(A) $3.5 \times 10^{-16} \text{ N}$	(B) $1.39 \times 10^{-16} \text{ N}$	(C) $9.43 \times 10^{-17} \text{ N}$	(D) $2.13 \times 10^{-17} \text{ N}$
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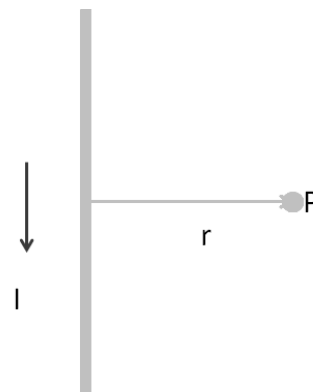
A4

If a proton is accelerated in a $2.0 \times 10^4 \text{ N/C}$ electric field, what is the magnitude of the acceleration? The mass of a proton is $1.6726 \times 10^{-27} \text{ kg}$.

(A) $1.9 \times 10^{12} \text{ m/s}$	(B) $2.8 \times 10^9 \text{ m/s}$	(C) $5.4 \times 10^7 \text{ m/s}$	(D) $8.4 \times 10^{10} \text{ m/s}$
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A5

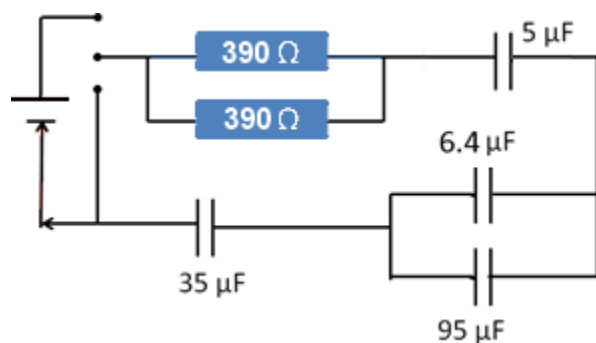
Calculate the magnitude of the magnetic field at point P, created when a current of 0.500 amps flows through the long straight wire shown in the figure. The distance $r = 1.00$ mm



(A) $1.0 \times 10^{-2} \text{ T}$	(B) 1.0 T	(C) $1.0 \times 10^{-2} \text{ T}$	(D) $1.0 \times 10^{-4} \text{ T}$
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A6

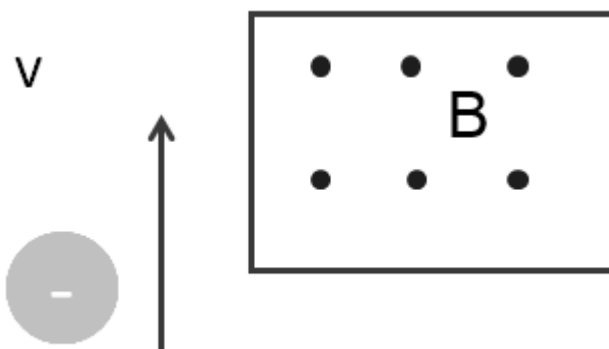
What is the time constant of this RC circuit?



(A) $16 \mu\text{s}$	(B) 0.82 ms	(C) 1.2 ms	(D) 0.15 s
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A7

A negatively charged particle enters a uniform magnetic field with a velocity vector perpendicular to the direction of the magnetic field. In what direction is the magnetic force exerted on the particle?



(A) Left	(B) Right	(C) Into the page	(D) Out of the page
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A8

A solenoid of length 15 cm, and with 45 turns, has a current of 1.25 amps flowing in it. What is the magnitude of the magnetic field inside the solenoid?

(A) $1.0 \times 10^{-5} \text{ T}$	(B) $1.2 \times 10^{-4} \text{ T}$	(C) $3.8 \times 10^{-3} \text{ T}$	(D) $7.0 \times 10^{-3} \text{ T}$
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A9

A coil is connected in series with a $10.0 \text{ k}\Omega$ resistor. An ideal 50.0V battery is connected across the two devices, and the current reaches 2.00 mA after 5.00 milliseconds. Find the inductance of the coil.

(A) 97.9 H	(B) 108 H	(C) 979 H	(D) $2.61 \times 10^3 \text{ H}$
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A10

In an oscillating LC circuit with $L = 65 \text{ mH}$ and $C = 4.0 \mu\text{F}$. The current is initially a maximum. How long will it take before the capacitor is fully charged for the first time?

(A) $7.1 \times 10^{-7} \text{ s}$	(B) $2.6 \times 10^{-6} \text{ s}$	(C) $4.0 \times 10^{-5} \text{ s}$	(D) $8.0 \times 10^{-4} \text{ s}$
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Section B

Answer **5** questions out of **6**. Use the check boxes on the front page to indicate which questions you want marked. If the check boxes are not filled in, the first five questions encountered will be marked. All questions are worth 10 marks. **Show all work**. Equations not on the formula sheet must be derived from first principles. The appropriate number of significant figures must be used in the final answer.

Section B questions continue on the next page.

B1

A 1.20×10^{-14} N force with a fixed orientation does work on a particle of mass 2.50×10^{-26} kg, as the particle moves through a displacement $\mathbf{d} = (2.00 \text{ m})\mathbf{i} - (4.00 \text{ m})\mathbf{j} + (3.00 \text{ m})\mathbf{k}$. The change in the particle's kinetic energy is $+3.00 \times 10^{-14}$ Joules. You may assume that no non-conservative forces act on the particle.

- (a) Calculate the angle between the force and the displacement (4 marks)
- (b) Derive an equation for the final speed in terms of mass m , change in kinetic energy ΔK and initial speed v_i (4 marks)
- (c) If the particle has an initial speed of 1.00×10^5 m/s, calculate the final speed. (2 marks)

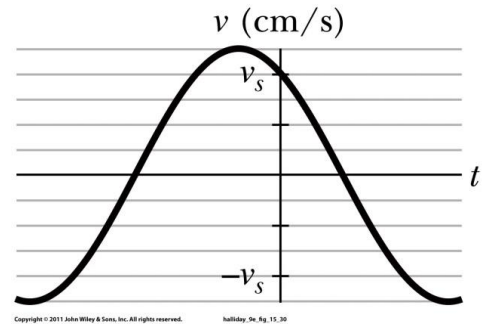
B2

A harmonic oscillator has the position function

$$x(t) = x_m \cos(\omega t + \phi)$$

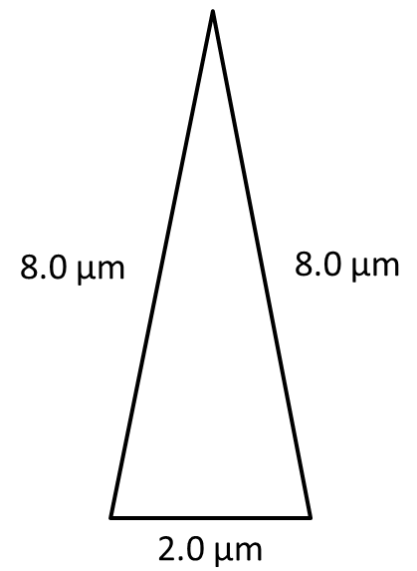
The velocity function, $v(t)$, is pictured on the right. The vertical scale has a value of v_s 4.0×10^6 cm/s at $t = 0$

(a) Calculate the phase constant ϕ (in radians) for the harmonic oscillator with the velocity function $v(t)$ given in the figure (6 marks)



(b) Calculate the position of the particle at $t = 1.0$ seconds, assuming $x_m = 1.0 \times 10^{-7}$ cm. If you did not find a value in part (a), use $\phi = -0.8$ instead. (4 marks)

B3 Calculate the potential energy in electron volts, stored by three protons, when they are arranged in an isosceles triangle with short side $2.0\ \mu\text{m}$, and equal sides of $8.0\ \mu\text{m}$. You may assume that the potential at infinite separation is zero.



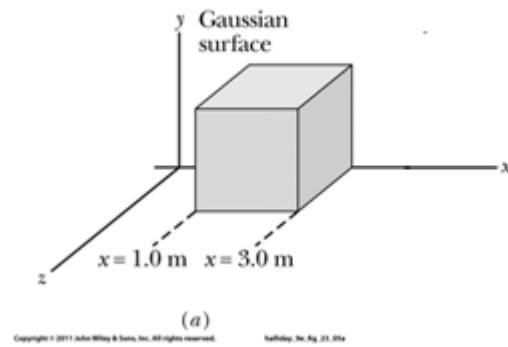
B4

The electric field inside this Gaussian cube of side 2.0 m has the function

$$\vec{E} = \left(\frac{1000}{x^2} \right) \hat{i} \text{ N/C, where } x \text{ is measured in metres.}$$

Determine

- The charge enclosed within the cube.
- The volume charge density
- The number of elementary charges enclosed in the box, and whether they correspond to excess protons or excess electrons

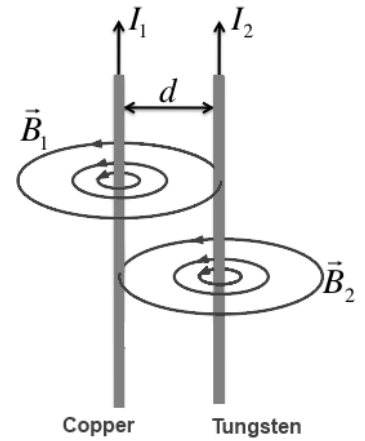


B5

The two cylindrical wires shown in the diagram are 1.00 metres long and have a diameter of 1.00 cm. A potential difference of 1.00 Volts is applied across the ends of each wire to make the current flow. One wire is made of copper, the other from tungsten.

- Calculate the current in each of the two wires.
- Calculate the force each wire exerts on the other due to the magnetic field.

Material	Resistivity at 20 °C ($\Omega \cdot \text{m}$)
Copper (Cu)	1.68×10^{-8}
Tungsten (W)	5.60×10^{-8}

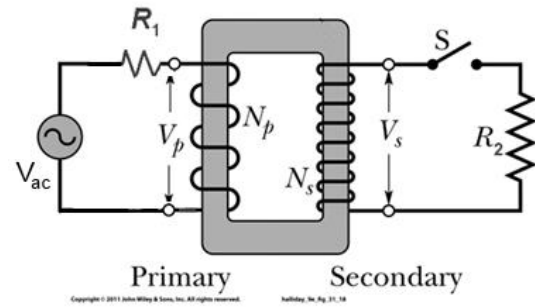


B6

The step up transformer in the figure has 40 turns on its primary coil and 120 turns on its secondary coil. The primary coil is connected to a $12.0 \text{ V}_{\text{rms}}$ 60 Hz AC power supply. The resistor R_1 has a value of 370Ω . A voltmeter measuring the potential across the primary coil reads $10.5 \text{ V}_{\text{rms}}$.

Calculate

- (a) The rms current in the primary coil.
- (b) The rms potential V_s across the secondary coil
- (c) The rms current passing through R_2 when the switch is closed
- (d) The value of R_2



Physical Constants and conversion factors

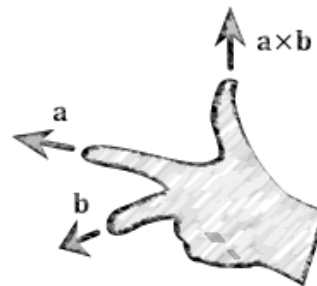
$$G = 6.67 \times 10^{-11} \text{ Nm}^2\text{kg}^{-2}; g = 9.81 \text{ m/s}^2; N_A = 6.02 \times 10^{23} \text{ mol}^{-1}$$

$$c = 3.00 \times 10^8 \text{ m/s}; m_e = 9.31 \times 10^{-31} \text{ kg}; m_p = 1.67 \times 10^{-27} \text{ kg}$$

$$k_B = 1.38 \times 10^{-23} \text{ J/K}; R = 8.314 \text{ J/mol.K}; e = 1.602 \times 10^{-19} \text{ C};$$

$$k = 8.99 \times 10^9 \text{ N.m}^2/\text{C}^2; \epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N.m}^2;$$

$$1 \text{ eV} = 1.60 \times 10^{-19} \text{ J}; \mu_0 = 4\pi \times 10^{-7} \text{ T.m/A};$$



Mathematics, Statistics and Geometry

$$\text{If } ax^2 + bx + c = 0 \text{ then } x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}; \frac{d}{dx}(x^n) = nx^{n-1}; \frac{d}{dx}(\sin ax) = a \cos ax;$$

$$\frac{d}{dx}(a \cos x) = -a \sin x; \int x^n dx = \frac{x^{n+1}}{n+1} + C; \int \sin ax = -\frac{1}{a} \cos ax + C; \int \cos ax = \frac{1}{a} \sin ax + C$$

$$\vec{a} \cdot \vec{b} = a_x b_x + a_y b_y + a_z b_z = ab \cos \theta; |\vec{a} \times \vec{b}| = ab \sin \theta; \frac{dx}{dt} = \frac{dx}{du} \frac{du}{dt};$$

$$\vec{c} = \vec{a} \times \vec{b} = (a_y b_z - b_y a_z)\mathbf{i} + (a_z b_x - b_z a_x)\mathbf{j} + (a_x b_y - b_x a_y)\mathbf{k}$$

$$A_{\text{circle}} = \pi r^2; C_{\text{circle}} = 2\pi r; V_{\text{sphere}} = \frac{4}{3} \pi r^3; A_{\text{sphere}} = 4\pi r^2; (1+x)^n \approx 1+nx \text{ if } x \ll 1$$

$$\sigma_f = \sqrt{\left(\frac{\partial f}{\partial x} \sigma_x\right)^2 + \left(\frac{\partial f}{\partial y} \sigma_y\right)^2 + \left(\frac{\partial f}{\partial z} \sigma_z\right)^2 + \dots}; \sigma = \frac{H-L}{\sqrt{N}}; \sigma_x = \frac{H-L}{N}$$

Kinematics, Work, Energy

$$v = \frac{dx}{dt}; a = \frac{dv}{dt} = \frac{d^2x}{dt^2}; \vec{x} = \vec{x}_0 + \vec{v}_0 t + \frac{1}{2} \vec{a} t^2; \vec{v} = \vec{v}_0 + \vec{a} t; \vec{v}_{av} = \frac{\vec{v}_0 + \vec{v}}{2}; v^2 = v_0^2 + 2a(x - x_0);$$

$$\vec{F}_{net} = m\vec{a}; \text{Hooke's Law: } \vec{F} = -k\vec{x}; \text{work } W = \vec{F} \cdot \vec{d}; W = \int_{r_A}^{r_B} \vec{F}(\vec{r}) \cdot d\vec{r}; K = \frac{1}{2}mv^2; W = \Delta K;$$

$$\bar{P} = \frac{\Delta W}{\Delta t}; P = \frac{dW}{dt}; P = \vec{F} \cdot \vec{v}; \Delta U = -W; \Delta U_g = mg\Delta y; U_E = \frac{1}{2}kx^2; E = K + U;$$

$$\Delta U = -\int_{x_i}^{x_f} F(x)dx; F = -\frac{dU}{dx}; W = \Delta E_{mec} + \Delta E_{th}; \vec{F} = -\left(\frac{GMm}{r^2}\right)\hat{r}; U(r) = -\frac{GMm}{r};$$

Oscillatory Motion and Waves

$$x(t) = x_m \cos(\omega t + \phi); v(t) = -\omega x_m \sin(\omega t + \phi); a = \frac{dv}{dt} = -\omega^2 x_m \cos(\omega t + \phi) = -\omega^2 x(t)$$

$$x(t) = Ae^{-\alpha t} \sin(\omega' t + \phi); \omega = 2\pi f; T = \frac{1}{f}; v = f\lambda = \frac{\lambda}{T} = \frac{\omega}{k}; \omega = \sqrt{\frac{k}{m}}; \omega = \sqrt{\frac{g}{L}}; E = \frac{1}{2} kx_m^2;$$

$$y(x, t) = y_m \sin(kx - \omega t); k = \frac{2\pi}{\lambda}; v = \sqrt{\frac{\tau}{\mu}}; P = \frac{\mu\omega^2 A^2 v}{2}; \frac{\partial^2 y}{\partial x^2} = \frac{1}{v^2} \frac{\partial^2 y}{\partial t^2}; \vec{F} = k \frac{q_1 q_2}{r^2} \hat{r}; i = \frac{dq}{dt};$$

Electrostatics

$$n_{electrons} = \frac{q_{total}}{e}; \vec{E} = \frac{\vec{F}}{q}; \vec{E} = k \frac{q}{r^2} \hat{r}; \vec{p} = q\vec{d}; E = \frac{1}{2\pi\epsilon_0} \frac{p}{z^3}; E_{total} = \frac{1}{4\pi\epsilon_0} \frac{qz}{(z^2 + R^2)^{\frac{3}{2}}};$$

$$E = \frac{\sigma}{2\epsilon_0} \left[1 - \frac{z}{\sqrt{(z^2 + R^2)}} \right]; E = \frac{\sigma}{2\epsilon_0}; \vec{\tau} = \vec{p} \times \vec{E}; U = -\vec{p} \cdot \vec{E}; \Phi = \sum \vec{E} \cdot \Delta \vec{A}; \Phi = \oint \vec{E} \cdot d\vec{A};$$

$$\epsilon_0 \Phi = q_{enc}; \epsilon_0 \oint \vec{E} \cdot d\vec{A} = q_{enc}; E = \frac{\sigma}{\epsilon_0}; \sigma = \frac{q}{A}; E = \frac{\lambda}{2\pi\epsilon_0 r}; \lambda = \frac{q}{L} E = \frac{\sigma}{2\epsilon_0}; E_{\parallel} = \frac{2\sigma_1}{\epsilon_0} = \frac{\sigma}{\epsilon_0}$$

$$V = \frac{U}{q}; \Delta V = \frac{\Delta U}{q} = \frac{-W}{q}; W = q_0 \int_i^f \vec{E} \cdot d\vec{s}; \Delta V = - \int_i^f \vec{E} \cdot d\vec{s}; V(r) = \frac{q}{4\pi\epsilon_0 r}; V = \frac{1}{4\pi\epsilon_0} \sum \frac{q_i}{r_i};$$

$$V_{dipole} = \frac{1}{4\pi\epsilon_0} \left[\frac{p \cos \theta}{r^2} \right]; E_s = -\frac{\partial V}{\partial s}; U = W = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r}; C = \frac{q}{V}; C = \frac{\epsilon_0 A}{d};$$

$$C_{cyl} = 2\pi\epsilon_0 \frac{L}{\ln(b/a)}; C_{sp} = 4\pi\epsilon_0 \frac{ab}{b-a}; C_{iso} = 4\pi\epsilon_0 R; C_{eq,p} = C_1 + C_2 + \dots \frac{1}{C_{eq,s}} = \frac{1}{C_1} + \frac{1}{C_2} + \dots$$

$$U = \frac{q^2}{2C} = \frac{1}{2} CV^2; u = \frac{1}{2} \epsilon_0 E^2; \epsilon_0 \oint \kappa \vec{E} \cdot d\vec{A} = q_{enc}; i = \frac{dq}{dt} = \int \vec{J} \cdot d\vec{A}; \vec{J} = ne\vec{v}_{drift};$$

Resistance and RC circuits

$$R = \frac{V}{i}; R = \frac{\rho L}{A}; \rho - \rho_0 = \rho_0 \alpha (T - T_0); P = iV = i^2 R = \frac{V^2}{R}; R_{eq,s} = R_1 + R_2 + \dots$$

$$\frac{1}{R_{eq,p}} = \frac{1}{R_1} + \frac{1}{R_2} + \dots q = C\xi(1 - e^{\frac{-t}{RC}}); \tau = RC; i = \frac{dq}{dt} = \pm \left(\frac{\xi}{R} \right) e^{\frac{-t}{RC}};$$

Magnetism

$$\begin{aligned}\vec{F}_B &= q\vec{v} \times \vec{B}; \quad |q|vB = \frac{mv^2}{r} \quad \vec{F}_B = i\vec{L} \times \vec{B}; \quad d\vec{F}_B = id\vec{L} \times \vec{B}; \quad \vec{\tau} = \vec{\mu} \times \vec{B}; \quad \mu = NiA; \quad U(\theta) = -\vec{\mu} \cdot \vec{B}; \\ d\vec{B} &= \frac{\mu_0}{4\pi} \frac{id\vec{s} \times \hat{r}}{r^2}; \quad B_{lsw} = \frac{\mu_0 i}{2\pi R}; \quad B_{arc} = \frac{\mu_0 i \phi}{4\pi R}; \quad F_{ba} = \frac{\mu_0 L i_a i_b}{2\pi d}; \\ \oint \vec{B} \cdot d\vec{s} &= \mu_0 i_{enc}; \quad B_{sol} = \mu_0 in; \quad B_{tor} = \frac{\mu_0 i N}{2\pi r}; \quad \vec{B}(z) = \frac{\mu_0 \vec{\mu}}{2\pi z^3}; \quad \Phi_B = \int \vec{B} \cdot d\vec{A};\end{aligned}$$

Inductance

$$\begin{aligned}\xi &= -\frac{d\Phi_B}{dt}; \quad \xi = -N \frac{d\Phi_B}{dt}; \quad \xi = \oint \vec{E} \cdot d\vec{s} \quad L = \frac{N\Phi_B}{i}; \quad \xi_L = -L \frac{di}{dt}; \quad i = \frac{\xi}{R} \left(1 - e^{\frac{-t}{\tau_L}}\right); \quad \tau_L = \frac{L}{R}; \quad i = i_0 e^{\frac{-t}{\tau_L}}; \\ U_B &= \frac{1}{2} Li^2; \quad u_B = \frac{B^2}{2\mu_0}; \quad \xi_2 = -M \frac{di_1}{dt} \text{ and } \xi_1 = -M \frac{di_2}{dt};\end{aligned}$$

LC Circuits, LCR Circuits and Resonance

$$\begin{aligned}L \frac{d^2 q}{dt^2} + \frac{1}{C} q &= 0; \quad q = Q \cos(\omega t + \phi); \quad \omega = \frac{1}{\sqrt{LC}}; \\ i &= -\omega Q \sin(\omega t + \phi); \quad L \frac{d^2 q}{dt^2} + R \frac{dq}{dt} + \frac{1}{C} q = 0; \quad q = Q e^{\frac{-Rt}{2L}} \cos(\omega' t + \phi); \quad \omega' = \sqrt{\omega^2 - \left(\frac{R}{2L}\right)^2} \\ V_C &= IX_C, \phi = -\pi/2; \\ V_L &= IX_L, \phi = +\pi/2; \quad I = \frac{\xi_m}{Z} = \frac{\xi_m}{\sqrt{R^2 + (\omega_d L - 1/\omega_d C)^2}}; \quad Z = \sqrt{R^2 + (X_L - X_C)^2}; \\ \tan \phi &= \frac{X_L - X_C}{R};\end{aligned}$$

AC Circuits

$$P_{avg} = I_{rms}^2 R = \xi_{rms} I_{rms} \cos \phi; \quad I_{rms} = I/\sqrt{2}; \quad V_{rms} = V/\sqrt{2}; \quad \xi_{rms} = \xi/\sqrt{2};$$

Transformers

$$V_s = V_p \frac{N_s}{N_p}; \quad I_s = I_p \frac{N_p}{N_s}; \quad R_{eq} = \left(\frac{N_p}{N_s}\right)^2 R;$$