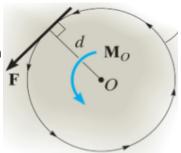
## Lecture 6 Note - Moments I (Moments in 2D)

Textbook Chapter 4.1-4.4

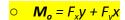
## What is a moment?

- A force vector that makes a body turn about an axis
  - They have magnitude, direction, & point of application
  - Affects rigid bodies (an object that can turn)
  - Moment = (Force)(distance) → M = Fd
  - A moment's axis is best imagined as an axle.
  - Where does a moment point? Use the right hand rule:
    If your hand is O and your fingers curl with the rotation, your thumb points with
    M<sub>a</sub>

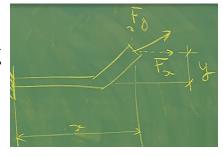


## How to solve 2D moment problems:

- In 2D moments rotate either clockwise (CW) or counterclockwise (CCW, + by default).
- A scalar approach can be used to solve 2D problems:  $\frac{CCW}{M_B} = \frac{\sum (Fd)}{\sum (Fd)}$
- Varignon's Theorem: Moments can be broken up into their component pieces and then applied over distance.
   The moment of a force acting on any point equals the ∑ of the moments' components acting on that point.



Skip calculating the distance from F<sub>o</sub> to O!



## How to solve 3D moment problems (using cross product):

- 3D problems can be solved with the cross product table method from high school.
- The moment vector of a force about a point can be described by  $\mathbf{A} \times \mathbf{B} = \mathbf{C}$ , such that:
  - C is the moment about point O; A is its force vector and B its position vector from O to that force vector. C is perpendicular to the plane containing A and B (the cross product of two vectors gives a 3rd vector perpendicular to both)
  - Note that position vector  $\mathbf{B}$  doesn't have to be perpendicular to  $\mathbf{A}$ , as long as it touches  $\mathbf{A}$ 's line of action. The  $\mathbf{d}$  in  $\mathbf{F}\mathbf{d}$  equals  $\mathbf{r}$  sin  $\mathbf{\theta}$ , where  $\mathbf{r}$  is the distance from  $\mathbf{B}$  to  $\mathbf{A}$ 's line of action, and  $\mathbf{\theta}$  is  $\mathbf{B}$ 's angle of elevation to  $\mathbf{A}$ 's line of action.
  - Key definitions:  $C = A \times B = \frac{\text{(AB sin}\theta)\mathbf{u}_c}{\text{(AB sin}\theta)\mathbf{u}_c}$ ; The magnitude of  $C = \frac{AB \sin\theta}{\text{(AB sin}\theta)\mathbf{u}_c}$
  - The direction of *C* can be obtained using the right-hand rule mentioned earlier.
- <u>Tip: Pick the simplest position vector with the most 0s to simplify calculations.</u> As long as it starts on the axis of the moment and ends on the line of action of the force, it's OK.
- $M_r$  about point O equals the sum of moments  $M_1 + M_2 + M_3$  about point O, OR  $F_R$  crossed with a position vector from it to point O.