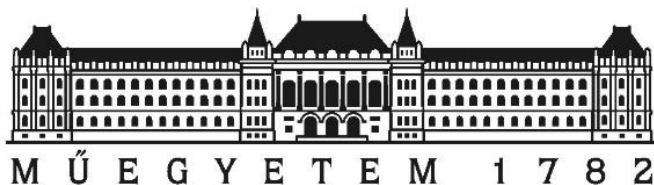


SMT-based effective formalization of reference types in Solidity

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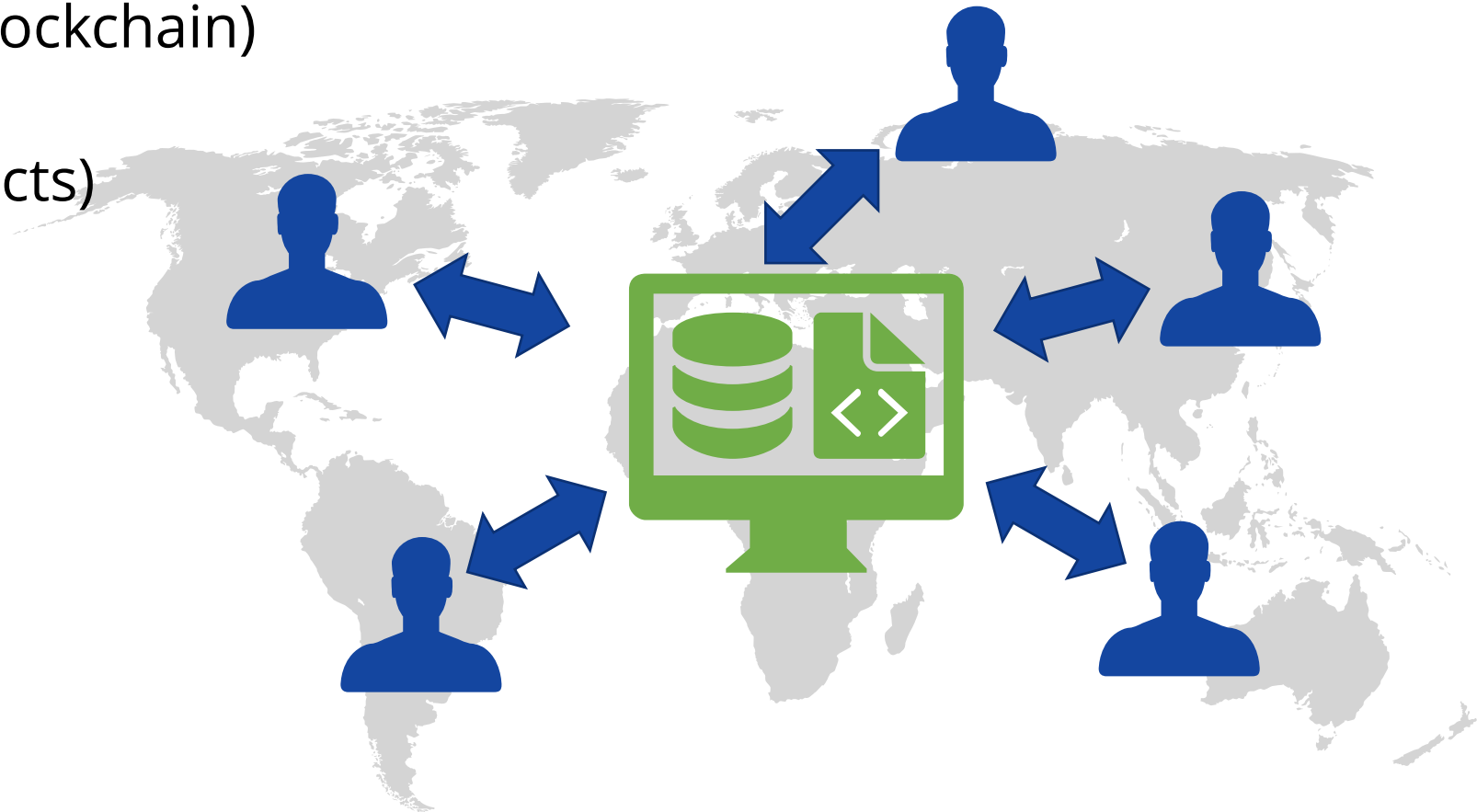
²*SRI International*



Solidity Smart Contracts

Decentralized Computing Platforms

- Conceptually a **single-world-computer** abstraction
 - Example: Ethereum
 - Store **data** (blockchain)
 - Execute **code** (smart contracts)



Decentralized Computing Platforms

- In reality
 - No trusted central party
 - Consensus protocol



Solidity Smart Contracts

```
contract DataStorage {  
    struct Record { bool set; int[] data; }  
    mapping(address=>Record) private records;  
  
    function append(address at, int d) public {  
        Record storage r = records[at];  
        r.set = true;  
        r.data.push(d);  
    }  
  
    function get(address at) public view returns (int[] memory ret) {  
        require(isset(records[at]));  
        ret = records[at].data;  
    }  
  
    function isset(Record storage r) internal view returns (bool s) {  
        s = r.set;  
    }  
}
```

Complex datatype

State variable(s): permanent storage (blockchain)

Function(s): called with transactions

Parameters, return values, local variables in transient memory

Pointers to storage in internal scope

Verification Landscape

- Bytecode-level tools
 - Slither, Mythril, KEVM, ...
 - Various formalizations
 - Mostly vulnerable patterns
 - Limited effectiveness and automation for high-level properties
- Solidity-level tools
 - SMTchecker, solc-verify, VeriSol, KSolidity, ...
 - High-level, functional properties
 - Usually based on SMT
 - Modular verification, bounded model checking, symbolic execution
 - Precise formalization required



Memory model lacks detailed and effective formalization

Target Language

- Simple **SMT-based** program
 - **Types**: primitive, datatype, array
 - **Variable** declarations
 - **Statements**: assign, assume, if-then-else
 - **Expressions**: identifier, array read/write, datatype constructor, member selector, conditional, basic arithmetic
- Can be **expressed in any SMT-based tool**
 - Boogie, Why3, Dafny, ...
 - Check by translating to **SSA**

```
Point(x : int, y : int)
```

```
pts : [int]Point
```

```
pts[0] := Point(1, 2)  
pts[1].x := pts[0].x + 1
```

Formalizing the Solidity memory model

Overview

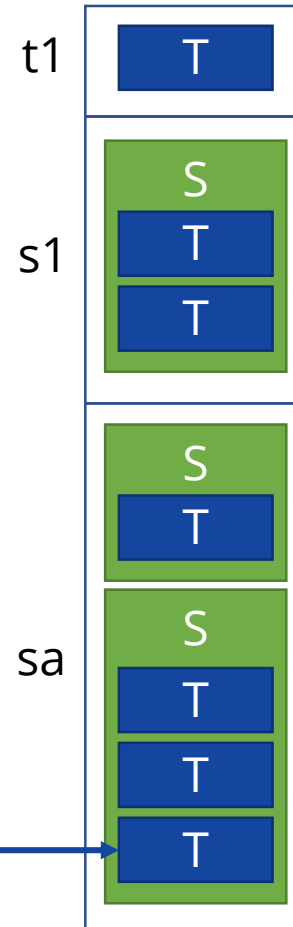
- Storage: value semantics

```
contract C {  
  struct S { int x; T[] ta; }  
  struct T { int z; }  
  
  T t1;  
  S s1;  
  S[] sa;  
}
```

- Local storage pointers

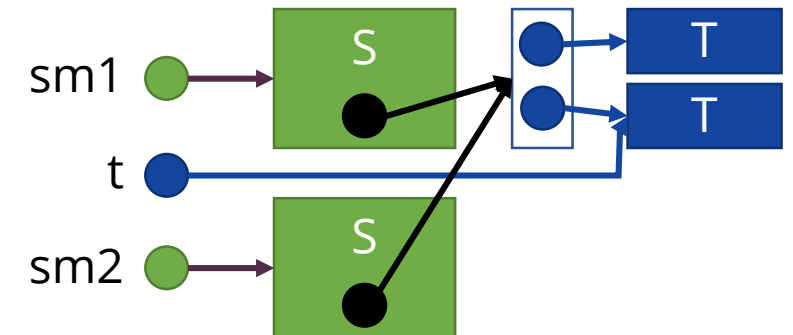
```
function f() public {  
  T storage tp = sa[1].ta[2];  
  g(tp);  
}  
function g(T storage t) internal {  
  t.z = 5;  
}
```

← No mixing →



- Memory: reference semantics

```
function f() public pure {  
  S memory sm1 = S(1, new T[](2));  
  T memory t = sm1.ta[1];  
  S memory sm2 = S(2, sm1.ta);  
}
```



Encoding the Memory

- Standard **heap model** (per type)
 - Pointer: SMT integer
 - Struct: SMT datatype
 - Array: SMT array + length
 - No null, default values recursively

```
S memory sm1 = S(1, new T[](2));
```

```
sm1 : int
heapT[0] := Tmem(0)
heapT[1] := Tmem(0)
heapTA[2] := Tmemarr([0, 1], 2)
heapS[3] := Smem(1, 2)
sm1 := 3
```

Allocation counter

```
struct T { int z; }
struct S { int x; T[] ta; }
```

```
Tmem(z : int)
Tmemarr(arr : [int]int, len : int)
Smem(x : int, ta : int)
```

```
heapT : [int]Tmem
heapTA : [int]Tmemarr
heapS : [int]Smem
```

```
sm1.ta[1].z;
```

```
heapT[heapTA[heapS[3].ta].arr[1]].z
```

Encoding the Memory

```
struct T { int z; }  
struct S { int x; T[] ta; }
```

- Scope limited to a single transaction
- **Non-aliasing** and new allocations
 - Require quantifiers in the general case (decidable fragment)

```
function f(S memory sm) {  
    ... = S(...)  
}
```

New allocations should
not alias with sm

Allocation counter

sm

```
assume(sm < refcnt)  
assume(heapS[sm].ta < refcnt)  
forall 0 <= i < heapTA[heapS[sm].ta].len:  
    assume(heapTA[heapS[sm].ta].arr[i] < refcnt)
```

sm.ta

sm.ta[i] (for each i)

Encoding the Storage

- Encode with **SMT datatypes** without heaps
 - **Non-aliasing** and **deep copy** ensured out-of-the-box
 - Especially useful in modular verification
 - Otherwise many framing conditions for functions

```
struct T { int z; }  
struct S { int x; T[] ta; }
```

```
contract C {  
  T    t1;  
  S    s1;  
  S[] sa;  
}
```

```
Tstor(z : int)  
Tstorarr(arr : [int]Tstor, len : int)  
Sstor(x : int, ta : Tstorarr)  
Sstorarr(arr : [int]Sstor, len : int)
```

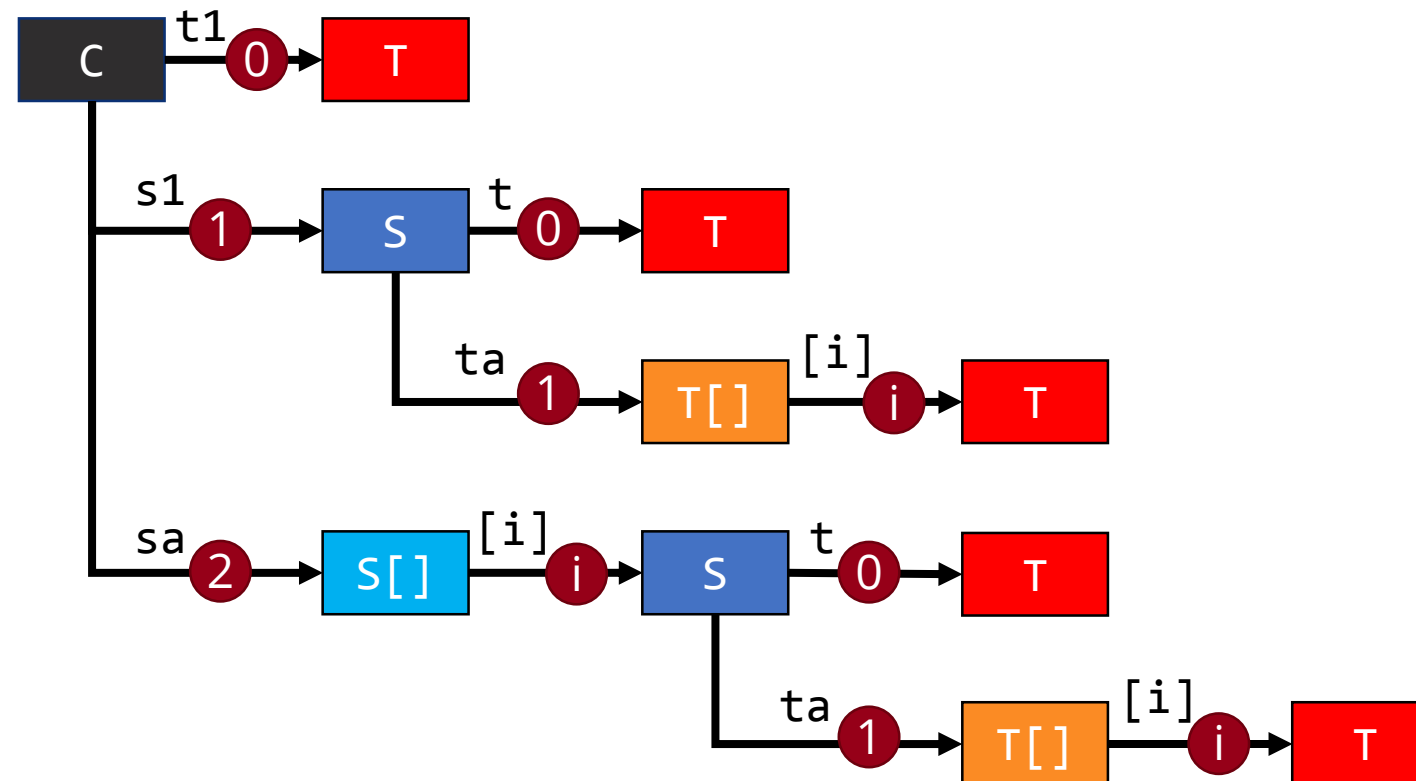
```
t1: Tstor  
s1: Sstor  
sa: Sstorarr
```

Local storage
pointers?

Local Storage Pointers

- Storage is a **finite-depth tree** of values*
- Each element identified by **path** → encode with **SMT integer array**

```
contract C {
  struct T {
    int z;
  }
  struct S {
    int x;
    T t;
    T[] ta;
  }
  T t1;
  S s1;
  S[] sa;
}
```



Local Storage Pointers

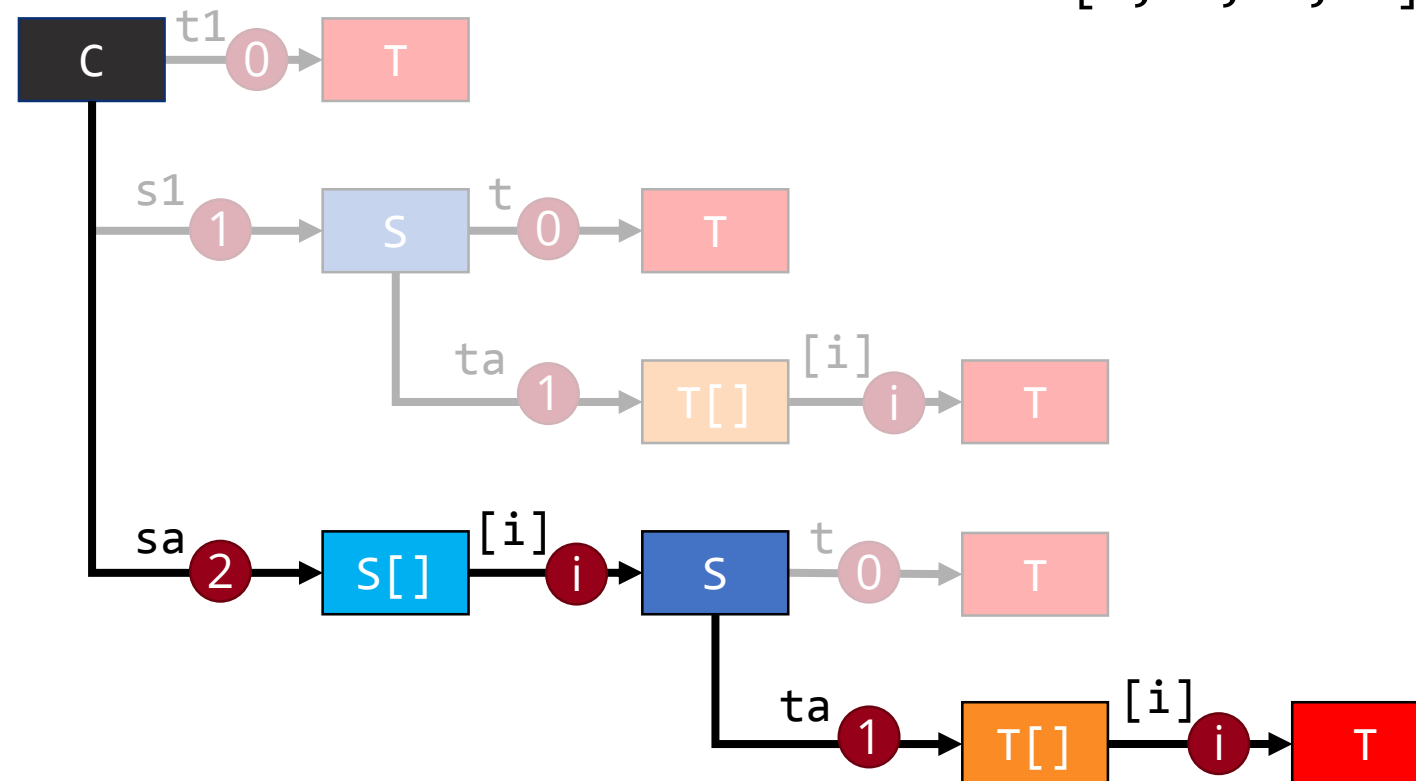
- **Packing:** expression to SMT array
 - Fit expression to tree

T storage t = sa[8].ta[5];

t : [int]int
t := [2, 8, 1, 5]

```
contract C {
  struct T {
    int z;
  }
  struct S {
    int x;
    T t;
    T[] ta;
  }

  T t1;
  S s1;
  S[] sa;
}
```

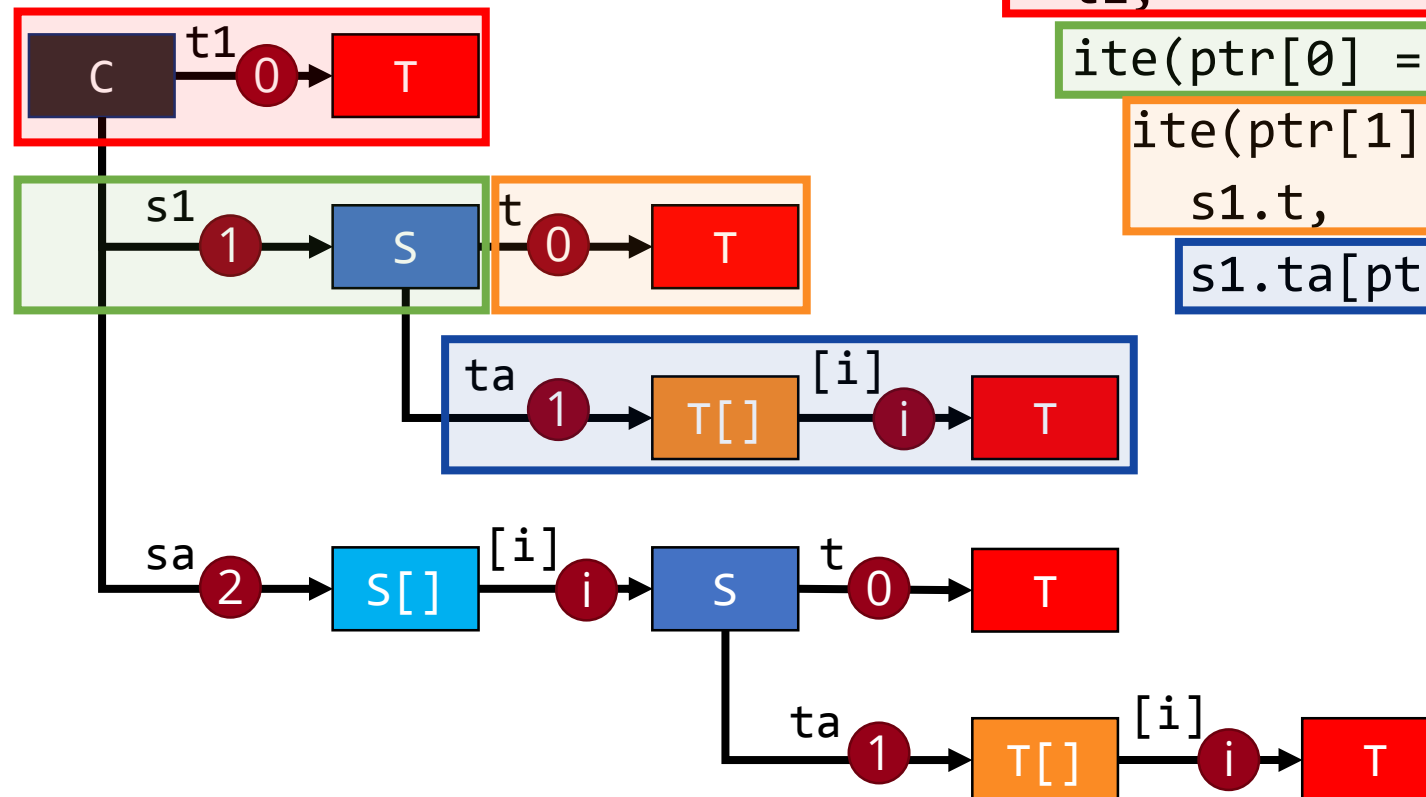


Local Storage Pointers

- **Unpacking:** SMT array to expression
 - Conditional based on tree

```
contract C {
  struct T {
    int z;
  }
  struct S {
    int x;
    T t;
    T[] ta;
  }

  T t1;
  S s1;
  S[] sa;
}
```



```
function f(T storage ptr) {
  ... ptr.z;
}
```

```
ite(ptr[0] = 0,
    t1,
```

```
ite(ptr[0] = 1,
```

```
ite(ptr[1] = 0,
    s1.t,
```

```
s1.ta[ptr[2]]), ... ).z
```

Assignments Between Data Locations

LHS/RHS	Storage	Memory	Storage ptr.
Storage	Deep copy	Deep copy	Deep copy
Memory	Deep copy	Pointer assign	Deep copy
Storage ptr.	Pointer assign	Error	Pointer assign

- Ensured by construction
- Ensured by pack/unpack
- Need manual copying
 - Requires quantifiers in the general case

Details in Paper

ESOP 2020 - arxiv.org/abs/2001.03256

$\mathcal{T}(\text{bool}) \doteq \text{bool}$
 $\mathcal{T}(\text{address}) \doteq \mathcal{T}(\text{int}) \doteq \mathcal{T}(\text{uint}) \doteq \text{int}$
 $\mathcal{T}(\text{mapping}(K \Rightarrow V) \text{ storage}) \doteq [\mathcal{T}(K)]\mathcal{T}(V)$
 $\mathcal{T}(\text{mapping}(K \Rightarrow V) \text{ storptr}) \doteq [\text{int}]\text{int}$
 $\mathcal{T}(\mathcal{T}[n] \text{ storage}) \doteq \mathcal{T}(\mathcal{T}[] \text{ storage})$
 $\mathcal{T}(\mathcal{T}[n] \text{ storptr}) \doteq \mathcal{T}(\mathcal{T}[] \text{ storptr})$
 $\mathcal{T}(\mathcal{T}[n] \text{ memory}) \doteq \mathcal{T}(\mathcal{T}[] \text{ memory})$

$\mathcal{T}(\mathcal{T}[])$ $\mathcal{S}[\mathcal{T} \text{ id}] \doteq [\text{id} : \mathcal{T}(T)]; \mathcal{A}(\text{id}, \text{defval}(T))$
 $\mathcal{T}(\mathcal{T}[])$ $\mathcal{S}[\mathcal{T} \text{ id} = \text{expr}] \doteq [\text{id} : \mathcal{T}(T)]; \mathcal{A}(\text{id}, \mathcal{E}(\text{expr}))$
 $\mathcal{T}(\mathcal{T}[])$ $\mathcal{S}[\text{delete } e] \doteq \mathcal{A}(\mathcal{E}(e), \text{defval}(\text{type}(e)))$

$\mathcal{T}(\text{str})$ $\mathcal{S}[l_1, \dots, l_n = r_1, \dots, r_n] \doteq [tmp_i : \mathcal{T}(\text{type}(r_i))] \text{ for } 1 \leq i \leq n$
 $\mathcal{T}(\text{str})$ $\mathcal{A}(tmp_i, \mathcal{E}(r_i)) \text{ for } 1 \leq i \leq n$
 $\mathcal{T}(\text{str})$ $\mathcal{A}(\mathcal{E}(l_i), tmp_i) \text{ for } n \geq i \geq 1$

$\mathcal{S}[e_1.\text{push}(e_2)] \doteq \mathcal{A}(\mathcal{E}(e_1).\text{arr}[\mathcal{E}(e_1).\text{length}], \mathcal{E}(e_2))$
 $\mathcal{E}(e_1).\text{length} := \mathcal{E}(e_1).\text{length} + 1$
 $\mathcal{S}[e.\text{pop}()] \doteq \mathcal{E}(e).\text{length} := \mathcal{E}(e).\text{length} - 1$
 $\mathcal{A}(\mathcal{E}(e).\text{arr}[\mathcal{E}(e).\text{length}], \text{defval}(\text{arrtype}(\mathcal{E}(e))))$

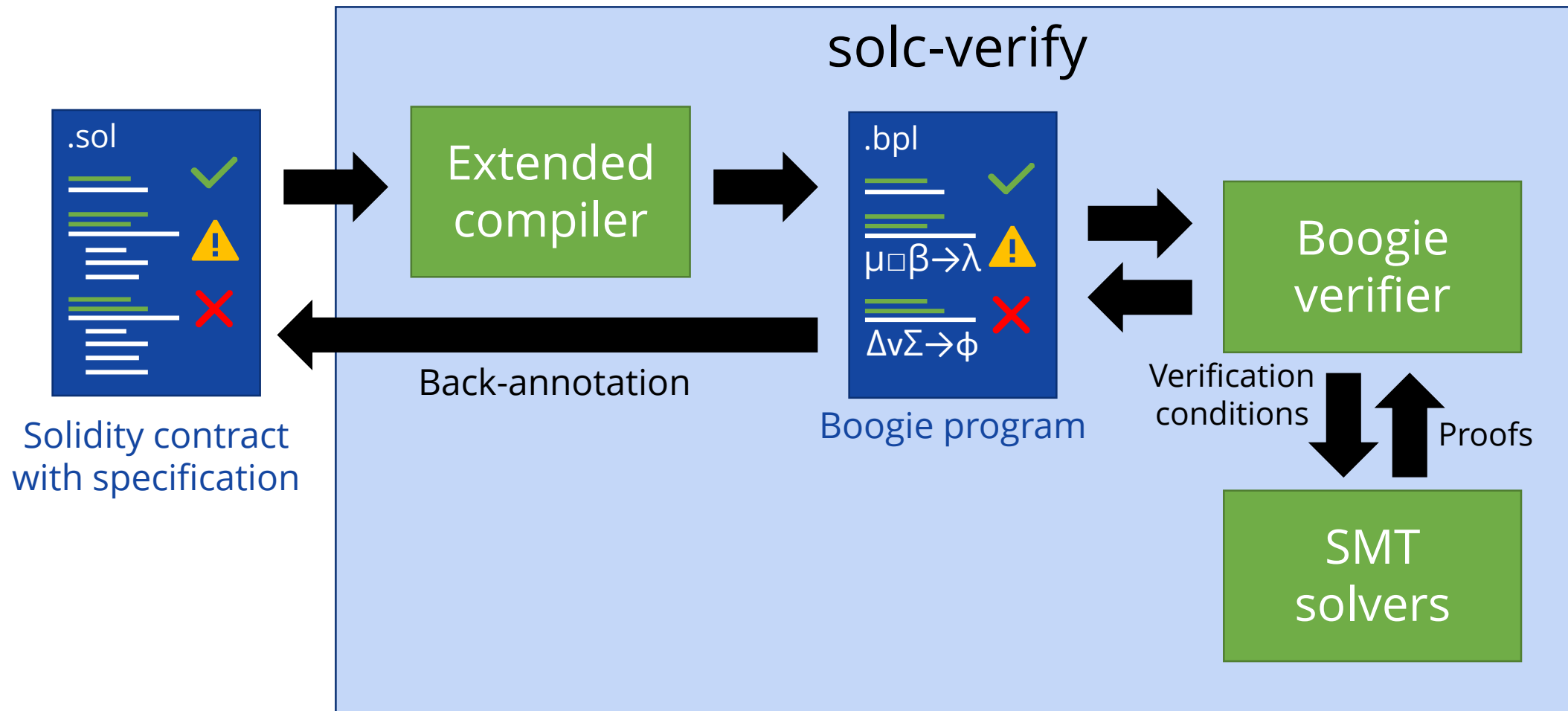
`def unpack(ptr):`
`return unpack(ptr, tree(type(ptr)), empty, 0);`
`def unpack(ptr, node, expr, d):`
`result := empty;`
`if node has no outgoing edges then result := expr;`
`if node is contract then`
`foreach edge node $\xrightarrow{id(i)}$ child do`
`result := ite(ptr[d] = i, unpack(ptr, child, id, d + 1), result);`
`if node is struct then`
`foreach child do`

$\mathcal{A}_S(\text{lhs} : \text{s}, \text{rhs} : \text{s}) \doteq \text{lhs} := \text{rhs}$
 $\mathcal{A}_S(\text{lhs} : \text{s}, \text{rhs} : \text{m}) \doteq \mathcal{A}(\text{lhs}.m_i, \text{structheap}_{\text{type}(\text{rhs})}[\text{rhs}].m_i) \text{ for each } m_i$
 $\mathcal{A}_S(\text{lhs} : \text{s}, \text{rhs} : \text{sp}) \doteq \mathcal{A}_S(\text{lhs}, \text{unpack}(\text{rhs}))$
 $\mathcal{A}_S(\text{lhs} : \text{m}, \text{rhs} : \text{m}) \doteq \text{lhs} := \text{rhs}$
 $\mathcal{A}_S(\text{lhs} : \text{m}, \text{rhs} : \text{s}) \doteq \text{lhs} := \text{refcnt} := \text{refcnt} + 1$
 $\mathcal{A}_S(\text{lhs} : \text{m}, \text{rhs} : \text{sp}) \doteq \mathcal{A}(\text{structheap}_{\text{type}(\text{lhs})}[\text{lhs}].m_i, \text{rhs}.m_i) \text{ for each } m_i$
 $\mathcal{A}_S(\text{lhs} : \text{m}, \text{rhs} : \text{sp}) \doteq \mathcal{A}_S(\text{lhs}, \text{unpack}(\text{rhs}))$
 $\mathcal{A}_S(\text{lhs} : \text{sp}, \text{rhs} : \text{s}) \doteq \text{lhs} := \text{pack}(\text{rhs})$
 $\mathcal{A}_S(\text{lhs} : \text{sp}, \text{rhs} : \text{sp}) \doteq \text{lhs} := \text{rhs}$

Tool & Evaluation

Implementation

- github.com/SRI-CSL/solidity
- arxiv.org/abs/1907.04262
- youtu.be/1q2gSm3NuQA



Specification Annotations

- Solidity provides
 - require, assert
- Annotation language
 - Features
 - Pre/postconditions
 - Contract level invariants
 - Loop invariants
 - Access control (modifies)
 - Events *in progress*
 - Solidity expressions (side effect free)
 - Extra: sum over collections
 - Quantifiers *in progress*

FMBC talk tomorrow!
fmbc.gitlab.io/2020

```
/// @notice invariant x == y
contract C {
    int x;
    int y;

    /// @notice precondition x == y
    /// @notice postcondition x == (y + n)
    /// @notice modifies x
    function add_to_x(int n) internal {
        x = x + n;
        require(x >= y);
    }

    /// @notice modifies x if n > 0
    /// @notice modifies y if n > 0
    function add(int n) public {
        require(n >= 0);
        add_to_x(n);
        /// @notice invariant y <= x
        while (y < x) {
            y = y + 1;
        }
    }
}
```

Compared Tools

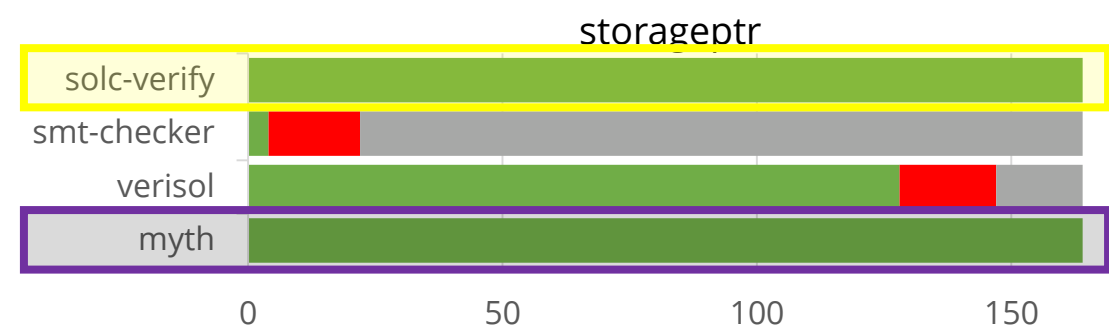
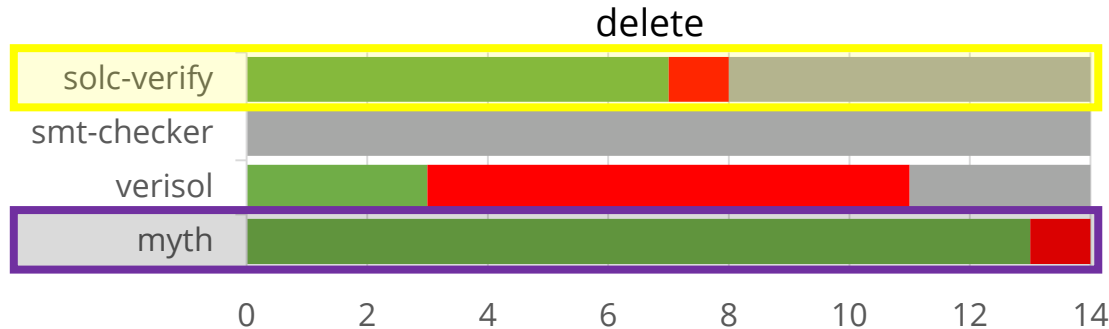
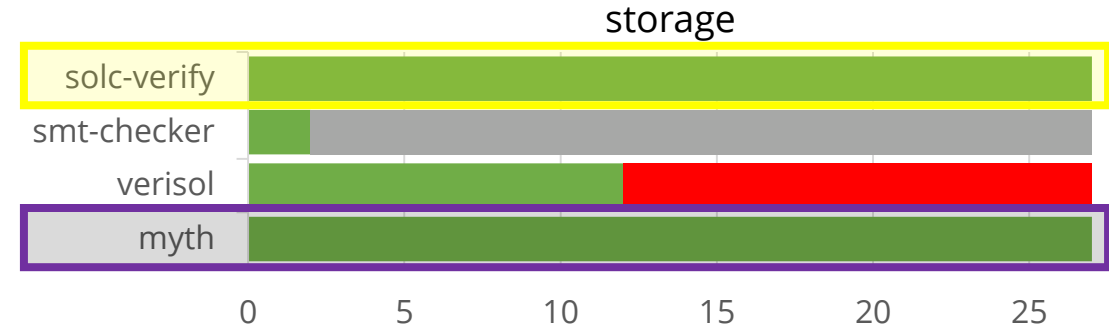
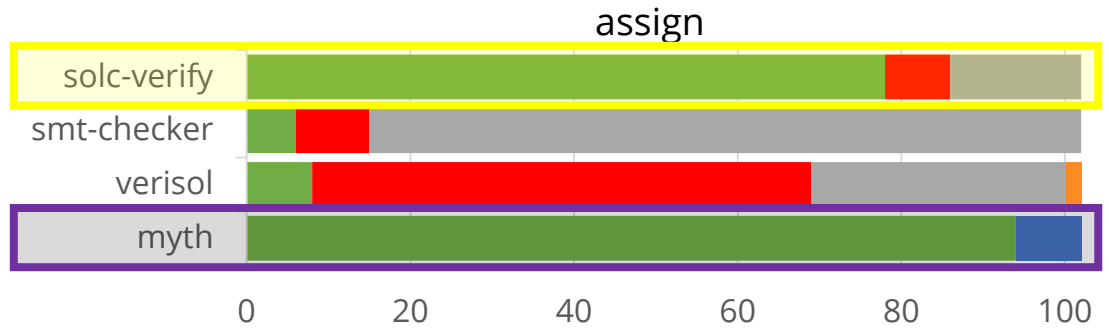
- **solc-verify** (our tool) github.com/SRI-CSL/solidity
 - Modular verifier based on Boogie/SMT and the presented encoding
- **Mythril** github.com/ConsenSys/mythril
 - Symbolic execution engine running over bytecode
- **VeriSol** github.com/microsoft/verisol
 - Modular/BMC tool based on Boogie/SMT
 - Heap-based modeling of both memory and storage
- **SMTchecker** github.com/ethereum/solidity
 - SMT-based intra-function analyzer built into the compiler

Tests

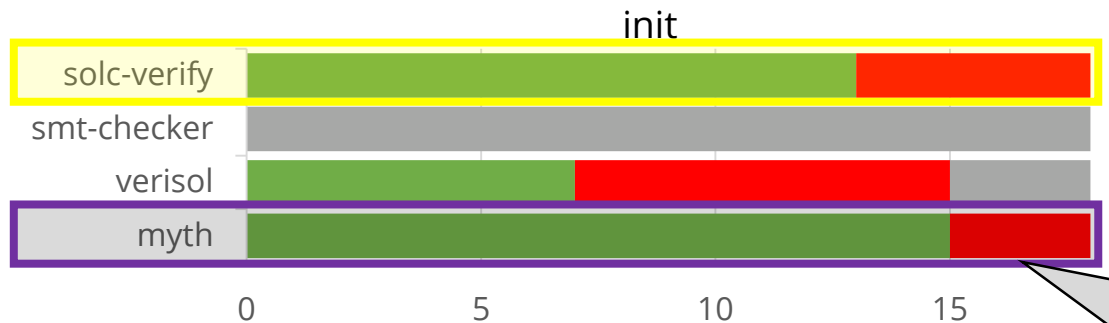
- “Real world” contracts: **limited** for evaluating memory semantics
 - Many old versions, new features are rare
 - Many toy examples, overrepresented categories
 - Complex contracts depend on other features
- **Manually developed tests**
 - 325 test cases organized into categories
 - Assign, delete, init, storage, storage pointer
 - Exercise a specific feature, check result with assertion

```
contract InitMemoryArrayFixedSize {  
    function test() public pure {  
        int[2] memory a;  
        assert(a.length == 2);  
        assert(a[0] == 0);  
        assert(a[1] == 0);  
    }  
}
```

Results



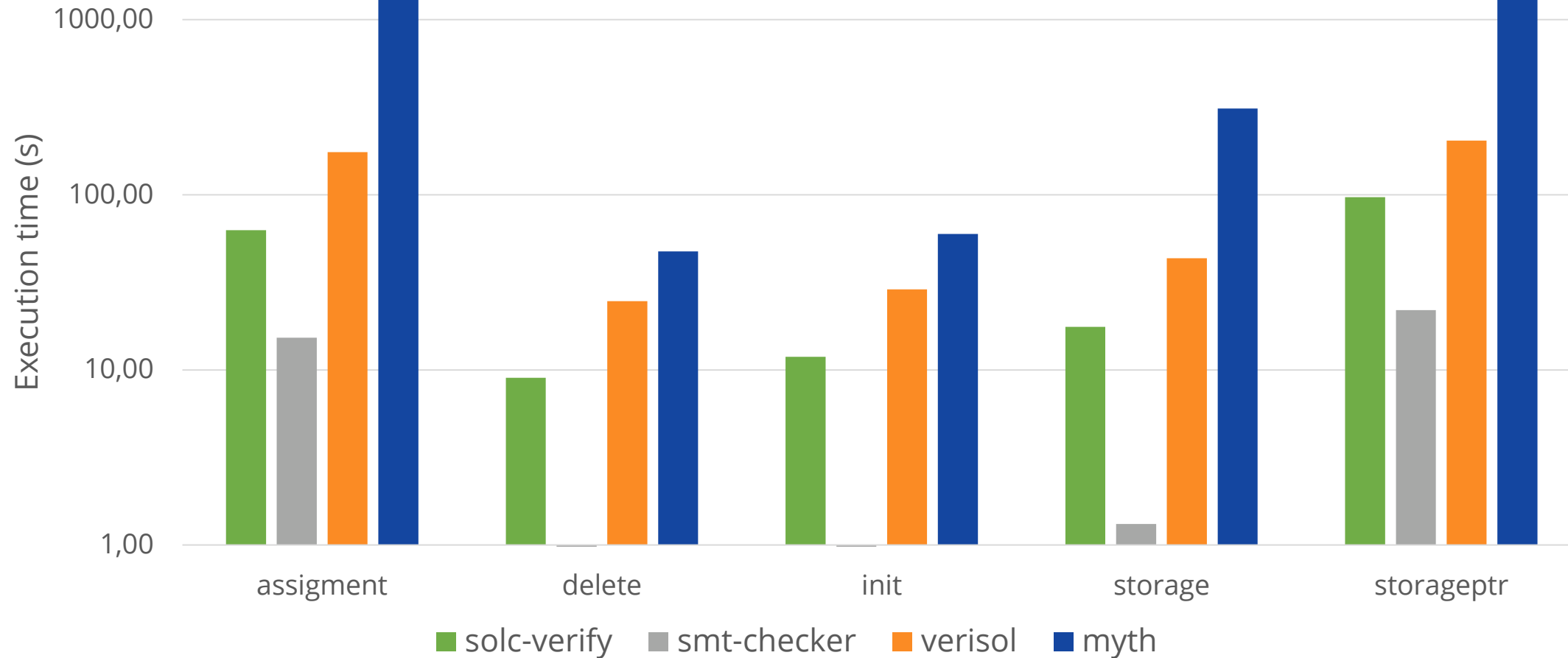
■ correct ■ incorrect ■ unsupported ■ unknown ■ timeout



- Bytecode level is precise
- solc-verify comes close
 - Some unimplemented features

Mythril bug report: github.com/ConsenSys/mythril/issues/1282

Results

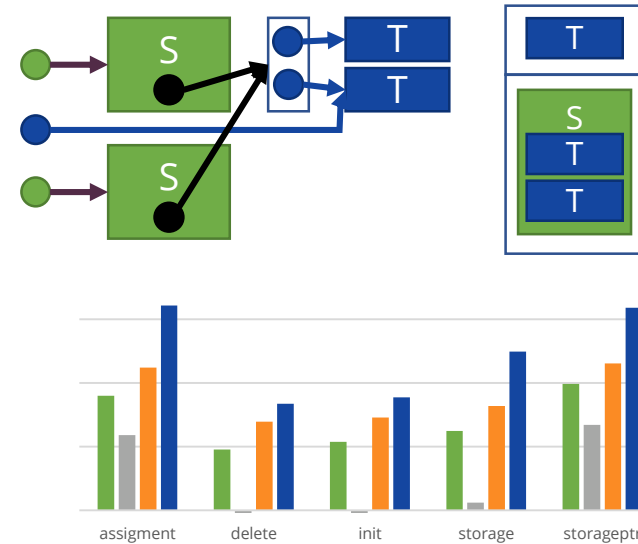


- Low computational cost for solc-verify

Summary

Summary

- SMT-based **formalization** of Solidity reference types
 - **Memory**: standard heap
 - **Storage**: values
 - Local storage **pointers**: encode path
- **Implementation**
 - solc-verify: modular verifier
 - Extensive set of test cases
 - **Effective**: on par with bytecode-level tools, at low computational cost



github.com/SRI-CSL/solidity
arxiv.org/abs/2001.03256
arxiv.org/abs/1907.04262

hajduakos.github.io
cs.l.sri.com/users/dejan