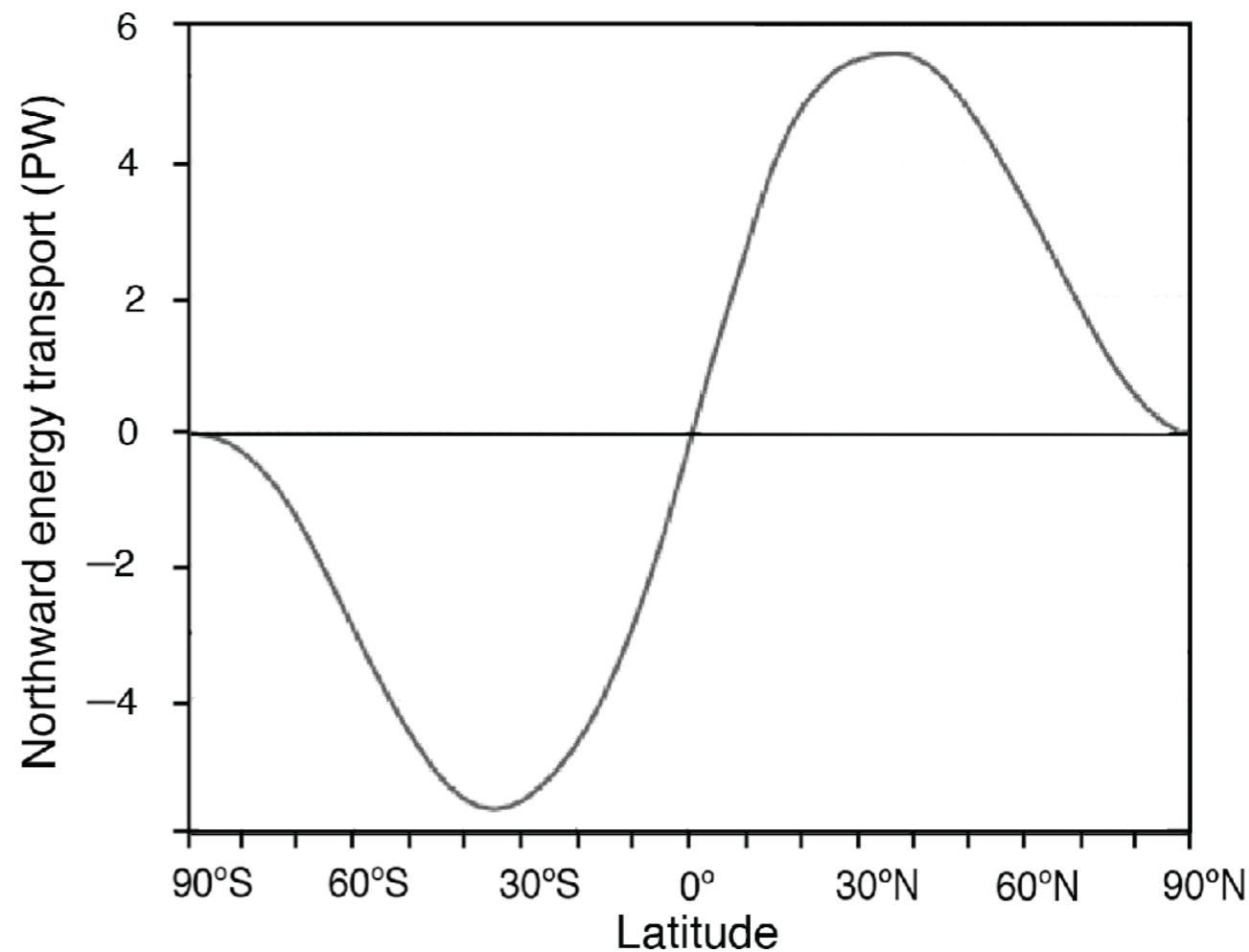
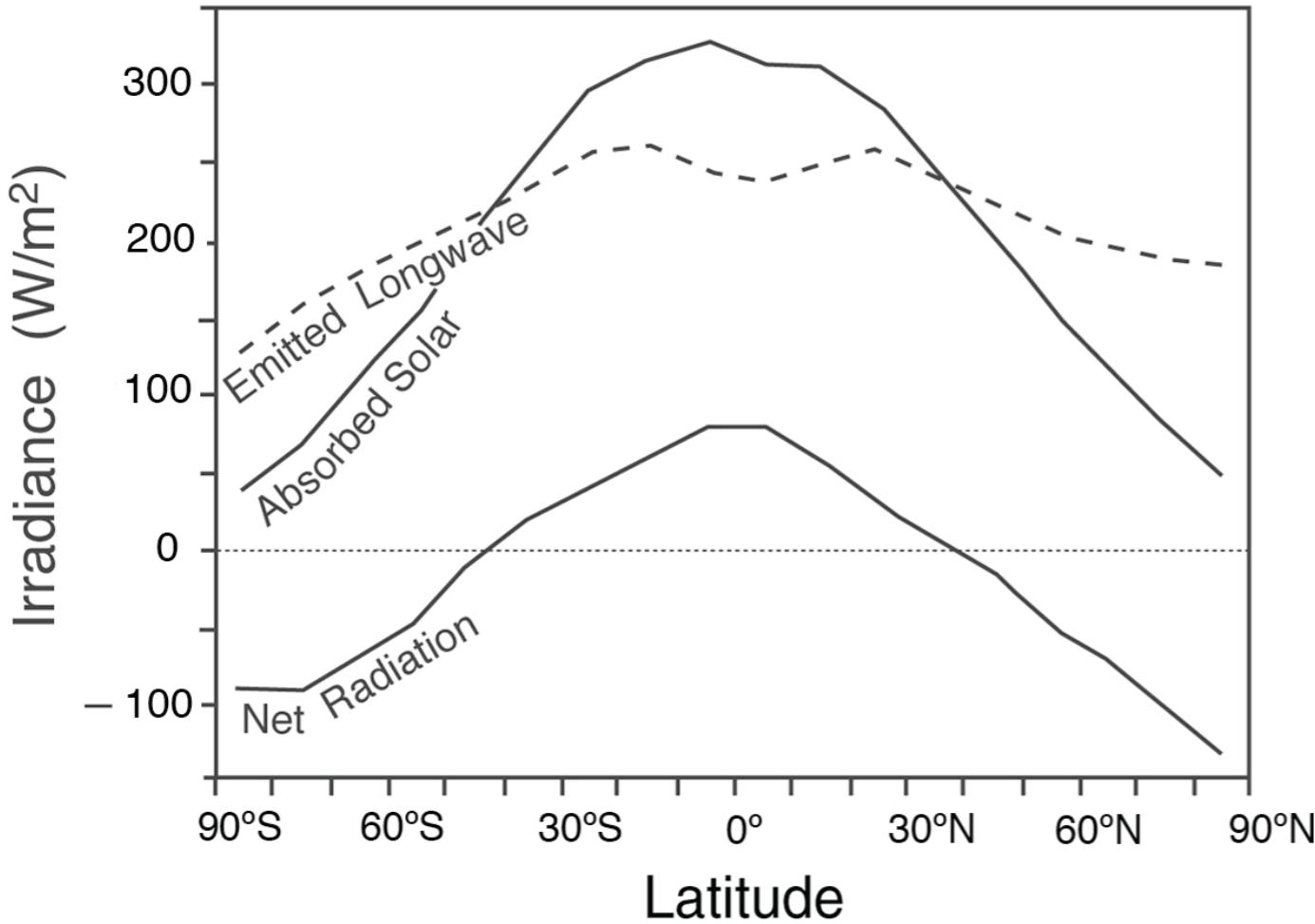


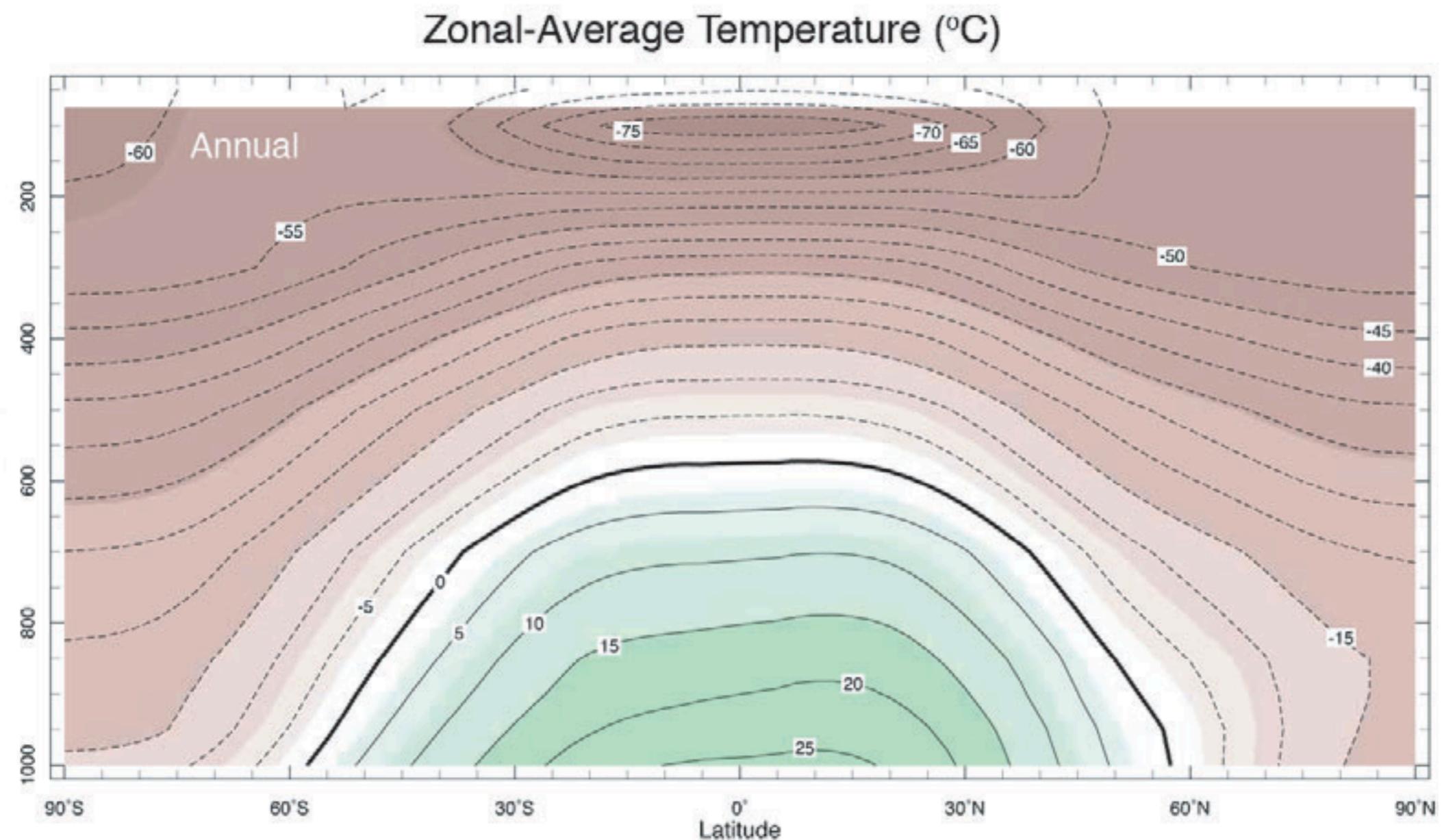
Chapter 5. Meridional structure of the atmosphere

1. Radiative imbalance

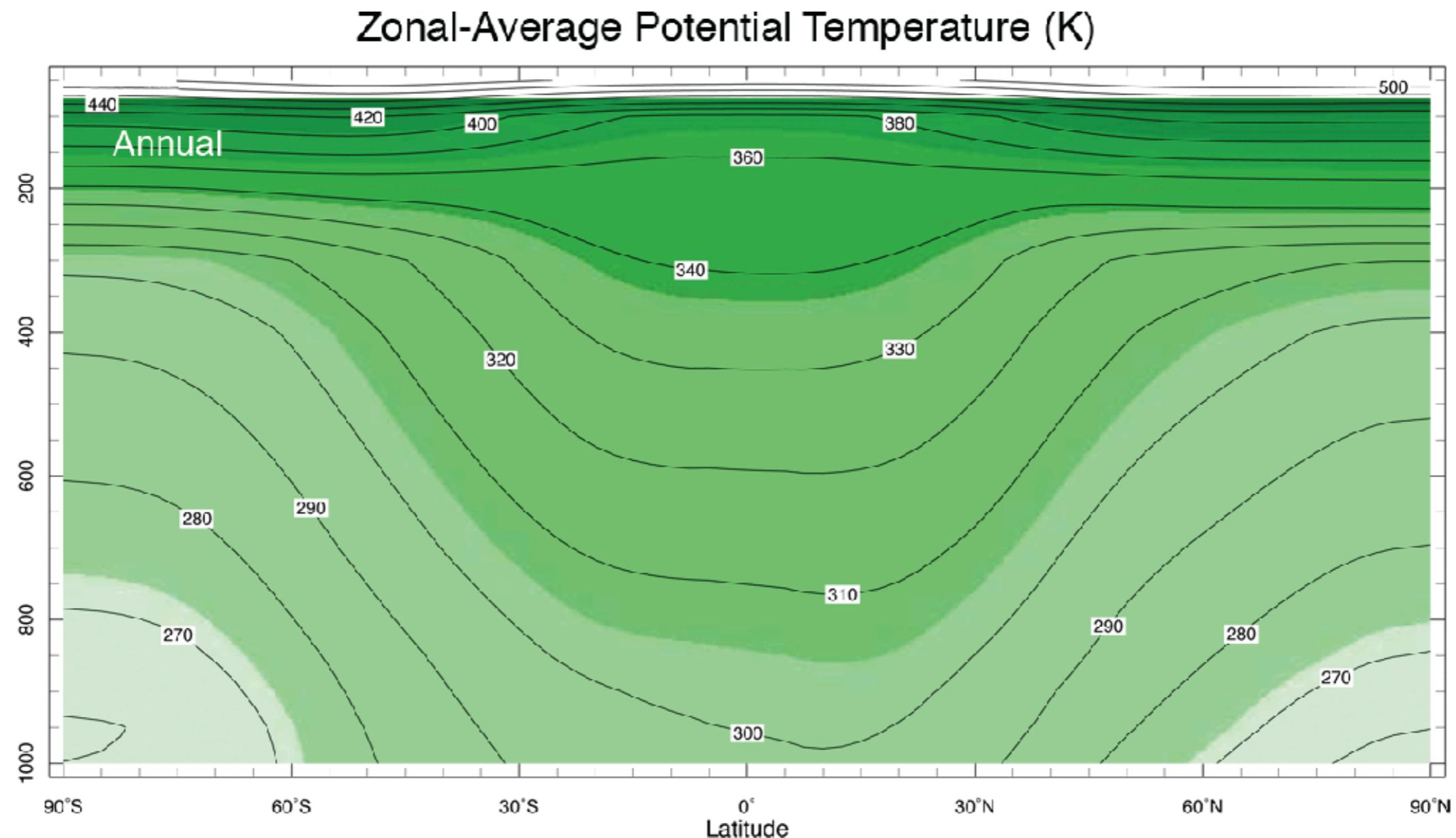


2. Temperature

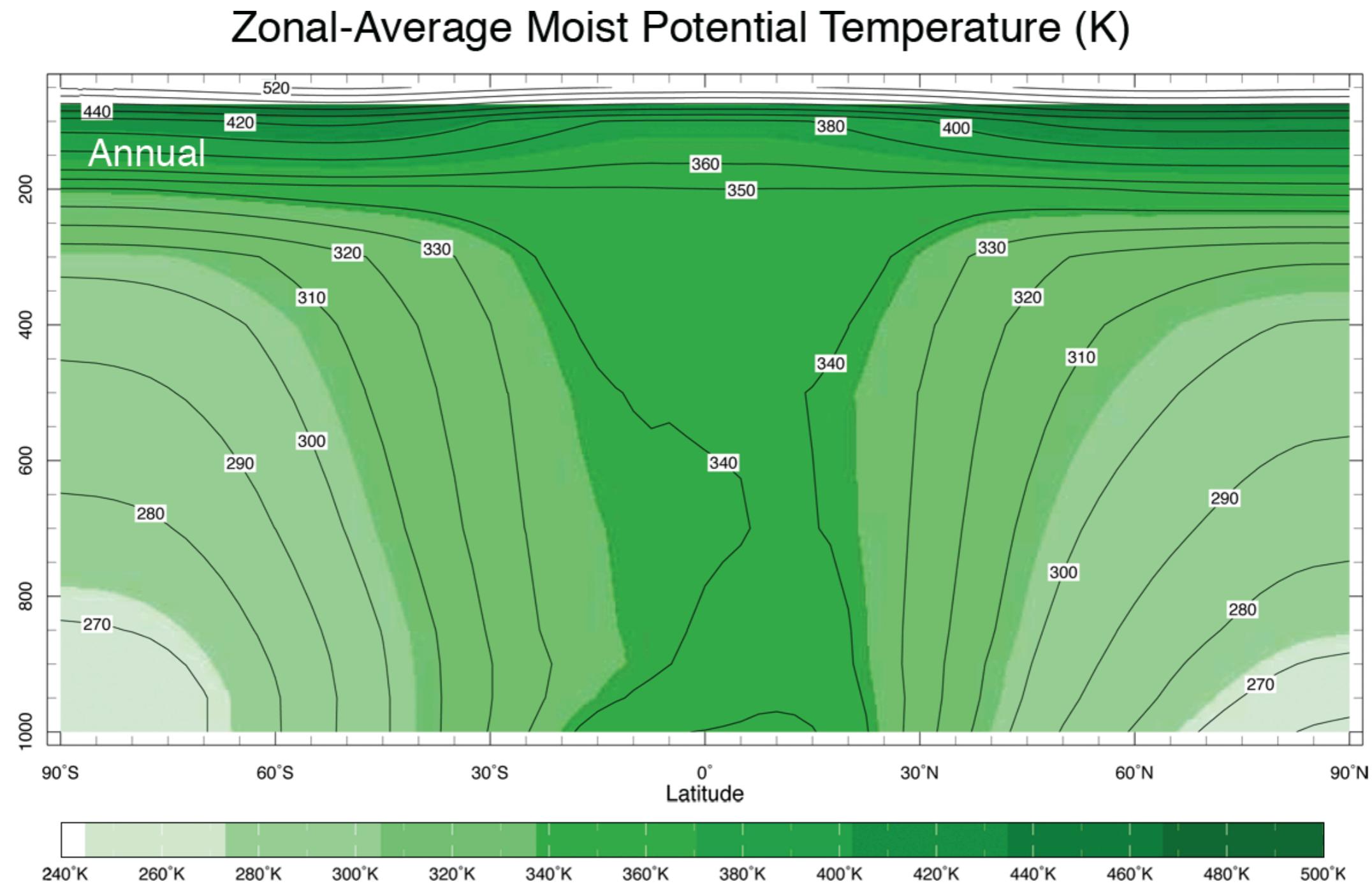
- See how the radiative imbalance shapes T



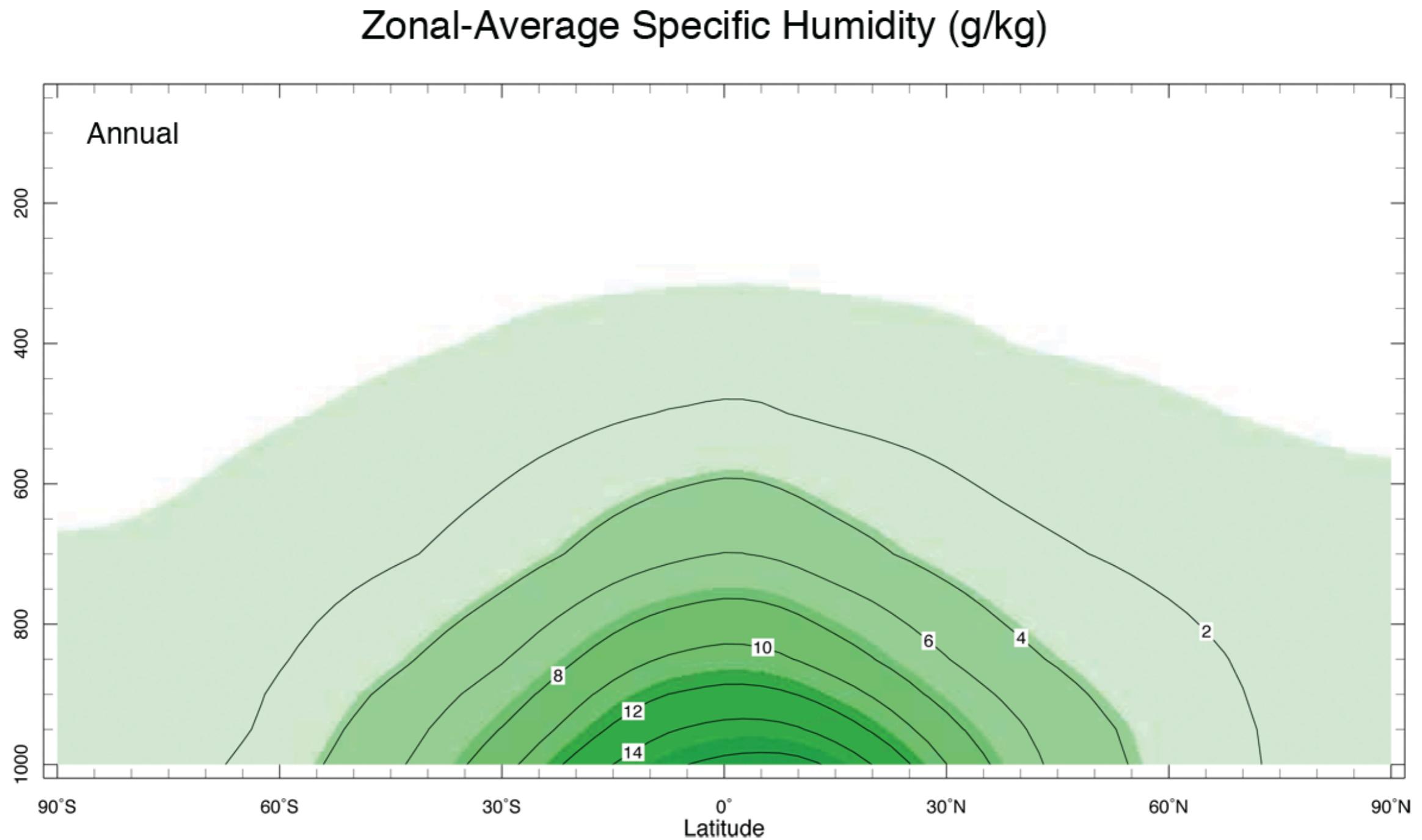
2. Temperature: potential temperature



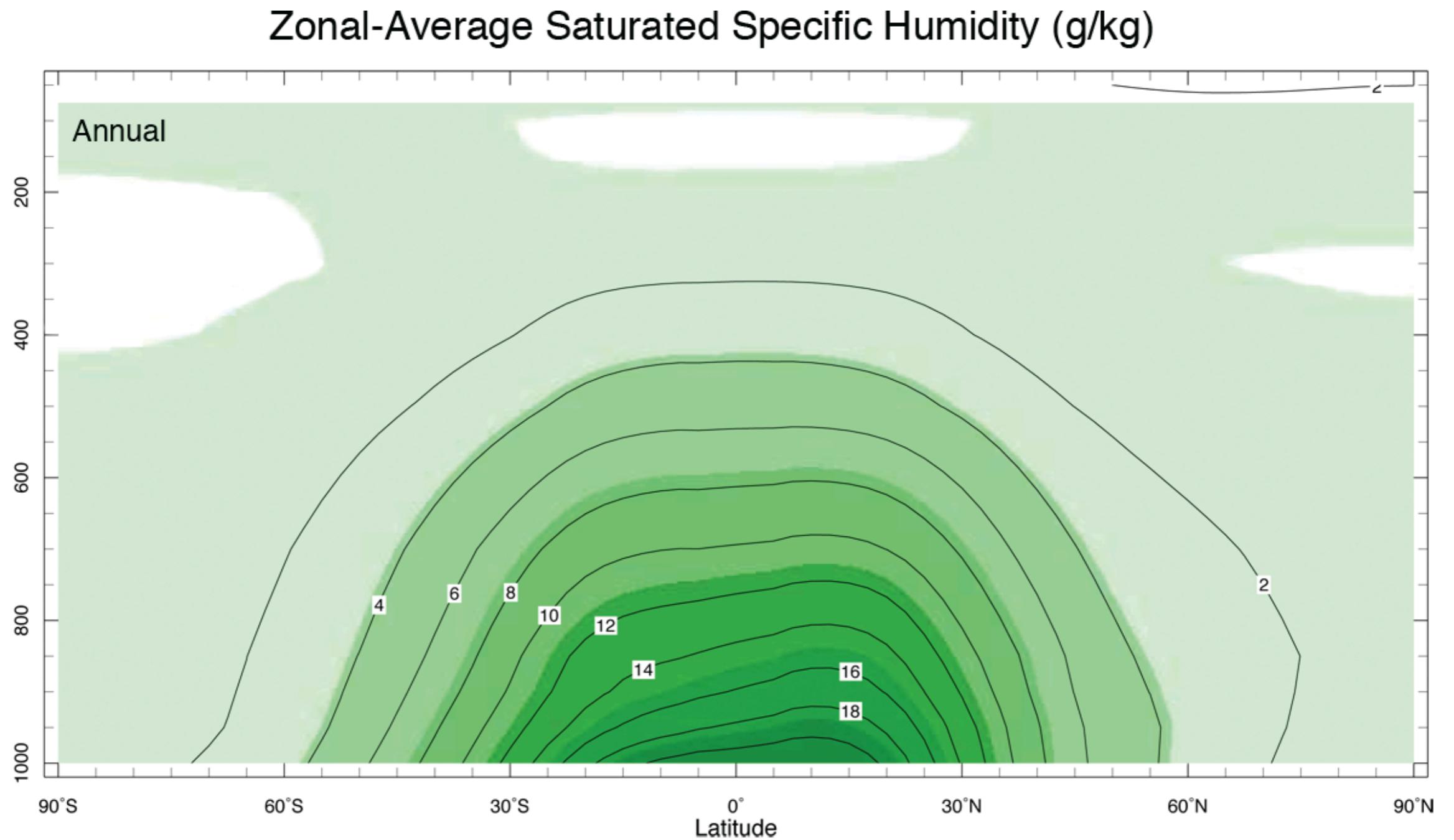
2. Temperature: equivalent potential temperature



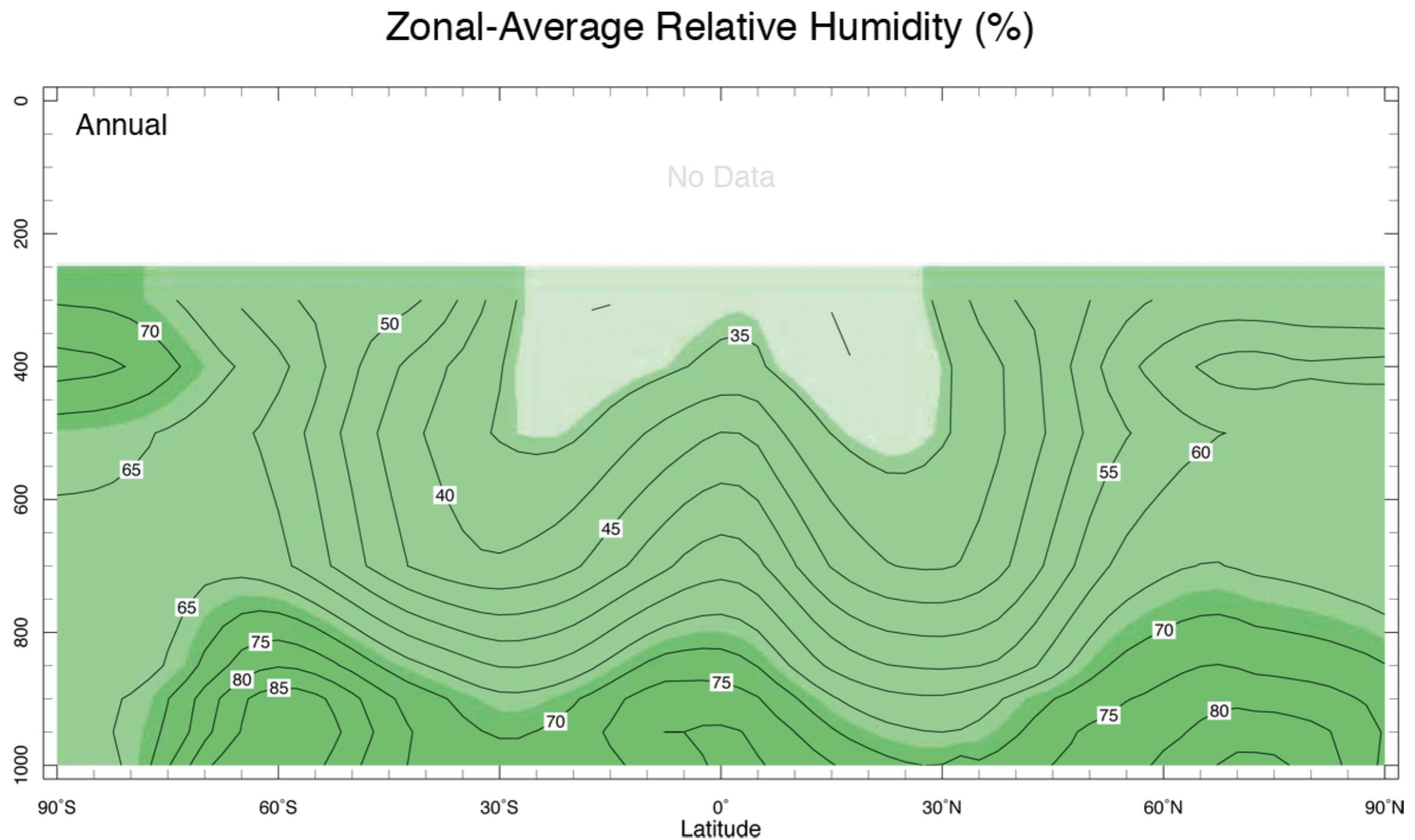
3. Humidity: specific humidity



3. Humidity: saturated specific humidity



3. Humidity: saturated specific humidity



Last time

- Saturated adiabatic lapse rate
- Equivalent potential temperature
- Convection
- Meridional structure of temperature
- Meridional structure of humidity

Today's topic

- Geopotential height
- Wind

4. Pressure / geopotential height

- From a hydrostatic balance and perfect gas law,

$$\frac{\partial z}{\partial p} = - \frac{RT}{gp}$$

$$z(p) = R \int_p^{p_s} \frac{T}{g} \frac{dp}{p}$$

- $z(p)$ is called **geopotential height**.
- If we assume that T and g does not vary a lot with p , geopotential height is higher when T increases.

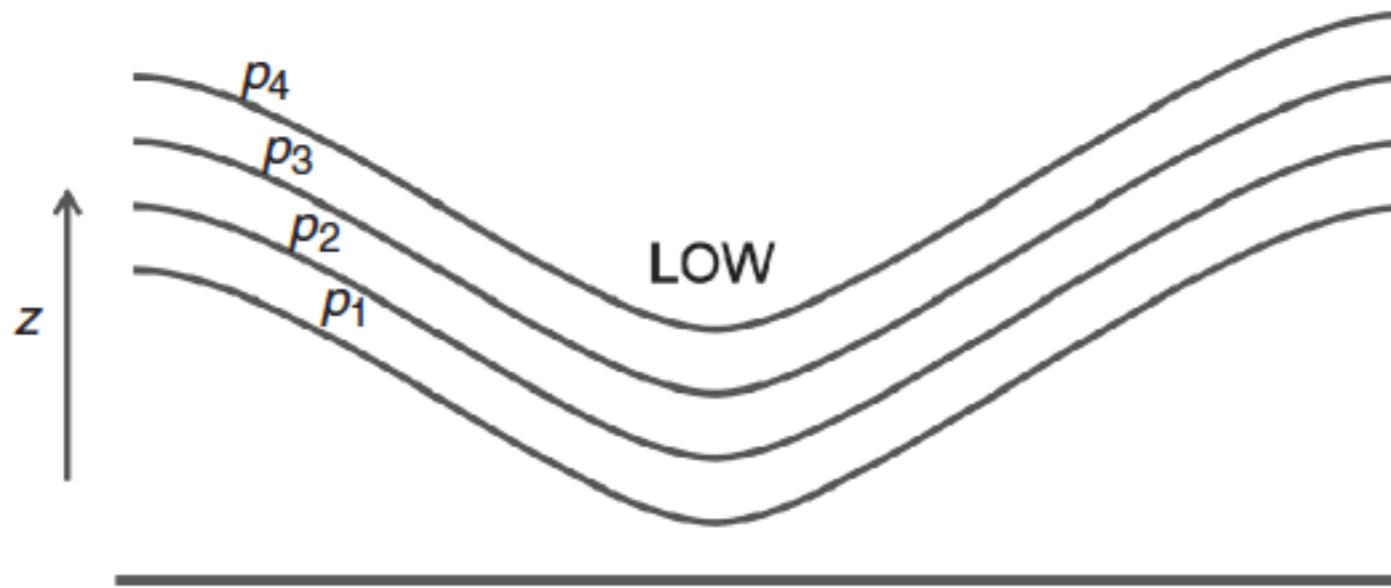
4. Pressure / geopotential height

- If we assume that g and T do not vary a lot with p ,

$$z(p) = \frac{RT}{g} (\ln p_s - \ln p)$$

- z increases as p decreases.
- Higher T increases geopotential height.

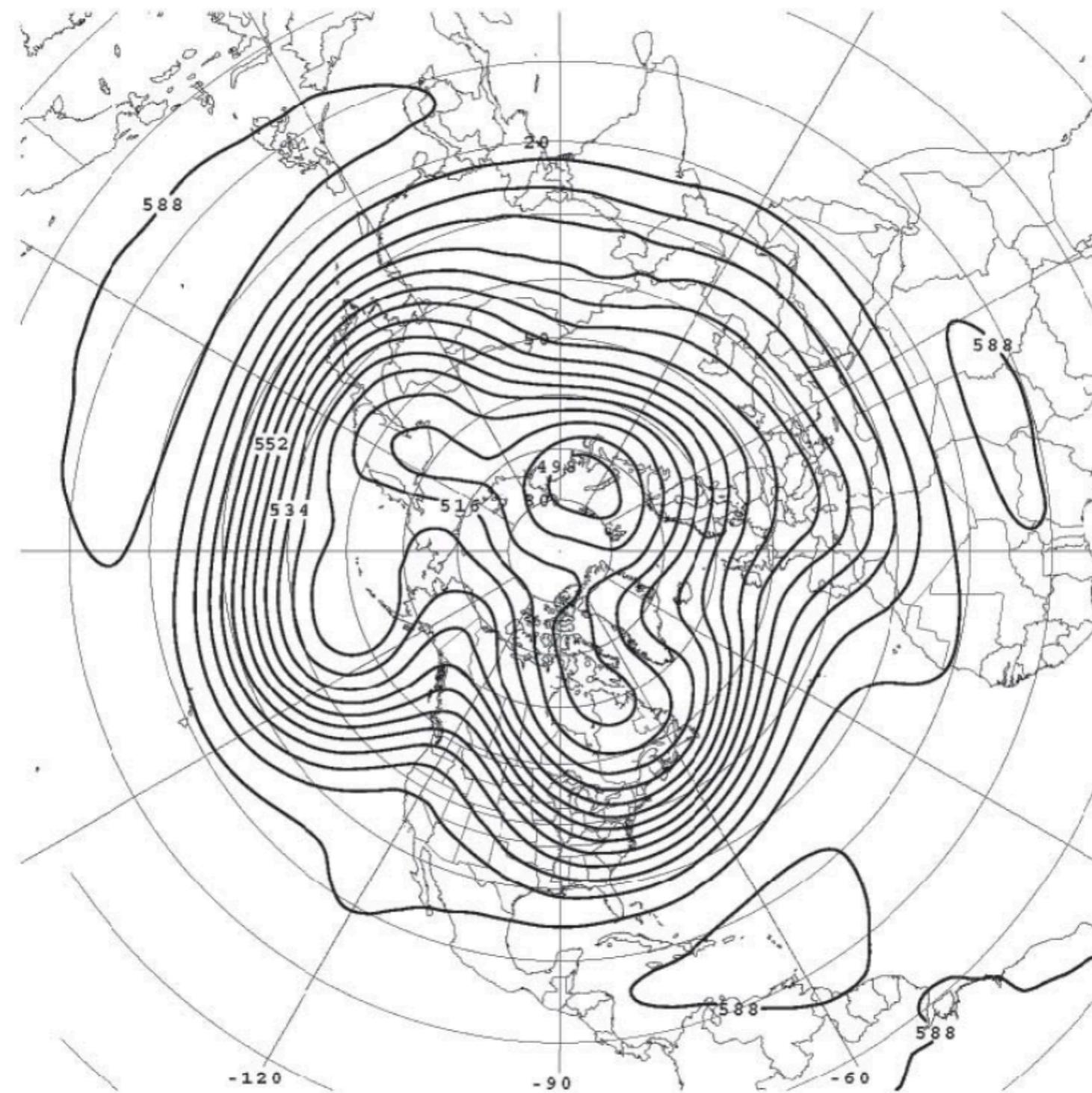
4. Pressure / geopotential height



- Geopotential height is lower at the low pressure system.
- Or the high pressure system corresponds to the high geopotential height.
- T tends to be low in the region of low geopotential height.

4. Pressure / geopotential height

The mean height of the 500 mbar surface in January , 2003



4. Pressure / geopotential height

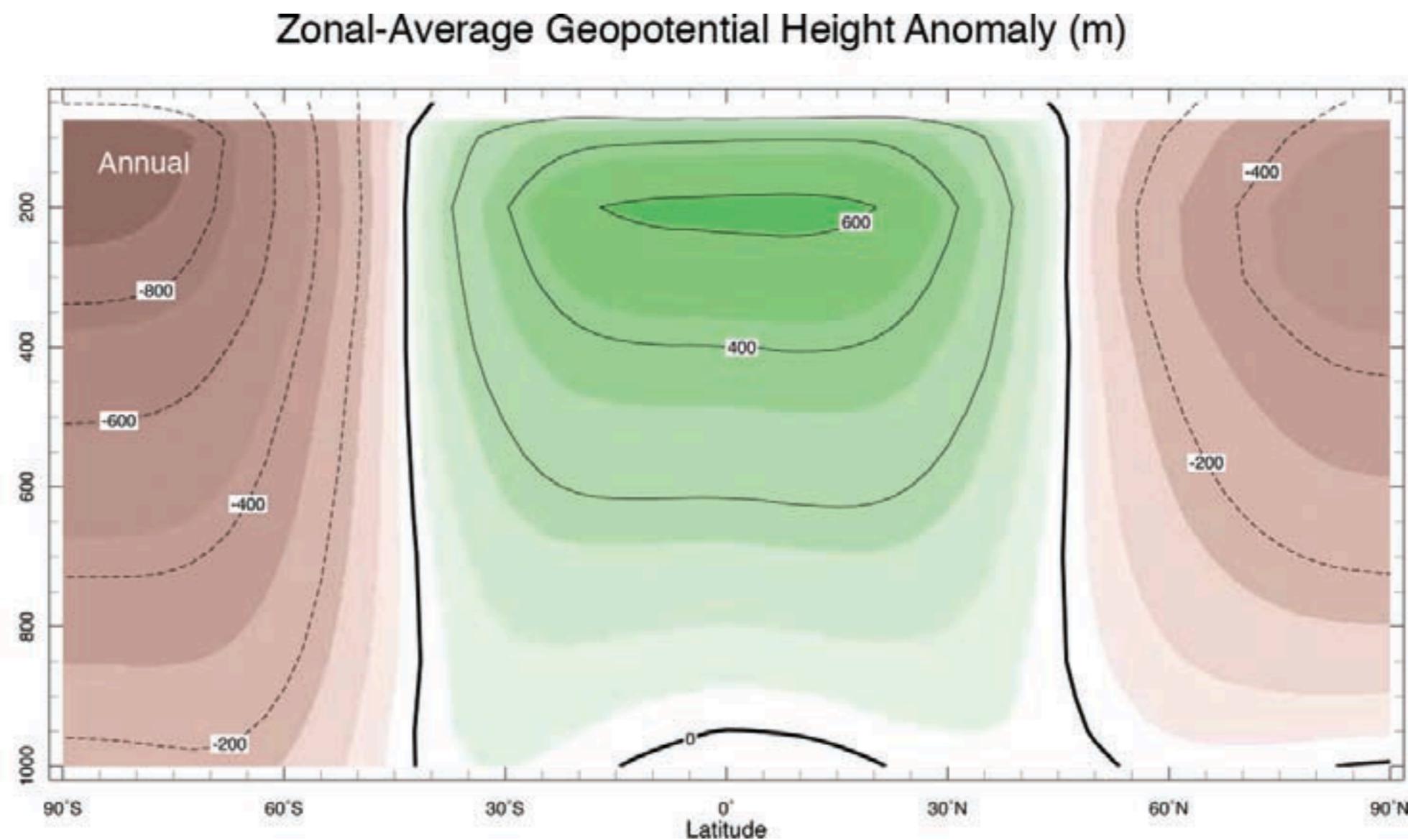
- We can discuss about the slope of the geopotential height if we know the temperature.

$$z_{warm} - z_{cold} = \frac{R}{g} (T_{warm} - T_{cold}) (\ln p_s - \ln p)$$

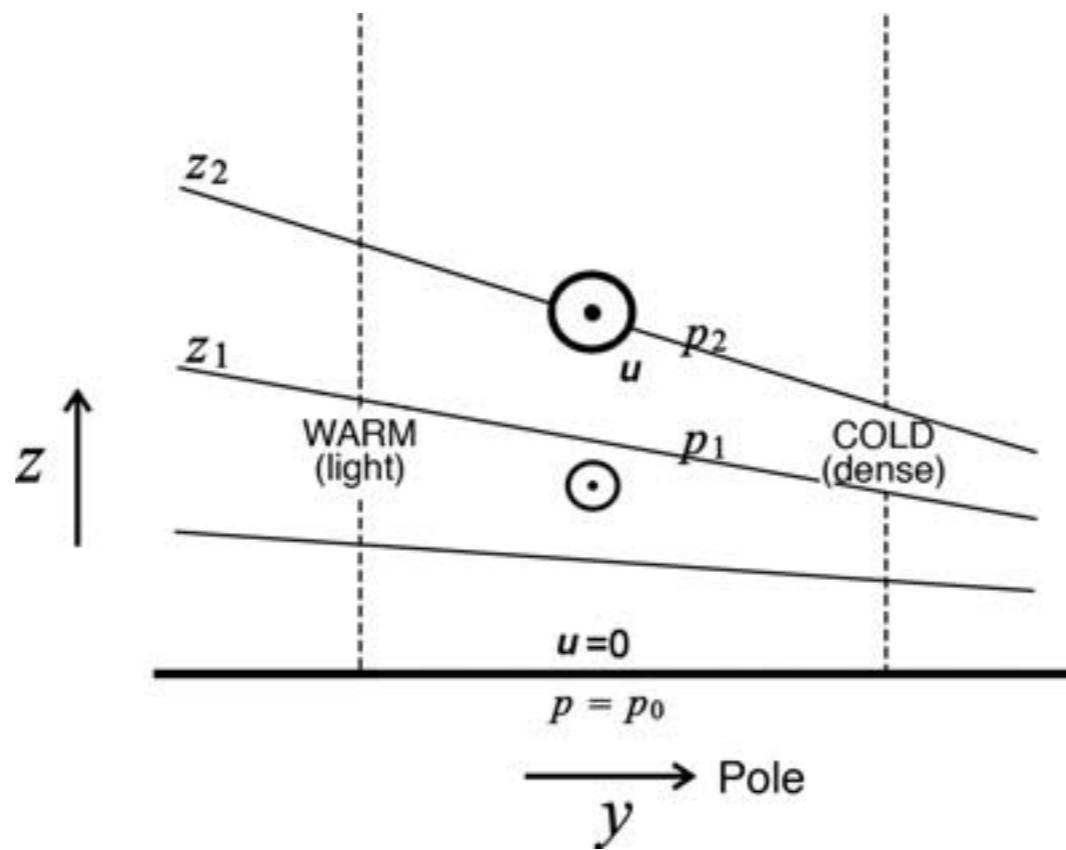
- We can also discuss about the thickness of an atmospheric layer if we know the temperature.

$$z_{p_1} - z_{p_2} = \frac{R\bar{T}}{g} (\ln p_2 - \ln p_1)$$

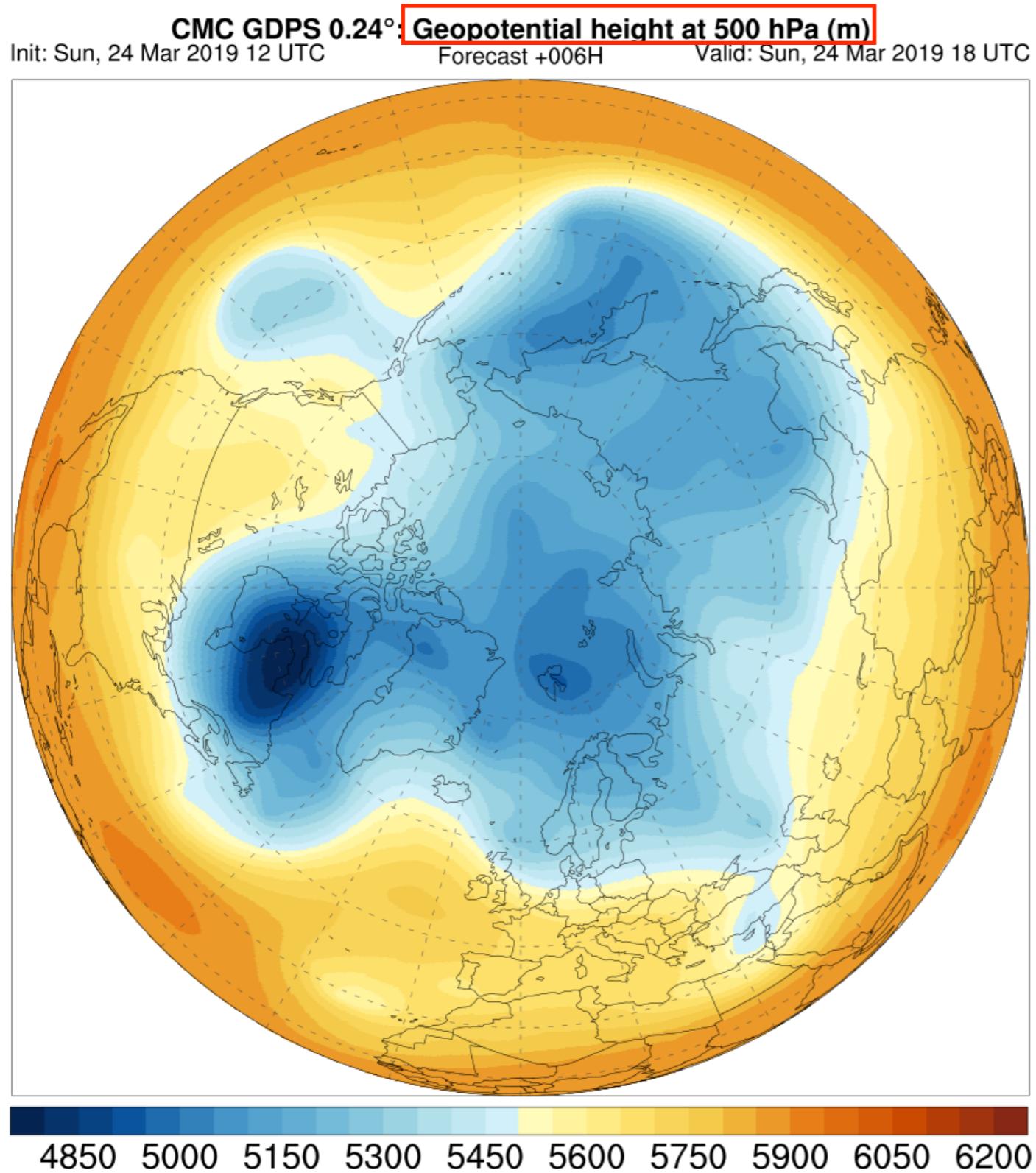
4. Pressure / geopotential height



4. Pressure / geopotential height



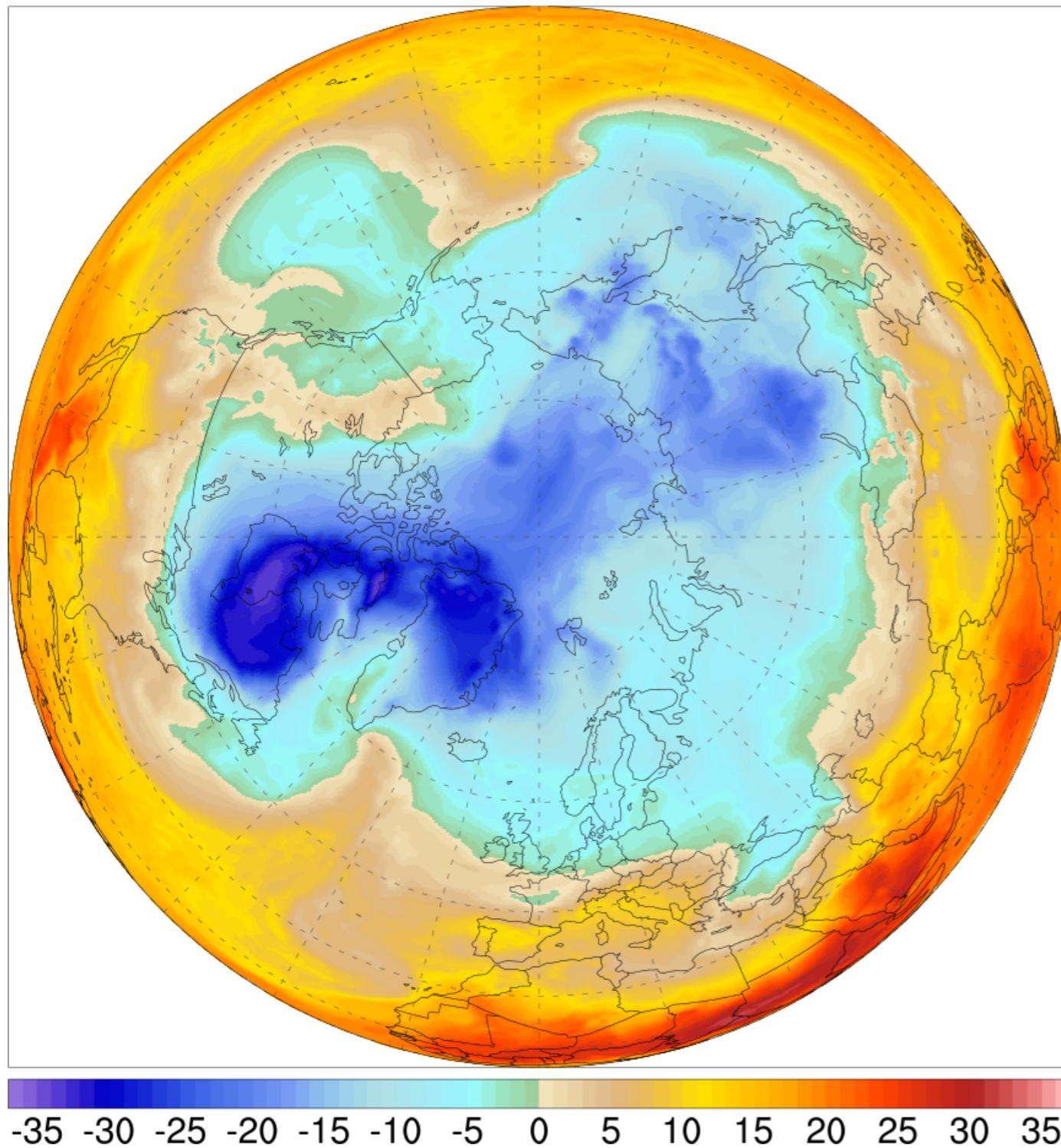
4. Pressure / geopotential height



From <http://www.genuineweather.com/?model=CMC-GDPS&run=12&zone=ART&type=G500&forecast=138>

4. Pressure / geopotential height

CMC GDPS 0.24°: Temperature at 850 hPa (°C)
Init: Sun, 24 Mar 2019 12 UTC Forecast +006H Valid: Sun, 24 Mar 2019 18 UTC



T at 850 hPa

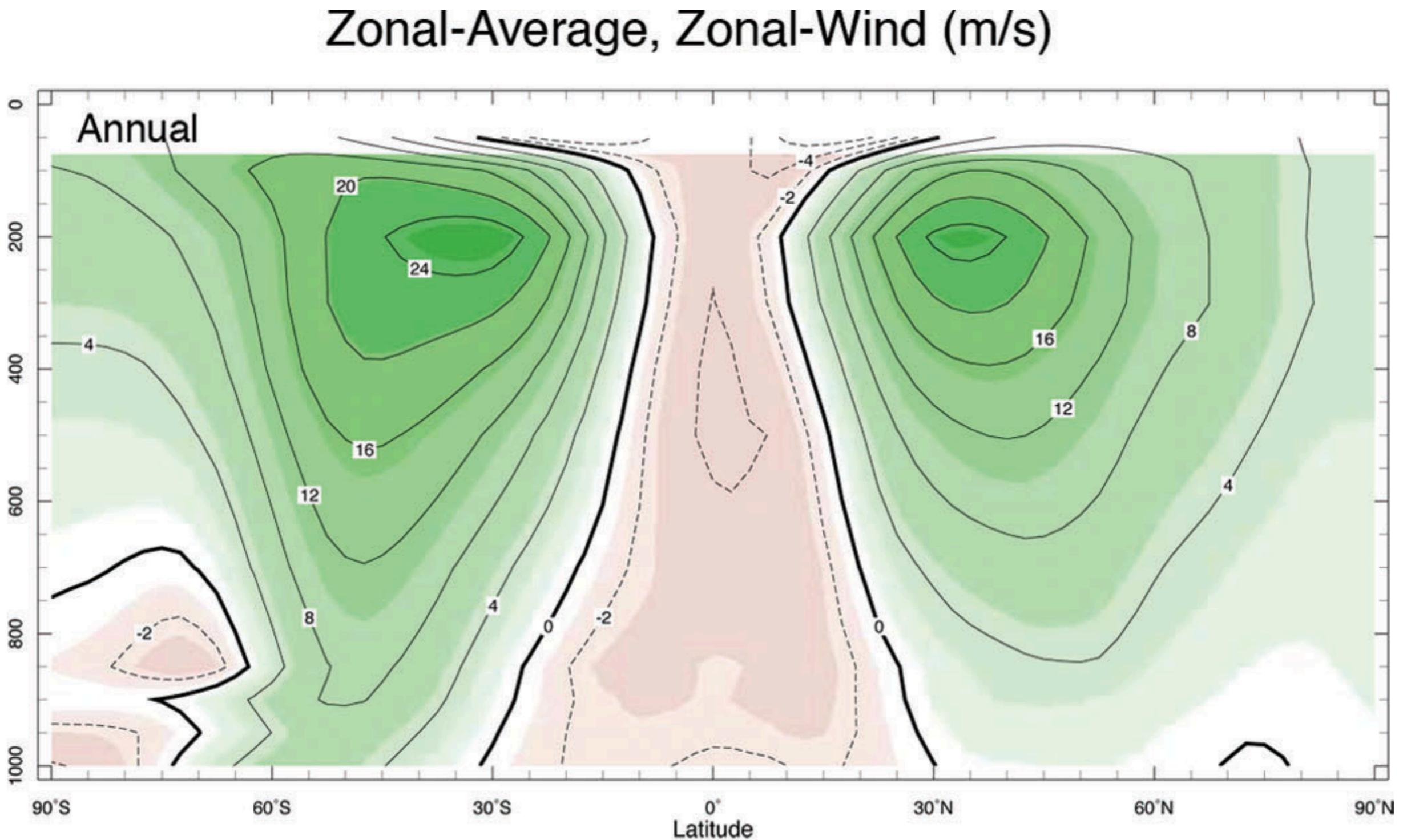
From <http://www.genuineweather.com/?model=CMC-GDPS&zone=ART&type=T850>

5. Wind

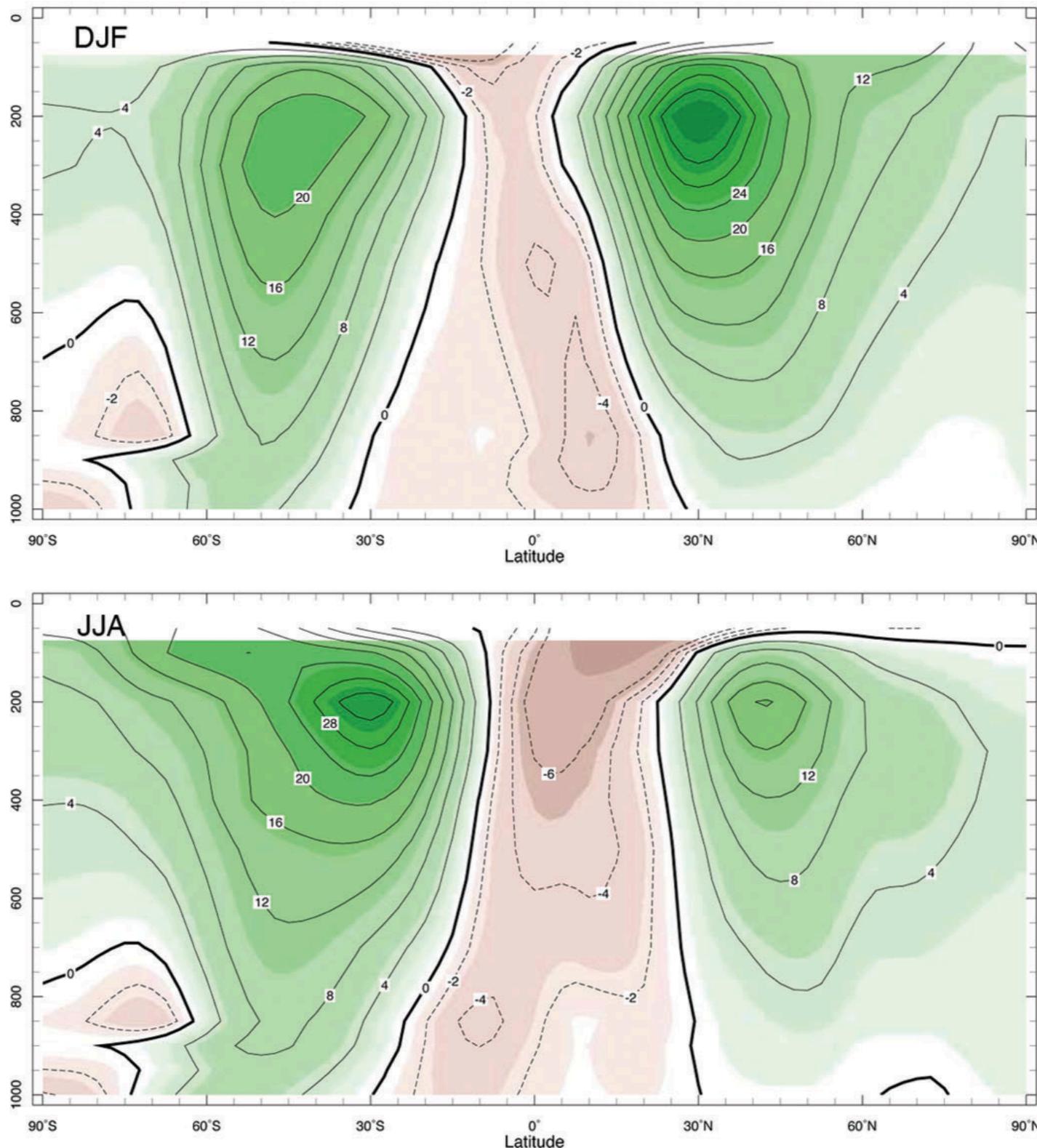
- There is a geopotential height slope from equator to pole
- We can expect that the pressure gradient force exists aloft.
- Wind has three dimensions: $\mathbf{u} = (u, v, w)$

Hard to measure
-

5. Wind - zonal wind (u)



5. Wind - zonal wind (u)

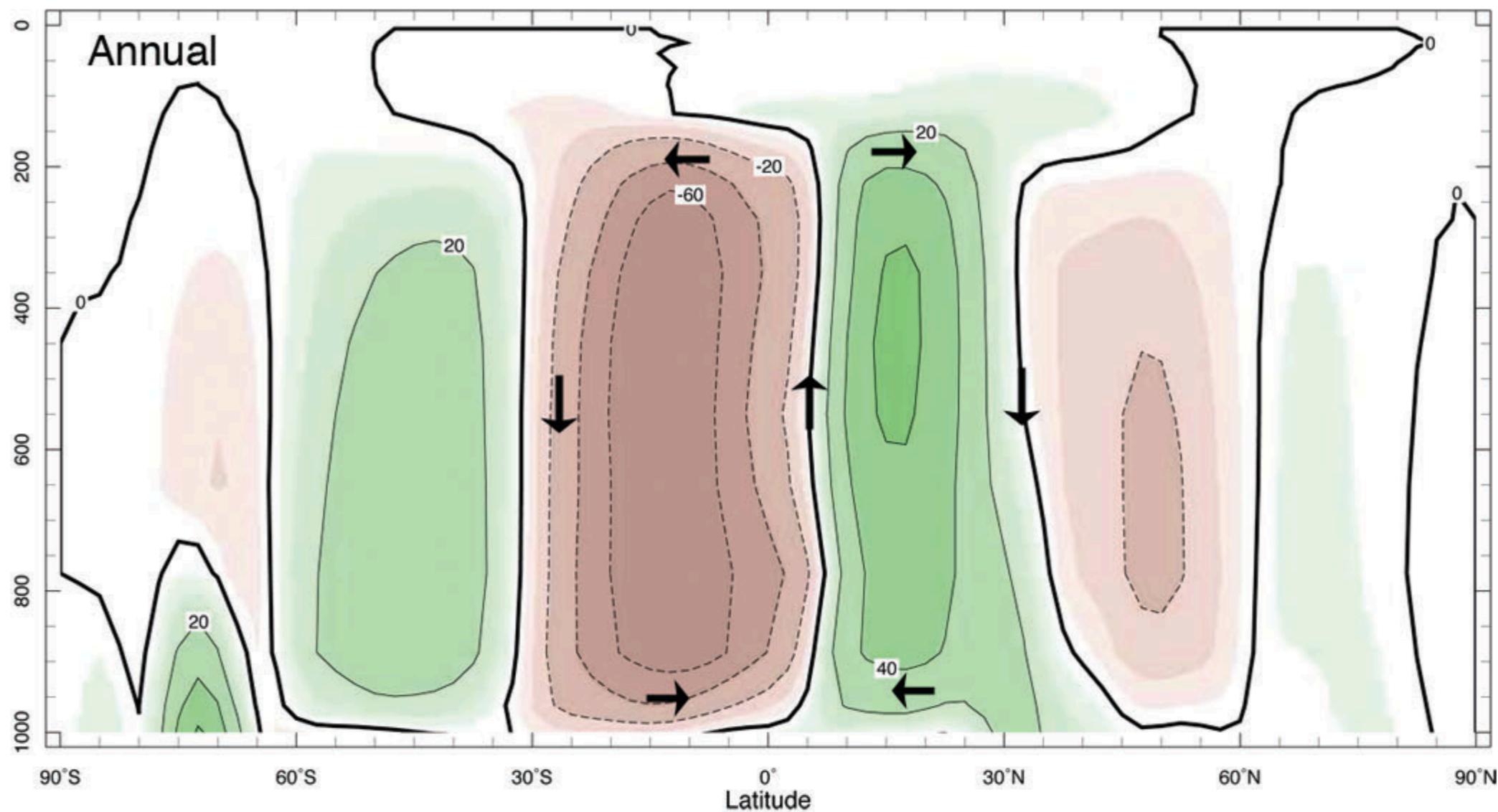


5. Wind - meridional wind (v)

$$v = -\frac{1}{\rho a \cos \phi} \frac{\partial \Psi}{\partial z}$$

$$w = \frac{1}{\rho a^2 \cos \phi} \frac{\partial \Psi}{\partial \phi}$$

Meridional Overturning Circulation (10^9 kg/s)



5. Wind - meridional wind (v)

$$v = -\frac{1}{\rho a \cos \phi} \frac{\partial \Psi}{\partial z}$$

$$w = \frac{1}{\rho a^2 \cos \phi} \frac{\partial \Psi}{\partial \phi}$$

