

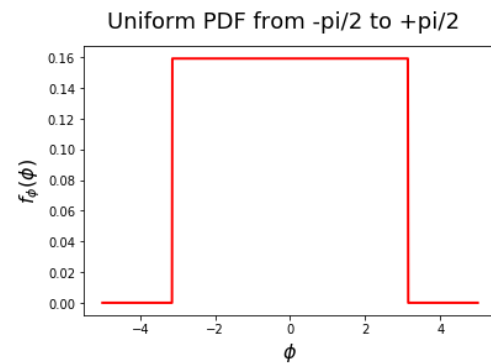
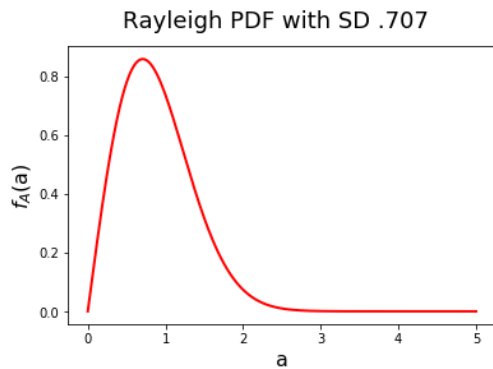
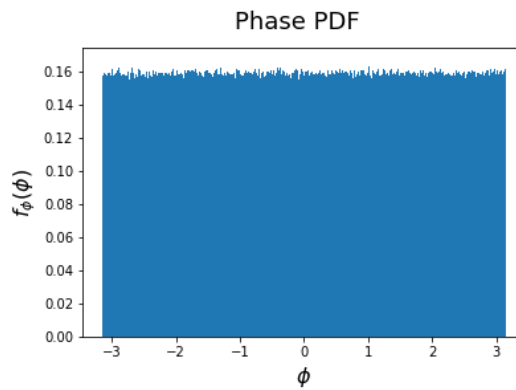
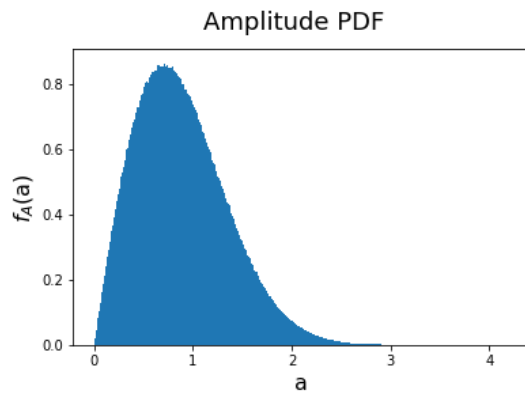
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1. """
2. PYTHON Assignment #0
3. Submitted by: M. Aravind
4. 21104403
5.
6. """
7. #Aim: Generate 1,00,00,000 iid instantiations of the Rayleigh fading channel. Plot
   Histograms of Magnitude and Phase as PDF from the data.
8. # Compare the plots with standard Rayleigh distribution (for magnitude) and Uniform
   distribution (for phase) curves.
9.
10. import numpy as np
11. import numpy.random as nr
12. import matplotlib.pyplot as plt
13.
14. nbins=1000
15. nSamples=10000000
16. #Real and Imaginary Parts of the noise channel model are iid Gaussian random variables
   with mean 0 and variance 1 each.
17. #Hence the resultant is Complex Gaussian distribution with mean=0 and variance=2.We also
   normalise it by dividing with the standard deviation.
18. h=(nr.normal(0,1,nSamples) + 1j*nr.normal(0,1,nSamples))/np.sqrt(2);
19. amp=np.abs(h)
20. phi=np.angle(h)
21.
22. #Amplitude PDF
23. plt.figure(1)
24. plt.hist(amp,nbins,density=True) #Density=true; plot as PDF
25. plt.suptitle("Amplitude PDF",fontsize=18)
26. plt.xlabel("a", fontsize=16)
27. plt.ylabel("$f_A(a)$", fontsize=16)
28.
29. #Phase PDF
30. plt.figure(2)
31. plt.hist(phi,nbins,density=True)
32. plt.suptitle("Phase PDF",fontsize=18)
33. plt.xlabel("$\phi$",fontsize=16)
34. plt.ylabel("$f_\phi(\phi)$",fontsize=16)
35.
36.
37. #Assumptions: PDFs of amplitude and phase of the above data follows Rayleigh and Uniform
   distributions respectively.
38. #To verify:
39.
40. #Rayleigh PDF
41. x=np.linspace(0,5,nbins)
42. a=np.zeros(nbins)
43. for i in range(nbins):
44.     a[i]=(2*x[i]*(np.exp(-x[i]**2)))
45. plt.figure(3)
46. plt.plot(x,a,color="red",linewidth=2)
47. plt.suptitle('Rayleigh PDF with SD .707',fontsize=18)
48. plt.xlabel("a",fontsize=16)
49. plt.ylabel("$f_A(a)$",fontsize=16)
50.
51. #Uniform PDF
52. y=np.linspace(-5,5,nbins)
53. p=np.zeros(nbins)
54. for i in range(nbins):
55.     if (-np.pi<y[i] and y[i]<np.pi):
56.         p[i]=1/(2*np.pi)
57. plt.figure(4)
58. plt.plot(y,p,color="red",linewidth=2)
59. plt.suptitle('Uniform PDF from -pi/2 to +pi/2',fontsize=18)
60. plt.xlabel("$\phi$",fontsize=16)
61. plt.ylabel("$f_\phi(\phi)$",fontsize=16)
62.
63. #Now superimposing Amplitude PDF and Rayleigh PDF
64. plt.figure(5)
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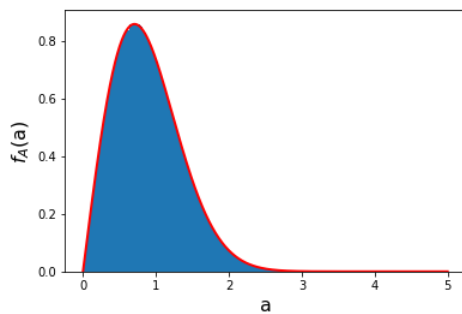
65. plt.hist(amp,nbins,density=True)
66. plt.plot(x,a,color="red",linewidth=2)
67. plt.suptitle('Channel Amplitude PDF superimposed with Rayleigh PDF',fontsize=16)
68. plt.xlabel("a",fontsize=16)
69. plt.ylabel("$f_A(a)$",fontsize=16)
70.
71. #Now superimposing Phase PDF and Uniform PDF
72. plt.figure(6)
73. plt.hist(phi,nbins,density=True)
74. plt.plot(y,p,color="red",linewidth=2)
75. plt.suptitle('Channel Phase PDF superimposed with Uniform PDF',fontsize=18)
76. plt.xlabel("$\phi$",fontsize=16)
77. plt.ylabel("$f_\phi(\phi)$",fontsize=16)
78.
79.

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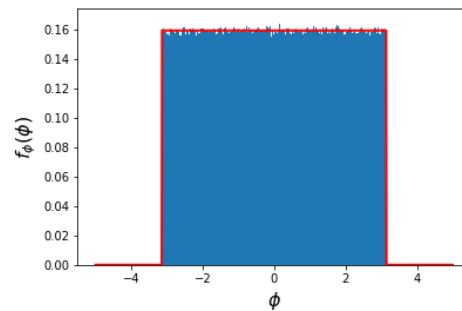
Output:



Channel Amplitude PDF superimposed with Rayleigh PDF



Channel Phase PDF superimposed with Uniform PDF



Observation:

The PDFs of amplitude and phase of the above generated complex baseband channel coefficient 'h' follows Rayleigh and Uniform distributions respectively. This is verified by superimposing them with the PDFs described in the class lectures.

The complex baseband channel coefficient 'h' is a Gaussian random variable with real and imaginary parts as zero mean, independent and identically distributed gaussian random variables. It is seen that the magnitude PDF follows Rayleigh distribution with variance 0.5 and the phase is uniformly distributed in the interval $[-\pi, +\pi]$