

a1_task4

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```
[1]: import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
```

```
[2]: columns={'name': ['Clover', 'Sunny', 'Rose', 'Daisy', 'Strawberry', 'Molly'],
              'race': ['Holstein', 'Ayrshire', 'Holstein', 'Ayrshire', 'Finncattle',
                      ↪ 'Ayrshire'],
              'age': [2.0, 2.0, 5.0, 4.0, 7.0, 8.0],
              'milk/d': [20.0, 10.0, 15.0, 25.0, 35.0, 45.0],
              'character': ['lively', 'kind', 'calm', 'calm', 'calm', 'kind'],
              'music': ['rock', 'rock', 'country', 'classical', 'classical',
                      ↪ 'country']}
table = pd.DataFrame(columns)
table
```

```
[2]:
```

	name	race	age	milk/d	character	music
0	Clover	Holstein	2.0	20.0	lively	rock
1	Sunny	Ayrshire	2.0	10.0	kind	rock
2	Rose	Holstein	5.0	15.0	calm	country
3	Daisy	Ayrshire	4.0	25.0	calm	classical
4	Strawberry	Finncattle	7.0	35.0	calm	classical
5	Molly	Ayrshire	8.0	45.0	kind	country

2.1 a)

```
[3]: # Helper function for minmax scaling
def minmax_scale(x):
    y = np.zeros_like(x)
    for i, x_i in enumerate(x):
        y[i] = (x_i - np.min(x)) / (np.max(x) - np.min(x))
    return y

# Scale the numerical features age and milk/d
```

```
table['age'] = minmax_scale(table['age'].values)
table['milk/d'] = minmax_scale(table['milk/d'].values)
table
```

```
[3]:
```

	name	race	age	milk/d	character	music
0	Clover	Holstein	0.000000	0.285714	lively	rock
1	Sunny	Ayrshire	0.000000	0.000000	kind	rock
2	Rose	Holstein	0.500000	0.142857	calm	country
3	Daisy	Ayrshire	0.333333	0.428571	calm	classical
4	Strawberry	Finncattle	0.833333	0.714286	calm	classical
5	Molly	Ayrshire	1.000000	1.000000	kind	country

```
[4]: # Calculating pairwise Euclidean distances between cows
def euclidean(x, y):
    return np.round(np.sqrt(np.sum((x-y)**2)), 2)

numsim = {} # Dict to store the similarities in
A = table[['age', 'milk/d']].values
cows = list(table.name.values)
n, d = A.shape
print("Pairwise Euclidean distances between cows...")
visited = []
for i in range(n):
    for j in range(n):
        if (j, i) not in visited:
            visited.append((i, j))
            if j != i:
                x = A[i,:].T
                y = A[j,:].T
                print("- ...{} and {} is {}".format(cows[i], cows[j],
↳euclidean(x, y)))

                # Add to the dict so that we can use the calculated distances
↳later...

                numsim[(cows[i], cows[j])] = euclidean(x, y)
```

Pairwise Euclidean distances between cows...

- ...Clover and Sunny is 0.29.
- ...Clover and Rose is 0.52.
- ...Clover and Daisy is 0.36.
- ...Clover and Strawberry is 0.94.
- ...Clover and Molly is 1.23.
- ...Sunny and Rose is 0.52.
- ...Sunny and Daisy is 0.54.
- ...Sunny and Strawberry is 1.1.
- ...Sunny and Molly is 1.41.
- ...Rose and Daisy is 0.33.

- ...Rose and Strawberry is 0.66.
- ...Rose and Molly is 0.99.
- ...Daisy and Strawberry is 0.58.
- ...Daisy and Molly is 0.88.
- ...Strawberry and Molly is 0.33.

2.2 b)

Defining Goodall similarity distance measure

$$d_G = 1 - G = 1 - \frac{\sum_{A_i \text{ shared}} (1 - p_i^2(\text{shared}))}{d}$$

where d is the number of features and $p_i^2(\text{shared})$ is the squared ratio of the pairs' shared feature value in its column (e.g. ratio of Holstein in race column is $2/6$).

```
[5]: data = table.set_index('name')[['race', 'character', 'music']]
      data
```

```
[5]:
```

	race	character	music
name			
Clover	Holstein	lively	rock
Sunny	Ayrshire	kind	rock
Rose	Holstein	calm	country
Daisy	Ayrshire	calm	classical
Strawberry	Finnccattle	calm	classical
Molly	Ayrshire	kind	country

```
[6]: catsim = {} # Dict to store the similarities in
n, d = data.shape
visited = []

print("Pairwise Goodall distances between cows...")

for cow1 in data.index.values:

    # Get the feature values for the cow1
    race1 = data.loc[cow1, 'race']
    char1 = data.loc[cow1, 'character']
    music1 = data.loc[cow1, 'music']

    # Count the ratios of the occurrences
    p_race = data.race.value_counts()[race1] / n
    p_char = data.character.value_counts()[char1] / n
    p_music = data.music.value_counts()[music1] / n

    for cow2 in data.index.values:
```

```

if (cow2, cow1) not in visited:
    visited.append((cow1, cow2))

# Get the feature values for cow2
if cow1 != cow2:
    race2 = data.loc[cow2, 'race']
    char2 = data.loc[cow2, 'character']
    music2 = data.loc[cow2, 'music']
    num = 0

    # If the pair shares some feature value, add 1 - p_i(shared)^2
    # to the numerator sum
    if race1 == race2:
        num += (1 - p_race**2)
    if char1 == char2:
        num += (1 - p_char**2)
    if music1 == music2:
        num += (1 - p_music**2)

    # Do the rest of the calculations needed
    G = num / d
    dist = 1 - G

    # Print the pairwise distance of the pair
    print("- ...{} and {} is {}".format(cow1, cow2, dist))

    # Add to the dict so that we can use the calculated distances
    ↪ later...
    catsim[(cow1, cow2)] = dist

```

Pairwise Goodall distances between cows...

- ...Clover and Sunny is 0.7037037037037037.
- ...Clover and Rose is 0.7037037037037037.
- ...Clover and Daisy is 1.0.
- ...Clover and Strawberry is 1.0.
- ...Clover and Molly is 1.0.
- ...Sunny and Rose is 1.0.
- ...Sunny and Daisy is 0.75.
- ...Sunny and Strawberry is 1.0.
- ...Sunny and Molly is 0.4537037037037037.
- ...Rose and Daisy is 0.75.
- ...Rose and Strawberry is 0.75.
- ...Rose and Molly is 0.7037037037037037.
- ...Daisy and Strawberry is 0.4537037037037037.
- ...Daisy and Molly is 0.75.
- ...Strawberry and Molly is 1.0.

2.3 c)

We stored the pairwise similarities in two dictionaries earlier:

```
[7]: numsim
```

```
[7]: {('Clover', 'Sunny'): 0.29,
      ('Clover', 'Rose'): 0.52,
      ('Clover', 'Daisy'): 0.36,
      ('Clover', 'Strawberry'): 0.94,
      ('Clover', 'Molly'): 1.23,
      ('Sunny', 'Rose'): 0.52,
      ('Sunny', 'Daisy'): 0.54,
      ('Sunny', 'Strawberry'): 1.1,
      ('Sunny', 'Molly'): 1.41,
      ('Rose', 'Daisy'): 0.33,
      ('Rose', 'Strawberry'): 0.66,
      ('Rose', 'Molly'): 0.99,
      ('Daisy', 'Strawberry'): 0.58,
      ('Daisy', 'Molly'): 0.88,
      ('Strawberry', 'Molly'): 0.33}
```

```
[8]: catsim
```

```
[8]: {('Clover', 'Sunny'): 0.7037037037037037,
      ('Clover', 'Rose'): 0.7037037037037037,
      ('Clover', 'Daisy'): 1.0,
      ('Clover', 'Strawberry'): 1.0,
      ('Clover', 'Molly'): 1.0,
      ('Sunny', 'Rose'): 1.0,
      ('Sunny', 'Daisy'): 0.75,
      ('Sunny', 'Strawberry'): 1.0,
      ('Sunny', 'Molly'): 0.4537037037037037,
      ('Rose', 'Daisy'): 0.75,
      ('Rose', 'Strawberry'): 0.75,
      ('Rose', 'Molly'): 0.7037037037037037,
      ('Daisy', 'Strawberry'): 0.4537037037037037,
      ('Daisy', 'Molly'): 0.75,
      ('Strawberry', 'Molly'): 1.0}
```

Using the following equation to get the combined distance measure:

$$Sim(x, y) = \frac{\lambda * L_2(x_{num}, y_{num})}{\sigma_{num}} + \frac{(1 - \lambda) * d_G(x_{cat}, y_{cat})}{\sigma_{cat}}$$

where σ_{num} and σ_{cat} are the standard deviations of the similarity values in the categorical and numerical components, respectively.

A natural choice is to use a value of λ that is equal to the fraction of numerical attributes in the data (Aggarwal sec. 3.2.3).

```
[9]: combsim = {}

lambda_ = 2 / 5
sigma_num = np.std(list(numsim.values()))
sigma_cat = np.std(list(catsim.values()))

print("Pairwise distances with the combined measure between cows...")
for pair in numsim.keys():

    cow1, cow2 = pair
    L2 = numsim[pair]
    dG = catsim[pair]
    sim = ((lambda_ * L2) / sigma_num) + (((1 - lambda_) * dG) / sigma_cat)
    combsim[pair] = sim

    print("- ...{} and {} is {}".format(cow1, cow2, sim))
```

Pairwise distances with the combined measure between cows...

```
- ...Clover and Sunny is 2.6095240334555116.
- ...Clover and Rose is 2.876530024375005.
- ...Clover and Daisy is 3.647782223512226.
- ...Clover and Strawberry is 4.3211016788744265.
- ...Clover and Molly is 4.657761406555527.
- ...Sunny and Rose is 3.833525521543178.
- ...Sunny and Daisy is 3.049278483061401.
- ...Sunny and Strawberry is 4.506844976905379.
- ...Sunny and Molly is 3.1022621689365284.
- ...Rose and Daisy is 2.8054904043957762.
- ...Rose and Strawberry is 3.188585956584615.
- ...Rose and Molly is 3.4221509623409263.
- ...Daisy and Strawberry is 2.138718810400966.
- ...Daisy and Molly is 3.4439829913771733.
- ...Strawberry and Molly is 3.6129553551314224.
```

2.4 d)

2.4.1 i)

```
[59]: # bins
b = 12

num = list(numsim.values())
cat = list(catsim.values())
comb = list(combsim.values())
```

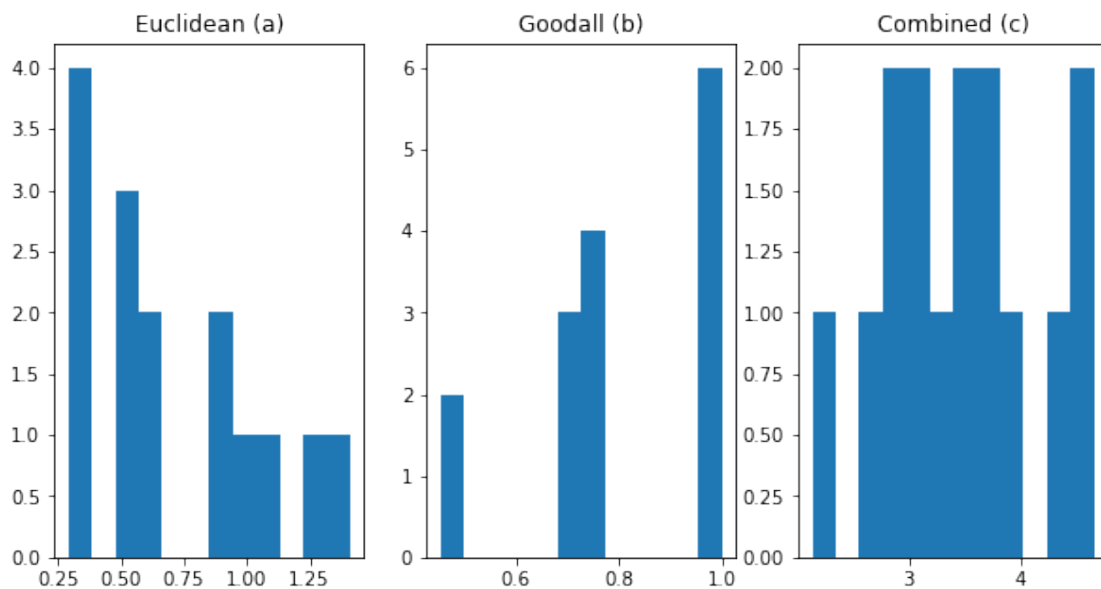
```
fig, ax = plt.subplots(1, 3, figsize=(10,5))

ax[0].hist(num, bins=b)
ax[0].set_title('Euclidean (a)')

ax[1].hist(cat, bins=b)
ax[1].set_title('Goodall (b)')

ax[2].hist(comb, bins=b)
ax[2].set_title('Combined (c)')
```

[59]: Text(0.5, 1.0, 'Combined (c)')



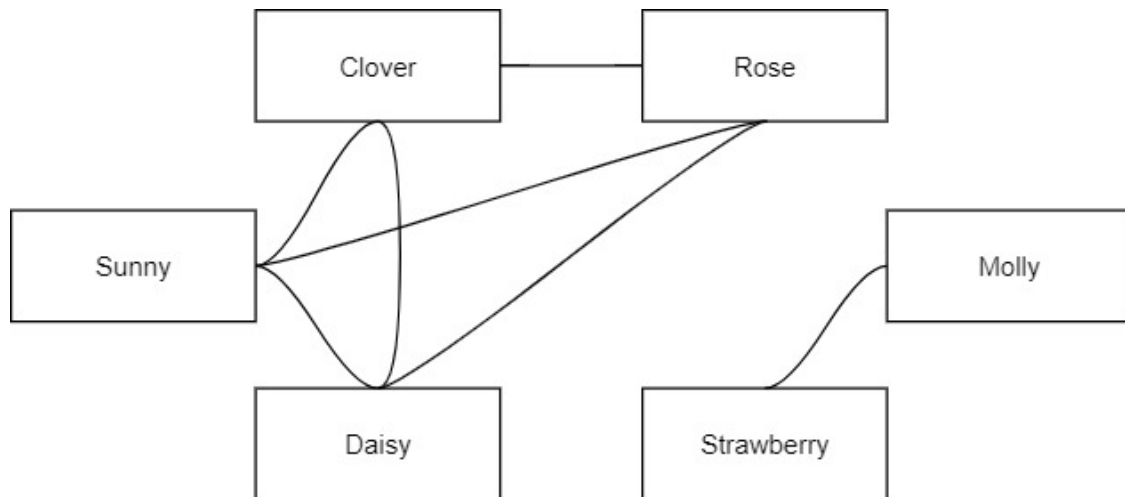
Based on this, the best measure to cluster the cows would be the method we used in part b. There we calculated pairwise Goodall distances for categorical variables. When using 12 bins, it is clear to see three separate clusters in the above middle plot.

2.4.2 ii)

a)

```
[3]: from IPython.display import Image
      Image(filename='clustering_a.jpg')
```

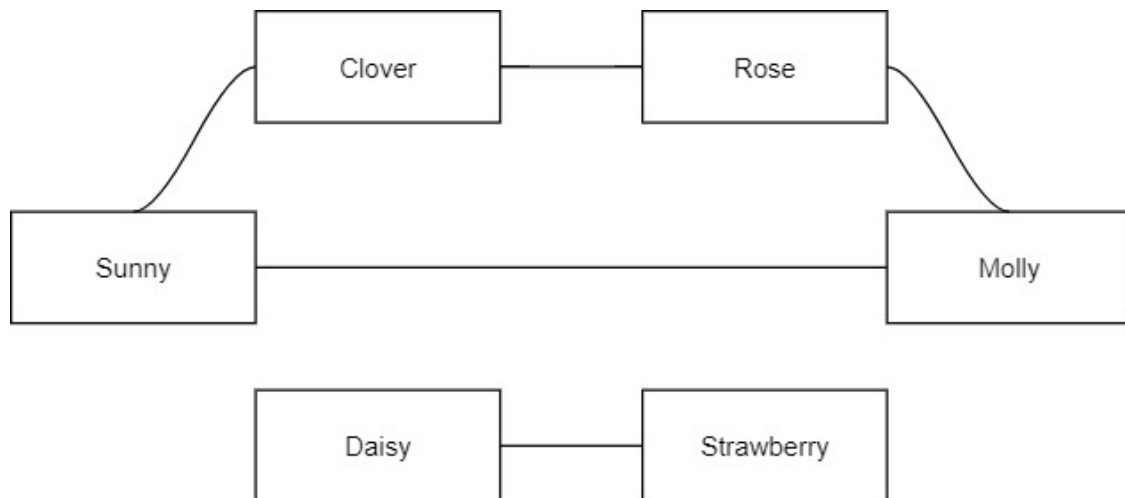
[3]:



b)

```
[4]: from IPython.display import Image
      Image(filename='clustering_b.jpg')
```

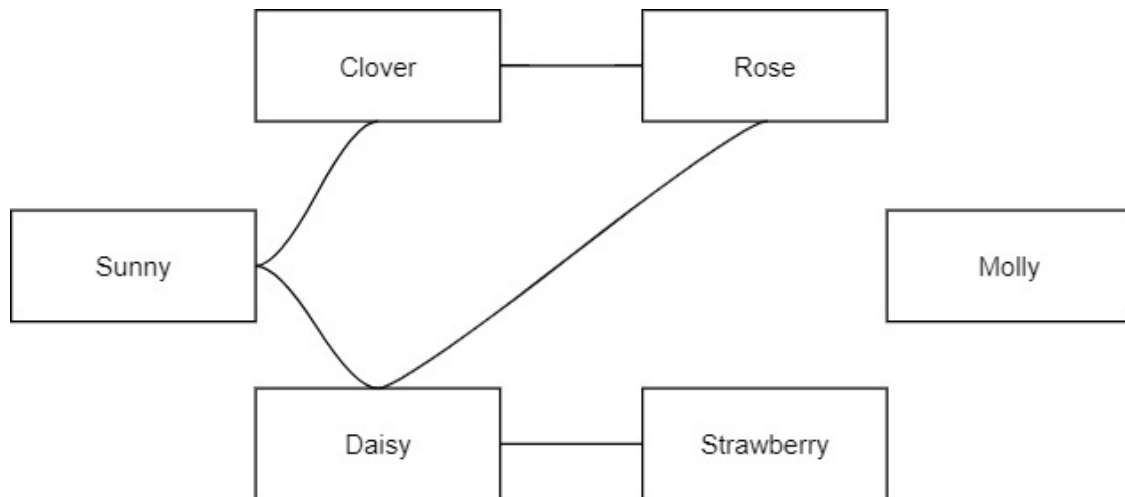
[4]:



c)

```
[5]: from IPython.display import Image
      Image(filename='clustering_c.jpg')
```

[5]:



Answer: Measure (a) produced the best clustering with this graph clustering method. This is because the most amount of edges/connections were preserved while achieving the two connected components via the longest distance edge removal procedure. In other words, the two clusters seem the clearest in measure a's edge-node graph.

[]: