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No.

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Aljabar Linear

1.
$$A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 2 & 5 \end{bmatrix}$$

a. matriks eselon baris

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 2 & 5 \end{bmatrix} \quad B2. \frac{1}{4} \begin{bmatrix} 1 & 2 & 3 \\ 1 & \frac{5}{4} & \frac{3}{2} \\ 7 & 2 & 5 \end{bmatrix}$$

$$B3. \frac{1}{7} \begin{bmatrix} 1 & 2 & 3 \\ 1 & \frac{5}{4} & \frac{3}{2} \\ 1 & \frac{2}{7} & \frac{5}{7} \end{bmatrix}$$

$$B2 - B1 \begin{bmatrix} 1 & 2 & 3 \\ 0 & -\frac{3}{4} & -\frac{3}{2} \\ 1 & \frac{2}{7} & \frac{5}{7} \end{bmatrix}$$

$$B3 - B1 \begin{bmatrix} 1 & 2 & 3 \\ 0 & -\frac{3}{4} & -\frac{3}{2} \\ 0 & -\frac{12}{7} & -\frac{16}{7} \end{bmatrix}$$

$$B2. \frac{-4}{3} \begin{bmatrix} 1 & 2 & 3 \\ 0 & 1 & 2 \\ 0 & -\frac{12}{7} & -\frac{16}{7} \end{bmatrix}$$

$$B3. \frac{-7}{12} \begin{bmatrix} 1 & 2 & 3 \\ 0 & 1 & 2 \\ 0 & 1 & \frac{4}{3} \end{bmatrix}$$

$$B3 - B2 \begin{bmatrix} 1 & 2 & 3 \\ 0 & 1 & 2 \\ 0 & 0 & -\frac{2}{3} \end{bmatrix}$$

$$B_3 - \frac{3}{2} \begin{bmatrix} 1 & 2 & 3 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{bmatrix} //$$

b. Matriks person teredousi

$$\begin{bmatrix} 1 & 2 & 3 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{bmatrix} \quad B_2 - 2 \cdot B_3 \quad \begin{bmatrix} 1 & 2 & 3 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$B_1 - 3 \cdot B_3 \quad \begin{bmatrix} 1 & 2 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$B_1 - 2 \cdot B_2 \quad \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} //$$

c. Rangkai matriks

$$\text{Rangkai matriks} = 3 //$$

karena matriks identitas 3x3 terbentuk

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

2. Nilai determinan dari matriks = $\begin{bmatrix} 1 & 6 & 7 \\ 2 & 5 & 2 \\ 3 & 4 & 5 \end{bmatrix}$

$$\det(A) = |A| = \begin{vmatrix} a & b & c \\ d & e & f \\ g & h & i \end{vmatrix} = \begin{vmatrix} a & b & c \\ d & e & f \\ g & h & i \end{vmatrix}$$

$$|A| = (a \cdot e \cdot i) + (b \cdot f \cdot g) + (c \cdot d \cdot h) - (c \cdot e \cdot g) - (a \cdot f \cdot h) - (b \cdot d \cdot i)$$

$$A = \begin{bmatrix} 1 & 6 & 7 \\ 2 & 5 & 2 \\ 3 & 4 & 5 \end{bmatrix}$$

$$\begin{aligned} |A| &= (1 \cdot 5 \cdot 5) + (6 \cdot 2 \cdot 3) + (7 \cdot 2 \cdot 4) - (7 \cdot 5 \cdot 3) - \\ &\quad (1 \cdot 2 \cdot 4) - (6 \cdot 2 \cdot 5) \\ &= 25 + 36 + 56 - 105 - 8 - 60 \\ &= -56 \end{aligned}$$

3. $A = \begin{bmatrix} 1 & 2 & 3 \\ 6 & 5 & 4 \\ 7 & 2 & 5 \end{bmatrix}$

a. minor matriks A

$$M_{11} = \begin{bmatrix} 5 & 4 \\ 2 & 5 \end{bmatrix} = 5 \cdot 5 - 4 \cdot 2 = 17$$

$$M_{12} = \begin{bmatrix} 6 & 4 \\ 7 & 5 \end{bmatrix} = 6 \cdot 5 - 4 \cdot 7 = 2$$

$$M_{13} = \begin{bmatrix} 6 & 5 \\ 7 & 2 \end{bmatrix} = 6 \cdot 2 - 5 \cdot 7 = -23$$

$$M_{21} = \begin{bmatrix} 2 & 3 \\ 2 & 5 \end{bmatrix} = 2 \cdot 5 - 3 \cdot 2 = 4$$

$$M_{22} = \begin{bmatrix} 1 & 3 \\ 7 & 5 \end{bmatrix} = 1 \cdot 5 - 3 \cdot 7 = -16$$

$$M_{23} = \begin{bmatrix} 1 & 2 \\ 7 & 2 \end{bmatrix} = 1 \cdot 2 - 2 \cdot 7 = -12$$

$$M_{31} = \begin{bmatrix} 2 & 3 \\ 5 & 4 \end{bmatrix} = 2 \cdot 4 - 3 \cdot 5 = -7$$

$$M_{32} = \begin{bmatrix} 1 & 3 \\ 6 & 4 \end{bmatrix} = 1 \cdot 4 - 3 \cdot 6 = -14$$

$$M_{33} = \begin{bmatrix} 1 & 2 \\ 6 & 5 \end{bmatrix} = 1 \cdot 5 - 2 \cdot 6 = -7$$

$$\text{Minor dari matriks } A = \begin{bmatrix} 17 & -2 & -23 \\ 4 & -16 & -12 \\ -7 & -14 & -7 \end{bmatrix} //$$

b. Kofaktor dari matriks A

$$\begin{bmatrix} + & - & + \\ - & + & - \\ + & - & + \end{bmatrix} \begin{bmatrix} 17 & -2 & -23 \\ 4 & -16 & -12 \\ -7 & 14 & -7 \end{bmatrix} //$$

c. Ekspansi Baris ke-3

$$1 \times a_{31} \times m_{31} = 1 \times 7 \times -7 = -49$$

$$-1 \times a_{32} \times m_{32} = -1 \times 2 \times -14 = 28$$

$$1 \times a_{33} \times m_{33} = 1 \times 5 \times -7 = -35$$

$$\det(A) = -49 + 28 + (-35) = -56 //$$

Ekspansi Kolom ke-3

$$1 \times a_{13} \times m_{13} = 1 \times 3 \times -23 = -69$$

$$-1 \times a_{23} \times m_{23} = -1 \times 4 \times -12 = 48$$

$$1 \times a_{33} \times m_{33} = 1 \times 5 \times -7 = -35$$

$$\det(A) = -69 + 48 + (-35) = -56 //$$

$$4. C = \begin{bmatrix} 1 & 2 \\ 2 & 5 \end{bmatrix}$$

$$a. \text{ Adjoin matrik } C = \begin{bmatrix} a & -b \\ -c & a \end{bmatrix}$$

$$= \begin{bmatrix} 5 & -2 \\ -2 & 1 \end{bmatrix} //$$

$$b. \text{ Invers matrik } C$$

$$= \left[\begin{array}{cc|cc} 1 & 2 & 1 & 0 \\ 2 & 5 & 0 & 1 \end{array} \right]$$

$$= \left[\begin{array}{cc|cc} 1 & 2 & 1 & 0 \\ 0 & 1 & -2 & 1 \end{array} \right]$$

$$= \left[\begin{array}{cc|cc} 1 & 0 & 5 & -2 \\ 0 & 1 & -2 & 1 \end{array} \right]$$

$$= \begin{bmatrix} 5 & -2 \\ -2 & 1 \end{bmatrix} //$$

$$5. \quad 2x - 5y + 3z = -10$$

$$3x + 4y + 7z = -11$$

$$5x + 3y + 7z = -8$$

$$\text{Nilai dari } x + y + z = 0$$

Eliminasi Persamaan 2 dan 1

$$3x + 4y + 7z = -11 \quad | \times 2 \quad 6x + 8y + 14z = -22$$

$$2x - 5y + 3z = -10 \quad | \times 3 \quad 6x - 15y + 9z = -30$$

$$\text{Persamaan 4} = 23y + 5z = 8$$

Eliminasi Persamaan 1 dan 3

$$\begin{array}{rcl} 2x - 5y + 3z = -10 & | \times 5 & 10x - 25y + 15z = -50 \\ 5x + 3y + 7z = -8 & | \times 2 & 10x + 6y + 14z = -16 \\ \hline \text{Persamaan 5} & & -31y + 2z = -34 \end{array}$$

Eliminasi Persamaan 4 dan 5

$$\begin{array}{rcl} 23y + 5z = 8 & | \times 1 & 23y + 5z = 8 \\ -31y + z = -34 & | \times 5 & -155y + 5z = -170 \\ \hline & & 178y = 178 \\ & & y = 1 // \end{array}$$

Substitusi y ke Persamaan 4

$$\begin{aligned} 23y + 5z &= 8 \\ 23(1) + 5z &= 8 \\ 23 + 5z &= 8 \\ 5z &= 8 - 23 \\ 5z &= -15 \\ z &= \frac{-15}{5} \\ z &= -3 // \end{aligned}$$

Substitusikan y dan z ke Persamaan 1

$$\begin{aligned} 2x - 5y + 3z &= -10 \\ 2x - 5(1) + 3(-3) &= -10 \\ 2x - 5 + (-9) &= -10 \\ 2x &= -10 + 5 + 9 \\ 2x &= 4 \\ x &= 2 // \end{aligned}$$

$$\text{Nilai } x + y + z = 2 + 1 + (-3) = 0 //$$

6. Buktikan fungsi vektor merupakan transformasi linear

$$f: \mathbb{R}^2 \rightarrow \mathbb{R}^3 \text{ dengan } f \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 2x + 3y \\ x^2 \\ x + 2y \end{bmatrix}$$

Misal $u, v \in \mathbb{R}^2$

$$u = (u_1, u_2)$$

$$v = (v_1, v_2)$$

$k = \text{skalar}$

Syarat 1

$$f(u+v) = f(u) + f(v)$$

Ruang kiri

$$\begin{aligned} f(u+v) &= f\left(\begin{bmatrix} u_1 \\ u_2 \end{bmatrix} + \begin{bmatrix} v_1 \\ v_2 \end{bmatrix}\right) = f\left(\begin{bmatrix} u_1 + v_1 \\ u_2 + v_2 \end{bmatrix}\right) \\ &= f\left(\begin{bmatrix} u_1 + v_1 \\ u_2 + v_2 \end{bmatrix}\right) \end{aligned}$$

Masukkan ke persamaan

$$f \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 2x + 3y \\ x^2 \\ x + 2y \end{bmatrix} = \begin{bmatrix} 2(u_1 + v_1) + 3(u_2 + v_2) \\ (u_1 + v_1) \cdot (u_1 + v_1) \\ (u_1 + v_1) + 2(u_2 + v_2) \end{bmatrix}$$

Ruang kanan

$$f(u) + f(v) = \begin{bmatrix} 2u_1 + 3u_2 \\ u_1 \cdot u_1 \\ u_1 + 2u_2 \end{bmatrix} + \begin{bmatrix} 2v_1 + 3v_2 \\ v_1 \cdot v_1 \\ v_1 + 2v_2 \end{bmatrix}$$

$$= \begin{bmatrix} 2u_1 + 3u_2 + 2v_1 + 3v_2 \\ u_1 \cdot u_1 + v_1 \cdot v_1 \\ u_1 + 2u_2 + v_1 + 2v_2 \end{bmatrix}$$

$$= \begin{bmatrix} 2(u_1 + v_1) + 3(u_2 + v_2) \\ (u_1 + v_1) \cdot (u_1 + v_1) \\ (u_1 + v_1) + 2(u_2 + v_2) \end{bmatrix}$$

karena ruas kiri dan kanan sama maka termasuk transformasi linear

Syarat 2

$$f(ku) = k \cdot f(u)$$

ruas kiri

$$f(ku) = f\left(k \begin{bmatrix} u_1 \\ u_2 \end{bmatrix}\right) = f \begin{bmatrix} k \cdot u_1 \\ k \cdot u_2 \end{bmatrix}$$

Masukkan ke persamaan

$$f \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 2x+3y \\ x^2 \\ x+2y \end{bmatrix} = \begin{bmatrix} 2(k \cdot u_1) + 3(k \cdot u_2) \\ (k \cdot u_1)(k \cdot u_1) \\ k \cdot u_1 + 2(k \cdot u_2) \end{bmatrix}$$

ruas kanan

$$\begin{aligned} k \cdot f(u) &= k \cdot \begin{bmatrix} 2x+3y \\ x^2 \\ x+2y \end{bmatrix} = \begin{bmatrix} 2u_1+3u_2 \\ u_1 \cdot u_1 \\ u_1+2u_2 \end{bmatrix} \\ &= \begin{bmatrix} 2(k \cdot u_1) + 3 \cdot (k \cdot u_2) \\ (k \cdot u_1)(k \cdot u_1) \\ k \cdot u_1 + 2(k \cdot u_2) \end{bmatrix} \end{aligned}$$

karena ruas kiri dan kanan sama maka termasuk transformasi linear.



UNIVERSITAS PAMULANG
KARTU UJIAN AKHIR SEMESTER GANJIL 2021/2022
NOMOR UJIAN : 830843514684

FAKULTAS / PRODI : TEKNIK / TEKNIK INFORMATIKA S1

NAMA MAHASISWA : ANDRI FIRMAN SAPUTRA

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SHIFT : REGULER A

No	Hari/ Tanggal	Waktu	Ruang	Kelas	Mata Kuliah	Paraf
1	-			03TPLP016	STRUKTUR DATA	1
2	-			03TPLP016	MATEMATIKA DISKRIT	2
3	-			03TPLP016	ALJABAR LINIER DAN MATRIKS	3
4	-			03TPLP016	STATISTIK DASAR	4
5	-			03TPLP016	GRAPH TERAPAN	5
6	-			03TPLP016	PRAKTIKUM FISIKA II	6
7	-			03TPLP016	BAHASA INGGRIS III	7
8	-			03TPLP016	JARINGAN KOMPUTER	8
9	-			03TPLP016	SISTEM BERKAS	9

Peraturan dan Tata Tertib Peserta Ujian

1. Peserta ujian harus berpakaian rapi, sopan dan memakai jaket Almamater
2. Peserta ujian sudah berada di ruangan sepuluh menit sebelum ujian dimulai
3. Peserta ujian yang terlambat diperkenankan mengikuti ujian setelah mendapat ijin, tanpa perpanjangan waktu
4. Peserta ujian hanya diperkenankan membawa alat-alat yang ditentukan oleh panitia ujian
5. Peserta ujian dilarang membantu teman, mencontoh dari teman dan tindakan-tindakan lainnya yang mengganggu peserta ujian lain
6. Peserta ujian yang melanggar tata tertib ujian dikenakan sanksi akademik



Tangerang Selatan, 1 Januari 2022
Ketua Panitia Ujian

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DATA PEMBAYARAN SEMESTER GANJIL 2021/2022

FAKULTAS / PRODI : TEKNIK / TEKNIK INFORMATIKA S1

NAMA MAHASISWA : ANDRI FIRMAN SAPUTRA

NIM : 201011402125

SHIFT : REGULER A

DATA PEMBAYARAN TAGIHAN UANG KULIAH

NO	NOMOR TAGIHAN	NO URUT	PEMBAYARAN	JML BAYAR	STATUS BAYAR	TGL BAYAR	CHANNEL	TEMPAT BAYAR
1	2110119141902201	1	REGISTRASI	400000	LUNAS	2021-08-13 13:24:24.306000	KASIR	BPR
2	2110119141902301	2	ANGSURAN KE-2	200000	LUNAS	2021-08-13 13:24:25.285000	KASIR	BPR
3	2110119141902401	3	ANGSURAN KE-3	200000	LUNAS	2021-08-13 13:24:26.287000	KASIR	BPR
4	2110119141900501	4	UTS	250000	LUNAS	2021-08-13 13:24:27.790000	KASIR	BPR
5	2110119141902501	5	ANGSURAN KE-4	200000	LUNAS	2021-12-15 13:21:56.721000	KASIR	BPR
6	2110119141902601	6	ANGSURAN KE-5	200000	LUNAS	2021-12-15 13:21:57.174000	KASIR	BPR
7	2110119141902701	7	ANGSURAN KE-6	200000	LUNAS	2021-12-15 13:21:57.487000	KASIR	BPR
8	2110119141900401	8	PRAKTEK	100000	LUNAS	2021-12-15 13:21:57.924000	KASIR	BPR
9	2110119141900601	9	UAS	250000	LUNAS	2021-12-15 13:21:58.409000	KASIR	BPR

DATA PEMBAYARAN TAGIHAN LAINNYA

NO	NOMOR TAGIHAN	NO URUT	PEMBAYARAN	JML BAYAR	STATUS BAYAR	TGL BAYAR	CHANNEL	TEMPAT BAYAR
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