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Kalkulus Pertemuan 10

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No

Date

1. Dik: $f(x) = \sqrt{x}$
 $g(x) = x + 1$

a. $f(x) \circ g(x)$
 $= (f \circ g)(x)$
 $= (f(g(x)))$
 $= \sqrt{x+1}$

b. $g(x) \circ f(x)$
 $= (g \circ f)(x)$
 $= (g(f(x)))$
 $= \sqrt{x} + 1$

c. $f(x) \circ f(x)$
 $= (f \circ f)(x)$
 $= (f(f(x)))$
 $= \sqrt{\sqrt{x}}$
 $= \sqrt[4]{x}$

d. $g(x) \circ g(x)$
 $= (g \circ g)(x)$
 $= (g(g(x)))$
 $= (x+1) + 1$
 $= x + 2$

2. Dia: $f(x) = x^2 + 2x + 5$
 $g(x) = 3x$

a. $f(x) \circ g(x)$
 $= (f \circ g)(x)$
 $= (f(g(x)))$
 $= (3x)^2 + 2(3x) + 5$
 $= 9x^2 + 6x + 5$

b. $g(x) \circ f(x)$
 $= (g \circ f)(x)$
 $= (g(f(x)))$
 $= 3(x^2 + 2x + 5)$
 $= 3x^2 + 6x + 15$

c. $f(x) + g(x)$
 $= (f+g)(x)$
 $= (x^2 + 2x + 5) + (3x)$
 $= x^2 + 2x + 3x + 5$
 $= x^2 + 5x + 5$

d. $g(x) - f(x)$
 $= (g-f)(x)$
 $= (3x) - (x^2 + 2x + 5)$
 $= 3x - x^2 - 2x - 5$
 $= -x^2 + x - 5$

3. Dik: $f(x) = x^2 + 1$

$$g(x) = 2x - 3$$

Dit: $(f \circ g)(x)$

$$= f(x) \circ g(x)$$

$$= x^2 + 1 \circ 2x - 3$$

$$= (2x - 3)^2 + 1$$

$$= 4x^2 - 9 + 1$$

$$= 4x^2 - 8$$

4. Dik: $f(x) = 3x - 1$

$$g(x) = x^2 + 2x + 5$$

Dit: $(f \circ g)(1)$ dan $(g \circ f)(2)$

$$= (f \circ g)(1) = 3(x^2 + 2x + 5)$$

$$= 3(1^2 + 2(1) + 5)$$

$$= 3(1 + 2 + 5)$$

$$= 3(8)$$

$$= 24$$

$$= (g \circ f)(2) = x^2 + 2x + 5 \circ 3x - 1$$

$$= (3(2) - 1)^2 + (2(3(2) - 1) + 5)$$

$$= (5)^2 + 2(5) + 5$$

$$= 25 + 10 + 5$$

$$= 40$$

5. Dik: $f(x) = 2x - 3$
 $g(x) = x^2 + 2x + 3$
dit: $(f \circ g)(a) = 33$, tentukan nilai dari S_a

$$\begin{aligned}(f \circ g)(x) &= 2(x^2 + 2x + 3) - 3 \\ &= 2x^2 + 4x + 6 - 3 \\ &= 2x^2 + 4x + 3\end{aligned}$$

$$33 = 2a^2 + 4a + 3$$

$$2a^2 + 4a - 30 = 0$$

$$a^2 + 2a - 15 = 0$$

$$(a + 5)(a - 3) = 0$$

$$a = -5 \text{ atau } a = 3$$

$$S_a = S(-5) = -25 \quad \text{atau} \quad S_a = S(3) = 15$$