## 1 Product 1

$$\begin{split} \varphi_1(0) &= \max \left\{ \begin{array}{l} 0.0 \\ 0.2489 \end{array} \right\} = 0.2489, \quad x_1^0 = 0 \\ \varphi_1(1) &= \max \left\{ \begin{array}{l} 0.0 \\ 0.2489 \\ 1.9824 \end{array} \right\} = 1.9824, \quad x_1^0 = 2 \\ \varphi_1(2) &= \max \left\{ \begin{array}{l} 0.0 \\ 0.2489 \\ 1.9824 \\ 3.7371 \end{array} \right\} = 3.7371, \quad x_1^0 = 3 \\ \varphi_1(3) &= \max \left\{ \begin{array}{l} 0.0 \\ 0.2489 \\ 1.9824 \\ 3.7371 \\ 4.6125 \end{array} \right\} = 4.6125, \quad x_1^0 = 4 \\ 3.7371 \\ 4.6125 \end{array} \\ \varphi_1(5) &= \max \left\{ \begin{array}{l} 0.0 \\ 0.2489 \\ 1.9824 \\ 3.7371 \\ 4.6125 \\ 4.9065 \end{array} \right\} = 4.9065, \quad x_1^0 = 5 \\ \varphi_1(6) &= \max \left\{ \begin{array}{l} 0.0 \\ 0.2489 \\ 1.9824 \\ 3.7371 \\ 4.6125 \\ 4.9065 \\ 4.9814 \end{array} \right\} = 4.9814, \quad x_1^0 = 6 \\ \varphi_1(7) &= \max \left\{ \begin{array}{l} 0.0 \\ 0.2489 \\ 1.9824 \\ 3.7371 \\ 4.6125 \\ 4.9065 \\ 4.9814 \end{array} \right\} = 4.9969, \quad x_1^0 = 7 \\ 4.9969 \end{array}$$

$$\varphi_1(8) = \max \left\{ \begin{array}{l} 0.0 \\ 0.2489 \\ 1.9824 \\ 3.7371 \\ 4.6125 \\ 4.9065 \\ 4.9814 \\ 4.9969 \\ 4.9995 \end{array} \right\} = 4.9995, \quad x_1^0 = 8$$

$$\varphi_1(9) = \max \left\{ \begin{array}{l} 0.0 \\ 0.2489 \\ 1.9824 \\ 3.7371 \\ 4.6125 \\ 4.9065 \\ 4.9814 \\ 4.9969 \\ 4.9995 \\ 4.9999 \end{array} \right\} = 4.9999, \quad x_1^0 = 9$$

$$\varphi_1(10) = \max \left\{ \begin{array}{l} 0.0 \\ 0.2489 \\ 1.9824 \\ 3.7371 \\ 4.6125 \\ 4.9065 \\ 4.9814 \\ 4.9969 \\ 4.9995 \\ 4.9999 \\ 5.0 \end{array} \right\} = 5.0, \quad x_1^0 = 10$$

$$\varphi_1(11) = \max \left\{ \begin{array}{l} 0.0 \\ 0.2489 \\ 1.9824 \\ 3.7371 \\ 4.6125 \\ 4.9065 \\ 4.9814 \\ 4.9969 \\ 4.9999 \\ 5.0 \end{array} \right\} = 5.0, \quad x_1^0 = 10$$

$$\varphi_1(11) = \max \left\{ \begin{array}{l} 0.0 \\ 0.2489 \\ 1.9824 \\ 3.7371 \\ 4.6125 \\ 4.9065 \\ 4.9814 \\ 4.9969 \\ 4.9999 \\ 5.0 \\ 5.0 \\ 5.0 \end{array} \right\} = 5.0, \quad x_1^0 = 10$$

$$\varphi_{1}(12) = \max \left\{ \begin{array}{c} 0.0 \\ 0.2489 \\ 1.9824 \\ 3.7371 \\ 4.6125 \\ 4.9065 \\ 4.9814 \\ 4.9969 \\ 4.9995 \\ 4.9999 \\ 5.0$$

$$\varphi_1(15) = \max \left\{ \begin{array}{l} 0.0 \\ 0.2489 \\ 1.9824 \\ 3.7371 \\ 4.6125 \\ 4.9065 \\ 4.9814 \\ 4.9969 \\ 4.9995 \\ 5.0 \\ 5.$$

$$\varphi_1(17) = \max \left\{ \begin{array}{l} 0.0 \\ 0.2489 \\ 1.9824 \\ 3.7371 \\ 4.6125 \\ 4.9065 \\ 4.9814 \\ 4.9999 \\ 4.9999 \\ 5.0 \\ 5$$

$$\varphi_1(19) = \max \left\{ \begin{array}{l} 0.0 \\ 0.2489 \\ 1.9824 \\ 3.7371 \\ 4.6125 \\ 4.9065 \\ 4.9814 \\ 4.9969 \\ 4.9999 \\ 5.0 \\ 5.$$

```
0.0
0.2489
1.9824
3.7371
4.6125
                          4.9065
4.9814
4.9969
4.9995
                          4.9999
                             5.0
5.0
                                        = 5.0, \quad x_1^0 = 10
\varphi_1(21) = \max \langle
                             5.0
                             5.0
5.0
                             5.0
                             5.0
                             5.0
5.0
                             5.0
                             5.0
                             5.0
                             0.0
                          0.2489
                          1.9824
                          3.7371
                          4.6125
                          4.9065
                          4.9814
                          4.9969
4.9995
4.9999
                             5.0
                             5.0
5.0
\varphi_1(22) = \max
                                       = 5.0, \quad x_1^0 = 10
                             5.0
                             5.0
                             5.0
5.0
5.0
                             5.0
                             5.0
                             5.0
                             5.0
                             5.0
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$$\varphi_1(23) = \max \left\{ \begin{array}{c} 0.0 \\ 0.2489 \\ 1.9824 \\ 3.7371 \\ 4.6125 \\ 4.9065 \\ 4.9814 \\ 4.9969 \\ 4.9999 \\ 5.0 \\ 5.$$

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 \varphi_1(24) = \max \left\{ \begin{array}{c} 0.0 \\ 0.2489 \\ 1.9824 \\ 3.7371 \\ 4.6125 \\ 4.9065 \\ 4.9814 \\ 4.9969 \\ 4.9999 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5
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\varphi_1(25) = \max \left\{ \begin{array}{c} 0.0 \\ 0.2489 \\ 1.9824 \\ 3.7371 \\ 4.6125 \\ 4.9065 \\ 4.9814 \\ 4.9969 \\ 4.9999 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.
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\varphi_1(26) = \max \left\{ \begin{array}{c} 0.0 \\ 0.2489 \\ 1.9824 \\ 3.7371 \\ 4.6125 \\ 4.9065 \\ 4.9814 \\ 4.9969 \\ 4.9999 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.
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\varphi_1(27) = \max \left\{ \begin{array}{c} 0.0 \\ 0.2489 \\ 1.9824 \\ 3.7371 \\ 4.6125 \\ 4.9065 \\ 4.9814 \\ 4.9969 \\ 4.9999 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.
```

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\varphi_1(28) = \max \left\{ \begin{array}{c} 0.0 \\ 0.2489 \\ 1.9824 \\ 3.7371 \\ 4.6125 \\ 4.9065 \\ 4.9814 \\ 4.9969 \\ 4.9999 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.
```

```
\varphi_1(29) = \max \left\{ \begin{array}{c} 0.0 \\ 0.2489 \\ 1.9824 \\ 3.7371 \\ 4.6125 \\ 4.9065 \\ 4.9814 \\ 4.9969 \\ 4.9999 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.
```

```
\varphi_1(30) = \max \left\{ \begin{array}{l} 0.0 \\ 0.2489 \\ 1.9824 \\ 3.7371 \\ 4.6125 \\ 4.9065 \\ 4.9814 \\ 4.9969 \\ 4.9999 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.
```

```
 \varphi_1(31) = \max \left\{ \begin{array}{c} 0.0 \\ 0.2489 \\ 1.9824 \\ 3.7371 \\ 4.6125 \\ 4.9065 \\ 4.9814 \\ 4.9969 \\ 4.9999 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5.0 \\ 5
```

```
0.0
0.2489
1.9824
3.7371
4.6125
4.9065
4.9814
4.9969
4.9995
4.9999
                                        5.0
5.0
5.0
                                        5.0
5.0
                                        5.0
                                                      = 5.0, \quad x_1^0 = 10
\varphi_1(32) = \max
                                        5.0
                                        5.0
5.0
5.0
                                        5.0
                                        5.0
5.0
                                        5.0
                                        5.0
5.0
5.0
5.0
                                        5.0
                                        5.0
                                        5.0
                                        5.0
                                        5.0
```

```
0.0
0.2489
1.9824
3.7371
4.6125
4.9065
4.9814
4.9969
4.9995
4.9999
                                           5.0
5.0
                                           5.0
                                           5.0
5.0
                                           5.0
                                           5.0
5.0
5.0
5.0
5.0
                                                             = 5.0, \quad x_1^0 = 10
\varphi_1(33) = \max
                                           5.0
5.0
                                           5.0
                                           5.0
5.0
5.0
5.0
                                           5.0
                                           5.0
                                           5.0
                                           5.0
                                           5.0
5.0
```

```
0.0
0.2489
1.9824
3.7371
4.6125
4.9065
4.9814
4.9969
4.9995
4.9999
                                               5.0
5.0
5.0
                                               5.0
5.0
                                               5.0
                                               5.0
                                               5.0
5.0
5.0
5.0
                                                                = 5.0, \quad x_1^0 = 10
\varphi_1(34) = \max
                                               5.0
5.0
5.0
                                               5.0
5.0
5.0
5.0
                                               5.0
                                              5.0
5.0
                                              5.0
                                              5.0
5.0
5.0
```

```
0.0
0.2489
1.9824
3.7371
4.6125
4.9065
4.9814
4.9969
4.9995
                               4.9999
                                  5.0
5.0
                                  5.0
                                  5.0
                                  5.0
                                  5.0
                                  5.0
                                  5.0
5.0
5.0
                                               =5.0, \quad x_1^0=10
\varphi_1(35) = \max
                                  5.0
                                  5.0
5.0
                                  5.0
                                  5.0
5.0
5.0
5.0
                                  5.0
                                  5.0
                                  5.0
                                  5.0
                                  5.0
                                  5.0
5.0
                                  5.0
```

```
0.0
                         0.2489
                         1.9824
3.7371
4.6125
                         4.9065
4.9814
4.9969
                         4.9995
                         4.9999
                           5.0
                           5.0
                           5.0
                           5.0
                           5.0
                           5.0
                           5.0
                           5.0
5.0
5.0
                                     = 5.0, \quad x_1^0 = 10
\varphi_1(36) = \max
                           5.0
                           5.0
                           5.0
                           5.0
                           5.0
                           5.0
5.0
5.0
                           5.0
                           5.0 \\ 5.0
                           5.0
                           5.0
                           5.0
                           5.0
                           5.0
5.0
```

## 2 Product 2

$$\varphi_2(0) = \max \{ 0.0 \} = 0.0, x_2^0 = 0$$

$$\begin{split} \varphi_2(1) &= \max \left\{ \begin{array}{l} 0.0 + 0.2489 \\ 0.0733 + 0.0 \end{array} \right\} = 0.2489, \quad x_2^0 = 0 \\ \varphi_2(2) &= \max \left\{ \begin{array}{l} 0.0 + 1.9824 \\ 0.0733 + 0.2489 \\ 1.0094 + 0.0 \end{array} \right\} = 1.9824, \quad x_2^0 = 0 \\ \varphi_2(3) &= \max \left\{ \begin{array}{l} 0.0 + 3.7371 \\ 0.0733 + 1.9824 \\ 1.0094 + 0.2489 \\ 2.4026 + 0.0 \end{array} \right\} = 3.7371, \quad x_2^0 = 0 \\ \varphi_2(4) &= \max \left\{ \begin{array}{l} 0.0 + 4.6125 \\ 0.0733 + 3.7371 \\ 1.0094 + 1.9824 \\ 2.4026 + 0.2489 \\ 3.3614 + 0.0 \end{array} \right\} = 4.6125, \quad x_2^0 = 0 \\ \varphi_2(5) &= \max \left\{ \begin{array}{l} 0.0 + 4.9065 \\ 0.0733 + 4.6125 \\ 1.0094 + 3.7371 \\ 2.4026 + 1.9824 \\ 3.3614 + 0.2489 \\ 3.7975 + 0.0 \end{array} \right\} = 4.9065, \quad x_2^0 = 0 \\ \varphi_2(6) &= \max \left\{ \begin{array}{l} 0.0 + 4.9814 \\ 0.0733 + 4.9065 \\ 1.0094 + 4.6125 \\ 2.4026 + 3.7371 \\ 3.3614 + 1.9824 \\ 3.7975 + 0.2489 \\ 3.9469 + 0.0 \end{array} \right\} = 6.1397, \quad x_2^0 = 3 \\ \varphi_2(7) &= \max \left\{ \begin{array}{l} 0.0 + 4.9969 \\ 0.0733 + 4.9814 \\ 1.0094 + 4.9065 \\ 2.4026 + 4.6125 \\ 3.3614 + 3.7371 \\ 3.9469 + 0.2489 \\ 3.9882 + 0.0 \end{array} \right\} = 7.0985, \quad x_2^0 = 4 \\ \varphi_2(8) &= \max \left\{ \begin{array}{l} 0.0 + 4.9995 \\ 0.0733 + 4.9969 \\ 1.0094 + 4.9814 \\ 2.4026 + 4.9065 \\ 3.3614 + 9.995 \\ 0.0733 + 4.9969 \\ 1.0094 + 4.9814 \\ 2.4026 + 4.9065 \\ 3.3614 + 9.913 \\ 3.9882 + 0.0 \end{array} \right\} = 7.9739, \quad x_2^0 = 4 \\ \varphi_2(8) &= \max \left\{ \begin{array}{l} 0.0 + 4.9995 \\ 0.0733 + 4.9969 \\ 1.0094 + 4.9814 \\ 2.4026 + 4.9065 \\ 3.3614 + 9.913 \\ 3.9882 + 0.0 \end{array} \right\} = 7.9739, \quad x_2^0 = 4 \\ \varphi_2(8) &= \max \left\{ \begin{array}{l} 0.0 + 4.9995 \\ 0.0733 + 4.9969 \\ 1.0094 + 4.9814 \\ 2.4026 + 4.9065 \\ 3.3614 + 9.913 \\ 3.9882 + 0.0 \end{array} \right\} = 7.9739, \quad x_2^0 = 4 \\ 3.9882 + 0.2489 \\ 3.9977 + 0.0 \end{array} \right\}$$

```
0.0 + 4.9999
                 0.0733 + 4.9995
                 1.0094 + 4.9969
                 2.4026 + 4.9814
                 3.3614 + 4.9065
\varphi_2(9) = \max
                                      = 8.41, \quad x_2^0 = 5
                 3.7975 + 4.6125
                 3.9469 + 3.7371
                 3.9882 + 1.9824
                 3.9977 + 0.2489
                   3.9996 + 0.0
                      0.0 + 5.0
                  0.0733 + 4.9999
                  1.0094 + 4.9995
                  2.4026 + 4.9969
                  3.3614 + 4.9814
                                      = 8.704, \quad x_2^0 = 5
\varphi_2(10) = \max
                  3.7975 + 4.9065
                  3.9469 + 4.6125
                  3.9882 + 3.7371
                  3.9977 + 1.9824
                  3.9996 + 0.2489
                    3.9999 + 0.0
                      0.0 + 5.0
                    0.0733 + 5.0
                  1.0094 + 4.9999
                  2.4026 + 4.9995
                  3.3614 + 4.9969
                  3.7975 + 4.9814
                                       = 8.8534, \quad x_2^0 = 6
\varphi_2(11) = \max
                  3.9469 + 4.9065
                  3.9882 + 4.6125
                  3.9977 + 3.7371
                  3.9996 + 1.9824
                  3.9999 + 0.2489
                      4.0 + 0.0
```

```
0.0 + 5.0
                    0.0733 + 5.0
                    1.0094 + 5.0
                  2.4026 + 4.9999
                  3.3614 + 4.9995
                  3.7975 + 4.9969
\varphi_2(12) = \max
                                      = 8.9283, \quad x_2^0 = 6
                  3.9469 + 4.9814
                  3.9882 + 4.9065
                  3.9977 + 4.6125
                  3.9996 + 3.7371
                  3.9999 + 1.9824
                    4.0 + 0.2489
                      4.0 + 0.0
                      0.0 + 5.0
                    0.0733 + 5.0
                    1.0094 + 5.0
                    2.4026 + 5.0
                  3.3614 + 4.9999
                  3.7975 + 4.9995
                  3.9469 + 4.9969
                                      = 8.9696, \quad x_2^0 = 7
\varphi_2(13) = \max
                  3.9882 + 4.9814
                  3.9977 + 4.9065
                  3.9996 + 4.6125
                  3.9999 + 3.7371
                    4.0 + 1.9824
                    4.0 + 0.2489
                      4.0 + 0.0
                      0.0 + 5.0
                    0.0733 + 5.0
                    1.0094 + 5.0
                    2.4026 + 5.0
                    3.3614 + 5.0
                  3.7975 + 4.9999
                  3.9469 + 4.9995
\varphi_2(14) = \max
                  3.9882 + 4.9969
                                      = 8.9851, \quad x_2^0 = 7
                  3.9977 + 4.9814
                  3.9996 + 4.9065
                  3.9999 + 4.6125
                    4.0 + 3.7371
                    4.0 + 1.9824
                    4.0 + 0.2489
                      4.0 + 0.0
```

```
0.0 + 5.0
                    0.0733 + 5.0
                    1.0094 + 5.0
                    2.4026 + 5.0
                    3.3614 + 5.0
                    3.7975 + 5.0
                  3.9469 + 4.9999
                  3.9882 + 4.9995
\varphi_2(15) = \max
                                       = 8.9946, \quad x_2^0 = 8
                  3.9977 + 4.9969
                  3.9996 + 4.9814
                  3.9999 + 4.9065
                    4.0 + 4.6125
                    4.0 + 3.7371
                    4.0 + 1.9824
                    4.0 + 0.2489
                      4.0+0.0
                      0.0 + 5.0
                    0.0733 + 5.0
                    1.0094 + 5.0
                    2.4026 + 5.0
                    3.3614 + 5.0
                    3.7975 + 5.0
                    3.9469 + 5.0
                  3.9882 + 4.9999
\varphi_2(16) = \max \langle
                  3.9977 + 4.9995
                                       = 8.9972, \quad x_2^0 = 8
                  3.9996 + 4.9969
                  3.9999 + 4.9814
                    4.0 + 4.9065
                    4.0 + 4.6125
                    4.0 + 3.7371
                    4.0 + 1.9824
                    4.0 + 0.2489
                      4.0 + 0.0
```

```
0.0 + 5.0
                    0.0733 + 5.0
                    1.0094 + 5.0
                    2.4026 + 5.0
                    3.3614 + 5.0
                    3.7975 + 5.0
                    3.9469 + 5.0
                    3.9882 + 5.0
                  3.9977 + 4.9999
                                      = 8.9991, \quad x_2^0 = 9
\varphi_2(17) = \max
                  3.9996 + 4.9995
                  3.9999 + 4.9969
                    4.0 + 4.9814
                    4.0 + 4.9065
                    4.0 + 4.6125
                    4.0 + 3.7371
                    4.0 + 1.9824
                    4.0 + 0.2489
                      4.0 + 0.0
                      0.0 + 5.0
                    0.0733 + 5.0
                    1.0094 + 5.0
                    2.4026 + 5.0
                    3.3614 + 5.0
                    3.7975 + 5.0
                    3.9469 + 5.0
                    3.9882 + 5.0
                    3.9977 + 5.0
\varphi_2(18) = \max
                                      = 8.9995, \quad x_2^0 = 9 
                  3.9996 + 4.9999
                  3.9999 + 4.9995
                    4.0 + 4.9969
                    4.0 + 4.9814
                    4.0 + 4.9065
                    4.0 + 4.6125
                    4.0 + 3.7371
                    4.0 + 1.9824
                    4.0 + 0.2489
                      4.0 + 0.0
```

```
0.0 + 5.0
                    0.0733 + 5.0
                    1.0094 + 5.0
                    2.4026 + 5.0
                    3.3614 + 5.0
                    3.7975 + 5.0
                    3.9469 + 5.0
                    3.9882 + 5.0
                    3.9977 + 5.0
                    3.9996 + 5.0
\varphi_2(19) = \max
                                      = 8.9998, \quad x_2^0 = 10
                  3.9999 + 4.9999
                    4.0 + 4.9995
                    4.0 + 4.9969
                    4.0 + 4.9814
                    4.0 + 4.9065
                    4.0 + 4.6125
                    4.0 + 3.7371
                    4.0 + 1.9824
                    4.0 + 0.2489
                      4.0 + 0.0
                    0.0 + 5.0
                  0.0733 + 5.0
                  1.0094 + 5.0
                  2.4026 + 5.0
                  3.3614 + 5.0
                  3.7975 + 5.0
                  3.9469 + 5.0
                  3.9882 + 5.0
                  3.9977 + 5.0
                  3.9996 + 5.0
                                   = 8.9999, \quad x_2^0 = 10
\varphi_2(20) = \max
                  3.9999 + 5.0
                  4.0 + 4.9999
                  4.0 + 4.9995
                  4.0 + 4.9969
                  4.0 + 4.9814
                  4.0 + 4.9065
                  4.0 + 4.6125
                  4.0 + 3.7371
                  4.0 + 1.9824
                  4.0 + 0.2489
                    4.0 + 0.0
```

```
0.0 + 5.0
                  0.0733 + 5.0
                  1.0094 + 5.0
                  2.4026 + 5.0
                  3.3614 + 5.0
                  3.7975 + 5.0
                  3.9469 + 5.0
                  3.9882 + 5.0
                  3.9977 + 5.0
                  3.9996 + 5.0
                  3.9999 + 5.0
                                   = 9.0, \quad x_2^0 = 11
\varphi_2(21) = \max
                    4.0 + 5.0
                  4.0 + 4.9999
                  4.0 + 4.9995
                  4.0 + 4.9969
                  4.0 + 4.9814
                  4.0 + 4.9065
                  4.0 + 4.6125
                  4.0 + 3.7371
                  4.0 + 1.9824
                  4.0 + 0.2489
                    4.0 + 0.0
                    0.0 + 5.0
                  0.0733 + 5.0
                  1.0094 + 5.0
                  2.4026 + 5.0
                  3.3614 + 5.0
                  3.7975 + 5.0
                  3.9469 + 5.0
                  3.9882 + 5.0
                  3.9977 + 5.0
                  3.9996 + 5.0
                  3.9999 + 5.0
\varphi_2(22) = \max
                                   = 9.0, \quad x_2^0 = 11
                    4.0 + 5.0
                    4.0 + 5.0
                  4.0 + 4.9999
                  4.0 + 4.9995
                  4.0 + 4.9969
                  4.0 + 4.9814
                  4.0 + 4.9065
                  4.0 + 4.6125
                  4.0 + 3.7371
                  4.0 + 1.9824
                  4.0 + 0.2489
                    4.0 + 0.0
```

```
0.0 + 5.0
                  0.0733 + 5.0
                  1.0094 + 5.0
                  2.4026 + 5.0
                  3.3614 + 5.0
                  3.7975 + 5.0
                  3.9469 + 5.0
                  3.9882 + 5.0
                  3.9977 + 5.0
                  3.9996 + 5.0
                  3.9999 + 5.0
                    4.0 + 5.0
                                   = 9.0, \quad x_2^0 = 11
\varphi_2(23) = \max
                    4.0 + 5.0
                    4.0 + 5.0
                  4.0 + 4.9999
                  4.0 + 4.9995
                  4.0 + 4.9969
                  4.0 + 4.9814
                  4.0 + 4.9065
                  4.0 + 4.6125
                  4.0 + 3.7371
                  4.0 + 1.9824
                  4.0 + 0.2489
                    4.0 + 0.0
```

```
0.0 + 5.0
                   0.0733 + 5.0
                   1.0094 + 5.0
                   2.4026 + 5.0
                   3.3614 + 5.0
                   3.7975 + 5.0
                   3.9469 + 5.0
                   3.9882 + 5.0
                   3.9977 + 5.0
                   3.9996 + 5.0
                   3.9999 + 5.0
                    4.0 + 5.0
                                    = 9.0, \quad x_2^0 = 11
\varphi_2(24) = \max \langle
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                   4.0 + 4.9999
                   4.0 + 4.9995
                   4.0 + 4.9969
                   4.0 + 4.9814
                   4.0 + 4.9065
                   4.0 + 4.6125
                   4.0 + 3.7371
                   4.0 + 1.9824
                   4.0 + 0.2489
                    4.0 + 0.0
```

```
0.0 + 5.0
                  0.0733 + 5.0
                  1.0094 + 5.0
                  2.4026 + 5.0
                  3.3614 + 5.0
                  3.7975 + 5.0
                  3.9469 + 5.0
                  3.9882 + 5.0
                  3.9977 + 5.0
                  3.9996 + 5.0
                  3.9999 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                                   = 9.0, \quad x_2^0 = 11
\varphi_2(25) = \max \langle
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0+5.0
                  4.0 + 4.9999
                  4.0 + 4.9995
                  4.0 + 4.9969
                  4.0 + 4.9814
                  4.0 + 4.9065
                  4.0 + 4.6125
                  4.0 + 3.7371
                  4.0 + 1.9824
                  4.0 + 0.2489
                    4.0 + 0.0
```

```
0.0 + 5.0
                  0.0733 + 5.0
                  1.0094 + 5.0
                  2.4026 + 5.0
                  3.3614 + 5.0
                  3.7975 + 5.0
                  3.9469 + 5.0
                  3.9882 + 5.0
                  3.9977 + 5.0
                  3.9996 + 5.0
                  3.9999 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                                   = 9.0, \quad x_2^0 = 11
\varphi_2(26) = \max
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                  4.0 + 4.9999
                  4.0 + 4.9995
                  4.0 + 4.9969
                  4.0 + 4.9814
                  4.0 + 4.9065
                  4.0 + 4.6125
                  4.0 + 3.7371
                  4.0 + 1.9824
                  4.0 + 0.2489
                    4.0+0.0
```

```
0.0 + 5.0
                  0.0733 + 5.0
                  1.0094 + 5.0
                  2.4026 + 5.0
                  3.3614 + 5.0
                  3.7975 + 5.0
                  3.9469 + 5.0
                  3.9882 + 5.0
                  3.9977 + 5.0
                  3.9996 + 5.0
                  3.9999 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                                  = 9.0, \quad x_2^0 = 11
\varphi_2(27) = \max
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0+5.0
                  4.0 + 4.9999
                  4.0 + 4.9995
                  4.0 + 4.9969
                  4.0 + 4.9814
                  4.0 + 4.9065
                  4.0 + 4.6125
                  4.0 + 3.7371
                  4.0 + 1.9824
                  4.0 + 0.2489
                    4.0+0.0
```

```
0.0 + 5.0
                  0.0733 + 5.0
                  1.0094 + 5.0
                  2.4026 + 5.0
                  3.3614 + 5.0
                  3.7975 + 5.0
                  3.9469 + 5.0
                  3.9882 + 5.0
                  3.9977 + 5.0
                  3.9996 + 5.0
                  3.9999 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                                 = 9.0, \quad x_2^0 = 11
\varphi_2(28) = \max
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                  4.0 + 4.9999
                  4.0 + 4.9995
                  4.0 + 4.9969
                  4.0 + 4.9814
                  4.0 + 4.9065
                  4.0 + 4.6125
                  4.0 + 3.7371
                  4.0 + 1.9824
                  4.0 + 0.2489
                    4.0 + 0.0
```

```
0.0 + 5.0
                  0.0733 + 5.0
                  1.0094 + 5.0
                  2.4026 + 5.0
                  3.3614 + 5.0
                  3.7975 + 5.0
                  3.9469 + 5.0
                  3.9882 + 5.0
                  3.9977 + 5.0
                  3.9996 + 5.0
                  3.9999 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                                   = 9.0, \quad x_2^0 = 11
\varphi_2(29) = \max
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                  4.0 + 4.9999
                  4.0 + 4.9995
                  4.0 + 4.9969
                  4.0 + 4.9814
                  4.0 + 4.9065
                  4.0 + 4.6125
                  4.0 + 3.7371
                  4.0 + 1.9824
                  4.0 + 0.2489
                    4.0 + 0.0
```

```
0.0 + 5.0
                  0.0733 + 5.0
                  1.0094 + 5.0
                  2.4026 + 5.0
                  3.3614 + 5.0
                  3.7975 + 5.0
                  3.9469 + 5.0
                  3.9882 + 5.0
                  3.9977 + 5.0
                  3.9996 + 5.0
                  3.9999 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                                   = 9.0, \quad x_2^0 = 11
\varphi_2(30) = \max
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                  4.0 + 4.9999
                  4.0 + 4.9995
                  4.0 + 4.9969
                  4.0 + 4.9814
                  4.0 + 4.9065
                  4.0 + 4.6125
                  4.0 + 3.7371
                  4.0 + 1.9824
                  4.0 + 0.2489
                    4.0 + 0.0
```

```
0.0 + 5.0
                  0.0733 + 5.0
                  1.0094 + 5.0
                  2.4026 + 5.0
                  3.3614 + 5.0
                  3.7975 + 5.0
                  3.9469 + 5.0
                  3.9882 + 5.0
                  3.9977 + 5.0
                  3.9996 + 5.0
                  3.9999 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                                  =9.0, \quad x_2^0=11
\varphi_2(31) = \max
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                  4.0 + 4.9999
                  4.0 + 4.9995
                  4.0 + 4.9969
                  4.0 + 4.9814
                  4.0 + 4.9065
                  4.0 + 4.6125
                  4.0 + 3.7371
                  4.0 + 1.9824
                  4.0 + 0.2489
                   4.0 + 0.0
```

```
0.0 + 5.0
                  0.0733 + 5.0
                  1.0094 + 5.0
                  2.4026 + 5.0
                  3.3614 + 5.0
                  3.7975 + 5.0
                  3.9469 + 5.0
                  3.9882 + 5.0
                  3.9977 + 5.0
                  3.9996 + 5.0
                  3.9999 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                                 = 9.0, \quad x_2^0 = 11
\varphi_2(32) = \max
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0+5.0
                  4.0 + 4.9999
                  4.0 + 4.9995
                  4.0 + 4.9969
                  4.0 + 4.9814
                  4.0 + 4.9065
                  4.0 + 4.6125
                  4.0 + 3.7371
                  4.0 + 1.9824
                  4.0 + 0.2489
                   4.0 + 0.0
```

```
0.0 + 5.0
                  0.0733 + 5.0
                  1.0094 + 5.0
                  2.4026 + 5.0
                  3.3614 + 5.0
                  3.7975 + 5.0
                  3.9469 + 5.0
                  3.9882 + 5.0
                  3.9977 + 5.0
                  3.9996 + 5.0
                  3.9999 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                                   = 9.0, \quad x_2^0 = 11
\varphi_2(33) = \max
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                  4.0 + 4.9999
                  4.0 + 4.9995
                  4.0 + 4.9969
                  4.0 + 4.9814
                  4.0 + 4.9065
                  4.0 + 4.6125
                  4.0 + 3.7371
                  4.0 + 1.9824
                  4.0 + 0.2489
                    4.0 + 0.0
```

```
0.0 + 5.0
                  0.0733 + 5.0
                  1.0094 + 5.0
                  2.4026 + 5.0
                  3.3614 + 5.0
                  3.7975 + 5.0
                  3.9469 + 5.0
                  3.9882 + 5.0
                  3.9977 + 5.0
                  3.9996 + 5.0
                  3.9999 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                                 = 9.0, \quad x_2^0 = 11
\varphi_2(34) = \max
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                  4.0 + 4.9999
                  4.0 + 4.9995
                  4.0 + 4.9969
                  4.0 + 4.9814
                  4.0 + 4.9065
                  4.0 + 4.6125
                  4.0 + 3.7371
                  4.0 + 1.9824
                  4.0 + 0.2489
                    4.0 + 0.0
```

```
0.0 + 5.0
                  0.0733 + 5.0
                  1.0094 + 5.0
                  2.4026 + 5.0
                  3.3614 + 5.0
                  3.7975 + 5.0
                  3.9469 + 5.0
                  3.9882 + 5.0
                  3.9977 + 5.0
                  3.9996 + 5.0
                  3.9999 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                                   x = 9.0, \quad x_2^0 = 11
\varphi_2(35) = \max \langle
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                  4.0 + 4.9999
                  4.0 + 4.9995
                  4.0 + 4.9969
                  4.0 + 4.9814
                  4.0 + 4.9065
                  4.0 + 4.6125
                  4.0 + 3.7371
                  4.0 + 1.9824
                  4.0 + 0.2489
                    4.0 + 0.0
```

```
0.0 + 5.0
                  0.0733 + 5.0
                  1.0094 + 5.0
                  2.4026 + 5.0
                  3.3614 + 5.0
                  3.7975 + 5.0
                  3.9469 + 5.0
                  3.9882 + 5.0
                  3.9977 + 5.0
                  3.9996 + 5.0
                  3.9999 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                                   = 9.0, \quad x_2^0 = 11
\varphi_2(36) = \max
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                    4.0 + 5.0
                  4.0 + 4.9999
                  4.0 + 4.9995
                  4.0 + 4.9969
                  4.0 + 4.9814
                  4.0 + 4.9065
                  4.0 + 4.6125
                  4.0 + 3.7371
                  4.0 + 1.9824
                  4.0 + 0.2489
                    4.0 + 0.0
```

## 3 Product 3

$$\varphi_3(0) = \max \left\{ \begin{array}{c} 0.0 \end{array} \right\} = 0.0, \quad x_3^0 = 0$$

$$\varphi_{3}(1) = \max \left\{ \begin{array}{l} 0.0 + 0.2489 \\ 0.0409 + 0.0 \end{array} \right\} = 0.2489, \quad x_{3}^{0} = 0$$

$$\varphi_{3}(2) = \max \left\{ \begin{array}{l} 0.0 + 1.9824 \\ 0.0409 + 0.2489 \\ 1.2377 + 0.0 \end{array} \right\} = 1.9824, \quad x_{3}^{0} = 0$$

$$\varphi_{3}(3) = \max \left\{ \begin{array}{l} 0.0 + 3.7371 \\ 0.0409 + 1.9824 \\ 1.2377 + 0.2489 \\ 4.0704 + 0.0 \end{array} \right\} = 4.0704, \quad x_{3}^{0} = 3$$

$$\varphi_{3}(4) = \max \left\{ \begin{array}{l} 0.0 + 4.6125 \\ 0.0409 + 3.7371 \\ 1.2377 + 1.9824 \\ 4.0704 + 0.2489 \\ 6.8836 + 0.0 \end{array} \right\} = 6.8836, \quad x_{3}^{0} = 4$$

$$\varphi_{3}(5) = \max \left\{ \begin{array}{l} 0.0 + 4.9065 \\ 0.0409 + 4.6125 \\ 1.2377 + 3.7371 \\ 4.0704 + 1.9824 \\ 6.8836 + 0.2489 \\ 8.6786 + 0.0 \end{array} \right\} = 8.6786, \quad x_{3}^{0} = 5$$

$$\varphi_{3}(6) = \max \left\{ \begin{array}{l} 0.0 + 6.1397 \\ 0.0409 + 4.9065 \\ 1.2377 + 4.6125 \\ 4.0704 + 3.7371 \\ 6.8836 + 1.9824 \\ 8.6786 + 0.2489 \\ 9.5327 + 0.0 \end{array} \right\} = 9.5327, \quad x_{3}^{0} = 6$$

$$\varphi_{3}(7) = \max \left\{ \begin{array}{l} 0.0 + 7.0985 \\ 0.0409 + 6.1397 \\ 1.2377 + 4.9065 \\ 4.0704 + 4.6125 \\ 6.8836 + 1.9824 \\ 9.5327 + 0.2489 \\ 9.8586 + 0.0 \end{array} \right\} = 10.661, \quad x_{3}^{0} = 5$$

$$\varphi_{3}(8) = \max \left\{ \begin{array}{l} 0.0 + 7.0985 \\ 0.0409 + 7.0985 \\ 1.2377 + 6.1397 \\ 4.0704 + 4.9065 \\ 6.8836 + 3.7371 \\ 9.5327 + 1.9824 \\ 9.8586 + 0.2489 \\ 9.9627 + 0.0 \end{array} \right\} = 12.4157, \quad x_{3}^{0} = 5$$

$$\varphi_{3}(8) = \max \left\{ \begin{array}{l} 0.0 + 7.9739 \\ 0.0409 + 7.0985 \\ 1.2377 + 6.1397 \\ 4.0704 + 4.9065 \\ 6.8836 + 3.7371 \\ 9.5327 + 1.9824 \\ 9.8586 + 0.2489 \\ 9.9627 + 0.0 \end{array} \right\} = 12.4157, \quad x_{3}^{0} = 5$$

```
0.0 + 8.41
                 0.0409 + 7.9739
                 1.2377 + 7.0985
                 4.0704 + 6.1397
                 6.8836 + 4.9065
                                     =13.2911,\quad x_3^0=5
\varphi_3(9) = \max
                 8.6786 + 4.6125
                 9.5327 + 3.7371
                 9.8586 + 1.9824
                 9.9627 + 0.2489
                   9.9913 + 0.0
                    0.0 + 8.704
                   0.0409 + 8.41
                  1.2377 + 7.9739
                  4.0704 + 7.0985
                  6.8836 + 6.1397
                                      = 14.1452, \quad x_3^0 = 6
\varphi_3(10) = \max
                  8.6786 + 4.9065
                  9.5327 + 4.6125
                  9.8586 + 3.7371
                  9.9627 + 1.9824
                  9.9913 + 0.2489
                    9.9982 + 0.0
                    0.0 + 8.8534
                   0.0409 + 8.704
                   1.2377 + 8.41
                  4.0704 + 7.9739
                  6.8836 + 7.0985
                  8.6786 + 6.1397
                                      = 14.8183, \quad x_3^0 = 5
\varphi_3(11) = \max
                  9.5327 + 4.9065
                  9.8586 + 4.6125
                  9.9627 + 3.7371
                  9.9913 + 1.9824
                  9.9982 + 0.2489
                    9.9997 + 0.0
```

```
0.0 + 8.9283
                  0.0409 + 8.8534
                  1.2377 + 8.704
                   4.0704 + 8.41
                  6.8836 + 7.9739
                  8.6786 + 7.0985
                                      = 15.7771, \quad x_3^0 = 5
\varphi_3(12) = \max
                  9.5327 + 6.1397
                  9.8586 + 4.9065
                  9.9627 + 4.6125
                  9.9913 + 3.7371
                  9.9982 + 1.9824
                  9.9997 + 0.2489
                    9.9999 + 0.0
                    0.0 + 8.9696
                  0.0409 + 8.9283
                  1.2377 + 8.8534
                  4.0704 + 8.704
                   6.8836 + 8.41
                  8.6786 + 7.9739
                  9.5327 + 7.0985
                                      = 16.6525, \quad x_3^0 = 5
\varphi_3(13) = \max
                  9.8586 + 6.1397
                  9.9627 + 4.9065
                  9.9913 + 4.6125
                  9.9982 + 3.7371
                  9.9997 + 1.9824
                  9.9999 + 0.2489
                        10.0
                    0.0 + 8.9851
                  0.0409 + 8.9696
                  1.2377 + 8.9283
                  4.0704 + 8.8534
                  6.8836 + 8.704
                   8.6786 + 8.41
                  9.5327 + 7.9739
\varphi_3(14) = \max
                  9.8586 + 7.0985
                                      = 17.5066, \quad x_3^0 = 6
                  9.9627 + 6.1397
                  9.9913 + 4.9065
                  9.9982 + 4.6125
                  9.9997 + 3.7371
                  9.9999 + 1.9824
                   10.0 + 0.2489
                        10.0
```

```
0.0 + 8.9946
                  0.0409 + 8.9851
                  1.2377 + 8.9696
                  4.0704 + 8.9283
                  6.8836 + 8.8534
                   8.6786 + 8.704
                   9.5327 + 8.41
                  9.8586 + 7.9739
                                      = 17.9427, \quad x_3^0 = 6
\varphi_3(15) = \max
                  9.9627 + 7.0985
                  9.9913 + 6.1397
                  9.9982 + 4.9065
                  9.9997 + 4.6125
                  9.9999 + 3.7371
                   10.0 + 1.9824
                   10.0 + 0.2489
                        10.0
                    0.0 + 8.9972
                  0.0409 + 8.9946
                  1.2377 + 8.9851
                  4.0704 + 8.9696
                  6.8836 + 8.9283
                  8.6786 + 8.8534
                   9.5327 + 8.704
                   9.8586 + 8.41
\varphi_3(16) = \max \langle
                  9.9627 + 7.9739
                                      = 18.2686, \quad x_3^0 = 7
                  9.9913 + 7.0985
                  9.9982 + 6.1397
                  9.9997 + 4.9065
                  9.9999 + 4.6125
                   10.0 + 3.7371
                   10.0 + 1.9824
                   10.0 + 0.2489
                        10.0
```

```
0.0 + 8.9991
                  0.0409 + 8.9972
                  1.2377 + 8.9946
                  4.0704 + 8.9851
                  6.8836 + 8.9696
                  8.6786 + 8.9283
                  9.5327 + 8.8534
                  9.8586 + 8.704
                   9.9627 + 8.41
                                                  x_3^0 = 7
\varphi_3(17) = \max
                                      = 18.5626,
                  9.9913 + 7.9739
                  9.9982 + 7.0985
                  9.9997 + 6.1397
                  9.9999 + 4.9065
                   10.0 + 4.6125
                   10.0 + 3.7371
                   10.0 + 1.9824
                   10.0 + 0.2489
                        10.0
                    0.0 + 8.9995
                  0.0409 + 8.9991
                  1.2377 + 8.9972
                  4.0704 + 8.9946
                  6.8836 + 8.9851
                  8.6786 + 8.9696
                  9.5327 + 8.9283
                  9.8586 + 8.8534
                  9.9627 + 8.704
                                    = 18.712, \quad x_3^0 = 7
\varphi_3(18) = \max \langle
                   9.9913 + 8.41
                  9.9982 + 7.9739
                  9.9997 + 7.0985
                  9.9999 + 6.1397
                   10.0 + 4.9065
                   10.0 + 4.6125
                   10.0 + 3.7371
                   10.0 + 1.9824
                   10.0 + 0.2489
                        10.0
```

```
0.0 + 8.9998
                  0.0409 + 8.9995
                  1.2377 + 8.9991
                  4.0704 + 8.9972
                  6.8836 + 8.9946
                  8.6786 + 8.9851
                  9.5327 + 8.9696
                  9.8586 + 8.9283
                  9.9627 + 8.8534
                  9.9913 + 8.704
                                     = 18.8161, \quad x_3^0 = 8
\varphi_3(19) = \max
                   9.9982 + 8.41
                  9.9997 + 7.9739
                  9.9999 + 7.0985
                   10.0 + 6.1397
                   10.0 + 4.9065
                   10.0 + 4.6125
                   10.0 + 3.7371
                   10.0 + 1.9824
                   10.0 + 0.2489
                       10.0
                   0.0 + 8.9999
                  0.0409 + 8.9998
                  1.2377 + 8.9995
                  4.0704 + 8.9991
                  6.8836 + 8.9972
                  8.6786 + 8.9946
                  9.5327 + 8.9851
                  9.8586 + 8.9696
                  9.9627 + 8.9283
                  9.9913 + 8.8534
                                     = 18.891, \quad x_3^0 = 8
\varphi_3(20) = \max
                  9.9982 + 8.704
                   9.9997 + 8.41
                  9.9999 + 7.9739
                   10.0 + 7.0985
                   10.0 + 6.1397
                   10.0 + 4.9065
                   10.0 + 4.6125
                   10.0 + 3.7371
                   10.0 + 1.9824
                   10.0 + 0.2489
                        10.0
```

```
0.0 + 9.0
                 0.0409 + 8.9999
                 1.2377 + 8.9998
                 4.0704 + 8.9995
                 6.8836 + 8.9991
                 8.6786 + 8.9972
                 9.5327 + 8.9946
                 9.8586 + 8.9851
                 9.9627 + 8.9696
                 9.9913 + 8.9283
                 9.9982 + 8.8534
                                                  x_3^0 = 8
\varphi_3(21) = \max
                                     = 18.9323,
                  9.9997 + 8.704
                  9.9999 + 8.41
                   10.0 + 7.9739
                   10.0 + 7.0985
                   10.0 + 6.1397
                   10.0 + 4.9065
                   10.0 + 4.6125
                   10.0 + 3.7371
                   10.0 + 1.9824
                   10.0 + 0.2489
                       10.0
                     0.0 + 9.0
                   0.0409 + 9.0
                 1.2377 + 8.9999
                 4.0704 + 8.9998
                 6.8836 + 8.9995
                 8.6786 + 8.9991
                 9.5327 + 8.9972
                 9.8586 + 8.9946
                 9.9627 + 8.9851
                 9.9913 + 8.9696
                 9.9982 + 8.9283
                                     = 18.9609, \quad x_3^0 = 9
\varphi_3(22) = \max
                 9.9997 + 8.8534
                  9.9999 + 8.704
                    10.0 + 8.41
                   10.0 + 7.9739
                   10.0 + 7.0985
                   10.0 + 6.1397
                   10.0 + 4.9065
                   10.0 + 4.6125
                   10.0 + 3.7371
                   10.0 + 1.9824
                   10.0 + 0.2489
                       10.0
```

```
0.0 + 9.0
                   0.0409 + 9.0
                   1.2377 + 9.0
                 4.0704 + 8.9999
                 6.8836 + 8.9998
                 8.6786 + 8.9995
                 9.5327 + 8.9991
                 9.8586 + 8.9972
                 9.9627 + 8.9946
                 9.9913 + 8.9851
                 9.9982 + 8.9696
                 9.9997 + 8.9283
                                     = 18.9764, \quad x_3^0 = 9
\varphi_3(23) = \max
                 9.9999 + 8.8534
                   10.0 + 8.704
                    10.0 + 8.41
                   10.0 + 7.9739
                   10.0 + 7.0985
                   10.0 + 6.1397
                   10.0 + 4.9065
                   10.0 + 4.6125
                  10.0 + 3.7371
                   10.0 + 1.9824
                   10.0 + 0.2489
                       10.0
```

```
0.0 + 9.0
                    0.0409 + 9.0
                    1.2377 + 9.0
                    4.0704 + 9.0
                  6.8836 + 8.9999
                  8.6786 + 8.9998
                  9.5327 + 8.9995
                  9.8586 + 8.9991
                  9.9627 + 8.9972
                  9.9913 + 8.9946
                  9.9982 + 8.9851
                  9.9997 + 8.9696
                                      = 18.9859, \quad x_3^0 = 9
\varphi_3(24) = \max \langle
                  9.9999 + 8.9283
                   10.0 + 8.8534
                    10.0 + 8.704
                    10.0 + 8.41
                   10.0 + 7.9739
                   10.0 + 7.0985
                   10.0 + 6.1397
                   10.0 + 4.9065
                   10.0 + 4.6125
                   10.0 + 3.7371
                   10.0 + 1.9824
                   10.0 + 0.2489
                        10.0
```

```
0.0 + 9.0
                   0.0409 + 9.0
                   1.2377 + 9.0
                   4.0704 + 9.0
                   6.8836 + 9.0
                 8.6786 + 8.9999
                 9.5327 + 8.9998
                 9.8586 + 8.9995
                 9.9627 + 8.9991
                 9.9913 + 8.9972
                 9.9982 + 8.9946
                 9.9997 + 8.9851
                 9.9999 + 8.9696
                                     =18.9928,\quad x_3^0=10
\varphi_3(25) = \max
                   10.0 + 8.9283
                   10.0 + 8.8534
                   10.0 + 8.704
                   10.0 + 8.41
                   10.0 + 7.9739
                   10.0 + 7.0985
                   10.0 + 6.1397
                   10.0 + 4.9065
                   10.0 + 4.6125
                   10.0 + 3.7371
                   10.0 + 1.9824
                   10.0 + 0.2489
                       10.0
```

```
0.0 + 9.0
                    0.0409 + 9.0
                    1.2377 + 9.0
                    4.0704 + 9.0
                    6.8836 + 9.0
                    8.6786 + 9.0
                  9.5327 + 8.9999
                  9.8586 + 8.9998
                  9.9627 + 8.9995
                  9.9913 + 8.9991
                  9.9982 + 8.9972
                  9.9997 + 8.9946
                  9.9999 + 8.9851
                                      = 18.9954, \quad x_3^0 = 10
\varphi_3(26) = \max \langle
                   10.0 + 8.9696
                   10.0 + 8.9283
                   10.0 + 8.8534
                    10.0 + 8.704
                    10.0 + 8.41
                   10.0 + 7.9739
                   10.0 + 7.0985
                   10.0 + 6.1397
                   10.0 + 4.9065
                   10.0 + 4.6125
                   10.0 + 3.7371
                   10.0 + 1.9824
                   10.0 + 0.2489
                        10.0
```

```
0.0 + 9.0
                   0.0409 + 9.0
                   1.2377 + 9.0
                   4.0704 + 9.0
                   6.8836 + 9.0
                   8.6786 + 9.0
                   9.5327 + 9.0
                 9.8586 + 8.9999
                 9.9627 + 8.9998
                 9.9913 + 8.9995
                 9.9982 + 8.9991
                 9.9997 + 8.9972
                 9.9999 + 8.9946
                   10.0 + 8.9851
                                    = 18.9973, \quad x_3^0 = 10
\varphi_3(27) = \max
                   10.0 + 8.9696
                   10.0 + 8.9283
                   10.0 + 8.8534
                   10.0 + 8.704
                   10.0 + 8.41
                   10.0 + 7.9739
                   10.0 + 7.0985
                   10.0 + 6.1397
                   10.0 + 4.9065
                   10.0 + 4.6125
                   10.0 + 3.7371
                  10.0 + 1.9824
                   10.0 + 0.2489
                       10.0
```

```
0.0 + 9.0
                    0.0409 + 9.0
                    1.2377 + 9.0
                    4.0704 + 9.0
                    6.8836 + 9.0
                    8.6786 + 9.0
                    9.5327 + 9.0
                    9.8586 + 9.0
                  9.9627 + 8.9999
                  9.9913 + 8.9998
                  9.9982 + 8.9995
                  9.9997 + 8.9991
                  9.9999 + 8.9972
                   10.0 + 8.9946
                                                  x_3^0 = 11
\varphi_3(28) = \max \langle
                                     = 18.9988, 
                   10.0 + 8.9851
                   10.0 + 8.9696
                   10.0 + 8.9283
                   10.0 + 8.8534
                    10.0 + 8.704
                    10.0 + 8.41
                   10.0 + 7.9739
                   10.0 + 7.0985
                   10.0 + 6.1397
                   10.0 + 4.9065
                   10.0 + 4.6125
                   10.0 + 3.7371
                   10.0 + 1.9824
                   10.0 + 0.2489
                        10.0
```

```
0.0 + 9.0
                   0.0409 + 9.0
                    1.2377 + 9.0
                   4.0704 + 9.0
                   6.8836 + 9.0
                   8.6786 + 9.0
                   9.5327 + 9.0
                   9.8586 + 9.0
                   9.9627 + 9.0
                  9.9913 + 8.9999
                  9.9982 + 8.9998
                  9.9997 + 8.9995
                  9.9999 + 8.9991
                   10.0 + 8.9972
                   10.0 + 8.9946
                                     = 18.9992, \quad x_3^0 = 11
\varphi_3(29) = \max
                   10.0 + 8.9851
                   10.0 + 8.9696
                   10.0 + 8.9283
                   10.0 + 8.8534
                   10.0 + 8.704
                    10.0 + 8.41
                   10.0 + 7.9739
                   10.0 + 7.0985
                   10.0 + 6.1397
                   10.0 + 4.9065
                   10.0 + 4.6125
                   10.0 + 3.7371
                   10.0 + 1.9824
                   10.0 + 0.2489
                        10.0
```

```
0.0 + 9.0
                   0.0409 + 9.0
                   1.2377 + 9.0
                   4.0704 + 9.0
                   6.8836 + 9.0
                   8.6786 + 9.0
                   9.5327 + 9.0
                   9.8586 + 9.0
                   9.9627 + 9.0
                   9.9913 + 9.0
                  9.9982 + 8.9999
                  9.9997 + 8.9998
                  9.9999 + 8.9995
                   10.0 + 8.9991
                   10.0 + 8.9972
                                     = 18.9995, \quad x_3^0 = 11
\varphi_3(30) = \max
                   10.0 + 8.9946
                   10.0 + 8.9851
                   10.0 + 8.9696
                   10.0 + 8.9283
                   10.0 + 8.8534
                   10.0 + 8.704
                   10.0 + 8.41
                   10.0 + 7.9739
                   10.0 + 7.0985
                   10.0 + 6.1397
                   10.0 + 4.9065
                   10.0 + 4.6125
                   10.0 + 3.7371
                   10.0 + 1.9824
                   10.0 + 0.2489
                       10.0
```

```
0.0 + 9.0
                    0.0409 + 9.0
                    1.2377 + 9.0
                   4.0704 + 9.0
                   6.8836 + 9.0
                    8.6786 + 9.0
                   9.5327 + 9.0
                   9.8586 + 9.0
                   9.9627 + 9.0
                   9.9913 + 9.0
                   9.9982 + 9.0
                  9.9997 + 8.9999
                  9.9999 + 8.9998
                   10.0 + 8.9995
                   10.0 + 8.9991
                   10.0 + 8.9972
                                     = 18.9997, \quad x_3^0 = 12
\varphi_3(31) = \max
                   10.0 + 8.9946
                   10.0 + 8.9851
                   10.0 + 8.9696
                   10.0 + 8.9283
                   10.0 + 8.8534
                   10.0 + 8.704
                    10.0 + 8.41
                   10.0 + 7.9739
                   10.0 + 7.0985
                   10.0 + 6.1397
                   10.0 + 4.9065
                   10.0 + 4.6125
                   10.0 + 3.7371
                   10.0 + 1.9824
                   10.0 + 0.2489
                       10.0
```

```
0.0 + 9.0
                   0.0409 + 9.0
                   1.2377 + 9.0
                   4.0704 + 9.0
                   6.8836 + 9.0
                   8.6786 + 9.0
                   9.5327 + 9.0
                   9.8586 + 9.0
                   9.9627 + 9.0
                   9.9913 + 9.0
                   9.9982 + 9.0
                   9.9997 + 9.0
                 9.9999 + 8.9999
                   10.0 + 8.9998
                   10.0 + 8.9995
                   10.0 + 8.9991
                                                  x_3^0 = 12
\varphi_3(32) = \max
                   10.0 + 8.9972
                                   = 18.9998,
                   10.0 + 8.9946
                   10.0 + 8.9851
                   10.0 + 8.9696
                   10.0 + 8.9283
                   10.0 + 8.8534
                   10.0 + 8.704
                   10.0 + 8.41
                   10.0 + 7.9739
                   10.0 + 7.0985
                   10.0 + 6.1397
                   10.0 + 4.9065
                   10.0 + 4.6125
                   10.0 + 3.7371
                   10.0 + 1.9824
                   10.0 + 0.2489
                       10.0
```

```
0.0 + 9.0
                  0.0409 + 9.0
                  1.2377 + 9.0
                  4.0704 + 9.0
                  6.8836 + 9.0
                  8.6786 + 9.0
                  9.5327 + 9.0
                  9.8586 + 9.0
                  9.9627 + 9.0
                  9.9913 + 9.0
                  9.9982 + 9.0
                  9.9997 + 9.0
                  9.9999 + 9.0
                 10.0 + 8.9999
                 10.0 + 8.9998
                 10.0 + 8.9995
                 10.0 + 8.9991
                                                x_3^0 = 12
\varphi_3(33) = \max
                                   = 18.9999,
                 10.0 + 8.9972
                 10.0 + 8.9946
                 10.0 + 8.9851
                 10.0 + 8.9696
                 10.0 + 8.9283
                 10.0 + 8.8534
                  10.0 + 8.704
                  10.0 + 8.41
                 10.0 + 7.9739
                 10.0 + 7.0985
                 10.0 + 6.1397
                 10.0 + 4.9065
                 10.0 + 4.6125
                 10.0 + 3.7371
                 10.0 + 1.9824
                 10.0 + 0.2489
                      10.0
```

```
0.0 + 9.0
                  0.0409 + 9.0
                  1.2377 + 9.0
                  4.0704 + 9.0
                  6.8836 + 9.0
                  8.6786 + 9.0
                  9.5327 + 9.0
                  9.8586 + 9.0
                  9.9627 + 9.0
                  9.9913 + 9.0
                  9.9982 + 9.0
                  9.9997 + 9.0
                  9.9999 + 9.0
                   10.0 + 9.0
                 10.0 + 8.9999
                 10.0 + 8.9998
                 10.0 + 8.9995
                                   = 19.0, \quad x_3^0 = 13
\varphi_3(34) = \max
                 10.0 + 8.9991
                 10.0 + 8.9972
                 10.0 + 8.9946
                 10.0 + 8.9851
                 10.0 + 8.9696
                 10.0 + 8.9283
                 10.0 + 8.8534
                  10.0 + 8.704
                   10.0 + 8.41
                 10.0 + 7.9739
                 10.0 + 7.0985
                 10.0 + 6.1397
                 10.0 + 4.9065
                 10.0 + 4.6125
                 10.0 + 3.7371
                 10.0 + 1.9824
                 10.0 + 0.2489
                      10.0
```

```
0.0 + 9.0
                  0.0409 + 9.0
                  1.2377 + 9.0
                  4.0704 + 9.0
                  6.8836 + 9.0
                  8.6786 + 9.0
                  9.5327 + 9.0
                  9.8586 + 9.0
                  9.9627 + 9.0
                  9.9913 + 9.0
                  9.9982 + 9.0
                  9.9997 + 9.0
                  9.9999 + 9.0
                    10.0 + 9.0
                    10.0 + 9.0
                  10.0 + 8.9999
                  10.0 + 8.9998
                  10.0 + 8.9995
                                   x = 19.0, \quad x_3^0 = 13
\varphi_3(35) = \max \langle
                  10.0 + 8.9991
                  10.0 + 8.9972
                  10.0 + 8.9946
                  10.0 + 8.9851
                  10.0 + 8.9696
                  10.0 + 8.9283
                  10.0 + 8.8534
                  10.0 + 8.704
                   10.0 + 8.41
                  10.0 + 7.9739
                  10.0 + 7.0985
                  10.0 + 6.1397
                  10.0 + 4.9065
                  10.0 + 4.6125
                  10.0 + 3.7371
                  10.0 + 1.9824
                  10.0 + 0.2489
                       10.0
```

```
0.0 + 9.0
                  0.0409 + 9.0
                  1.2377 + 9.0
                  4.0704 + 9.0
                  6.8836 + 9.0
                  8.6786 + 9.0
                  9.5327 + 9.0
                  9.8586 + 9.0
                  9.9627 + 9.0
                  9.9913 + 9.0
                  9.9982 + 9.0
                  9.9997 + 9.0
                  9.9999 + 9.0
                    10.0 + 9.0
                   10.0 + 9.0
                   10.0+9.0
                  10.0 + 8.9999
                  10.0 + 8.9998
                                  = 19.0, \quad x_3^0 = 13
\varphi_3(36) = \max
                  10.0 + 8.9995
                  10.0 + 8.9991
                  10.0 + 8.9972
                  10.0 + 8.9946
                  10.0 + 8.9851
                  10.0 + 8.9696
                  10.0 + 8.9283
                  10.0 + 8.8534
                  10.0 + 8.704
                   10.0 + 8.41
                  10.0 + 7.9739
                  10.0 + 7.0985
                  10.0 + 6.1397
                  10.0 + 4.9065
                  10.0 + 4.6125
                  10.0 + 3.7371
                  10.0 + 1.9824
                  10.0 + 0.2489
                      10.0
```

## 4 Product 4

$$\varphi_4(0) = \max \left\{ \begin{array}{c} 0.0 \end{array} \right\} = 0.0, \quad x_4^0 = 0$$

$$\varphi_4(1) = \max \left\{ \begin{array}{l} 0.0 + 0.2489 \\ 0.3983 + 0.0 \end{array} \right\} = 0.3983, \quad x_4^0 = 1 \\ \varphi_4(2) = \max \left\{ \begin{array}{l} 0.0 + 1.9824 \\ 0.3983 + 0.2489 \\ 3.1718 + 0.0 \end{array} \right\} = 3.1718, \quad x_4^0 = 2 \\ \varphi_4(3) = \max \left\{ \begin{array}{l} 0.0 + 4.0704 \\ 0.3983 + 1.9824 \\ 3.1718 + 0.2489 \\ 5.9794 + 0.0 \end{array} \right\} = 5.9794, \quad x_4^0 = 3 \\ \varphi_4(4) = \max \left\{ \begin{array}{l} 0.0 + 6.8836 \\ 0.3983 + 4.0704 \\ 3.1718 + 1.9824 \\ 5.9794 + 0.2489 \\ 7.38 + 0.0 \end{array} \right\} = 7.38, \quad x_4^0 = 4 \\ \varphi_4(5) = \max \left\{ \begin{array}{l} 0.0 + 8.6786 \\ 0.3983 + 6.8836 \\ 3.1718 + 4.0704 \\ 5.9794 + 1.9824 \\ 7.38 + 0.2489 \\ 7.8504 + 0.0 \end{array} \right\} = 8.6786, \quad x_4^0 = 0 \\ \varphi_4(6) = \max \left\{ \begin{array}{l} 0.0 + 9.5327 \\ 0.3983 + 8.6786 \\ 3.1718 + 6.8836 \\ 5.9794 + 4.0704 \\ 7.38 + 1.9824 \\ 7.8504 + 0.2489 \\ 7.9703 + 0.0 \end{array} \right\} = 10.0554, \quad x_4^0 = 2 \\ \varphi_4(7) = \max \left\{ \begin{array}{l} 0.0 + 10.661 \\ 0.3983 + 9.5327 \\ 3.1718 + 8.6786 \\ 5.9794 + 6.8836 \\ 7.38 + 4.0704 \\ 7.8504 + 1.9824 \\ 7.9703 + 0.2489 \\ 7.995 + 0.0 \end{array} \right\} = 12.863, \quad x_4^0 = 3 \\ \varphi_4(8) = \max \left\{ \begin{array}{l} 0.0 + 12.4157 \\ 0.3983 + 10.661 \\ 3.1718 + 9.5327 \\ 5.9794 + 8.6786 \\ 7.38 + 6.8836 \\ 7.8504 + 4.0704 \\ 7.9703 + 1.9824 \\ 7.995 + 0.2489 \\ 7.995 + 0.2489 \\ 7.995 + 0.2489 \\ 7.9993 + 0.0 \end{array} \right\} = 14.658, \quad x_4^0 = 3 \\ =$$

```
0.0 + 13.2911
                 0.3983 + 12.4157
                 3.1718 + 10.661
                 5.9794 + 9.5327
                  7.38 + 8.6786
\varphi_4(9) = \max
                                      =16.0586,\quad x_4^0=4
                 7.8504 + 6.8836
                 7.9703 + 4.0704
                  7.995 + 1.9824
                 7.9993 + 0.2489
                   7.9999 + 0.0
                    0.0 + 14.1452
                  0.3983 + 13.2911
                  3.1718 + 12.4157
                  5.9794 + 10.661
                    7.38 + 9.5327
                                                    x_4^0 = 4
\varphi_4(10) = \max
                   7.8504 + 8.6786
                                       = 16.9127,
                   7.9703 + 6.8836
                   7.995 + 4.0704
                   7.9993 + 1.9824
                   7.9999 + 0.2489
                      8.0 + 0.0
                    0.0 + 14.8183
                  0.3983 + 14.1452
                  3.1718 + 13.2911
                  5.9794 + 12.4157
                    7.38 + 10.661
                   7.8504 + 9.5327
                                       = 18.3951, \quad x_4^0 = 3
\varphi_4(11) = \max
                   7.9703 + 8.6786
                   7.995 + 6.8836
                   7.9993 + 4.0704
                   7.9999 + 1.9824
                    8.0 + 0.2489
                      8.0 + 0.0
```

```
0.0 + 15.7771
                  0.3983 + 14.8183
                  3.1718 + 14.1452
                  5.9794 + 13.2911
                   7.38 + 12.4157
                   7.8504 + 10.661
\varphi_4(12) = \max
                                       = 19.7957, \quad x_4^0 = 4
                   7.9703 + 9.5327
                   7.995 + 8.6786
                   7.9993 + 6.8836
                   7.9999 + 4.0704
                    8.0 + 1.9824
                    8.0 + 0.2489
                      8.0 + 0.0
                    0.0 + 16.6525
                  0.3983 + 15.7771
                  3.1718 + 14.8183
                  5.9794 + 14.1452
                   7.38 + 13.2911
                  7.8504 + 12.4157
                  7.9703 + 10.661
                                       = 20.6711, \quad x_4^0 = 4
\varphi_4(13) = \max
                   7.995 + 9.5327
                   7.9993 + 8.6786
                   7.9999 + 6.8836
                    8.0 + 4.0704
                    8.0 + 1.9824
                    8.0 + 0.2489
                      8.0 + 0.0
                    0.0 + 17.5066
                  0.3983 + 16.6525
                  3.1718 + 15.7771
                  5.9794 + 14.8183
                   7.38 + 14.1452
                  7.8504 + 13.2911
                  7.9703 + 12.4157
\varphi_4(14) = \max
                                       = 21.5252, \quad x_4^0 = 4
                   7.995 + 10.661
                  7.9993 + 9.5327
                   7.9999 + 8.6786
                    8.0 + 6.8836
                    8.0 + 4.0704
                    8.0 + 1.9824
                    8.0 + 0.2489
                      8.0 + 0.0
```

```
0.0 + 17.9427
                  0.3983 + 17.5066
                  3.1718 + 16.6525
                  5.9794 + 15.7771
                   7.38 + 14.8183
                  7.8504 + 14.1452
                  7.9703 + 13.2911
                  7.995 + 12.4157
\varphi_4(15) = \max
                                       = 22.1983, \quad x_4^0 = 4
                   7.9993 + 10.661
                   7.9999 + 9.5327
                    8.0 + 8.6786
                    8.0 + 6.8836
                    8.0 + 4.0704
                    8.0 + 1.9824
                    8.0 + 0.2489
                      8.0+0.0
                    0.0 + 18.2686
                  0.3983 + 17.9427
                  3.1718 + 17.5066
                  5.9794 + 16.6525
                   7.38 + 15.7771
                  7.8504 + 14.8183
                  7.9703 + 14.1452
                  7.995 + 13.2911
\varphi_4(16) = \max \langle
                  7.9993 + 12.4157
                                       = 23.1571, \quad x_4^0 = 4
                  7.9999 + 10.661
                    8.0 + 9.5327
                    8.0 + 8.6786
                    8.0 + 6.8836
                    8.0 + 4.0704
                    8.0 + 1.9824
                    8.0 + 0.2489
                      8.0 + 0.0
```

```
0.0 + 18.5626
                 0.3983 + 18.2686
                 3.1718 + 17.9427
                 5.9794 + 17.5066
                   7.38 + 16.6525
                 7.8504 + 15.7771
                 7.9703 + 14.8183
                  7.995 + 14.1452
                 7.9993 + 13.2911
                                                   x_4^0 = 4
                                      = 24.0325,
\varphi_4(17) = \max
                 7.9999 + 12.4157
                    8.0 + 10.661
                    8.0 + 9.5327
                    8.0 + 8.6786
                    8.0 + 6.8836
                    8.0 + 4.0704
                    8.0 + 1.9824
                    8.0 + 0.2489
                     8.0 + 0.0
                    0.0 + 18.712
                 0.3983 + 18.5626
                 3.1718 + 18.2686
                 5.9794 + 17.9427
                   7.38 + 17.5066
                 7.8504 + 16.6525
                 7.9703 + 15.7771
                  7.995 + 14.8183
                 7.9993 + 14.1452
\varphi_4(18) = \max
                                      =24.8866,\quad x_4^0=4
                 7.9999 + 13.2911
                   8.0 + 12.4157
                    8.0 + 10.661
                    8.0 + 9.5327
                    8.0 + 8.6786
                    8.0 + 6.8836
                    8.0 + 4.0704
                    8.0 + 1.9824
                    8.0 + 0.2489
                     8.0 + 0.0
```

```
0.0 + 18.8161
                  0.3983 + 18.712
                  3.1718 + 18.5626
                  5.9794 + 18.2686
                   7.38 + 17.9427
                  7.8504 + 17.5066
                  7.9703 + 16.6525
                  7.995 + 15.7771
                  7.9993 + 14.8183
                  7.9999 + 14.1452
\varphi_4(19) = \max
                                       = 25.357, \quad x_4^0 = 5
                   8.0 + 13.2911
                    8.0 + 12.4157
                    8.0 + 10.661
                    8.0 + 9.5327
                    8.0 + 8.6786
                    8.0 + 6.8836
                    8.0 + 4.0704
                    8.0 + 1.9824
                    8.0 + 0.2489
                      8.0 + 0.0
                    0.0 + 18.891
                  0.3983 + 18.8161
                  3.1718 + 18.712
                  5.9794 + 18.5626
                   7.38 + 18.2686
                  7.8504 + 17.9427
                  7.9703 + 17.5066
                  7.995 + 16.6525
                  7.9993 + 15.7771
                  7.9999 + 14.8183
                                       = 25.7931, \quad x_4^0 = 5
\varphi_4(20) = \max
                    8.0 + 14.1452
                    8.0 + 13.2911
                    8.0 + 12.4157
                    8.0 + 10.661
                    8.0 + 9.5327
                    8.0 + 8.6786
                    8.0 + 6.8836
                    8.0 + 4.0704
                    8.0 + 1.9824
                    8.0 + 0.2489
                      8.0 + 0.0
```

```
0.0 + 18.9323
                  0.3983 + 18.891
                  3.1718 + 18.8161
                  5.9794 + 18.712
                   7.38 + 18.5626
                  7.8504 + 18.2686
                  7.9703 + 17.9427
                  7.995 + 17.5066
                  7.9993 + 16.6525
                  7.9999 + 15.7771
                    8.0 + 14.8183
                                       = 26.119, \quad x_4^0 = 5
\varphi_4(21) = \max
                   8.0 + 14.1452
                    8.0 + 13.2911
                    8.0 + 12.4157
                    8.0 + 10.661
                    8.0 + 9.5327
                    8.0 + 8.6786
                    8.0 + 6.8836
                    8.0 + 4.0704
                    8.0 + 1.9824
                    8.0 + 0.2489
                      8.0 + 0.0
                    0.0 + 18.9609
                  0.3983 + 18.9323
                  3.1718 + 18.891
                  5.9794 + 18.8161
                    7.38 + 18.712
                  7.8504 + 18.5626
                  7.9703 + 18.2686
                  7.995 + 17.9427
                  7.9993 + 17.5066
                  7.9999 + 16.6525
                   8.0 + 15.7771
                                       =26.413,\quad x_4^0=5
\varphi_4(22) = \max
                    8.0 + 14.8183
                   8.0 + 14.1452
                    8.0 + 13.2911
                    8.0 + 12.4157
                    8.0 + 10.661
                    8.0 + 9.5327
                    8.0 + 8.6786
                    8.0 + 6.8836
                    8.0 + 4.0704
                    8.0 + 1.9824
                    8.0 + 0.2489
                      8.0 + 0.0
```

```
0.0 + 18.9764
                  0.3983 + 18.9609
                  3.1718 + 18.9323
                  5.9794 + 18.891
                  7.38 + 18.8161
                  7.8504 + 18.712
                  7.9703 + 18.5626
                  7.995 + 18.2686
                  7.9993 + 17.9427
                  7.9999 + 17.5066
                   8.0 + 16.6525
                   8.0 + 15.7771
                                       = 26.5624, \quad x_4^0 = 5
\varphi_4(23) = \max
                   8.0 + 14.8183
                   8.0 + 14.1452
                   8.0 + 13.2911
                   8.0 + 12.4157
                    8.0 + 10.661
                    8.0 + 9.5327
                    8.0 + 8.6786
                    8.0 + 6.8836
                    8.0 + 4.0704
                    8.0 + 1.9824
                    8.0 + 0.2489
                      8.0 + 0.0
```

```
0.0 + 18.9859
                 0.3983 + 18.9764
                 3.1718 + 18.9609
                 5.9794 + 18.9323
                   7.38 + 18.891
                 7.8504 + 18.8161
                  7.9703 + 18.712
                  7.995 + 18.5626
                 7.9993 + 18.2686
                 7.9999 + 17.9427
                   8.0 + 17.5066
                   8.0 + 16.6525
\varphi_4(24) = \max
                   8.0 + 15.7771
                                      =26.6823,\quad x_4^0=6
                   8.0 + 14.8183
                   8.0 + 14.1452
                   8.0 + 13.2911
                   8.0 + 12.4157
                    8.0 + 10.661
                    8.0 + 9.5327
                    8.0 + 8.6786
                    8.0 + 6.8836
                    8.0 + 4.0704
                    8.0 + 1.9824
                    8.0 + 0.2489
                     8.0 + 0.0
```

```
0.0 + 18.9928
                 0.3983 + 18.9859
                 3.1718 + 18.9764
                 5.9794 + 18.9609
                  7.38 + 18.9323
                  7.8504 + 18.891
                 7.9703 + 18.8161
                  7.995 + 18.712
                 7.9993 + 18.5626
                 7.9999 + 18.2686
                   8.0 + 17.9427
                   8.0 + 17.5066
                   8.0 + 16.6525
\varphi_4(25) = \max
                                      =26.7864,\quad x_4^0=6
                   8.0 + 15.7771
                   8.0 + 14.8183
                   8.0 + 14.1452
                   8.0 + 13.2911
                   8.0 + 12.4157
                    8.0 + 10.661
                    8.0 + 9.5327
                    8.0 + 8.6786
                    8.0 + 6.8836
                    8.0 + 4.0704
                    8.0 + 1.9824
                    8.0 + 0.2489
                     8.0 + 0.0
```

```
0.0 + 18.9954
                 0.3983 + 18.9928
                 3.1718 + 18.9859
                 5.9794 + 18.9764
                  7.38 + 18.9609
                 7.8504 + 18.9323
                  7.9703 + 18.891
                  7.995 + 18.8161
                  7.9993 + 18.712
                 7.9999 + 18.5626
                   8.0 + 18.2686
                   8.0 + 17.9427
                   8.0 + 17.5066
\varphi_4(26) = \max
                                      =26.8613,\quad x_4^0=6
                   8.0 + 16.6525
                   8.0 + 15.7771
                   8.0 + 14.8183
                   8.0 + 14.1452
                   8.0 + 13.2911
                   8.0 + 12.4157
                    8.0 + 10.661
                    8.0 + 9.5327
                    8.0 + 8.6786
                    8.0 + 6.8836
                    8.0 + 4.0704
                    8.0 + 1.9824
                    8.0 + 0.2489
                     8.0 + 0.0
```

```
0.0 + 18.9973
                 0.3983 + 18.9954
                 3.1718 + 18.9928
                 5.9794 + 18.9859
                  7.38 + 18.9764
                 7.8504 + 18.9609
                 7.9703 + 18.9323
                   7.995 + 18.891
                 7.9993 + 18.8161
                  7.9999 + 18.712
                   8.0 + 18.5626
                   8.0 + 18.2686
                   8.0 + 17.9427
                   8.0 + 17.5066
                                      = 26.9026, \quad x_4^0 = 6
\varphi_4(27) = \max
                   8.0 + 16.6525
                   8.0 + 15.7771
                   8.0 + 14.8183
                   8.0 + 14.1452
                   8.0 + 13.2911
                   8.0 + 12.4157
                    8.0 + 10.661
                    8.0 + 9.5327
                    8.0 + 8.6786
                    8.0 + 6.8836
                    8.0 + 4.0704
                    8.0 + 1.9824
                    8.0 + 0.2489
                      8.0 + 0.0
```

```
0.0 + 18.9988
                  0.3983 + 18.9973
                  3.1718 + 18.9954
                  5.9794 + 18.9928
                  7.38 + 18.9859
                  7.8504 + 18.9764
                  7.9703 + 18.9609
                  7.995 + 18.9323
                  7.9993 + 18.891
                  7.9999 + 18.8161
                    8.0 + 18.712
                   8.0 + 18.5626
                   8.0 + 18.2686
                   8.0 + 17.9427
                                      = 26.9312, \quad x_4^0 = 6
\varphi_4(28) = \max
                   8.0 + 17.5066
                   8.0 + 16.6525
                   8.0 + 15.7771
                   8.0 + 14.8183
                   8.0 + 14.1452
                   8.0 + 13.2911
                   8.0 + 12.4157
                    8.0 + 10.661
                    8.0 + 9.5327
                    8.0 + 8.6786
                    8.0 + 6.8836
                    8.0 + 4.0704
                    8.0 + 1.9824
                    8.0 + 0.2489
                      8.0 + 0.0
```

```
0.0 + 18.9992
                 0.3983 + 18.9988
                 3.1718 + 18.9973
                 5.9794 + 18.9954
                  7.38 + 18.9928
                 7.8504 + 18.9859
                 7.9703 + 18.9764
                  7.995 + 18.9609
                 7.9993 + 18.9323
                  7.9999 + 18.891
                   8.0 + 18.8161
                   8.0 + 18.712
                   8.0 + 18.5626
                   8.0 + 18.2686
                   8.0 + 17.9427
\varphi_4(29) = \max
                                      =26.9559,\quad x_4^0=7
                   8.0 + 17.5066
                   8.0 + 16.6525
                   8.0 + 15.7771
                   8.0 + 14.8183
                   8.0 + 14.1452
                   8.0 + 13.2911
                   8.0 + 12.4157
                    8.0 + 10.661
                    8.0 + 9.5327
                    8.0 + 8.6786
                    8.0 + 6.8836
                    8.0 + 4.0704
                    8.0 + 1.9824
                    8.0 + 0.2489
                     8.0 + 0.0
```

```
0.0 + 18.9995
                 0.3983 + 18.9992
                 3.1718 + 18.9988
                 5.9794 + 18.9973
                  7.38 + 18.9954
                 7.8504 + 18.9928
                 7.9703 + 18.9859
                  7.995 + 18.9764
                 7.9993 + 18.9609
                 7.9999 + 18.9323
                   8.0 + 18.891
                   8.0 + 18.8161
                   8.0 + 18.712
                   8.0 + 18.5626
                   8.0 + 18.2686
                                      =26.9714,\quad x_4^0=7
\varphi_4(30) = \max
                   8.0 + 17.9427
                   8.0 + 17.5066
                   8.0 + 16.6525
                   8.0 + 15.7771
                   8.0 + 14.8183
                   8.0 + 14.1452
                   8.0 + 13.2911
                   8.0 + 12.4157
                   8.0 + 10.661
                   8.0 + 9.5327
                   8.0 + 8.6786
                   8.0 + 6.8836
                   8.0 + 4.0704
                   8.0 + 1.9824
                   8.0 + 0.2489
                     8.0 + 0.0
```

```
0.0 + 18.9997
                 0.3983 + 18.9995
                 3.1718 + 18.9992
                 5.9794 + 18.9988
                  7.38 + 18.9973
                 7.8504 + 18.9954
                 7.9703 + 18.9928
                  7.995 + 18.9859
                 7.9993 + 18.9764
                 7.9999 + 18.9609
                   8.0 + 18.9323
                    8.0 + 18.891
                   8.0 + 18.8161
                    8.0 + 18.712
                   8.0 + 18.5626
                   8.0 + 18.2686
                                      = 26.9809, \quad x_4^0 = 7
\varphi_4(31) = \max
                   8.0 + 17.9427
                   8.0 + 17.5066
                   8.0 + 16.6525
                   8.0 + 15.7771
                   8.0 + 14.8183
                   8.0 + 14.1452
                   8.0 + 13.2911
                   8.0 + 12.4157
                    8.0 + 10.661
                    8.0 + 9.5327
                    8.0 + 8.6786
                    8.0 + 6.8836
                    8.0 + 4.0704
                    8.0 + 1.9824
                    8.0 + 0.2489
                      8.0 + 0.0
```

```
0.0 + 18.9998
                 0.3983 + 18.9997
                 3.1718 + 18.9995
                 5.9794 + 18.9992
                   7.38 + 18.9988
                 7.8504 + 18.9973
                 7.9703 + 18.9954
                  7.995 + 18.9928
                 7.9993 + 18.9859
                 7.9999 + 18.9764
                   8.0 + 18.9609
                   8.0 + 18.9323
                    8.0 + 18.891
                   8.0 + 18.8161
                    8.0 + 18.712
                   8.0 + 18.5626
                                      = 26.9878, \quad x_4^0 = 7
\varphi_4(32) = \max
                   8.0 + 18.2686
                   8.0 + 17.9427
                   8.0 + 17.5066
                   8.0 + 16.6525
                   8.0 + 15.7771
                   8.0 + 14.8183
                   8.0 + 14.1452
                   8.0 + 13.2911
                   8.0 + 12.4157
                    8.0 + 10.661
                    8.0 + 9.5327
                    8.0 + 8.6786
                    8.0 + 6.8836
                    8.0 + 4.0704
                    8.0 + 1.9824
                    8.0 + 0.2489
                      8.0 + 0.0
```

```
0.0 + 18.9999
                 0.3983 + 18.9998
                 3.1718 + 18.9997
                 5.9794 + 18.9995
                  7.38 + 18.9992
                 7.8504 + 18.9988
                 7.9703 + 18.9973
                  7.995 + 18.9954
                 7.9993 + 18.9928
                 7.9999 + 18.9859
                   8.0 + 18.9764
                   8.0 + 18.9609
                   8.0 + 18.9323
                   8.0 + 18.891
                   8.0 + 18.8161
                   8.0 + 18.712
                   8.0 + 18.5626
\varphi_4(33) = \max
                                      = 26.9921, \quad x_4^0 = 8
                   8.0 + 18.2686
                   8.0 + 17.9427
                   8.0 + 17.5066
                   8.0 + 16.6525
                   8.0 + 15.7771
                   8.0 + 14.8183
                   8.0 + 14.1452
                   8.0 + 13.2911
                   8.0 + 12.4157
                    8.0 + 10.661
                    8.0 + 9.5327
                    8.0 + 8.6786
                    8.0 + 6.8836
                    8.0 + 4.0704
                    8.0 + 1.9824
                    8.0 + 0.2489
                     8.0 + 0.0
```

```
0.0 + 19.0
                 0.3983 + 18.9999
                 3.1718 + 18.9998
                 5.9794 + 18.9997
                  7.38 + 18.9995
                 7.8504 + 18.9992
                 7.9703 + 18.9988
                  7.995 + 18.9973
                 7.9993 + 18.9954
                 7.9999 + 18.9928
                   8.0 + 18.9859
                   8.0 + 18.9764
                   8.0 + 18.9609
                   8.0 + 18.9323
                   8.0 + 18.891
                   8.0 + 18.8161
                   8.0 + 18.712
\varphi_4(34) = \max
                                      = 26.9947, \quad x_4^0 = 8
                   8.0 + 18.5626
                   8.0 + 18.2686
                   8.0 + 17.9427
                   8.0 + 17.5066
                   8.0 + 16.6525
                   8.0 + 15.7771
                   8.0 + 14.8183
                   8.0 + 14.1452
                   8.0 + 13.2911
                   8.0 + 12.4157
                    8.0 + 10.661
                    8.0 + 9.5327
                    8.0 + 8.6786
                    8.0 + 6.8836
                    8.0 + 4.0704
                    8.0 + 1.9824
                    8.0 + 0.2489
                     8.0 + 0.0
```

```
0.0 + 19.0
                   0.3983 + 19.0
                 3.1718 + 18.9999
                 5.9794 + 18.9998
                  7.38 + 18.9997
                 7.8504 + 18.9995
                 7.9703 + 18.9992
                  7.995 + 18.9988
                 7.9993 + 18.9973
                 7.9999 + 18.9954
                   8.0 + 18.9928
                   8.0 + 18.9859
                   8.0 + 18.9764
                   8.0 + 18.9609
                   8.0 + 18.9323
                   8.0 + 18.891
                   8.0 + 18.8161
                    8.0 + 18.712
                                                  x_4^0 = 8
\varphi_4(35) = \max
                                      = 26.9966,
                   8.0 + 18.5626
                   8.0 + 18.2686
                   8.0 + 17.9427
                   8.0 + 17.5066
                   8.0 + 16.6525
                   8.0 + 15.7771
                   8.0 + 14.8183
                   8.0 + 14.1452
                   8.0 + 13.2911
                   8.0 + 12.4157
                    8.0 + 10.661
                    8.0 + 9.5327
                    8.0 + 8.6786
                    8.0 + 6.8836
                    8.0 + 4.0704
                    8.0 + 1.9824
                    8.0 + 0.2489
                     8.0 + 0.0
```

```
0.0+19.0
                   0.3983 + 19.0
                   3.1718 + 19.0
                  5.9794 + 18.9999
                   7.38 + 18.9998
                  7.8504 + 18.9997
                  7.9703 + 18.9995
                  7.995 + 18.9992
                  7.9993 + 18.9988
                  7.9999 + 18.9973
                   8.0 + 18.9954
                   8.0 + 18.9928
                   8.0 + 18.9859
                   8.0 + 18.9764
                   8.0 + 18.9609
                   8.0 + 18.9323
                    8.0 + 18.891
                   8.0 + 18.8161
\varphi_4(36) = \max
                    8.0 + 18.712
                                       = 26.9981, \quad x_4^0 = 8
                   8.0 + 18.5626
                   8.0 + 18.2686
                   8.0 + 17.9427
                   8.0 + 17.5066
                   8.0 + 16.6525
                   8.0 + 15.7771
                   8.0 + 14.8183
                   8.0 + 14.1452
                   8.0 + 13.2911
                   8.0 + 12.4157
                    8.0 + 10.661
                    8.0 + 9.5327
                    8.0 + 8.6786
                    8.0 + 6.8836
                    8.0 + 4.0704
                    8.0 + 1.9824
                    8.0 + 0.2489
                      8.0 + 0.0
```

## 5 Product 5

$$\varphi_5(0) = \max\{0.0\} = 0.0, x_5^0 = 0$$

$$\varphi_{5}(1) = \max \left\{ \begin{array}{l} 0.0 + 0.3983 \\ 0.0333 + 0.0 \end{array} \right\} = 0.3983, \quad x_{5}^{0} = 0$$

$$\varphi_{5}(2) = \max \left\{ \begin{array}{l} 0.0 + 3.1718 \\ 0.0333 + 0.3983 \\ 0.5991 + 0.0 \end{array} \right\} = 3.1718, \quad x_{5}^{0} = 0$$

$$\varphi_{5}(3) = \max \left\{ \begin{array}{l} 0.0 + 5.9794 \\ 0.0333 + 3.1718 \\ 0.5991 + 0.3983 \\ 1.5934 + 0.0 \end{array} \right\} = 5.9794, \quad x_{5}^{0} = 0$$

$$\varphi_{5}(4) = \max \left\{ \begin{array}{l} 0.0 + 7.38 \\ 0.033 + 5.9794 \\ 0.5991 + 3.1718 \\ 1.5934 + 0.3983 \\ 2.3759 + 0.0 \end{array} \right\} = 7.38, \quad x_{5}^{0} = 0$$

$$\varphi_{5}(5) = \max \left\{ \begin{array}{l} 0.0 + 8.6786 \\ 0.033 + 7.38 \\ 0.5991 + 5.9794 \\ 1.5934 + 3.1718 \\ 2.3759 + 0.3983 \\ 2.7792 + 0.0 \end{array} \right\} = 8.6786, \quad x_{5}^{0} = 0$$

$$\varphi_{5}(6) = \max \left\{ \begin{array}{l} 0.0 + 10.0554 \\ 0.0333 + 8.6786 \\ 0.5991 + 7.38 \\ 1.5934 + 5.9794 \\ 2.3759 + 3.1718 \\ 2.3759 + 3.1718 \\ 2.3759 + 3.1718 \\ 2.7792 + 0.3983 \\ 2.9353 + 0.0 \end{array} \right\} = 10.0554, \quad x_{5}^{0} = 0$$

$$\varphi_{5}(7) = \max \left\{ \begin{array}{l} 0.0 + 12.863 \\ 0.0333 + 10.0554 \\ 0.5991 + 8.6786 \\ 1.5934 + 7.38 \\ 2.3759 + 5.9794 \\ 2.7792 + 3.1718 \\ 2.9353 + 0.3983 \\ 2.9935 + 0.0 \end{array} \right\} = 12.863, \quad x_{5}^{0} = 0$$

$$\varphi_{5}(8) = \max \left\{ \begin{array}{l} 0.0 + 12.863 \\ 0.0333 + 10.0554 \\ 0.5991 + 8.6786 \\ 1.5934 + 7.38 \\ 2.7792 + 3.1718 \\ 2.9353 + 0.3983 \\ 2.9935 + 0.0 \end{array} \right\} = 12.863, \quad x_{5}^{0} = 0$$

$$\varphi_{5}(8) = \max \left\{ \begin{array}{l} 0.0 + 14.658 \\ 0.0333 + 12.863 \\ 0.0333 + 12.863 \\ 0.5991 + 10.0554 \\ 1.5934 + 8.6786 \\ 2.3759 + 7.38 \\ 2.7792 + 5.9794 \\ 2.9353 + 3.1718 \\ 2.9838 + 0.3983 \\ 2.99353 + 3.1718 \\ 2.9838 + 0.3983 \\ 2.99353 + 0.3983 \\ 2.99353 + 0.3983 \\ 2.99353 + 0.3983 \\ 2.99353 + 0.3983 \\ 2.99353 + 0.3983 \\ 2.99353 + 0.3983 \\ 2.99353 + 0.3983 \\ 2.99353 + 0.3983 \\ 2.99353 + 0.3983 \\ 2.99353 + 0.3983 \\ 2.99353 + 0.3983 \\ 2.99353 + 0.3983 \\ 2.99353 + 0.3983 \\ 2.99353 + 0.3983 \\ 2.99353 + 0.3983 \\ 2.99353 + 0.00 \\ 3.99353 + 0.3983 \\ 3.99353 + 0.3983 \\ 3.99353 + 0.3983 \\ 3.99353 + 0.3983 \\ 3.99353 + 0.3983 \\ 3.99353 + 0.3983 \\ 3.99353 + 0.3983 \\ 3.99353 + 0.3983 \\ 3.99353 + 0.3983 \\ 3.99353 + 0.3983 \\ 3.99353 + 0.3983 \\ 3.99353 + 0.3983 \\ 3.99353 + 0.3983 \\ 3.99353 + 0.3983 \\ 3.99353 + 0.3983 \\ 3.99353 + 0.3983 \\ 3.99353 + 0.3983 \\ 3.99353 + 0.3983 \\ 3.99353 + 0.3983 \\ 3.99353 + 0.398$$

$$\varphi_{5}(9) = \max \left\{ \begin{array}{l} 0.0 + 16.0586 \\ 0.0333 + 14.658 \\ 0.5991 + 12.863 \\ 1.5934 + 10.0554 \\ 2.3759 + 8.6786 \\ 2.7792 + 7.38 \\ 2.9838 + 3.1718 \\ 2.9965 + 0.3983 \\ 2.9993 + 0.0 \end{array} \right\} = 16.0586, \quad x_{5}^{0} = 0$$

$$\varphi_{5}(10) = \max \left\{ \begin{array}{l} 0.0 + 16.9127 \\ 0.0333 + 16.0586 \\ 0.5991 + 14.658 \\ 1.5934 + 12.863 \\ 2.3759 + 10.0554 \\ 2.7792 + 8.6786 \\ 2.9353 + 7.38 \\ 2.9933 + 0.3983 \\ 2.9993 + 0.3983 \\ 2.9999 + 0.0 \end{array} \right\} = 16.9127, \quad x_{5}^{0} = 0$$

$$\varphi_{5}(11) = \max \left\{ \begin{array}{l} 0.0 + 18.3951 \\ 0.0333 + 16.9127 \\ 0.5991 + 16.0586 \\ 1.5934 + 14.658 \\ 2.3759 + 12.863 \\ 2.3759 + 12.863 \\ 2.7792 + 10.0554 \\ 2.9353 + 8.6786 \\ 2.9353 + 8.6786 \\ 2.9838 + 7.38 \\ 2.9965 + 5.9794 \\ 2.9933 + 3.1718 \\ 2.9999 + 0.3983 \\ 3.0 + 0.0 \end{array} \right\} = 18.3951, \quad x_{5}^{0} = 0$$

```
0.0 + 19.7957
                  0.0333 + 18.3951
                  0.5991 + 16.9127
                  1.5934 + 16.0586
                  2.3759 + 14.658
                  2.7792 + 12.863
\varphi_5(12) = \max
                                       = 19.7957, \quad x_5^0 = 0
                  2.9353 + 10.0554
                  2.9838 + 8.6786
                   2.9965 + 7.38
                  2.9993 + 5.9794
                  2.9999 + 3.1718
                    3.0 + 0.3983
                      3.0 + 0.0
                   0.0 + 20.6711
                  0.0333 + 19.7957
                  0.5991 + 18.3951
                  1.5934 + 16.9127
                  2.3759 + 16.0586
                  2.7792 + 14.658
                  2.9353 + 12.863
                                       =20.6711, \quad x_5^0=0
\varphi_5(13) = \max
                  2.9838 + 10.0554
                  2.9965 + 8.6786
                   2.9993 + 7.38
                  2.9999 + 5.9794
                    3.0 + 3.1718
                    3.0 + 0.3983
                      3.0 + 0.0
                   0.0 + 21.5252
                  0.0333 + 20.6711
                  0.5991 + 19.7957
                  1.5934 + 18.3951
                  2.3759 + 16.9127
                  2.7792 + 16.0586
                  2.9353 + 14.658
\varphi_5(14) = \max
                  2.9838 + 12.863
                                       =21.5252, \quad x_5^0=0
                  2.9965 + 10.0554
                  2.9993 + 8.6786
                   2.9999 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.1718
                    3.0 + 0.3983
                      3.0 + 0.0
```

```
0.0 + 22.1983
                  0.0333 + 21.5252
                  0.5991 + 20.6711
                  1.5934 + 19.7957
                  2.3759 + 18.3951
                  2.7792 + 16.9127
                  2.9353 + 16.0586
                  2.9838 + 14.658
\varphi_5(15) = \max
                                       =22.1983, \quad x_5^0=0
                  2.9965 + 12.863
                  2.9993 + 10.0554
                  2.9999 + 8.6786
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.1718
                    3.0 + 0.3983
                      3.0 + 0.0
                    0.0 + 23.1571
                  0.0333 + 22.1983
                  0.5991 + 21.5252
                  1.5934 + 20.6711
                  2.3759 + 19.7957
                  2.7792 + 18.3951
                  2.9353 + 16.9127
                  2.9838 + 16.0586
\varphi_5(16) = \max \langle
                  2.9965 + 14.658
                                       =23.1571, \quad x_5^0=0
                  2.9993 + 12.863
                  2.9999 + 10.0554
                    3.0 + 8.6786
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.1718
                    3.0 + 0.3983
                      3.0 + 0.0
```

```
0.0 + 24.0325
                  0.0333 + 23.1571
                  0.5991 + 22.1983
                  1.5934 + 21.5252
                  2.3759 + 20.6711
                  2.7792 + 19.7957
                  2.9353 + 18.3951
                  2.9838 + 16.9127
                  2.9965 + 16.0586
                                       = 24.0325,
                                                   x_5^0 = 0
\varphi_5(17) = \max
                  2.9993 + 14.658
                  2.9999 + 12.863
                   3.0 + 10.0554
                    3.0 + 8.6786
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.1718
                    3.0 + 0.3983
                      3.0 + 0.0
                   0.0 + 24.8866
                  0.0333 + 24.0325
                  0.5991 + 23.1571
                  1.5934 + 22.1983
                  2.3759 + 21.5252
                  2.7792 + 20.6711
                  2.9353 + 19.7957
                  2.9838 + 18.3951
                  2.9965 + 16.9127
\varphi_5(18) = \max \langle
                                       = 24.8866, \quad x_5^0 = 0
                  2.9993 + 16.0586
                  2.9999 + 14.658
                    3.0 + 12.863
                   3.0 + 10.0554
                    3.0 + 8.6786
                     3.0+7.38
                    3.0 + 5.9794
                    3.0 + 3.1718
                    3.0 + 0.3983
                      3.0 + 0.0
```

```
0.0 + 25.357
                  0.0333 + 24.8866
                  0.5991 + 24.0325
                  1.5934 + 23.1571
                  2.3759 + 22.1983
                  2.7792 + 21.5252
                  2.9353 + 20.6711
                  2.9838 + 19.7957
                  2.9965 + 18.3951
                  2.9993 + 16.9127
                                       = 25.357, \quad x_5^0 = 0
\varphi_5(19) = \max
                  2.9999 + 16.0586
                    3.0 + 14.658
                    3.0 + 12.863
                   3.0 + 10.0554
                    3.0 + 8.6786
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.1718
                    3.0 + 0.3983
                      3.0 + 0.0
                   0.0 + 25.7931
                  0.0333 + 25.357
                  0.5991 + 24.8866
                  1.5934 + 24.0325
                  2.3759 + 23.1571
                  2.7792 + 22.1983
                  2.9353 + 21.5252
                  2.9838 + 20.6711
                  2.9965 + 19.7957
                  2.9993 + 18.3951
                                       = 25.7931, \quad x_5^0 = 0
\varphi_5(20) = \max
                  2.9999 + 16.9127
                   3.0 + 16.0586
                    3.0 + 14.658
                    3.0 + 12.863
                   3.0 + 10.0554
                    3.0 + 8.6786
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.1718
                    3.0 + 0.3983
                      3.0 + 0.0
```

```
0.0 + 26.119
                  0.0333 + 25.7931
                  0.5991 + 25.357
                  1.5934 + 24.8866
                  2.3759 + 24.0325
                  2.7792 + 23.1571
                  2.9353 + 22.1983
                  2.9838 + 21.5252
                  2.9965 + 20.6711
                  2.9993 + 19.7957
                  2.9999 + 18.3951
                                       = 26.48, \quad x_5^0 = 3
\varphi_5(21) = \max
                   3.0 + 16.9127
                   3.0 + 16.0586
                    3.0 + 14.658
                    3.0 + 12.863
                   3.0 + 10.0554
                    3.0 + 8.6786
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.1718
                    3.0 + 0.3983
                      3.0 + 0.0
                    0.0 + 26.413
                  0.0333 + 26.119
                  0.5991 + 25.7931
                  1.5934 + 25.357
                  2.3759 + 24.8866
                  2.7792 + 24.0325
                  2.9353 + 23.1571
                  2.9838 + 22.1983
                  2.9965 + 21.5252
                  2.9993 + 20.6711
                  2.9999 + 19.7957
\varphi_5(22) = \max
                                                   x_5^0 = 4
                                       = 27.2625,
                   3.0 + 18.3951
                   3.0 + 16.9127
                   3.0 + 16.0586
                    3.0 + 14.658
                    3.0 + 12.863
                   3.0 + 10.0554
                    3.0 + 8.6786
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.1718
                    3.0 + 0.3983
                      3.0 + 0.0
```

```
0.0 + 26.5624
                  0.0333 + 26.413
                  0.5991 + 26.119
                 1.5934 + 25.7931
                  2.3759 + 25.357
                 2.7792 + 24.8866
                 2.9353 + 24.0325
                 2.9838 + 23.1571
                 2.9965 + 22.1983
                 2.9993 + 21.5252
                 2.9999 + 20.6711
                   3.0 + 19.7957
                                      = 27.7329, \quad x_5^0 = 4
\varphi_5(23) = \max
                   3.0 + 18.3951
                   3.0 + 16.9127
                   3.0 + 16.0586
                    3.0 + 14.658
                    3.0 + 12.863
                   3.0 + 10.0554
                   3.0 + 8.6786
                    3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.1718
                    3.0 + 0.3983
                     3.0 + 0.0
```

```
0.0 + 26.6823
                  0.0333 + 26.5624
                  0.5991 + 26.413
                  1.5934 + 26.119
                  2.3759 + 25.7931
                  2.7792 + 25.357
                  2.9353 + 24.8866
                  2.9838 + 24.0325
                  2.9965 + 23.1571
                  2.9993 + 22.1983
                  2.9999 + 21.5252
                    3.0 + 20.6711
                                       = 28.169, \quad x_5^0 = 4
\varphi_5(24) = \max \langle
                    3.0 + 19.7957
                    3.0 + 18.3951
                    3.0 + 16.9127
                    3.0 + 16.0586
                    3.0 + 14.658
                    3.0 + 12.863
                    3.0 + 10.0554
                    3.0 + 8.6786
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.1718
                    3.0 + 0.3983
                      3.0 + 0.0
```

```
0.0 + 26.7864
                 0.0333 + 26.6823
                 0.5991 + 26.5624
                  1.5934 + 26.413
                  2.3759 + 26.119
                 2.7792 + 25.7931
                  2.9353 + 25.357
                 2.9838 + 24.8866
                 2.9965 + 24.0325
                 2.9993 + 23.1571
                 2.9999 + 22.1983
                   3.0 + 21.5252
                   3.0 + 20.6711
                                      =28.5723, \quad x_5^0=5
\varphi_5(25) = \max
                   3.0 + 19.7957
                   3.0 + 18.3951
                   3.0 + 16.9127
                   3.0 + 16.0586
                    3.0 + 14.658
                    3.0 + 12.863
                   3.0 + 10.0554
                    3.0 + 8.6786
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.1718
                    3.0 + 0.3983
                     3.0 + 0.0
```

```
0.0 + 26.8613
                 0.0333 + 26.7864
                 0.5991 + 26.6823
                 1.5934 + 26.5624
                  2.3759 + 26.413
                  2.7792 + 26.119
                 2.9353 + 25.7931
                  2.9838 + 25.357
                 2.9965 + 24.8866
                 2.9993 + 24.0325
                 2.9999 + 23.1571
                   3.0 + 22.1983
                   3.0 + 21.5252
\varphi_5(26) = \max
                   3.0 + 20.6711
                                      =28.8982,\quad x_5^0=5
                   3.0 + 19.7957
                   3.0 + 18.3951
                   3.0 + 16.9127
                   3.0 + 16.0586
                   3.0 + 14.658
                   3.0 + 12.863
                   3.0 + 10.0554
                   3.0 + 8.6786
                    3.0 + 7.38
                   3.0 + 5.9794
                   3.0 + 3.1718
                   3.0 + 0.3983
                     3.0 + 0.0
```

```
0.0 + 26.9026
                 0.0333 + 26.8613
                 0.5991 + 26.7864
                 1.5934 + 26.6823
                 2.3759 + 26.5624
                  2.7792 + 26.413
                  2.9353 + 26.119
                 2.9838 + 25.7931
                  2.9965 + 25.357
                 2.9993 + 24.8866
                 2.9999 + 24.0325
                   3.0 + 23.1571
                   3.0 + 22.1983
                   3.0 + 21.5252
                                      = 29.1922, \quad x_5^0 = 5
\varphi_5(27) = \max
                   3.0 + 20.6711
                   3.0 + 19.7957
                   3.0 + 18.3951
                   3.0 + 16.9127
                   3.0 + 16.0586
                    3.0 + 14.658
                    3.0 + 12.863
                   3.0 + 10.0554
                    3.0 + 8.6786
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.1718
                    3.0 + 0.3983
                     3.0 + 0.0
```

```
0.0 + 26.9312
                  0.0333 + 26.9026
                  0.5991 + 26.8613
                  1.5934 + 26.7864
                  2.3759 + 26.6823
                  2.7792 + 26.5624
                  2.9353 + 26.413
                  2.9838 + 26.119
                  2.9965 + 25.7931
                  2.9993 + 25.357
                  2.9999 + 24.8866
                   3.0 + 24.0325
                   3.0 + 23.1571
                   3.0 + 22.1983
                                      = 29.3483, \quad x_5^0 = 6
\varphi_5(28) = \max
                   3.0 + 21.5252
                   3.0 + 20.6711
                   3.0 + 19.7957
                   3.0 + 18.3951
                   3.0 + 16.9127
                   3.0 + 16.0586
                    3.0 + 14.658
                    3.0 + 12.863
                   3.0 + 10.0554
                    3.0 + 8.6786
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.1718
                    3.0 + 0.3983
                      3.0 + 0.0
```

```
0.0 + 26.9559
                 0.0333 + 26.9312
                 0.5991 + 26.9026
                 1.5934 + 26.8613
                 2.3759 + 26.7864
                 2.7792 + 26.6823
                 2.9353 + 26.5624
                  2.9838 + 26.413
                  2.9965 + 26.119
                 2.9993 + 25.7931
                  2.9999 + 25.357
                   3.0 + 24.8866
                   3.0 + 24.0325
                   3.0 + 23.1571
                   3.0 + 22.1983
\varphi_5(29) = \max
                                      = 29.4977, \quad x_5^0 = 6
                   3.0 + 21.5252
                   3.0 + 20.6711
                   3.0 + 19.7957
                   3.0 + 18.3951
                   3.0 + 16.9127
                   3.0 + 16.0586
                    3.0 + 14.658
                    3.0 + 12.863
                   3.0 + 10.0554
                    3.0 + 8.6786
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.1718
                    3.0 + 0.3983
                      3.0 + 0.0
```

```
0.0 + 26.9714
                 0.0333 + 26.9559
                 0.5991 + 26.9312
                 1.5934 + 26.9026
                 2.3759 + 26.8613
                 2.7792 + 26.7864
                 2.9353 + 26.6823
                 2.9838 + 26.5624
                  2.9965 + 26.413
                  2.9993 + 26.119
                 2.9999 + 25.7931
                    3.0 + 25.357
                   3.0 + 24.8866
                   3.0 + 24.0325
                   3.0 + 23.1571
                                      = 29.6176, \quad x_5^0 = 6
\varphi_5(30) = \max
                   3.0 + 22.1983
                   3.0 + 21.5252
                   3.0 + 20.6711
                   3.0 + 19.7957
                   3.0 + 18.3951
                   3.0 + 16.9127
                   3.0 + 16.0586
                    3.0 + 14.658
                    3.0 + 12.863
                   3.0 + 10.0554
                   3.0 + 8.6786
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.1718
                    3.0 + 0.3983
                     3.0 + 0.0
```

```
0.0 + 26.9809
                 0.0333 + 26.9714
                 0.5991 + 26.9559
                 1.5934 + 26.9312
                 2.3759 + 26.9026
                 2.7792 + 26.8613
                 2.9353 + 26.7864
                 2.9838 + 26.6823
                 2.9965 + 26.5624
                  2.9993 + 26.413
                  2.9999 + 26.119
                   3.0 + 25.7931
                   3.0 + 25.357
                   3.0 + 24.8866
                   3.0 + 24.0325
                   3.0 + 23.1571
                                      = 29.7217, \quad x_5^0 = 6
\varphi_5(31) = \max
                   3.0 + 22.1983
                   3.0 + 21.5252
                   3.0 + 20.6711
                   3.0 + 19.7957
                   3.0 + 18.3951
                   3.0 + 16.9127
                   3.0 + 16.0586
                    3.0 + 14.658
                    3.0 + 12.863
                   3.0 + 10.0554
                   3.0 + 8.6786
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.1718
                    3.0 + 0.3983
                     3.0 + 0.0
```

```
0.0 + 26.9878
                 0.0333 + 26.9809
                 0.5991 + 26.9714
                 1.5934 + 26.9559
                 2.3759 + 26.9312
                 2.7792 + 26.9026
                 2.9353 + 26.8613
                 2.9838 + 26.7864
                 2.9965 + 26.6823
                 2.9993 + 26.5624
                  2.9999 + 26.413
                   3.0 + 26.119
                   3.0 + 25.7931
                   3.0 + 25.357
                   3.0 + 24.8866
                   3.0 + 24.0325
                                                   x_5^0 = 6
\varphi_5(32) = \max
                   3.0 + 23.1571
                                      = 29.7966,
                   3.0 + 22.1983
                   3.0 + 21.5252
                   3.0 + 20.6711
                   3.0 + 19.7957
                   3.0 + 18.3951
                   3.0 + 16.9127
                   3.0 + 16.0586
                   3.0 + 14.658
                   3.0 + 12.863
                   3.0 + 10.0554
                   3.0 + 8.6786
                     3.0 + 7.38
                   3.0 + 5.9794
                   3.0 + 3.1718
                   3.0 + 0.3983
                     3.0 + 0.0
```

```
0.0 + 26.9921
                 0.0333 + 26.9878
                 0.5991 + 26.9809
                 1.5934 + 26.9714
                 2.3759 + 26.9559
                 2.7792 + 26.9312
                 2.9353 + 26.9026
                 2.9838 + 26.8613
                 2.9965 + 26.7864
                 2.9993 + 26.6823
                 2.9999 + 26.5624
                    3.0 + 26.413
                    3.0 + 26.119
                   3.0 + 25.7931
                    3.0 + 25.357
                   3.0 + 24.8866
                   3.0 + 24.0325
\varphi_5(33) = \max
                                      = 29.8451, \quad x_5^0 = 7
                   3.0 + 23.1571
                   3.0 + 22.1983
                   3.0 + 21.5252
                   3.0 + 20.6711
                   3.0 + 19.7957
                   3.0 + 18.3951
                   3.0 + 16.9127
                   3.0 + 16.0586
                    3.0 + 14.658
                    3.0 + 12.863
                   3.0 + 10.0554
                    3.0 + 8.6786
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.1718
                    3.0 + 0.3983
                     3.0 + 0.0
```

```
0.0 + 26.9947
                 0.0333 + 26.9921
                 0.5991 + 26.9878
                 1.5934 + 26.9809
                 2.3759 + 26.9714
                 2.7792 + 26.9559
                 2.9353 + 26.9312
                 2.9838 + 26.9026
                 2.9965 + 26.8613
                 2.9993 + 26.7864
                 2.9999 + 26.6823
                   3.0 + 26.5624
                    3.0 + 26.413
                    3.0 + 26.119
                   3.0 + 25.7931
                   3.0 + 25.357
                   3.0 + 24.8866
\varphi_5(34) = \max
                                      = 29.8864, \quad x_5^0 = 7
                   3.0 + 24.0325
                   3.0 + 23.1571
                   3.0 + 22.1983
                   3.0 + 21.5252
                   3.0 + 20.6711
                   3.0 + 19.7957
                   3.0 + 18.3951
                   3.0 + 16.9127
                   3.0 + 16.0586
                   3.0 + 14.658
                    3.0 + 12.863
                   3.0 + 10.0554
                    3.0 + 8.6786
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.1718
                    3.0 + 0.3983
                     3.0 + 0.0
```

```
0.0 + 26.9966
                 0.0333 + 26.9947
                 0.5991 + 26.9921
                 1.5934 + 26.9878
                 2.3759 + 26.9809
                 2.7792 + 26.9714
                 2.9353 + 26.9559
                 2.9838 + 26.9312
                 2.9965 + 26.9026
                 2.9993 + 26.8613
                 2.9999 + 26.7864
                   3.0 + 26.6823
                   3.0 + 26.5624
                    3.0 + 26.413
                    3.0 + 26.119
                   3.0 + 25.7931
                   3.0 + 25.357
                   3.0 + 24.8866
                                      = 29.915, \quad x_5^0 = 7
\varphi_5(35) = \max
                   3.0 + 24.0325
                   3.0 + 23.1571
                   3.0 + 22.1983
                   3.0 + 21.5252
                   3.0 + 20.6711
                   3.0 + 19.7957
                   3.0 + 18.3951
                   3.0 + 16.9127
                   3.0 + 16.0586
                    3.0 + 14.658
                    3.0 + 12.863
                   3.0 + 10.0554
                    3.0 + 8.6786
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.1718
                    3.0 + 0.3983
                     3.0 + 0.0
```

```
0.0 + 26.9981
                 0.0333 + 26.9966
                 0.5991 + 26.9947
                 1.5934 + 26.9921
                 2.3759 + 26.9878
                 2.7792 + 26.9809
                 2.9353 + 26.9714
                 2.9838 + 26.9559
                 2.9965 + 26.9312
                 2.9993 + 26.9026
                 2.9999 + 26.8613
                   3.0 + 26.7864
                   3.0 + 26.6823
                   3.0 + 26.5624
                    3.0 + 26.413
                    3.0 + 26.119
                   3.0 + 25.7931
                   3.0 + 25.357
\varphi_5(36) = \max
                   3.0 + 24.8866
                                      = 29.9397,
                                                  x_5^0 = 7
                   3.0 + 24.0325
                   3.0 + 23.1571
                   3.0 + 22.1983
                   3.0 + 21.5252
                   3.0 + 20.6711
                   3.0 + 19.7957
                   3.0 + 18.3951
                   3.0 + 16.9127
                   3.0 + 16.0586
                    3.0 + 14.658
                    3.0 + 12.863
                   3.0 + 10.0554
                    3.0 + 8.6786
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.1718
                    3.0 + 0.3983
                     3.0 + 0.0
```

## 6 Product 6

$$\varphi_6(0) = \max\{0.0\} = 0.0, x_6^0 = 0$$

$$\varphi_{6}(1) = \max \left\{ \begin{array}{l} 0.0 + 0.3983 \\ 0.5746 + 0.0 \end{array} \right\} = 0.5746, \quad x_{6}^{0} = 1 \\ \varphi_{6}(2) = \max \left\{ \begin{array}{l} 0.0 + 3.1718 \\ 0.5746 + 0.3983 \\ 3.4365 + 0.0 \end{array} \right\} = 3.4365, \quad x_{6}^{0} = 2 \\ \varphi_{6}(3) = \max \left\{ \begin{array}{l} 0.0 + 5.9794 \\ 0.5746 + 3.1718 \\ 3.4365 + 0.3983 \\ 5.7348 + 0.0 \end{array} \right\} = 5.9794, \quad x_{6}^{0} = 0 \\ \varphi_{6}(4) = \max \left\{ \begin{array}{l} 0.0 + 7.38 \\ 0.5746 + 5.9794 \\ 3.4365 + 3.1718 \\ 5.7348 + 0.3983 \\ 6.6735 + 0.0 \end{array} \right\} = 7.38, \quad x_{6}^{0} = 0 \\ \varphi_{6}(5) = \max \left\{ \begin{array}{l} 0.0 + 8.6786 \\ 0.5746 + 7.38 \\ 3.4365 + 5.9794 \\ 5.7348 + 3.1718 \\ 6.6735 + 0.3983 \\ 6.934 + 0.0 \end{array} \right\} = 9.4159, \quad x_{6}^{0} = 2 \\ \varphi_{6}(6) = \max \left\{ \begin{array}{l} 0.0 + 10.0554 \\ 0.5746 + 8.6786 \\ 3.4365 + 7.38 \\ 5.7348 + 5.9794 \\ 6.6735 + 3.1718 \\ 6.934 + 0.3983 \\ 6.989 + 0.0 \end{array} \right\} = 11.7142, \quad x_{6}^{0} = 3 \\ \varphi_{6}(7) = \max \left\{ \begin{array}{l} 0.0 + 12.863 \\ 0.5746 + 10.0554 \\ 3.4365 + 8.6786 \\ 3.4365 + 8.6786 \\ 5.7348 + 7.38 \\ 6.6735 + 5.9794 \\ 6.934 + 3.1718 \\ 6.989 + 0.3983 \\ 6.9985 + 0.0 \end{array} \right\} = 13.1148, \quad x_{6}^{0} = 3 \\ \varphi_{6}(8) = \max \left\{ \begin{array}{l} 0.0 + 12.863 \\ 0.5746 + 10.0554 \\ 3.4365 + 8.6786 \\ 5.7348 + 7.38 \\ 6.934 + 3.1718 \\ 6.9985 + 0.0 \\ 0.0 + 14.658 \\ 0.5746 + 12.863 \\ 3.4365 + 10.0554 \\ 5.7348 + 8.6786 \\ 6.6735 + 7.38 \\ 6.934 + 5.9794 \\ 6.934 + 5.9794 \\ 6.989 + 3.1718 \\ 6.9985 + 0.3983 \\ 6.9985 + 0.3983 \\ 6.9985 + 0.3983 \\ 6.9985 + 0.3983 \\ 6.9985 + 0.3983 \\ 6.9985 + 0.3983 \\ 6.9985 + 0.3983 \\ 6.9998 + 0.0 \end{array} \right\} = 14.658, \quad x_{6}^{0} = 0$$

$$\varphi_{6}(9) = \max \left\{ \begin{array}{l} 0.0 + 16.0586 \\ 0.5746 + 14.658 \\ 3.4365 + 12.863 \\ 5.7348 + 10.0554 \\ 6.6735 + 8.6786 \\ 6.934 + 7.38 \\ 6.989 + 5.9794 \\ 6.9998 + 0.3983 \\ 7.0 + 0.0 \end{array} \right\} = 16.2995, \quad x_{6}^{0} = 2$$

$$\left\{ \begin{array}{l} 0.0 + 16.9127 \\ 0.5746 + 16.0586 \\ 3.4365 + 14.658 \\ 5.7348 + 12.863 \\ 6.6735 + 10.0554 \\ 6.934 + 8.6786 \\ 6.989 + 7.38 \\ 6.9985 + 5.9794 \\ 6.9998 + 3.1718 \\ 7.0 + 0.3983 \\ 7.0 + 0.0 \end{array} \right\} = 18.5978, \quad x_{6}^{0} = 3$$

$$\left\{ \begin{array}{l} 0.0 + 18.3951 \\ 0.5746 + 16.9127 \\ 3.4365 + 16.0586 \\ 5.7348 + 14.658 \\ 6.6735 + 12.863 \\ 6.934 + 10.0554 \\ 6.989 + 8.6786 \\ 6.9985 + 7.38 \\ 6.9998 + 5.9794 \\ 7.0 + 3.1718 \\ 7.0 + 0.3983 \\ 7.0 + 0.0 \end{array} \right\} = 20.3928, \quad x_{6}^{0} = 3$$

```
0.0 + 19.7957
                  0.5746 + 18.3951
                  3.4365 + 16.9127
                  5.7348 + 16.0586
                  6.6735 + 14.658
                   6.934 + 12.863
\varphi_6(12) = \max
                                       = 21.7934, \quad x_6^0 = 3
                   6.989 + 10.0554
                   6.9985 + 8.6786
                    6.9998 + 7.38
                    7.0 + 5.9794
                    7.0 + 3.1718
                    7.0 + 0.3983
                      7.0 + 0.0
                    0.0 + 20.6711
                  0.5746 + 19.7957
                  3.4365 + 18.3951
                  5.7348 + 16.9127
                  6.6735 + 16.0586
                   6.934 + 14.658
                   6.989 + 12.863
                                       =22.7321, \quad x_6^0=4
\varphi_6(13) = \max
                  6.9985 + 10.0554
                  6.9998 + 8.6786
                     7.0 + 7.38
                    7.0 + 5.9794
                    7.0 + 3.1718
                    7.0 + 0.3983
                      7.0 + 0.0
                    0.0 + 21.5252
                  0.5746 + 20.6711
                  3.4365 + 19.7957
                  5.7348 + 18.3951
                  6.6735 + 16.9127
                  6.934+16.0586
                   6.989 + 14.658
\varphi_6(14) = \max
                   6.9985 + 12.863
                                       = 24.1299, \quad x_6^0 = 3
                  6.9998 + 10.0554
                    7.0 + 8.6786
                     7.0 + 7.38
                    7.0 + 5.9794
                    7.0 + 3.1718
                    7.0 + 0.3983
                      7.0 + 0.0
```

```
0.0 + 22.1983
                  0.5746 + 21.5252
                  3.4365 + 20.6711
                  5.7348 + 19.7957
                  6.6735 + 18.3951
                   6.934 + 16.9127
                   6.989 + 16.0586
                   6.9985 + 14.658
\varphi_6(15) = \max
                                        = 25.5305, \quad x_6^0 = 3
                   6.9998 + 12.863
                    7.0 + 10.0554
                    7.0 + 8.6786
                     7.0 + 7.38
                    7.0 + 5.9794
                    7.0 + 3.1718
                    7.0 + 0.3983
                      7.0 + 0.0
                    0.0 + 23.1571
                  0.5746 + 22.1983
                  3.4365 + 21.5252
                  5.7348 + 20.6711
                  6.6735 + 19.7957
                   6.934 + 18.3951
                   6.989 + 16.9127
                  6.9985 + 16.0586
\varphi_6(16) = \max \epsilon
                   6.9998+14.658
                                        = 26.4692, \quad x_6^0 = 4
                    7.0 + 12.863
                    7.0 + 10.0554
                    7.0 + 8.6786
                     7.0 + 7.38
                    7.0 + 5.9794
                    7.0 + 3.1718
                    7.0 + 0.3983
                      7.0 + 0.0
```

```
0.0 + 24.0325
                  0.5746 + 23.1571
                  3.4365 + 22.1983
                  5.7348 + 21.5252
                  6.6735 + 20.6711
                  6.934 + 19.7957
                  6.989 + 18.3951
                  6.9985 + 16.9127
                  6.9998 + 16.0586
                                       = 27.3446, \quad x_6^0 = 4
\varphi_6(17) = \max
                    7.0 + 14.658
                    7.0 + 12.863
                    7.0 + 10.0554
                    7.0 + 8.6786
                     7.0 + 7.38
                    7.0 + 5.9794
                    7.0 + 3.1718
                    7.0 + 0.3983
                      7.0 + 0.0
                    0.0 + 24.8866
                  0.5746 + 24.0325
                  3.4365 + 23.1571
                  5.7348 + 22.1983
                  6.6735 + 21.5252
                  6.934 + 20.6711
                  6.989 + 19.7957
                  6.9985 + 18.3951
                  6.9998 + 16.9127
                                       = 28.1987, \quad x_6^0 = 4
\varphi_6(18) = \max
                    7.0 + 16.0586
                    7.0 + 14.658
                    7.0 + 12.863
                    7.0 + 10.0554
                    7.0 + 8.6786
                     7.0+7.38
                    7.0 + 5.9794
                    7.0 + 3.1718
                    7.0 + 0.3983
                      7.0 + 0.0
```

```
0.0 + 25.357
                  0.5746 + 24.8866
                  3.4365 + 24.0325
                  5.7348 + 23.1571
                  6.6735 + 22.1983
                  6.934 + 21.5252
                  6.989 + 20.6711
                  6.9985 + 19.7957
                  6.9998 + 18.3951
                   7.0 + 16.9127
\varphi_6(19) = \max
                                       =28.8919, \quad x_6^0=3
                   7.0 + 16.0586
                    7.0 + 14.658
                    7.0 + 12.863
                   7.0 + 10.0554
                    7.0 + 8.6786
                     7.0 + 7.38
                    7.0 + 5.9794
                    7.0 + 3.1718
                    7.0 + 0.3983
                      7.0 + 0.0
                   0.0 + 25.7931
                  0.5746 + 25.357
                  3.4365 + 24.8866
                  5.7348 + 24.0325
                  6.6735 + 23.1571
                  6.934 + 22.1983
                  6.989 + 21.5252
                  6.9985 + 20.6711
                  6.9998 + 19.7957
                   7.0 + 18.3951
\varphi_6(20) = \max
                                       = 29.8306, \quad x_6^0 = 4
                   7.0 + 16.9127
                   7.0 + 16.0586
                    7.0 + 14.658
                    7.0 + 12.863
                   7.0 + 10.0554
                    7.0 + 8.6786
                     7.0 + 7.38
                    7.0 + 5.9794
                    7.0 + 3.1718
                    7.0 + 0.3983
                      7.0 + 0.0
```

```
0.0 + 26.48
                  0.5746 + 25.7931
                  3.4365 + 25.357
                  5.7348 + 24.8866
                  6.6735 + 24.0325
                  6.934 + 23.1571
                  6.989 + 22.1983
                  6.9985 + 21.5252
                  6.9998 + 20.6711
                   7.0 + 19.7957
                   7.0 + 18.3951
                                       = 30.706, \quad x_6^0 = 4
\varphi_6(21) = \max
                   7.0 + 16.9127
                    7.0 + 16.0586
                    7.0 + 14.658
                    7.0 + 12.863
                    7.0 + 10.0554
                    7.0 + 8.6786
                     7.0 + 7.38
                    7.0 + 5.9794
                    7.0 + 3.1718
                    7.0 + 0.3983
                      7.0 + 0.0
                   0.0 + 27.2625
                   0.5746 + 26.48
                  3.4365 + 25.7931
                  5.7348 + 25.357
                  6.6735 + 24.8866
                  6.934 + 24.0325
                  6.989 + 23.1571
                  6.9985 + 22.1983
                  6.9998 + 21.5252
                   7.0 + 20.6711
                   7.0 + 19.7957
\varphi_6(22) = \max
                                       = 31.5601, \quad x_6^0 = 4
                    7.0 + 18.3951
                    7.0 + 16.9127
                    7.0 + 16.0586
                    7.0 + 14.658
                    7.0 + 12.863
                    7.0 + 10.0554
                    7.0 + 8.6786
                     7.0 + 7.38
                    7.0 + 5.9794
                    7.0 + 3.1718
                    7.0 + 0.3983
                      7.0 + 0.0
```

```
0.0 + 27.7329
                  0.5746 + 27.2625
                   3.4365 + 26.48
                  5.7348 + 25.7931
                   6.6735 + 25.357
                   6.934 + 24.8866
                   6.989 + 24.0325
                  6.9985 + 23.1571
                  6.9998 + 22.1983
                    7.0 + 21.5252
                    7.0 + 20.6711
                    7.0 + 19.7957
                                        = 32.0305, \quad x_6^0 = 4
\varphi_6(23) = \max
                    7.0 + 18.3951
                    7.0 + 16.9127
                    7.0 + 16.0586
                    7.0 + 14.658
                    7.0 + 12.863
                    7.0 + 10.0554
                    7.0 + 8.6786
                     7.0 + 7.38
                    7.0 + 5.9794
                    7.0 + 3.1718
7.0 + 0.3983
                      7.0 + 0.0
```

```
0.0 + 28.169
                 0.5746 + 27.7329
                 3.4365 + 27.2625
                  5.7348 + 26.48
                 6.6735 + 25.7931
                  6.934 + 25.357
                  6.989 + 24.8866
                 6.9985 + 24.0325
                 6.9998 + 23.1571
                   7.0 + 22.1983
                   7.0 + 21.5252
                   7.0 + 20.6711
                                      =32.4666,\quad x_6^0=4
\varphi_6(24) = \max
                   7.0 + 19.7957
                   7.0 + 18.3951
                   7.0 + 16.9127
                   7.0 + 16.0586
                    7.0 + 14.658
                    7.0 + 12.863
                   7.0 + 10.0554
                    7.0 + 8.6786
                     7.0 + 7.38
                    7.0 + 5.9794
                    7.0 + 3.1718
                    7.0 + 0.3983
                     7.0 + 0.0
```

```
0.0 + 28.5723
                  0.5746 + 28.169
                 3.4365 + 27.7329
                 5.7348 + 27.2625
                  6.6735 + 26.48
                  6.934 + 25.7931
                  6.989 + 25.357
                 6.9985 + 24.8866
                 6.9998 + 24.0325
                   7.0 + 23.1571
                   7.0 + 22.1983
                   7.0 + 21.5252
                   7.0 + 20.6711
                                      = 33.1535, \quad x_6^0 = 4
\varphi_6(25) = \max
                   7.0 + 19.7957
                   7.0 + 18.3951
                   7.0 + 16.9127
                   7.0 + 16.0586
                    7.0 + 14.658
                   7.0 + 12.863
                   7.0 + 10.0554
                    7.0 + 8.6786
                     7.0+7.38
                    7.0 + 5.9794
                    7.0 + 3.1718
                    7.0 + 0.3983
                     7.0 + 0.0
```

```
0.0 + 28.8982
                  0.5746 + 28.5723
                   3.4365 + 28.169
                  5.7348 + 27.7329
                  6.6735 + 27.2625
                    6.934 + 26.48
                   6.989 + 25.7931
                   6.9985 + 25.357
                  6.9998 + 24.8866
                    7.0 + 24.0325
                    7.0 + 23.1571
                    7.0 + 22.1983
                    7.0 + 21.5252
                                        = 33.936, \quad x_6^0 = 4
\varphi_6(26) = \max
                    7.0 + 20.6711
                    7.0 + 19.7957
                    7.0 + 18.3951
                    7.0 + 16.9127
                    7.0 + 16.0586
                    7.0 + 14.658
                    7.0 + 12.863
                    7.0 + 10.0554
                    7.0 + 8.6786
                     7.0 + 7.38
                    7.0 + 5.9794
                    7.0 + 3.1718
7.0 + 0.3983
                      7.0 + 0.0
```

```
0.0 + 29.1922
                  0.5746 + 28.8982
                  3.4365 + 28.5723
                  5.7348 + 28.169
                  6.6735 + 27.7329
                  6.934 + 27.2625
                   6.989 + 26.48
                  6.9985 + 25.7931
                  6.9998 + 25.357
                   7.0 + 24.8866
                   7.0 + 24.0325
                   7.0 + 23.1571
                   7.0 + 22.1983
                   7.0 + 21.5252
\varphi_6(27) = \max
                                      = 34.4064, \quad x_6^0 = 4
                   7.0 + 20.6711
                   7.0 + 19.7957
                   7.0 + 18.3951
                   7.0 + 16.9127
                   7.0 + 16.0586
                    7.0 + 14.658
                    7.0 + 12.863
                   7.0 + 10.0554
                    7.0 + 8.6786
                     7.0 + 7.38
                    7.0 + 5.9794
                    7.0 + 3.1718
                    7.0 + 0.3983
                      7.0 + 0.0
```

```
0.0 + 29.3483
                 0.5746 + 29.1922
                 3.4365 + 28.8982
                 5.7348 + 28.5723
                  6.6735 + 28.169
                  6.934 + 27.7329
                  6.989 + 27.2625
                  6.9985 + 26.48
                 6.9998 + 25.7931
                   7.0 + 25.357
                   7.0 + 24.8866
                   7.0 + 24.0325
                   7.0 + 23.1571
                   7.0 + 22.1983
                                      = 34.8425, \quad x_6^0 = 4
\varphi_6(28) = \max
                   7.0 + 21.5252
                   7.0 + 20.6711
                   7.0 + 19.7957
                   7.0 + 18.3951
                   7.0 + 16.9127
                   7.0 + 16.0586
                    7.0 + 14.658
                    7.0 + 12.863
                   7.0 + 10.0554
                    7.0 + 8.6786
                     7.0 + 7.38
                    7.0 + 5.9794
                    7.0 + 3.1718
                    7.0 + 0.3983
                      7.0 + 0.0
```

```
0.0 + 29.4977
                 0.5746 + 29.3483
                 3.4365 + 29.1922
                 5.7348 + 28.8982
                 6.6735 + 28.5723
                  6.934 + 28.169
                  6.989 + 27.7329
                 6.9985 + 27.2625
                  6.9998 + 26.48
                   7.0 + 25.7931
                   7.0 + 25.357
                   7.0 + 24.8866
                   7.0 + 24.0325
                   7.0 + 23.1571
                   7.0 + 22.1983
\varphi_6(29) = \max
                                      = 35.2458, \quad x_6^0 = 4
                   7.0 + 21.5252
                   7.0 + 20.6711
                   7.0 + 19.7957
                   7.0 + 18.3951
                   7.0 + 16.9127
                   7.0 + 16.0586
                    7.0 + 14.658
                    7.0 + 12.863
                   7.0 + 10.0554
                    7.0 + 8.6786
                    7.0 + 7.38
                    7.0 + 5.9794
                    7.0 + 3.1718
                    7.0 + 0.3983
                      7.0 + 0.0
```

```
0.0 + 29.6176
                 0.5746 + 29.4977
                 3.4365 + 29.3483
                 5.7348 + 29.1922
                 6.6735 + 28.8982
                  6.934 + 28.5723
                  6.989 + 28.169
                 6.9985 + 27.7329
                 6.9998 + 27.2625
                    7.0 + 26.48
                   7.0 + 25.7931
                   7.0 + 25.357
                   7.0 + 24.8866
                   7.0 + 24.0325
                   7.0 + 23.1571
                                      =35.5717, \quad x_6^0=4
\varphi_6(30) = \max
                   7.0 + 22.1983
                   7.0 + 21.5252
                   7.0 + 20.6711
                   7.0 + 19.7957
                   7.0 + 18.3951
                   7.0 + 16.9127
                   7.0 + 16.0586
                    7.0 + 14.658
                    7.0 + 12.863
                   7.0 + 10.0554
                   7.0 + 8.6786
                     7.0 + 7.38
                    7.0 + 5.9794
                    7.0 + 3.1718
                    7.0 + 0.3983
                     7.0 + 0.0
```

```
0.0 + 29.7217
                 0.5746 + 29.6176
                 3.4365 + 29.4977
                 5.7348 + 29.3483
                 6.6735 + 29.1922
                  6.934 + 28.8982
                  6.989 + 28.5723
                  6.9985 + 28.169
                 6.9998 + 27.7329
                   7.0 + 27.2625
                    7.0 + 26.48
                   7.0 + 25.7931
                   7.0 + 25.357
                   7.0 + 24.8866
                   7.0 + 24.0325
                   7.0 + 23.1571
                                      = 35.8657, \quad x_6^0 = 4
\varphi_6(31) = \max
                   7.0 + 22.1983
                   7.0 + 21.5252
                   7.0 + 20.6711
                   7.0 + 19.7957
                   7.0 + 18.3951
                   7.0 + 16.9127
                   7.0 + 16.0586
                    7.0 + 14.658
                   7.0 + 12.863
                   7.0 + 10.0554
                    7.0 + 8.6786
                     7.0 + 7.38
                    7.0 + 5.9794
                    7.0 + 3.1718
                    7.0 + 0.3983
                     7.0 + 0.0
```

```
0.0 + 29.7966
                 0.5746 + 29.7217
                 3.4365 + 29.6176
                 5.7348 + 29.4977
                 6.6735 + 29.3483
                  6.934 + 29.1922
                  6.989 + 28.8982
                 6.9985 + 28.5723
                  6.9998 + 28.169
                   7.0 + 27.7329
                   7.0 + 27.2625
                    7.0 + 26.48
                   7.0 + 25.7931
                    7.0 + 25.357
                   7.0 + 24.8866
                   7.0 + 24.0325
                                      = 36.1262, \quad x_6^0 = 5
\varphi_6(32) = \max
                   7.0 + 23.1571
                   7.0 + 22.1983
                   7.0 + 21.5252
                   7.0 + 20.6711
                   7.0 + 19.7957
                   7.0 + 18.3951
                   7.0 + 16.9127
                   7.0 + 16.0586
                    7.0 + 14.658
                   7.0 + 12.863
                   7.0 + 10.0554
                    7.0 + 8.6786
                     7.0 + 7.38
                    7.0 + 5.9794
                    7.0 + 3.1718
                    7.0 + 0.3983
                     7.0 + 0.0
```

```
0.0 + 29.8451
                 0.5746 + 29.7966
                 3.4365 + 29.7217
                 5.7348 + 29.6176
                 6.6735 + 29.4977
                  6.934 + 29.3483
                  6.989 + 29.1922
                 6.9985 + 28.8982
                 6.9998 + 28.5723
                   7.0 + 28.169
                   7.0 + 27.7329
                   7.0 + 27.2625
                    7.0 + 26.48
                   7.0 + 25.7931
                   7.0 + 25.357
                   7.0 + 24.8866
                   7.0 + 24.0325
\varphi_6(33) = \max
                                      = 36.2823, \quad x_6^0 = 5
                   7.0 + 23.1571
                   7.0 + 22.1983
                   7.0 + 21.5252
                   7.0 + 20.6711
                   7.0 + 19.7957
                   7.0 + 18.3951
                   7.0 + 16.9127
                   7.0 + 16.0586
                   7.0 + 14.658
                   7.0 + 12.863
                   7.0 + 10.0554
                   7.0 + 8.6786
                     7.0 + 7.38
                   7.0 + 5.9794
                   7.0 + 3.1718
                   7.0 + 0.3983
                     7.0 + 0.0
```

```
0.0 + 29.8864
                 0.5746 + 29.8451
                 3.4365 + 29.7966
                 5.7348 + 29.7217
                 6.6735 + 29.6176
                  6.934 + 29.4977
                  6.989 + 29.3483
                 6.9985 + 29.1922
                 6.9998 + 28.8982
                   7.0 + 28.5723
                   7.0 + 28.169
                   7.0 + 27.7329
                   7.0 + 27.2625
                    7.0 + 26.48
                   7.0 + 25.7931
                   7.0 + 25.357
                   7.0 + 24.8866
\varphi_6(34) = \max
                                      = 36.4317, \quad x_6^0 = 5
                   7.0 + 24.0325
                   7.0 + 23.1571
                   7.0 + 22.1983
                   7.0 + 21.5252
                   7.0 + 20.6711
                   7.0 + 19.7957
                   7.0 + 18.3951
                   7.0 + 16.9127
                   7.0 + 16.0586
                    7.0 + 14.658
                   7.0 + 12.863
                   7.0 + 10.0554
                    7.0 + 8.6786
                     7.0 + 7.38
                    7.0 + 5.9794
                    7.0 + 3.1718
                    7.0 + 0.3983
                      7.0 + 0.0
```

```
0.0 + 29.915
                 0.5746 + 29.8864
                 3.4365 + 29.8451
                 5.7348 + 29.7966
                 6.6735 + 29.7217
                  6.934 + 29.6176
                  6.989 + 29.4977
                 6.9985 + 29.3483
                 6.9998 + 29.1922
                   7.0 + 28.8982
                   7.0 + 28.5723
                   7.0 + 28.169
                   7.0 + 27.7329
                   7.0 + 27.2625
                    7.0 + 26.48
                   7.0 + 25.7931
                   7.0 + 25.357
                   7.0 + 24.8866
                                      =36.5516,\quad x_6^0=5
\varphi_6(35) = \max
                   7.0 + 24.0325
                   7.0 + 23.1571
                   7.0 + 22.1983
                   7.0 + 21.5252
                   7.0 + 20.6711
                   7.0 + 19.7957
                   7.0 + 18.3951
                   7.0 + 16.9127
                   7.0 + 16.0586
                   7.0 + 14.658
                    7.0 + 12.863
                   7.0 + 10.0554
                    7.0 + 8.6786
                     7.0 + 7.38
                    7.0 + 5.9794
                    7.0 + 3.1718
                    7.0 + 0.3983
                     7.0 + 0.0
```

```
0.0 + 29.9397
                  0.5746 + 29.915
                  3.4365 + 29.8864
                  5.7348 + 29.8451
                  6.6735 + 29.7966
                  6.934 + 29.7217
                  6.989 + 29.6176
                  6.9985 + 29.4977
                  6.9998 + 29.3483
                   7.0 + 29.1922
                   7.0 + 28.8982
                   7.0 + 28.5723
                    7.0 + 28.169
                   7.0 + 27.7329
                   7.0 + 27.2625
                    7.0 + 26.48
                   7.0 + 25.7931
                    7.0 + 25.357
\varphi_6(36) = \max
                    7.0 + 24.8866
                                       = 36.6557, \quad x_6^0 = 5
                   7.0 + 24.0325
                    7.0 + 23.1571
                    7.0 + 22.1983
                    7.0 + 21.5252
                   7.0 + 20.6711
                   7.0 + 19.7957
                   7.0 + 18.3951
                   7.0 + 16.9127
                   7.0 + 16.0586
                    7.0 + 14.658
                    7.0 + 12.863
                   7.0 + 10.0554
                    7.0 + 8.6786
                     7.0 + 7.38
                    7.0 + 5.9794
                    7.0 + 3.1718
                    7.0 + 0.3983
                      7.0 + 0.0
```

## 7 Product 7

$$\varphi_7(0) = \max\{0.0\} = 0.0, x_7^0 = 0$$

$$\varphi_{7}(1) = \max \left\{ \begin{array}{l} 0.0 + 0.5746 \\ 0.0366 + 0.0 \end{array} \right\} = 0.5746, \quad x_{7}^{0} = 0$$

$$\varphi_{7}(2) = \max \left\{ \begin{array}{l} 0.0 + 3.4365 \\ 0.366 + 0.5746 \\ 0.5047 + 0.0 \end{array} \right\} = 3.4365, \quad x_{7}^{0} = 0$$

$$\varphi_{7}(3) = \max \left\{ \begin{array}{l} 0.0 + 5.9794 \\ 0.0366 + 3.4365 \\ 0.5047 + 0.5746 \\ 1.2013 + 0.0 \end{array} \right\} = 5.9794, \quad x_{7}^{0} = 0$$

$$\varphi_{7}(4) = \max \left\{ \begin{array}{l} 0.0 + 7.38 \\ 0.366 + 5.9794 \\ 0.5047 + 3.4365 \\ 1.2013 + 0.5746 \\ 1.6807 + 0.0 \end{array} \right\} = 7.38, \quad x_{7}^{0} = 0$$

$$\varphi_{7}(5) = \max \left\{ \begin{array}{l} 0.0 + 7.38 \\ 0.366 + 7.38 \\ 0.5047 + 5.9794 \\ 1.2013 + 3.4365 \\ 1.6807 + 0.5746 \\ 1.8987 + 0.0 \end{array} \right\} = 9.4159, \quad x_{7}^{0} = 0$$

$$\varphi_{7}(6) = \max \left\{ \begin{array}{l} 0.0 + 11.7142 \\ 0.0366 + 7.38 \\ 1.2013 + 3.4365 \\ 1.6807 + 7.38 \\ 1.2013 + 5.9794 \\ 1.6807 + 3.4365 \\ 1.9735 + 0.0 \end{array} \right\} = 11.7142, \quad x_{7}^{0} = 0$$

$$\varphi_{7}(7) = \max \left\{ \begin{array}{l} 0.0 + 11.7142 \\ 0.0366 + 9.4159 \\ 0.5047 + 7.38 \\ 1.6807 + 5.9794 \\ 1.8987 + 0.5746 \\ 1.9735 + 0.5746 \\ 1.9941 + 0.0 \end{array} \right\} = 13.1148, \quad x_{7}^{0} = 0$$

$$\varphi_{7}(8) = \max \left\{ \begin{array}{l} 0.0 + 13.1148 \\ 0.366 + 13.1148 \\ 0.366 + 13.1148 \\ 0.366 + 13.1148 \\ 0.366 + 13.1148 \\ 0.5047 + 11.7142 \\ 1.2013 + 9.4159 \\ 1.6807 + 7.38 \\ 1.6807 + 7.38 \\ 1.6807 + 7.38 \\ 1.6807 + 7.38 \\ 1.8987 + 5.9794 \\ 1.9735 + 3.4365 \\ 1.9941 + 0.0 \end{array} \right\} = 14.658, \quad x_{7}^{0} = 0$$

$$\varphi_{7}(8) = \max \left\{ \begin{array}{l} 1.6807 + 7.38 \\ 1.6807 + 7.38 \\ 1.6807 + 7.38 \\ 1.9941 + 0.0 \end{array} \right\} = 14.658, \quad x_{7}^{0} = 0$$

```
0.0 + 16.2995
                 0.0366 + 14.658
                 0.5047 + 13.1148
                 1.2013 + 11.7142
                 1.6807 + 9.4159
\varphi_7(9) = \max
                                      = 16.2995, \quad x_7^0 = 0
                  1.8987 + 7.38
                 1.9735 + 5.9794
                 1.9941 + 3.4365
                 1.9989 + 0.5746
                   1.9998 + 0.0
                   0.0 + 18.5978
                  0.0366 + 16.2995
                  0.5047 + 14.658
                  1.2013 + 13.1148
                  1.6807 + 11.7142
\varphi_7(10) = \max
                  1.8987 + 9.4159
                                       = 18.5978,
                                                    x_7^0 = 0
                   1.9735 + 7.38
                  1.9941 + 5.9794
                  1.9989 + 3.4365
                  1.9998 + 0.5746
                      2.0 + 0.0
                   0.0 + 20.3928
                  0.0366 + 18.5978
                  0.5047 + 16.2995
                  1.2013 + 14.658
                  1.6807 + 13.1148
                  1.8987 + 11.7142
                                                   x_7^0 = 0
\varphi_7(11) = \max
                                       =20.3928,
                  1.9735 + 9.4159
                   1.9941 + 7.38
                  1.9989 + 5.9794
                  1.9998 + 3.4365
                    2.0 + 0.5746
                      2.0 + 0.0
```

```
0.0 + 21.7934
                  0.0366 + 20.3928
                  0.5047 + 18.5978
                  1.2013 + 16.2995
                  1.6807 + 14.658
                  1.8987 + 13.1148
\varphi_7(12) = \max
                                       =21.7934, \quad x_7^0=0
                  1.9735 + 11.7142
                  1.9941 + 9.4159
                    1.9989 + 7.38
                  1.9998 + 5.9794
                    2.0 + 3.4365
                    2.0 + 0.5746
                      2.0 + 0.0
                    0.0 + 22.7321
                  0.0366 + 21.7934
                  0.5047 + 20.3928
                  1.2013 + 18.5978
                  1.6807 + 16.2995
                  1.8987 + 14.658
                  1.9735 + 13.1148
                                       =22.7321, \quad x_7^0=0
\varphi_7(13) = \max
                  1.9941 + 11.7142
                  1.9989 + 9.4159
                    1.9998 + 7.38
                    2.0 + 5.9794
                    2.0 + 3.4365
                    2.0 + 0.5746
                      2.0 + 0.0
                    0.0 + 24.1299
                  0.0366 + 22.7321
                  0.5047 + 21.7934
                  1.2013 + 20.3928
                  1.6807 + 18.5978
                  1.8987 + 16.2995
                  1.9735 + 14.658
\varphi_7(14) = \max
                                       = 24.1299, \quad x_7^0 = 0
                  1.9941 + 13.1148
                  1.9989 + 11.7142
                  1.9998 + 9.4159
                     2.0 + 7.38
                    2.0 + 5.9794
                    2.0 + 3.4365
                    2.0 + 0.5746
                      2.0 + 0.0
```

```
0.0 + 25.5305
                  0.0366 + 24.1299
                  0.5047 + 22.7321
                  1.2013 + 21.7934
                  1.6807 + 20.3928
                  1.8987 + 18.5978
                  1.9735 + 16.2995
                  1.9941 + 14.658
\varphi_7(15) = \max
                                       =25.5305,
                                                    x_7^0 = 0
                  1.9989 + 13.1148
                  1.9998 + 11.7142
                    2.0 + 9.4159
                     2.0 + 7.38
                    2.0 + 5.9794
                    2.0 + 3.4365
                    2.0 + 0.5746
                      2.0 + 0.0
                    0.0 + 26.4692
                  0.0366 + 25.5305
                  0.5047 + 24.1299
                  1.2013 + 22.7321
                  1.6807 + 21.7934
                  1.8987 + 20.3928
                  1.9735 + 18.5978
                  1.9941 + 16.2995
\varphi_7(16) = \max \langle
                  1.9989 + 14.658
                                       = 26.4692, \quad x_7^0 = 0
                  1.9998 + 13.1148
                    2.0 + 11.7142
                    2.0 + 9.4159
                     2.0 + 7.38
                    2.0 + 5.9794
                    2.0 + 3.4365
                    2.0 + 0.5746
                      2.0 + 0.0
```

```
0.0 + 27.3446
                 0.0366 + 26.4692
                 0.5047 + 25.5305
                 1.2013 + 24.1299
                 1.6807 + 22.7321
                 1.8987 + 21.7934
                 1.9735 + 20.3928
                 1.9941 + 18.5978
                 1.9989 + 16.2995
                                                  x_7^0 = 0
\varphi_7(17) = \max
                                      = 27.3446,
                  1.9998 + 14.658
                   2.0 + 13.1148
                   2.0 + 11.7142
                    2.0 + 9.4159
                     2.0 + 7.38
                    2.0 + 5.9794
                    2.0 + 3.4365
                    2.0 + 0.5746
                      2.0 + 0.0
                   0.0 + 28.1987
                 0.0366 + 27.3446
                 0.5047 + 26.4692
                 1.2013 + 25.5305
                 1.6807 + 24.1299
                 1.8987 + 22.7321
                 1.9735 + 21.7934
                 1.9941 + 20.3928
                 1.9989 + 18.5978
\varphi_7(18) = \max
                                      =28.1987, \quad x_7^0=0
                 1.9998 + 16.2995
                    2.0 + 14.658
                   2.0 + 13.1148
                   2.0 + 11.7142
                    2.0 + 9.4159
                     2.0+7.38
                    2.0 + 5.9794
                    2.0 + 3.4365
                    2.0 + 0.5746
                     2.0 + 0.0
```

```
0.0 + 28.8919
                 0.0366 + 28.1987
                 0.5047 + 27.3446
                 1.2013 + 26.4692
                 1.6807 + 25.5305
                 1.8987 + 24.1299
                 1.9735 + 22.7321
                 1.9941 + 21.7934
                 1.9989 + 20.3928
                 1.9998 + 18.5978
\varphi_7(19) = \max
                                       = 28.8919, \quad x_7^0 = 0
                   2.0 + 16.2995
                    2.0 + 14.658
                   2.0 + 13.1148
                   2.0 + 11.7142
                    2.0 + 9.4159
                     2.0+7.38
                    2.0 + 5.9794
                    2.0 + 3.4365
                    2.0 + 0.5746
                      2.0 + 0.0
                   0.0 + 29.8306
                 0.0366 + 28.8919
                 0.5047 + 28.1987
                 1.2013 + 27.3446
                 1.6807 + 26.4692
                 1.8987 + 25.5305
                 1.9735 + 24.1299
                 1.9941 + 22.7321
                 1.9989 + 21.7934
                 1.9998 + 20.3928
                                       = 29.8306, \quad x_7^0 = 0
\varphi_7(20) = \max
                   2.0 + 18.5978
                   2.0 + 16.2995
                    2.0 + 14.658
                   2.0 + 13.1148
                   2.0 + 11.7142
                    2.0 + 9.4159
                     2.0+7.38
                    2.0 + 5.9794
                    2.0 + 3.4365
                    2.0 + 0.5746
                      2.0 + 0.0
```

```
0.0 + 30.706
                  0.0366 + 29.8306
                  0.5047 + 28.8919
                  1.2013 + 28.1987
                  1.6807 + 27.3446
                  1.8987 + 26.4692
                  1.9735 + 25.5305
                  1.9941 + 24.1299
                  1.9989 + 22.7321
                  1.9998 + 21.7934
                    2.0 + 20.3928
                                       =30.706, \quad x_7^0=0
\varphi_7(21) = \max
                   2.0 + 18.5978
                   2.0 + 16.2995
                    2.0 + 14.658
                   2.0 + 13.1148
                   2.0 + 11.7142
                    2.0 + 9.4159
                     2.0 + 7.38
                    2.0 + 5.9794
                    2.0 + 3.4365
                    2.0 + 0.5746
                      2.0 + 0.0
                   0.0 + 31.5601
                  0.0366 + 30.706
                  0.5047 + 29.8306
                  1.2013 + 28.8919
                  1.6807 + 28.1987
                  1.8987 + 27.3446
                  1.9735 + 26.4692
                  1.9941 + 25.5305
                  1.9989 + 24.1299
                  1.9998 + 22.7321
                    2.0 + 21.7934
                                       =31.5601, \quad x_7^0=0
\varphi_7(22) = \max
                    2.0 + 20.3928
                    2.0 + 18.5978
                    2.0 + 16.2995
                    2.0 + 14.658
                    2.0 + 13.1148
                   2.0 + 11.7142
                    2.0 + 9.4159
                     2.0 + 7.38
                    2.0 + 5.9794
                    2.0 + 3.4365
                    2.0 + 0.5746
                      2.0 + 0.0
```

```
0.0 + 32.0305
                 0.0366 + 31.5601
                  0.5047 + 30.706
                 1.2013 + 29.8306
                 1.6807 + 28.8919
                 1.8987 + 28.1987
                 1.9735 + 27.3446
                 1.9941 + 26.4692
                 1.9989 + 25.5305
                 1.9998 + 24.1299
                   2.0 + 22.7321
                   2.0 + 21.7934
                                      = 32.0305, \quad x_7^0 = 0
\varphi_7(23) = \max
                   2.0 + 20.3928
                   2.0 + 18.5978
                   2.0 + 16.2995
                   2.0 + 14.658
                   2.0 + 13.1148
                   2.0 + 11.7142
                   2.0 + 9.4159
                     2.0 + 7.38
                    2.0 + 5.9794
                    2.0 + 3.4365
                    2.0 + 0.5746
                     2.0 + 0.0
```

```
0.0 + 32.4666
                 0.0366 + 32.0305
                 0.5047 + 31.5601
                  1.2013 + 30.706
                 1.6807 + 29.8306
                 1.8987 + 28.8919
                 1.9735 + 28.1987
                 1.9941 + 27.3446
                 1.9989 + 26.4692
                 1.9998 + 25.5305
                   2.0 + 24.1299
                   2.0 + 22.7321
\varphi_7(24) = \max
                   2.0 + 21.7934
                                      =32.4666,\quad x_7^0=0
                   2.0 + 20.3928
                   2.0 + 18.5978
                   2.0 + 16.2995
                   2.0 + 14.658
                   2.0 + 13.1148
                   2.0 + 11.7142
                    2.0 + 9.4159
                     2.0 + 7.38
                    2.0 + 5.9794
                    2.0 + 3.4365
                    2.0 + 0.5746
                     2.0 + 0.0
```

```
0.0 + 33.1535
                  0.0366 + 32.4666
                  0.5047 + 32.0305
                  1.2013 + 31.5601
                  1.6807 + 30.706
                  1.8987 + 29.8306
                  1.9735 + 28.8919
                  1.9941 + 28.1987
                  1.9989 + 27.3446
                  1.9998 + 26.4692
                   2.0 + 25.5305
                   2.0 + 24.1299
                   2.0 + 22.7321
                                       = 33.1535, \quad x_7^0 = 0
\varphi_7(25) = \max
                   2.0 + 21.7934
                   2.0 + 20.3928
                   2.0 + 18.5978
                   2.0 + 16.2995
                   2.0 + 14.658
                   2.0 + 13.1148
                   2.0 + 11.7142
                    2.0 + 9.4159
                     2.0 + 7.38
                    2.0 + 5.9794
                    2.0 + 3.4365
                    2.0 + 0.5746
                      2.0 + 0.0
```

```
0.0 + 33.936
                 0.0366 + 33.1535
                 0.5047 + 32.4666
                 1.2013 + 32.0305
                 1.6807 + 31.5601
                  1.8987 + 30.706
                 1.9735 + 29.8306
                 1.9941 + 28.8919
                 1.9989 + 28.1987
                 1.9998 + 27.3446
                   2.0 + 26.4692
                   2.0 + 25.5305
                   2.0 + 24.1299
                                       = 33.936, \quad x_7^0 = 0
\varphi_7(26) = \max
                   2.0 + 22.7321
                   2.0 + 21.7934
                   2.0 + 20.3928
                   2.0 + 18.5978
                   2.0 + 16.2995
                   2.0 + 14.658
                   2.0 + 13.1148
                   2.0 + 11.7142
                    2.0 + 9.4159
                     2.0 + 7.38
                    2.0 + 5.9794
                    2.0 + 3.4365
                    2.0 + 0.5746
                     2.0 + 0.0
```

```
0.0 + 34.4064
                  0.0366 + 33.936
                 0.5047 + 33.1535
                 1.2013 + 32.4666
                 1.6807 + 32.0305
                 1.8987 + 31.5601
                  1.9735 + 30.706
                 1.9941 + 29.8306
                 1.9989 + 28.8919
                 1.9998 + 28.1987
                   2.0 + 27.3446
                   2.0 + 26.4692
                   2.0 + 25.5305
                   2.0 + 24.1299
                                      = 34.4064, \quad x_7^0 = 0
\varphi_7(27) = \max
                   2.0 + 22.7321
                   2.0 + 21.7934
                   2.0 + 20.3928
                   2.0 + 18.5978
                   2.0 + 16.2995
                   2.0 + 14.658
                   2.0 + 13.1148
                   2.0 + 11.7142
                    2.0 + 9.4159
                     2.0+7.38
                    2.0 + 5.9794
                    2.0 + 3.4365
                    2.0 + 0.5746
                     2.0 + 0.0
```

```
0.0 + 34.8425
                  0.0366 + 34.4064
                  0.5047 + 33.936
                  1.2013 + 33.1535
                  1.6807 + 32.4666
                  1.8987 + 32.0305
                  1.9735 + 31.5601
                  1.9941 + 30.706
                  1.9989 + 29.8306
                  1.9998 + 28.8919
                   2.0 + 28.1987
                   2.0 + 27.3446
                   2.0 + 26.4692
                   2.0 + 25.5305
                                      = 34.8425, \quad x_7^0 = 0
\varphi_7(28) = \max
                   2.0 + 24.1299
                   2.0 + 22.7321
                   2.0 + 21.7934
                   2.0 + 20.3928
                   2.0 + 18.5978
                   2.0 + 16.2995
                    2.0 + 14.658
                   2.0 + 13.1148
                   2.0 + 11.7142
                    2.0 + 9.4159
                     2.0 + 7.38
                    2.0 + 5.9794
                    2.0 + 3.4365
                    2.0 + 0.5746
                      2.0 + 0.0
```

```
0.0 + 35.2458
                 0.0366 + 34.8425
                 0.5047 + 34.4064
                  1.2013 + 33.936
                 1.6807 + 33.1535
                 1.8987 + 32.4666
                 1.9735 + 32.0305
                 1.9941 + 31.5601
                  1.9989 + 30.706
                 1.9998 + 29.8306
                   2.0 + 28.8919
                   2.0 + 28.1987
                   2.0 + 27.3446
                   2.0 + 26.4692
                   2.0 + 25.5305
\varphi_7(29) = \max
                                      =35.2458, \quad x_7^0=0
                   2.0 + 24.1299
                   2.0 + 22.7321
                   2.0 + 21.7934
                   2.0 + 20.3928
                   2.0 + 18.5978
                   2.0 + 16.2995
                    2.0 + 14.658
                   2.0 + 13.1148
                   2.0 + 11.7142
                    2.0 + 9.4159
                     2.0 + 7.38
                    2.0 + 5.9794
                    2.0 + 3.4365
                    2.0 + 0.5746
                      2.0 + 0.0
```

```
0.0 + 35.5717
                 0.0366 + 35.2458
                 0.5047 + 34.8425
                 1.2013 + 34.4064
                  1.6807 + 33.936
                 1.8987 + 33.1535
                 1.9735 + 32.4666
                 1.9941 + 32.0305
                 1.9989 + 31.5601
                  1.9998 + 30.706
                   2.0 + 29.8306
                   2.0 + 28.8919
                   2.0 + 28.1987
                   2.0 + 27.3446
                   2.0 + 26.4692
                                      = 35.6167, \quad x_7^0 = 4
\varphi_7(30) = \max
                   2.0 + 25.5305
                   2.0 + 24.1299
                   2.0 + 22.7321
                   2.0 + 21.7934
                   2.0 + 20.3928
                   2.0 + 18.5978
                   2.0 + 16.2995
                    2.0 + 14.658
                   2.0 + 13.1148
                   2.0 + 11.7142
                   2.0 + 9.4159
                     2.0 + 7.38
                    2.0 + 5.9794
                    2.0 + 3.4365
                    2.0 + 0.5746
                     2.0 + 0.0
```

```
0.0 + 35.8657
                 0.0366 + 35.5717
                 0.5047 + 35.2458
                 1.2013 + 34.8425
                 1.6807 + 34.4064
                  1.8987 + 33.936
                 1.9735 + 33.1535
                 1.9941 + 32.4666
                 1.9989 + 32.0305
                 1.9998 + 31.5601
                    2.0 + 30.706
                   2.0 + 29.8306
                   2.0 + 28.8919
                   2.0 + 28.1987
                   2.0 + 27.3446
                   2.0 + 26.4692
                                      = 36.0871, \quad x_7^0 = 4
\varphi_7(31) = \max
                   2.0 + 25.5305
                   2.0 + 24.1299
                   2.0 + 22.7321
                   2.0 + 21.7934
                   2.0 + 20.3928
                   2.0 + 18.5978
                   2.0 + 16.2995
                   2.0 + 14.658
                   2.0 + 13.1148
                   2.0 + 11.7142
                   2.0 + 9.4159
                     2.0+7.38
                    2.0 + 5.9794
                    2.0 + 3.4365
                    2.0 + 0.5746
                     2.0 + 0.0
```

```
0.0 + 36.1262
                 0.0366 + 35.8657
                 0.5047 + 35.5717
                 1.2013 + 35.2458
                 1.6807 + 34.8425
                 1.8987 + 34.4064
                  1.9735 + 33.936
                 1.9941 + 33.1535
                 1.9989 + 32.4666
                 1.9998 + 32.0305
                   2.0 + 31.5601
                   2.0 + 30.706
                   2.0 + 29.8306
                   2.0 + 28.8919
                   2.0 + 28.1987
                   2.0 + 27.3446
                                                   x_7^0 = 4
\varphi_7(32) = \max
                   2.0 + 26.4692
                                      = 36.5232,
                   2.0 + 25.5305
                   2.0 + 24.1299
                   2.0 + 22.7321
                   2.0 + 21.7934
                   2.0 + 20.3928
                   2.0 + 18.5978
                   2.0 + 16.2995
                   2.0 + 14.658
                   2.0 + 13.1148
                   2.0 + 11.7142
                   2.0 + 9.4159
                     2.0 + 7.38
                   2.0 + 5.9794
                   2.0 + 3.4365
                   2.0 + 0.5746
                     2.0 + 0.0
```

```
0.0 + 36.2823
                 0.0366 + 36.1262
                 0.5047 + 35.8657
                 1.2013 + 35.5717
                 1.6807 + 35.2458
                 1.8987 + 34.8425
                 1.9735 + 34.4064
                  1.9941 + 33.936
                 1.9989 + 33.1535
                 1.9998 + 32.4666
                   2.0 + 32.0305
                   2.0 + 31.5601
                   2.0 + 30.706
                   2.0 + 29.8306
                   2.0 + 28.8919
                   2.0 + 28.1987
                   2.0 + 27.3446
\varphi_7(33) = \max
                                      = 36.9265,
                                                   x_7^0 = 4
                   2.0 + 26.4692
                   2.0 + 25.5305
                   2.0 + 24.1299
                   2.0 + 22.7321
                   2.0 + 21.7934
                   2.0 + 20.3928
                   2.0 + 18.5978
                   2.0 + 16.2995
                   2.0 + 14.658
                   2.0 + 13.1148
                   2.0 + 11.7142
                   2.0 + 9.4159
                    2.0 + 7.38
                   2.0 + 5.9794
                   2.0 + 3.4365
                   2.0 + 0.5746
                     2.0 + 0.0
```

```
0.0 + 36.4317
                 0.0366 + 36.2823
                 0.5047 + 36.1262
                 1.2013 + 35.8657
                 1.6807 + 35.5717
                 1.8987 + 35.2458
                 1.9735 + 34.8425
                 1.9941 + 34.4064
                  1.9989 + 33.936
                 1.9998 + 33.1535
                   2.0 + 32.4666
                   2.0 + 32.0305
                   2.0 + 31.5601
                    2.0 + 30.706
                   2.0 + 29.8306
                   2.0 + 28.8919
                   2.0 + 28.1987
\varphi_7(34) = \max
                                      = 37.2524, \quad x_7^0 = 4
                   2.0 + 27.3446
                   2.0 + 26.4692
                   2.0 + 25.5305
                   2.0 + 24.1299
                   2.0 + 22.7321
                   2.0 + 21.7934
                   2.0 + 20.3928
                   2.0 + 18.5978
                   2.0 + 16.2995
                   2.0 + 14.658
                   2.0 + 13.1148
                   2.0 + 11.7142
                    2.0 + 9.4159
                     2.0 + 7.38
                    2.0 + 5.9794
                    2.0 + 3.4365
                    2.0 + 0.5746
                      2.0 + 0.0
```

```
0.0 + 36.5516
                 0.0366 + 36.4317
                 0.5047 + 36.2823
                 1.2013 + 36.1262
                 1.6807 + 35.8657
                 1.8987 + 35.5717
                 1.9735 + 35.2458
                 1.9941 + 34.8425
                 1.9989 + 34.4064
                  1.9998 + 33.936
                   2.0 + 33.1535
                   2.0 + 32.4666
                   2.0 + 32.0305
                   2.0 + 31.5601
                   2.0 + 30.706
                   2.0 + 29.8306
                   2.0 + 28.8919
                   2.0 + 28.1987
\varphi_7(35) = \max
                                      = 37.5464, \quad x_7^0 = 4
                   2.0 + 27.3446
                   2.0 + 26.4692
                   2.0 + 25.5305
                   2.0 + 24.1299
                   2.0 + 22.7321
                   2.0 + 21.7934
                   2.0 + 20.3928
                   2.0 + 18.5978
                   2.0 + 16.2995
                   2.0 + 14.658
                   2.0 + 13.1148
                   2.0 + 11.7142
                    2.0 + 9.4159
                     2.0 + 7.38
                    2.0 + 5.9794
                    2.0 + 3.4365
                    2.0 + 0.5746
                      2.0 + 0.0
```

```
0.0 + 36.6557
                 0.0366 + 36.5516
                 0.5047 + 36.4317
                 1.2013 + 36.2823
                 1.6807 + 36.1262
                 1.8987 + 35.8657
                 1.9735 + 35.5717
                 1.9941 + 35.2458
                 1.9989 + 34.8425
                 1.9998 + 34.4064
                    2.0 + 33.936
                   2.0 + 33.1535
                   2.0 + 32.4666
                   2.0 + 32.0305
                   2.0 + 31.5601
                   2.0 + 30.706
                   2.0 + 29.8306
                   2.0 + 28.8919
\varphi_7(36) = \max
                   2.0 + 28.1987
                                      = 37.8069,
                                                   x_7^0 = 4
                   2.0 + 27.3446
                   2.0 + 26.4692
                   2.0 + 25.5305
                   2.0 + 24.1299
                   2.0 + 22.7321
                   2.0 + 21.7934
                   2.0 + 20.3928
                   2.0 + 18.5978
                   2.0 + 16.2995
                   2.0 + 14.658
                   2.0 + 13.1148
                   2.0 + 11.7142
                    2.0 + 9.4159
                     2.0 + 7.38
                    2.0 + 5.9794
                    2.0 + 3.4365
                    2.0 + 0.5746
                      2.0 + 0.0
```

## 8 Product 8

$$\varphi_8(0) = \max\{0.0\} = 0.0, x_8^0 = 0$$

$$\varphi_8(1) = \max \left\{ \begin{array}{l} 0.0 + 0.5746 \\ 0.0539 + 0.0 \end{array} \right\} = 0.5746, \quad x_8^0 = 0$$

$$\varphi_8(2) = \max \left\{ \begin{array}{l} 0.0 + 3.4365 \\ 0.0539 + 0.5746 \\ 1.2595 + 0.0 \end{array} \right\} = 3.4365, \quad x_8^0 = 0$$

$$\varphi_8(3) = \max \left\{ \begin{array}{l} 0.0 + 5.9794 \\ 0.0539 + 3.4365 \\ 1.2595 + 0.5746 \\ 3.7307 + 0.0 \end{array} \right\} = 5.9794, \quad x_8^0 = 0$$

$$\varphi_8(4) = \max \left\{ \begin{array}{l} 0.0 + 7.38 \\ 0.0539 + 5.9794 \\ 1.2595 + 3.4365 \\ 3.7307 + 0.5746 \\ 5.9267 + 0.0 \end{array} \right\} = 7.38, \quad x_8^0 = 0$$

$$\varphi_8(5) = \max \left\{ \begin{array}{l} 0.0 + 9.4159 \\ 0.0539 + 7.38 \\ 1.2595 + 5.9794 \\ 3.7307 + 3.4365 \\ 5.9267 + 0.5746 \\ 7.1926 + 0.0 \end{array} \right\} = 9.4159, \quad x_8^0 = 0$$

$$\varphi_8(6) = \max \left\{ \begin{array}{l} 0.0 + 11.7142 \\ 0.0539 + 7.38 \\ 3.7307 + 5.9794 \\ 5.9267 + 0.5746 \\ 7.1926 + 0.0 \end{array} \right\} = 11.7142, \quad x_8^0 = 0$$

$$\varphi_8(7) = \max \left\{ \begin{array}{l} 0.0 + 11.7142 \\ 0.0539 + 9.4159 \\ 1.2595 + 7.38 \\ 3.7307 + 5.9794 \\ 5.9267 + 3.4365 \\ 7.1926 + 0.5746 \\ 7.7386 + 0.0 \end{array} \right\} = 11.7142, \quad x_8^0 = 0$$

$$\varphi_8(7) = \max \left\{ \begin{array}{l} 0.0 + 13.1148 \\ 0.0539 + 11.7142 \\ 1.2595 + 9.4159 \\ 3.7307 + 7.38 \\ 5.9267 + 5.9794 \\ 7.1926 + 3.4365 \\ 7.7386 + 0.5746 \\ 7.9278 + 0.0 \end{array} \right\} = 13.1148, \quad x_8^0 = 0$$

$$\varphi_8(8) = \max \left\{ \begin{array}{l} 0.0 + 14.658 \\ 0.0539 + 13.1148 \\ 1.2595 + 11.7142 \\ 3.7307 + 9.4159 \\ 5.9267 + 7.38 \\ 7.9278 + 0.0 \end{array} \right\} = 14.658, \quad x_8^0 = 0$$

$$\varphi_8(8) = \max \left\{ \begin{array}{l} 0.0 + 14.658 \\ 0.0539 + 13.1148 \\ 1.2595 + 11.7142 \\ 3.7307 + 9.4159 \\ 5.9267 + 7.38 \\ 7.9278 + 0.5746 \\$$

$$\varphi_8(9) = \max \left\{ \begin{array}{l} 0.0 + 16.2995 \\ 0.0539 + 14.658 \\ 1.2595 + 13.1148 \\ 3.7307 + 11.7142 \\ 5.9267 + 9.4159 \\ 7.1926 + 7.38 \\ 7.7386 + 5.9794 \\ 7.9278 + 3.4365 \\ 7.9826 + 0.5746 \\ 7.9963 + 0.0 \end{array} \right\} = 16.2995, \quad x_8^0 = 0$$

$$\varphi_8(10) = \max \left\{ \begin{array}{l} 0.0 + 18.5978 \\ 0.0539 + 16.2995 \\ 1.2595 + 14.658 \\ 3.7307 + 13.1148 \\ 5.9267 + 11.7142 \\ 7.1926 + 9.4159 \\ 7.7386 + 7.38 \\ 7.9278 + 5.9794 \\ 7.9826 + 3.4365 \\ 7.9963 + 0.5746 \\ 7.9993 + 0.0 \end{array} \right\} = 18.5978, \quad x_8^0 = 0$$

$$\varphi_8(11) = \max \left\{ \begin{array}{l} 0.0 + 20.3928 \\ 0.0539 + 18.5978 \\ 1.2595 + 16.2995 \\ 3.7307 + 14.658 \\ 5.9267 + 13.1148 \\ 7.1926 + 11.7142 \\ 7.7386 + 9.4159 \\ 7.9278 + 7.38 \\ 7.9278 + 7.38 \\ 7.9278 + 7.38 \\ 7.9928 + 7.38 \\ 7.9928 + 5.9794 \\ 7.9963 + 3.4365 \\ 7.9993 + 0.5746 \\ 7.9999 + 0.0 \end{array} \right\} = 20.3928, \quad x_8^0 = 0$$

```
0.0 + 21.7934
                  0.0539 + 20.3928
                  1.2595 + 18.5978
                  3.7307 + 16.2995
                  5.9267 + 14.658
                  7.1926 + 13.1148
\varphi_8(12) = \max
                                       =21.7934, \quad x_8^0=0
                  7.7386 + 11.7142
                  7.9278 + 9.4159
                   7.9826 + 7.38
                  7.9963 + 5.9794
                  7.9993 + 3.4365
                  7.9999 + 0.5746
                      8.0 + 0.0
                   0.0 + 22.7321
                  0.0539 + 21.7934
                  1.2595 + 20.3928
                  3.7307 + 18.5978
                  5.9267 + 16.2995
                  7.1926 + 14.658
                  7.7386 + 13.1148
                                       =22.7321, \quad x_8^0=0
\varphi_8(13) = \max
                  7.9278 + 11.7142
                  7.9826 + 9.4159
                   7.9963 + 7.38
                  7.9993 + 5.9794
                  7.9999 + 3.4365
                    8.0 + 0.5746
                      8.0 + 0.0
                   0.0 + 24.1299
                  0.0539 + 22.7321
                  1.2595 + 21.7934
                  3.7307 + 20.3928
                  5.9267 + 18.5978
                  7.1926 + 16.2995
                  7.7386 + 14.658
\varphi_8(14) = \max
                                       = 24.5245, \quad x_8^0 = 4
                  7.9278 + 13.1148
                  7.9826 + 11.7142
                  7.9963 + 9.4159
                   7.9993 + 7.38
                  7.9999 + 5.9794
                    8.0 + 3.4365
                    8.0 + 0.5746
                      8.0 + 0.0
```

```
0.0 + 25.5305
                  0.0539 + 24.1299
                  1.2595 + 22.7321
                  3.7307 + 21.7934
                  5.9267 + 20.3928
                  7.1926 + 18.5978
                  7.7386 + 16.2995
                  7.9278 + 14.658
\varphi_8(15) = \max
                                       = 26.3195, \quad x_8^0 = 4
                  7.9826+13.1148
                  7.9963 + 11.7142
                  7.9993 + 9.4159
                    7.9999 + 7.38
                    8.0 + 5.9794
                    8.0 + 3.4365
                    8.0 + 0.5746
                      8.0+0.0
                    0.0 + 26.4692
                  0.0539 + 25.5305
                  1.2595 + 24.1299
                  3.7307 + 22.7321
                  5.9267 + 21.7934
                  7.1926 + 20.3928
                  7.7386 + 18.5978
                  7.9278 + 16.2995
\varphi_8(16) = \max \epsilon
                  7.9826+14.658
                                       = 27.7201, \quad x_8^0 = 4
                  7.9963 + 13.1148
                  7.9993 + 11.7142
                  7.9999 + 9.4159
                     8.0 + 7.38
                    8.0 + 5.9794
                    8.0 + 3.4365
                    8.0 + 0.5746
                      8.0 + 0.0
```

```
0.0 + 27.3446
                  0.0539 + 26.4692
                  1.2595 + 25.5305
                  3.7307 + 24.1299
                  5.9267 + 22.7321
                  7.1926 + 21.7934
                  7.7386 + 20.3928
                  7.9278 + 18.5978
                  7.9826 + 16.2995
                                       = 28.986, \quad x_8^0 = 5
\varphi_8(17) = \max
                  7.9963 + 14.658
                  7.9993 + 13.1148
                  7.9999 + 11.7142
                    8.0 + 9.4159
                     8.0 + 7.38
                    8.0 + 5.9794
                    8.0 + 3.4365
                    8.0 + 0.5746
                      8.0 + 0.0
                    0.0 + 28.1987
                  0.0539 + 27.3446
                  1.2595 + 26.4692
                  3.7307 + 25.5305
                  5.9267 + 24.1299
                  7.1926 + 22.7321
                  7.7386 + 21.7934
                  7.9278 + 20.3928
                  7.9826 + 18.5978
\varphi_8(18) = \max \langle
                                       = 30.0566, \quad x_8^0 = 4
                  7.9963 + 16.2995
                  7.9993 + 14.658
                  7.9999 + 13.1148
                    8.0 + 11.7142
                    8.0 + 9.4159
                     8.0 + 7.38
                    8.0 + 5.9794
                    8.0 + 3.4365
                    8.0 + 0.5746
                      8.0 + 0.0
```

```
0.0 + 28.8919
                 0.0539 + 28.1987
                 1.2595 + 27.3446
                 3.7307 + 26.4692
                 5.9267 + 25.5305
                 7.1926 + 24.1299
                 7.7386 + 22.7321
                 7.9278 + 21.7934
                 7.9826 + 20.3928
                 7.9963 + 18.5978
\varphi_8(19) = \max
                                      = 31.4572, \quad x_8^0 = 4
                 7.9993 + 16.2995
                  7.9999 + 14.658
                   8.0 + 13.1148
                   8.0 + 11.7142
                    8.0 + 9.4159
                     8.0+7.38
                    8.0 + 5.9794
                    8.0 + 3.4365
                    8.0 + 0.5746
                      8.0 + 0.0
                   0.0 + 29.8306
                 0.0539 + 28.8919
                 1.2595 + 28.1987
                 3.7307 + 27.3446
                 5.9267 + 26.4692
                 7.1926 + 25.5305
                 7.7386 + 24.1299
                 7.9278 + 22.7321
                 7.9826 + 21.7934
                 7.9963 + 20.3928
                                      = 32.7231, \quad x_8^0 = 5
\varphi_8(20) = \max
                 7.9993 + 18.5978
                 7.9999 + 16.2995
                    8.0 + 14.658
                   8.0 + 13.1148
                   8.0 + 11.7142
                    8.0 + 9.4159
                     8.0+7.38
                    8.0 + 5.9794
                    8.0 + 3.4365
                    8.0 + 0.5746
                     8.0 + 0.0
```

```
0.0 + 30.706
                 0.0539 + 29.8306
                 1.2595 + 28.8919
                 3.7307 + 28.1987
                 5.9267 + 27.3446
                 7.1926 + 26.4692
                 7.7386 + 25.5305
                 7.9278 + 24.1299
                 7.9826 + 22.7321
                 7.9963 + 21.7934
                 7.9993 + 20.3928
\varphi_8(21) = \max
                                      = 33.6618,
                                                   x_8^0 = 5
                 7.9999 + 18.5978
                   8.0 + 16.2995
                    8.0 + 14.658
                   8.0 + 13.1148
                   8.0 + 11.7142
                    8.0 + 9.4159
                     8.0 + 7.38
                    8.0 + 5.9794
                    8.0 + 3.4365
                    8.0 + 0.5746
                      8.0 + 0.0
                   0.0 + 31.5601
                  0.0539 + 30.706
                 1.2595 + 29.8306
                 3.7307 + 28.8919
                 5.9267 + 28.1987
                 7.1926 + 27.3446
                 7.7386 + 26.4692
                 7.9278 + 25.5305
                 7.9826 + 24.1299
                 7.9963 + 22.7321
                 7.9993 + 21.7934
\varphi_8(22) = \max
                 7.9999 + 20.3928
                                      = 34.5372, \quad x_8^0 = 5
                   8.0 + 18.5978
                   8.0 + 16.2995
                    8.0 + 14.658
                   8.0 + 13.1148
                   8.0 + 11.7142
                    8.0 + 9.4159
                     8.0 + 7.38
                    8.0 + 5.9794
                    8.0 + 3.4365
                    8.0 + 0.5746
                      8.0 + 0.0
```

```
0.0 + 32.0305
                 0.0539 + 31.5601
                  1.2595 + 30.706
                 3.7307 + 29.8306
                 5.9267 + 28.8919
                 7.1926 + 28.1987
                 7.7386 + 27.3446
                 7.9278 + 26.4692
                 7.9826 + 25.5305
                 7.9963 + 24.1299
                 7.9993 + 22.7321
                 7.9999 + 21.7934
\varphi_8(23) = \max
                                      = 35.3913, \quad x_8^0 = 5
                   8.0 + 20.3928
                   8.0 + 18.5978
                   8.0 + 16.2995
                   8.0 + 14.658
                   8.0 + 13.1148
                   8.0 + 11.7142
                    8.0 + 9.4159
                     8.0 + 7.38
                    8.0 + 5.9794
                    8.0 + 3.4365
                    8.0 + 0.5746
                     8.0 + 0.0
```

```
0.0 + 32.4666
                 0.0539 + 32.0305
                 1.2595 + 31.5601
                  3.7307 + 30.706
                 5.9267 + 29.8306
                 7.1926 + 28.8919
                 7.7386 + 28.1987
                 7.9278 + 27.3446
                 7.9826 + 26.4692
                 7.9963 + 25.5305
                 7.9993 + 24.1299
                 7.9999 + 22.7321
\varphi_8(24) = \max
                   8.0 + 21.7934
                                      =36.0845,\quad x_8^0=5
                   8.0 + 20.3928
                   8.0 + 18.5978
                   8.0 + 16.2995
                   8.0 + 14.658
                   8.0 + 13.1148
                   8.0 + 11.7142
                    8.0 + 9.4159
                     8.0 + 7.38
                    8.0 + 5.9794
                    8.0 + 3.4365
                    8.0 + 0.5746
                     8.0 + 0.0
```

```
0.0 + 33.1535
                 0.0539 + 32.4666
                 1.2595 + 32.0305
                 3.7307 + 31.5601
                  5.9267 + 30.706
                 7.1926 + 29.8306
                 7.7386 + 28.8919
                 7.9278 + 28.1987
                 7.9826 + 27.3446
                 7.9963 + 26.4692
                 7.9993 + 25.5305
                 7.9999 + 24.1299
                   8.0 + 22.7321
\varphi_8(25) = \max
                                      = 37.0232, \quad x_8^0 = 5
                   8.0 + 21.7934
                   8.0 + 20.3928
                   8.0 + 18.5978
                   8.0 + 16.2995
                   8.0 + 14.658
                   8.0 + 13.1148
                   8.0 + 11.7142
                    8.0 + 9.4159
                     8.0 + 7.38
                    8.0 + 5.9794
                    8.0 + 3.4365
                    8.0 + 0.5746
                     8.0 + 0.0
```

```
0.0 + 33.936
                 0.0539 + 33.1535
                 1.2595 + 32.4666
                 3.7307 + 32.0305
                 5.9267 + 31.5601
                  7.1926 + 30.706
                 7.7386 + 29.8306
                 7.9278 + 28.8919
                 7.9826 + 28.1987
                 7.9963 + 27.3446
                 7.9993 + 26.4692
                 7.9999 + 25.5305
                   8.0 + 24.1299
\varphi_8(26) = \max
                   8.0 + 22.7321
                                      =37.8986,\quad x_8^0=5
                   8.0 + 21.7934
                   8.0 + 20.3928
                   8.0 + 18.5978
                   8.0 + 16.2995
                   8.0 + 14.658
                   8.0 + 13.1148
                   8.0 + 11.7142
                   8.0 + 9.4159
                     8.0 + 7.38
                   8.0 + 5.9794
                   8.0 + 3.4365
                   8.0 + 0.5746
                     8.0 + 0.0
```

```
0.0 + 34.4064
                  0.0539 + 33.936
                 1.2595 + 33.1535
                 3.7307 + 32.4666
                 5.9267 + 32.0305
                 7.1926 + 31.5601
                  7.7386 + 30.706
                 7.9278 + 29.8306
                 7.9826 + 28.8919
                 7.9963 + 28.1987
                 7.9993 + 27.3446
                 7.9999 + 26.4692
                   8.0 + 25.5305
                   8.0 + 24.1299
                                      =38.7527, \quad x_8^0=5
\varphi_8(27) = \max
                   8.0 + 22.7321
                   8.0 + 21.7934
                   8.0 + 20.3928
                   8.0 + 18.5978
                   8.0 + 16.2995
                   8.0 + 14.658
                   8.0 + 13.1148
                   8.0 + 11.7142
                    8.0 + 9.4159
                     8.0 + 7.38
                    8.0 + 5.9794
                    8.0 + 3.4365
                    8.0 + 0.5746
                     8.0 + 0.0
```

```
0.0 + 34.8425
                 0.0539 + 34.4064
                  1.2595 + 33.936
                 3.7307 + 33.1535
                 5.9267 + 32.4666
                 7.1926 + 32.0305
                 7.7386 + 31.5601
                  7.9278 + 30.706
                 7.9826 + 29.8306
                 7.9963 + 28.8919
                 7.9993 + 28.1987
                 7.9999 + 27.3446
                   8.0 + 26.4692
                   8.0 + 25.5305
                                      = 39.2987, \quad x_8^0 = 6
\varphi_8(28) = \max
                   8.0 + 24.1299
                   8.0 + 22.7321
                   8.0 + 21.7934
                   8.0 + 20.3928
                   8.0 + 18.5978
                   8.0 + 16.2995
                    8.0 + 14.658
                   8.0 + 13.1148
                   8.0 + 11.7142
                    8.0 + 9.4159
                     8.0 + 7.38
                    8.0 + 5.9794
                    8.0 + 3.4365
                    8.0 + 0.5746
                      8.0 + 0.0
```

```
0.0 + 35.2458
                 0.0539 + 34.8425
                 1.2595 + 34.4064
                  3.7307 + 33.936
                 5.9267 + 33.1535
                 7.1926 + 32.4666
                 7.7386 + 32.0305
                 7.9278 + 31.5601
                  7.9826 + 30.706
                 7.9963 + 29.8306
                 7.9993 + 28.8919
                 7.9999 + 28.1987
                   8.0 + 27.3446
                   8.0 + 26.4692
                   8.0 + 25.5305
\varphi_8(29) = \max
                                      = 39.7691, \quad x_8^0 = 6
                   8.0 + 24.1299
                   8.0 + 22.7321
                   8.0 + 21.7934
                   8.0 + 20.3928
                   8.0 + 18.5978
                   8.0 + 16.2995
                    8.0 + 14.658
                   8.0 + 13.1148
                   8.0 + 11.7142
                    8.0 + 9.4159
                     8.0 + 7.38
                    8.0 + 5.9794
                    8.0 + 3.4365
                    8.0 + 0.5746
                      8.0 + 0.0
```

```
0.0 + 35.6167
                 0.0539 + 35.2458
                 1.2595 + 34.8425
                 3.7307 + 34.4064
                  5.9267 + 33.936
                 7.1926 + 33.1535
                 7.7386 + 32.4666
                 7.9278 + 32.0305
                 7.9826 + 31.5601
                  7.9963 + 30.706
                 7.9993 + 29.8306
                 7.9999 + 28.8919
                   8.0 + 28.1987
                   8.0 + 27.3446
                   8.0 + 26.4692
\varphi_8(30) = \max
                   8.0 + 25.5305
                                      =40.3461, \quad x_8^0=5
                   8.0 + 24.1299
                   8.0 + 22.7321
                   8.0 + 21.7934
                   8.0 + 20.3928
                   8.0 + 18.5978
                   8.0 + 16.2995
                   8.0 + 14.658
                   8.0 + 13.1148
                   8.0 + 11.7142
                   8.0 + 9.4159
                     8.0 + 7.38
                    8.0 + 5.9794
                    8.0 + 3.4365
                    8.0 + 0.5746
                     8.0 + 0.0
```

```
0.0 + 36.0871
                 0.0539 + 35.6167
                 1.2595 + 35.2458
                 3.7307 + 34.8425
                 5.9267 + 34.4064
                  7.1926 + 33.936
                 7.7386 + 33.1535
                 7.9278 + 32.4666
                 7.9826 + 32.0305
                 7.9963 + 31.5601
                  7.9993 + 30.706
                 7.9999 + 29.8306
                   8.0 + 28.8919
                   8.0 + 28.1987
                   8.0 + 27.3446
                   8.0 + 26.4692
\varphi_8(31) = \max
                                      =41.1286, \quad x_8^0=5
                   8.0 + 25.5305
                   8.0 + 24.1299
                   8.0 + 22.7321
                   8.0 + 21.7934
                   8.0 + 20.3928
                   8.0 + 18.5978
                   8.0 + 16.2995
                   8.0 + 14.658
                   8.0 + 13.1148
                   8.0 + 11.7142
                   8.0 + 9.4159
                     8.0+7.38
                    8.0 + 5.9794
                    8.0 + 3.4365
                    8.0 + 0.5746
                     8.0 + 0.0
```

```
0.0 + 36.5232
                 0.0539 + 36.0871
                 1.2595 + 35.6167
                 3.7307 + 35.2458
                 5.9267 + 34.8425
                 7.1926 + 34.4064
                  7.7386 + 33.936
                 7.9278 + 33.1535
                 7.9826 + 32.4666
                 7.9963 + 32.0305
                 7.9993 + 31.5601
                  7.9999 + 30.706
                   8.0 + 29.8306
                   8.0 + 28.8919
                   8.0 + 28.1987
                   8.0 + 27.3446
                                      =41.6746, \quad x_8^0=6
\varphi_8(32) = \max
                   8.0 + 26.4692
                   8.0 + 25.5305
                   8.0 + 24.1299
                   8.0 + 22.7321
                   8.0 + 21.7934
                   8.0 + 20.3928
                   8.0 + 18.5978
                   8.0 + 16.2995
                   8.0 + 14.658
                   8.0 + 13.1148
                   8.0 + 11.7142
                   8.0 + 9.4159
                     8.0 + 7.38
                    8.0 + 5.9794
                    8.0 + 3.4365
                    8.0 + 0.5746
                     8.0 + 0.0
```

```
0.0 + 36.9265
                 0.0539 + 36.5232
                 1.2595 + 36.0871
                 3.7307 + 35.6167
                 5.9267 + 35.2458
                 7.1926 + 34.8425
                 7.7386 + 34.4064
                  7.9278 + 33.936
                 7.9826 + 33.1535
                 7.9963 + 32.4666
                 7.9993 + 32.0305
                 7.9999 + 31.5601
                    8.0 + 30.706
                   8.0 + 29.8306
                   8.0 + 28.8919
                   8.0 + 28.1987
                   8.0 + 27.3446
\varphi_8(33) = \max
                                      =42.145, \quad x_8^0=6
                   8.0 + 26.4692
                   8.0 + 25.5305
                   8.0 + 24.1299
                   8.0 + 22.7321
                   8.0 + 21.7934
                   8.0 + 20.3928
                   8.0 + 18.5978
                   8.0 + 16.2995
                   8.0 + 14.658
                   8.0 + 13.1148
                   8.0 + 11.7142
                    8.0 + 9.4159
                     8.0 + 7.38
                    8.0 + 5.9794
                    8.0 + 3.4365
                    8.0 + 0.5746
                     8.0 + 0.0
```

```
0.0 + 37.2524
                 0.0539 + 36.9265
                 1.2595 + 36.5232
                 3.7307 + 36.0871
                 5.9267 + 35.6167
                 7.1926 + 35.2458
                 7.7386 + 34.8425
                 7.9278 + 34.4064
                  7.9826 + 33.936
                 7.9963 + 33.1535
                 7.9993 + 32.4666
                 7.9999 + 32.0305
                   8.0 + 31.5601
                   8.0 + 30.706
                   8.0 + 29.8306
                   8.0 + 28.8919
                   8.0 + 28.1987
\varphi_8(34) = \max
                                      =42.5811, \quad x_8^0=6
                   8.0 + 27.3446
                   8.0 + 26.4692
                   8.0 + 25.5305
                   8.0 + 24.1299
                   8.0 + 22.7321
                   8.0 + 21.7934
                   8.0 + 20.3928
                   8.0 + 18.5978
                   8.0 + 16.2995
                   8.0 + 14.658
                   8.0 + 13.1148
                   8.0 + 11.7142
                   8.0 + 9.4159
                     8.0 + 7.38
                    8.0 + 5.9794
                    8.0 + 3.4365
                    8.0 + 0.5746
                     8.0 + 0.0
```

```
0.0 + 37.5464
                 0.0539 + 37.2524
                 1.2595 + 36.9265
                 3.7307 + 36.5232
                 5.9267 + 36.0871
                 7.1926 + 35.6167
                 7.7386 + 35.2458
                 7.9278 + 34.8425
                 7.9826 + 34.4064
                  7.9963 + 33.936
                 7.9993 + 33.1535
                 7.9999 + 32.4666
                   8.0 + 32.0305
                   8.0 + 31.5601
                   8.0 + 30.706
                   8.0 + 29.8306
                   8.0 + 28.8919
                   8.0 + 28.1987
                                      =42.9844, \quad x_8^0=6
\varphi_8(35) = \max
                   8.0 + 27.3446
                   8.0 + 26.4692
                   8.0 + 25.5305
                   8.0 + 24.1299
                   8.0 + 22.7321
                   8.0 + 21.7934
                   8.0 + 20.3928
                   8.0 + 18.5978
                   8.0 + 16.2995
                   8.0 + 14.658
                   8.0 + 13.1148
                   8.0 + 11.7142
                   8.0 + 9.4159
                     8.0 + 7.38
                   8.0 + 5.9794
                   8.0 + 3.4365
                   8.0 + 0.5746
                     8.0 + 0.0
```

```
0.0 + 37.8069
                 0.0539 + 37.5464
                 1.2595 + 37.2524
                 3.7307 + 36.9265
                 5.9267 + 36.5232
                 7.1926 + 36.0871
                 7.7386 + 35.6167
                 7.9278 + 35.2458
                 7.9826 + 34.8425
                 7.9963 + 34.4064
                  7.9993 + 33.936
                 7.9999 + 33.1535
                   8.0 + 32.4666
                   8.0 + 32.0305
                   8.0 + 31.5601
                    8.0 + 30.706
                   8.0 + 29.8306
                   8.0 + 28.8919
\varphi_8(36) = \max
                   8.0 + 28.1987
                                      =43.3553, \quad x_8^0=6
                   8.0 + 27.3446
                   8.0 + 26.4692
                   8.0 + 25.5305
                   8.0 + 24.1299
                   8.0 + 22.7321
                   8.0 + 21.7934
                   8.0 + 20.3928
                   8.0 + 18.5978
                   8.0 + 16.2995
                    8.0 + 14.658
                   8.0 + 13.1148
                   8.0 + 11.7142
                    8.0 + 9.4159
                     8.0 + 7.38
                    8.0 + 5.9794
                    8.0 + 3.4365
                    8.0 + 0.5746
                     8.0 + 0.0
```

## 9 Product 9

$$\varphi_9(0) = \max\{0.0\} = 0.0, x_9^0 = 0$$

$$\varphi_{9}(1) = \max \left\{ \begin{array}{l} 0.0 + 0.5746 \\ 0.0333 + 0.0 \end{array} \right\} = 0.5746, \quad x_{9}^{0} = 0$$

$$\varphi_{9}(2) = \max \left\{ \begin{array}{l} 0.0 + 3.4365 \\ 0.0333 + 0.5746 \\ 0.5991 + 0.0 \end{array} \right\} = 3.4365, \quad x_{9}^{0} = 0$$

$$\varphi_{9}(3) = \max \left\{ \begin{array}{l} 0.0 + 5.9794 \\ 0.0333 + 3.4365 \\ 0.5991 + 0.5746 \\ 1.5934 + 0.0 \end{array} \right\} = 5.9794, \quad x_{9}^{0} = 0$$

$$\varphi_{9}(4) = \max \left\{ \begin{array}{l} 0.0 + 7.38 \\ 0.033 + 5.9794 \\ 0.5991 + 3.4365 \\ 1.5934 + 0.5746 \\ 2.3759 + 0.0 \end{array} \right\} = 7.38, \quad x_{9}^{0} = 0$$

$$\varphi_{9}(5) = \max \left\{ \begin{array}{l} 0.0 + 9.4159 \\ 0.0333 + 7.38 \\ 0.5991 + 5.9794 \\ 1.5934 + 3.4365 \\ 2.3759 + 0.5746 \\ 2.7792 + 0.0 \end{array} \right\} = 9.4159, \quad x_{9}^{0} = 0$$

$$\varphi_{9}(6) = \max \left\{ \begin{array}{l} 0.0 + 11.7142 \\ 0.0333 + 9.4159 \\ 0.5991 + 7.38 \\ 1.5934 + 5.9794 \\ 2.3759 + 3.4365 \\ 2.7792 + 0.5746 \\ 2.9353 + 0.0 \end{array} \right\} = 11.7142, \quad x_{9}^{0} = 0$$

$$\varphi_{9}(7) = \max \left\{ \begin{array}{l} 0.0 + 11.1148 \\ 0.0333 + 11.7142 \\ 0.5991 + 9.4159 \\ 1.5934 + 7.38 \\ 2.3759 + 5.9794 \\ 2.7792 + 3.4365 \\ 2.9353 + 0.0 \end{array} \right\} = 13.1148, \quad x_{9}^{0} = 0$$

$$\varphi_{9}(8) = \max \left\{ \begin{array}{l} 0.0 + 13.1148 \\ 0.0333 + 13.1148 \\ 0.0333 + 13.1148 \\ 0.5991 + 11.7142 \\ 1.5934 + 9.4159 \\ 2.3759 + 7.38 \\ 2.7792 + 5.9794 \\ 2.9353 + 3.4365 \\ 2.9838 + 0.0 \end{array} \right\} = 14.658, \quad x_{9}^{0} = 0$$

$$\varphi_{9}(8) = \max \left\{ \begin{array}{l} 0.0 + 14.658 \\ 0.0333 + 13.1148 \\ 0.5991 + 11.7142 \\ 1.5934 + 9.4159 \\ 2.3759 + 7.38 \\ 2.7792 + 5.9794 \\ 2.9353 + 3.4365 \\ 2.9838 + 0.5746 \\ 2.9965 + 0.0 \end{array} \right\} = 14.658, \quad x_{9}^{0} = 0$$

$$\varphi_{9}(9) = \max \begin{cases} 0.0 + 16.2995 \\ 0.0333 + 14.658 \\ 0.5991 + 13.1148 \\ 1.5934 + 11.7142 \\ 2.3759 + 9.4159 \\ 2.7792 + 7.38 \\ 2.9353 + 5.9794 \\ 2.9838 + 3.4365 \\ 2.9993 + 0.0 \end{cases} = 16.2995, \quad x_{9}^{0} = 0$$

$$\begin{cases} 0.0 + 18.5978 \\ 0.0333 + 16.2995 \\ 0.5991 + 14.658 \\ 1.5934 + 13.1148 \\ 2.3759 + 11.7142 \\ 2.7792 + 9.4159 \\ 2.9353 + 7.38 \\ 2.9938 + 5.9794 \\ 2.9965 + 3.4365 \\ 2.9993 + 0.5746 \\ 2.9999 + 0.0 \end{cases} = 18.5978, \quad x_{9}^{0} = 0$$

$$\begin{cases} 0.0 + 20.3928 \\ 0.0333 + 18.5978 \\ 0.5991 + 16.2995 \\ 1.5934 + 14.658 \\ 2.3759 + 13.1148 \\ 2.7792 + 11.7142 \\ 2.9353 + 9.4159 \\ 2.9353 + 9.4159 \\ 2.9838 + 7.38 \\ 2.9965 + 5.9794 \\ 2.9993 + 3.4365 \\ 2.9993 + 3.4365 \\ 2.9999 + 0.5746 \\ 3.0 + 0.0 \end{cases} = 20.3928, \quad x_{9}^{0} = 0$$

```
0.0 + 21.7934
                  0.0333 + 20.3928
                  0.5991 + 18.5978
                  1.5934 + 16.2995
                  2.3759 + 14.658
                  2.7792 + 13.1148
\varphi_9(12) = \max
                                       =21.7934, \quad x_9^0=0
                  2.9353 + 11.7142
                  2.9838 + 9.4159
                   2.9965 + 7.38
                  2.9993 + 5.9794
                  2.9999 + 3.4365
                    3.0 + 0.5746
                      3.0 + 0.0
                   0.0 + 22.7321
                  0.0333 + 21.7934
                  0.5991 + 20.3928
                  1.5934 + 18.5978
                  2.3759 + 16.2995
                  2.7792 + 14.658
                  2.9353 + 13.1148
                                       =22.7321, \quad x_9^0=0
\varphi_9(13) = \max
                  2.9838 + 11.7142
                  2.9965 + 9.4159
                   2.9993 + 7.38
                  2.9999 + 5.9794
                    3.0 + 3.4365
                    3.0 + 0.5746
                      3.0 + 0.0
                   0.0 + 24.5245
                  0.0333 + 22.7321
                  0.5991 + 21.7934
                  1.5934 + 20.3928
                  2.3759 + 18.5978
                  2.7792 + 16.2995
                  2.9353 + 14.658
\varphi_9(14) = \max
                                       =24.5245,\quad x_9^0=0
                  2.9838 + 13.1148
                  2.9965 + 11.7142
                  2.9993 + 9.4159
                   2.9999 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.4365
                    3.0 + 0.5746
                      3.0 + 0.0
```

```
0.0 + 26.3195
                  0.0333 + 24.5245
                  0.5991 + 22.7321
                  1.5934 + 21.7934
                  2.3759 + 20.3928
                  2.7792 + 18.5978
                  2.9353 + 16.2995
                  2.9838 + 14.658
\varphi_9(15) = \max
                                       = 26.3195, \quad x_9^0 = 0
                  2.9965 + 13.1148
                  2.9993 + 11.7142
                  2.9999 + 9.4159
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.4365
                    3.0 + 0.5746
                      3.0 + 0.0
                    0.0 + 27.7201
                  0.0333 + 26.3195
                  0.5991 + 24.5245
                  1.5934 + 22.7321
                  2.3759 + 21.7934
                  2.7792 + 20.3928
                  2.9353 + 18.5978
                  2.9838 + 16.2995
\varphi_9(16) = \max \langle
                  2.9965 + 14.658
                                       = 27.7201, \quad x_9^0 = 0
                  2.9993 + 13.1148
                  2.9999 + 11.7142
                    3.0 + 9.4159
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.4365
                    3.0 + 0.5746
                      3.0 + 0.0
```

```
0.0 + 28.986
                 0.0333 + 27.7201
                 0.5991 + 26.3195
                 1.5934 + 24.5245
                 2.3759 + 22.7321
                 2.7792 + 21.7934
                 2.9353 + 20.3928
                 2.9838 + 18.5978
                 2.9965 + 16.2995
                                      = 28.986, \quad x_9^0 = 0
\varphi_9(17) = \max
                  2.9993 + 14.658
                 2.9999 + 13.1148
                   3.0 + 11.7142
                    3.0 + 9.4159
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.4365
                    3.0 + 0.5746
                      3.0 + 0.0
                   0.0 + 30.0566
                  0.0333 + 28.986
                 0.5991 + 27.7201
                 1.5934 + 26.3195
                 2.3759 + 24.5245
                 2.7792 + 22.7321
                 2.9353 + 21.7934
                 2.9838 + 20.3928
                 2.9965 + 18.5978
\varphi_9(18) = \max
                                      = 30.0566,
                                                   x_9^0 = 0
                 2.9993 + 16.2995
                  2.9999 + 14.658
                   3.0 + 13.1148
                   3.0 + 11.7142
                    3.0 + 9.4159
                     3.0+7.38
                    3.0 + 5.9794
                    3.0 + 3.4365
                    3.0 + 0.5746
                      3.0 + 0.0
```

```
0.0 + 31.4572
                  0.0333 + 30.0566
                  0.5991 + 28.986
                  1.5934 + 27.7201
                  2.3759 + 26.3195
                  2.7792 + 24.5245
                  2.9353 + 22.7321
                  2.9838 + 21.7934
                  2.9965 + 20.3928
                  2.9993 + 18.5978
\varphi_9(19) = \max
                                       = 31.4572, \quad x_9^0 = 0
                  2.9999 + 16.2995
                    3.0 + 14.658
                   3.0 + 13.1148
                   3.0 + 11.7142
                    3.0 + 9.4159
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.4365
                    3.0 + 0.5746
                      3.0 + 0.0
                   0.0 + 32.7231
                  0.0333 + 31.4572
                  0.5991 + 30.0566
                  1.5934 + 28.986
                  2.3759 + 27.7201
                  2.7792 + 26.3195
                  2.9353 + 24.5245
                  2.9838 + 22.7321
                  2.9965 + 21.7934
                  2.9993 + 20.3928
                                       = 32.7231, \quad x_9^0 = 0
\varphi_9(20) = \max
                  2.9999 + 18.5978
                   3.0 + 16.2995
                    3.0 + 14.658
                   3.0 + 13.1148
                   3.0 + 11.7142
                    3.0 + 9.4159
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.4365
                    3.0 + 0.5746
                      3.0 + 0.0
```

```
0.0 + 33.6618
                  0.0333 + 32.7231
                  0.5991 + 31.4572
                  1.5934 + 30.0566
                  2.3759 + 28.986
                  2.7792 + 27.7201
                  2.9353 + 26.3195
                  2.9838 + 24.5245
                  2.9965 + 22.7321
                  2.9993 + 21.7934
                  2.9999 + 20.3928
                                                    x_9^0 = 0
\varphi_9(21) = \max
                                       = 33.6618,
                   3.0 + 18.5978
                   3.0 + 16.2995
                    3.0 + 14.658
                   3.0 + 13.1148
                   3.0 + 11.7142
                    3.0 + 9.4159
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.4365
                    3.0 + 0.5746
                      3.0 + 0.0
                   0.0 + 34.5372
                  0.0333 + 33.6618
                  0.5991 + 32.7231
                  1.5934 + 31.4572
                  2.3759 + 30.0566
                  2.7792 + 28.986
                  2.9353 + 27.7201
                  2.9838 + 26.3195
                  2.9965 + 24.5245
                  2.9993 + 22.7321
                  2.9999 + 21.7934
                                       = 34.5372, \quad x_9^0 = 0
\varphi_9(22) = \max
                   3.0 + 20.3928
                   3.0 + 18.5978
                   3.0 + 16.2995
                    3.0 + 14.658
                   3.0 + 13.1148
                   3.0 + 11.7142
                    3.0 + 9.4159
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.4365
                    3.0 + 0.5746
                      3.0 + 0.0
```

```
0.0 + 35.3913
                 0.0333 + 34.5372
                 0.5991 + 33.6618
                 1.5934 + 32.7231
                 2.3759 + 31.4572
                 2.7792 + 30.0566
                  2.9353 + 28.986
                 2.9838 + 27.7201
                 2.9965 + 26.3195
                 2.9993 + 24.5245
                 2.9999 + 22.7321
                   3.0 + 21.7934
                                      = 35.3913, \quad x_9^0 = 0
\varphi_9(23) = \max
                   3.0 + 20.3928
                   3.0 + 18.5978
                   3.0 + 16.2995
                   3.0 + 14.658
                   3.0 + 13.1148
                   3.0 + 11.7142
                   3.0 + 9.4159
                    3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.4365
                    3.0 + 0.5746
                     3.0 + 0.0
```

```
0.0 + 36.0845
                  0.0333 + 35.3913
                  0.5991 + 34.5372
                  1.5934 + 33.6618
                  2.3759 + 32.7231
                  2.7792 + 31.4572
                  2.9353 + 30.0566
                  2.9838 + 28.986
                  2.9965 + 27.7201
                  2.9993 + 26.3195
                  2.9999 + 24.5245
                   3.0 + 22.7321
\varphi_9(24) = \max \langle
                   3.0 + 21.7934
                                       =36.0845,\quad x_9^0=0
                   3.0 + 20.3928
                    3.0 + 18.5978
                   3.0 + 16.2995
                    3.0 + 14.658
                   3.0 + 13.1148
                   3.0 + 11.7142
                    3.0 + 9.4159
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.4365
                    3.0 + 0.5746
                      3.0 + 0.0
```

```
0.0 + 37.0232
                  0.0333 + 36.0845
                  0.5991 + 35.3913
                  1.5934 + 34.5372
                  2.3759 + 33.6618
                  2.7792 + 32.7231
                  2.9353 + 31.4572
                  2.9838 + 30.0566
                  2.9965 + 28.986
                  2.9993 + 27.7201
                  2.9999 + 26.3195
                   3.0 + 24.5245
                   3.0 + 22.7321
                                       = 37.0232, \quad x_9^0 = 0
\varphi_9(25) = \max
                   3.0 + 21.7934
                   3.0 + 20.3928
                   3.0 + 18.5978
                   3.0 + 16.2995
                   3.0 + 14.658
                   3.0 + 13.1148
                   3.0 + 11.7142
                    3.0 + 9.4159
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.4365
                    3.0 + 0.5746
                      3.0 + 0.0
```

```
0.0 + 37.8986
                 0.0333 + 37.0232
                 0.5991 + 36.0845
                 1.5934 + 35.3913
                 2.3759 + 34.5372
                 2.7792 + 33.6618
                 2.9353 + 32.7231
                 2.9838 + 31.4572
                 2.9965 + 30.0566
                  2.9993 + 28.986
                 2.9999 + 27.7201
                   3.0 + 26.3195
                   3.0 + 24.5245
\varphi_9(26) = \max
                   3.0 + 22.7321
                                      = 37.8986, \quad x_9^0 = 0
                   3.0 + 21.7934
                   3.0 + 20.3928
                   3.0 + 18.5978
                   3.0 + 16.2995
                   3.0 + 14.658
                   3.0 + 13.1148
                   3.0 + 11.7142
                    3.0 + 9.4159
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.4365
                    3.0 + 0.5746
                     3.0 + 0.0
```

```
0.0 + 38.7527
                 0.0333 + 37.8986
                 0.5991 + 37.0232
                 1.5934 + 36.0845
                 2.3759 + 35.3913
                 2.7792 + 34.5372
                 2.9353 + 33.6618
                 2.9838 + 32.7231
                 2.9965 + 31.4572
                 2.9993 + 30.0566
                  2.9999 + 28.986
                   3.0 + 27.7201
                   3.0 + 26.3195
                   3.0 + 24.5245
\varphi_9(27) = \max
                                      =38.7527, \quad x_9^0=0
                   3.0 + 22.7321
                   3.0 + 21.7934
                   3.0 + 20.3928
                   3.0 + 18.5978
                   3.0 + 16.2995
                   3.0 + 14.658
                   3.0 + 13.1148
                   3.0 + 11.7142
                   3.0 + 9.4159
                    3.0 + 7.38
                   3.0 + 5.9794
                   3.0 + 3.4365
                   3.0 + 0.5746
                     3.0 + 0.0
```

```
0.0 + 39.2987
                  0.0333 + 38.7527
                  0.5991 + 37.8986
                  1.5934 + 37.0232
                  2.3759 + 36.0845
                  2.7792 + 35.3913
                  2.9353 + 34.5372
                  2.9838 + 33.6618
                  2.9965 + 32.7231
                  2.9993 + 31.4572
                  2.9999 + 30.0566
                    3.0 + 28.986
                   3.0 + 27.7201
                   3.0 + 26.3195
                                      = 39.2987, \quad x_9^0 = 0
\varphi_9(28) = \max
                   3.0 + 24.5245
                   3.0 + 22.7321
                   3.0 + 21.7934
                   3.0 + 20.3928
                   3.0 + 18.5978
                   3.0 + 16.2995
                    3.0 + 14.658
                   3.0 + 13.1148
                   3.0 + 11.7142
                    3.0 + 9.4159
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.4365
                    3.0 + 0.5746
                      3.0 + 0.0
```

```
0.0 + 39.7691
                  0.0333 + 39.2987
                  0.5991 + 38.7527
                  1.5934 + 37.8986
                  2.3759 + 37.0232
                  2.7792 + 36.0845
                  2.9353 + 35.3913
                  2.9838 + 34.5372
                  2.9965 + 33.6618
                  2.9993 + 32.7231
                  2.9999 + 31.4572
                   3.0 + 30.0566
                    3.0 + 28.986
                   3.0 + 27.7201
                   3.0 + 26.3195
\varphi_9(29) = \max
                                       = 39.7691, \quad x_9^0 = 0
                   3.0 + 24.5245
                   3.0 + 22.7321
                   3.0 + 21.7934
                   3.0 + 20.3928
                   3.0 + 18.5978
                   3.0 + 16.2995
                    3.0 + 14.658
                   3.0 + 13.1148
                   3.0 + 11.7142
                    3.0 + 9.4159
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.4365
                    3.0 + 0.5746
                      3.0 + 0.0
```

```
0.0 + 40.3461
                 0.0333 + 39.7691
                 0.5991 + 39.2987
                 1.5934 + 38.7527
                 2.3759 + 37.8986
                 2.7792 + 37.0232
                 2.9353 + 36.0845
                 2.9838 + 35.3913
                 2.9965 + 34.5372
                 2.9993 + 33.6618
                 2.9999 + 32.7231
                   3.0 + 31.4572
                   3.0 + 30.0566
                    3.0 + 28.986
                   3.0 + 27.7201
                                      =40.3461, \quad x_9^0=0
\varphi_9(30) = \max
                   3.0 + 26.3195
                   3.0 + 24.5245
                   3.0 + 22.7321
                   3.0 + 21.7934
                   3.0 + 20.3928
                   3.0 + 18.5978
                   3.0 + 16.2995
                    3.0 + 14.658
                   3.0 + 13.1148
                   3.0 + 11.7142
                   3.0 + 9.4159
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.4365
                    3.0 + 0.5746
                     3.0 + 0.0
```

```
0.0 + 41.1286
                 0.0333 + 40.3461
                 0.5991 + 39.7691
                 1.5934 + 39.2987
                 2.3759 + 38.7527
                 2.7792 + 37.8986
                 2.9353 + 37.0232
                 2.9838 + 36.0845
                 2.9965 + 35.3913
                 2.9993 + 34.5372
                 2.9999 + 33.6618
                   3.0 + 32.7231
                   3.0 + 31.4572
                   3.0 + 30.0566
                    3.0 + 28.986
                   3.0 + 27.7201
\varphi_9(31) = \max
                                      =41.1286, \quad x_9^0=0
                   3.0 + 26.3195
                   3.0 + 24.5245
                   3.0 + 22.7321
                   3.0 + 21.7934
                   3.0 + 20.3928
                   3.0 + 18.5978
                   3.0 + 16.2995
                   3.0 + 14.658
                   3.0 + 13.1148
                   3.0 + 11.7142
                   3.0 + 9.4159
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.4365
                    3.0 + 0.5746
                     3.0 + 0.0
```

```
0.0 + 41.6746
                 0.0333 + 41.1286
                 0.5991 + 40.3461
                 1.5934 + 39.7691
                 2.3759 + 39.2987
                 2.7792 + 38.7527
                 2.9353 + 37.8986
                 2.9838 + 37.0232
                 2.9965 + 36.0845
                 2.9993 + 35.3913
                 2.9999 + 34.5372
                   3.0 + 33.6618
                   3.0 + 32.7231
                   3.0 + 31.4572
                   3.0 + 30.0566
                   3.0 + 28.986
                                                   x_9^0 = 0
\varphi_9(32) = \max
                   3.0 + 27.7201
                                    = 41.6746,
                   3.0 + 26.3195
                   3.0 + 24.5245
                   3.0 + 22.7321
                   3.0 + 21.7934
                   3.0 + 20.3928
                   3.0 + 18.5978
                   3.0 + 16.2995
                   3.0 + 14.658
                   3.0 + 13.1148
                   3.0 + 11.7142
                   3.0 + 9.4159
                    3.0 + 7.38
                   3.0 + 5.9794
                   3.0 + 3.4365
                   3.0 + 0.5746
                     3.0 + 0.0
```

```
0.0 + 42.145
                 0.0333 + 41.6746
                 0.5991 + 41.1286
                 1.5934 + 40.3461
                 2.3759 + 39.7691
                 2.7792 + 39.2987
                 2.9353 + 38.7527
                 2.9838 + 37.8986
                 2.9965 + 37.0232
                 2.9993 + 36.0845
                 2.9999 + 35.3913
                   3.0 + 34.5372
                   3.0 + 33.6618
                   3.0 + 32.7231
                   3.0 + 31.4572
                   3.0 + 30.0566
                   3.0 + 28.986
\varphi_9(33) = \max
                                      =42.145, \quad x_9^0=0
                   3.0 + 27.7201
                   3.0 + 26.3195
                   3.0 + 24.5245
                   3.0 + 22.7321
                   3.0 + 21.7934
                   3.0 + 20.3928
                   3.0 + 18.5978
                   3.0 + 16.2995
                   3.0 + 14.658
                   3.0 + 13.1148
                   3.0 + 11.7142
                   3.0 + 9.4159
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.4365
                    3.0 + 0.5746
                     3.0 + 0.0
```

```
0.0 + 42.5811
                  0.0333 + 42.145
                 0.5991 + 41.6746
                 1.5934 + 41.1286
                 2.3759 + 40.3461
                 2.7792 + 39.7691
                 2.9353 + 39.2987
                 2.9838 + 38.7527
                 2.9965 + 37.8986
                 2.9993 + 37.0232
                 2.9999 + 36.0845
                   3.0 + 35.3913
                   3.0 + 34.5372
                   3.0 + 33.6618
                   3.0 + 32.7231
                   3.0 + 31.4572
                   3.0 + 30.0566
\varphi_9(34) = \max
                                      =42.722, \quad x_9^0=3
                   3.0 + 28.986
                   3.0 + 27.7201
                   3.0 + 26.3195
                   3.0 + 24.5245
                   3.0 + 22.7321
                   3.0 + 21.7934
                   3.0 + 20.3928
                   3.0 + 18.5978
                   3.0 + 16.2995
                   3.0 + 14.658
                   3.0 + 13.1148
                   3.0 + 11.7142
                    3.0 + 9.4159
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.4365
                    3.0 + 0.5746
                     3.0 + 0.0
```

```
0.0 + 42.9844
                 0.0333 + 42.5811
                  0.5991 + 42.145
                 1.5934 + 41.6746
                 2.3759 + 41.1286
                 2.7792 + 40.3461
                 2.9353 + 39.7691
                 2.9838 + 39.2987
                 2.9965 + 38.7527
                 2.9993 + 37.8986
                 2.9999 + 37.0232
                   3.0 + 36.0845
                   3.0 + 35.3913
                   3.0 + 34.5372
                   3.0 + 33.6618
                   3.0 + 32.7231
                   3.0 + 31.4572
                   3.0 + 30.0566
                                      =43.5045, \quad x_9^0=4
\varphi_9(35) = \max
                   3.0 + 28.986
                   3.0 + 27.7201
                   3.0 + 26.3195
                   3.0 + 24.5245
                   3.0 + 22.7321
                   3.0 + 21.7934
                   3.0 + 20.3928
                   3.0 + 18.5978
                   3.0 + 16.2995
                   3.0 + 14.658
                   3.0 + 13.1148
                   3.0 + 11.7142
                    3.0 + 9.4159
                     3.0 + 7.38
                    3.0 + 5.9794
                    3.0 + 3.4365
                    3.0 + 0.5746
                     3.0 + 0.0
```

```
0.0 + 43.3553
                 0.0333 + 42.9844
                 0.5991 + 42.5811
                  1.5934 + 42.145
                 2.3759 + 41.6746
                 2.7792 + 41.1286
                 2.9353 + 40.3461
                 2.9838 + 39.7691
                 2.9965 + 39.2987
                 2.9993 + 38.7527
                 2.9999 + 37.8986
                   3.0 + 37.0232
                   3.0 + 36.0845
                   3.0 + 35.3913
                   3.0 + 34.5372
                   3.0 + 33.6618
                   3.0 + 32.7231
                   3.0 + 31.4572
\varphi_9(36) = \max
                   3.0 + 30.0566
                                      =44.0505,
                                                   x_9^0 = 4
                   3.0 + 28.986
                   3.0 + 27.7201
                   3.0 + 26.3195
                   3.0 + 24.5245
                   3.0 + 22.7321
                   3.0 + 21.7934
                   3.0 + 20.3928
                   3.0 + 18.5978
                   3.0 + 16.2995
                   3.0 + 14.658
                   3.0 + 13.1148
                   3.0 + 11.7142
                   3.0 + 9.4159
                    3.0 + 7.38
                   3.0 + 5.9794
                   3.0 + 3.4365
                   3.0 + 0.5746
                     3.0 + 0.0
```