

# Package ‘CPAT’

October 28, 2018

**Title** Change Point Analysis Tests

**Version** 0.1.0

**Date** 2018-10-16

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**Description** Implements several statistical tests for structural change, specifically the tests featured in Horváth, Rice and Miller (in press).

**Depends** R (>= 3.2)

**Suggests** coinReg (>= 0.2), foreach (>= 1.4), doRNG (>= 1.7),  
doParallel (>= 1.0), ggplot2 (>= 2.2), dplyr (>= 0.7),  
tikzDevice (>= 0.12), testthat (>= 2.0)

**Imports** stats (>= 3.2), utils (>= 3.2), grDevices (>= 3.2), Rdpack (>= 0.9), methods (>= 3.2), Rcpp (>= 0.12), purrr (>= 0.2)

**RdMacros** Rdpack

**SystemRequirements** GNU make

**License** MIT + file LICENSE

**Encoding** UTF-8

**LazyData** true

**LinkingTo** Rcpp, RcppArmadillo

**RoxygenNote** 6.1.0

**NeedsCompilation** yes

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.onAttach	<i>Package Attach Hook Function</i>
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**Description**

Hook triggered when package attached

**Usage**

.onAttach(lib, pkg)

**Arguments**

- |     |  |
|-----|--|
| lib | a character string giving the library directory where the package defining the namespace was found |
| pkg | a character string giving the name of the package  |

**Examples**

CPAT:::.onAttach(.libPaths()[1], "CPAT")

---

Andrews.test	<i>Andrews' Test for End-of-Sample Structural Change</i>
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---

### Description

Performs Andrews' test for end-of-sample structural change, as described in (Andrews 2003). This function works for both univariate and multivariate data depending on the nature of `x` and whether formula is specified. This function is thus an interface to [andrews\\_test](#) and [andrews\\_test\\_reg](#); see the documentation of those functions for more details.

### Usage

```
Andrews.test(x, M, formula = NULL)
```

### Arguments

<code>x</code>	Data to test for change in mean (either a vector or <code>data.frame</code> )
<code>M</code>	Numeric index of the location of the first potential change point
<code>formula</code>	The regression formula, which will be passed to <a href="#">lm</a>

### Value

A `htest`-class object containing the results of the test

### References

Andrews DWK (2003). "End-of-Sample Instability Tests." *Econometrica*, **71**(6), 1661–1694. ISSN 00129682, 14680262, <https://www.jstor.org/stable/1555535>.

### Examples

```
Andrews.test(rnorm(1000), M = 900)
x <- rnorm(1000)
y <- 1 + 2 * x + rnorm(1000)
df <- data.frame(x, y)
Andrews.test(df, y ~ x, M = 900)
```

---

<code>andrews_test</code>	<i>Univariate Andrews Test for End-of-Sample Structural Change</i>
---------------------------	--

---

### Description

This implements Andrews' test for end-of-sample change, as described by Andrews (2003). This test was derived for detecting a change in univariate data. See (Andrews 2003) for a description of the test.

### Usage

```
andrews_test(x, M, pval = TRUE, stat = TRUE)
```

**Arguments**

x	Vector of the data to test
M	Numeric index of the location of the first potential change point
pval	If TRUE, return a p-value
stat	If TRUE, return a test statistic

**Value**

If both `pval` and `stat` are TRUE, a list containing both; otherwise, a number for one or the other, depending on which is TRUE

**References**

Andrews DWK (2003). “End-of-Sample Instability Tests.” *Econometrica*, **71**(6), 1661–1694. ISSN 00129682, 14680262, <https://www.jstor.org/stable/1555535>.

**Examples**

```
CPAT:::andrews_test(rnorm(1000), M = 900)
```

---

andrews_test_reg	<i>Multivariate Andrews’ Test for End-of-Sample Structural Change</i>
------------------	---

---

**Description**

This implements Andrews’ test for end-of-sample change, as described by Andrews (2003). This test was derived for detecting a change in multivariate data, also originally described. See (Andrews 2003) for a description of the test.

**Usage**

```
andrews_test_reg(formula, data, M, pval = TRUE, stat = TRUE)
```

**Arguments**

formula	The regression formula, which will be passed to <a href="#">lm</a>
data	<code>data.frame</code> containing the data
M	Numeric index of the location of the first potential change point
pval	If TRUE, return a p-value
stat	If TRUE, return a test statistic

**Value**

If both `pval` and `stat` are TRUE, a list containing both; otherwise, a number for one or the other, depending on which is TRUE

**References**

Andrews DWK (2003). “End-of-Sample Instability Tests.” *Econometrica*, **71**(6), 1661–1694. ISSN 00129682, 14680262, <https://www.jstor.org/stable/1555535>.

### Examples

```
x <- rnorm(1000)
y <- 1 + 2 * x + rnorm(1000)
df <- data.frame(x, y)
CPAT::andrews_test_reg(y ~ x, data = df, M = 900)
```

---

banks	<i>Bank Portfolio Returns</i>
-------	-------------------------------

---

### Description

Data set representing the returns of an industry portfolio representing the banking industry based on company four-digit SIC codes, obtained from the data library maintained by Kenneth French. Data ranges from July 1, 1926 to October 31, 2017.

### Usage

```
banks
```

### Format

A data frame with 24099 rows and 1 variable:

**Banks** The return of a portfolio representing the banking industry

Row names are dates in YYYY-MM-DD format.

### Source

[http://mba.tuck.dartmouth.edu/pages/faculty/ken.french/data\\_library.html](http://mba.tuck.dartmouth.edu/pages/faculty/ken.french/data_library.html)

---

CPAT_startup_message	<i>Create Package Startup Message</i>
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---

### Description

Makes package startup message.

### Usage

```
CPAT_startup_message()
```

### Examples

```
CPAT::CPAT_startup_message()
```

---

cpt_consistent_var	<i>Variance Estimation Consistent Under Change</i>
--------------------	--

---

### Description

Estimate the variance (using the sum of squared errors) with an estimator that is consistent when the mean changes at a known point.

### Usage

```
cpt_consistent_var(x, k)
```

### Arguments

x	A numeric vector for the data set
k	The potential change point at which the data set is split

### Details

This is the estimator

$$\hat{\sigma}_{T,t}^2 = T^{-1} \left( \sum_{s=1}^t (X_s - \bar{X}_t)^2 + \sum_{s=t+1}^T (X_s - \tilde{X}_{T-t})^2 \right)$$

where  $\bar{X}_t = t^{-1} \sum_{s=1}^t X_s$  and  $\tilde{X}_{T-t} = (T-t)^{-1} \sum_{s=t+1}^T X_s$ . In this implementation,  $T$  is computed automatically as `length(x)` and  $k$  corresponds to  $t$ , a potential change point.

### Value

The estimated change-consistent variance

### Examples

```
CPAT::cpt_consistent_var(c(rnorm(500, mean = 0), rnorm(500, mean = 1)), k = 500)
```

---

CUSUM.test	<i>CUSUM Test</i>
------------	-------------------

---

### Description

Performs the (univariate) CUSUM test for change in mean, as described in (Rice et al. ). This is effectively an interface to [stat\\_Vn](#); see its documentation for more details. p-values are computed using [pkolmogorov](#), which represents the limiting distribution of the statistic under the null hypothesis.

### Usage

```
CUSUM.test(x, use_kernel_var = FALSE, stat_plot = FALSE,
  kernel = "ba", bandwidth = "and")
```

**Arguments**

x	Data to test for change in mean
use_kernel_var	Set to TRUE to use kernel methods for long-run variance estimation (typically used when the data is believed to be correlated); if FALSE, then the long-run variance is estimated using $\hat{\sigma}_{T,t}^2 = T^{-1} \left( \sum_{s=1}^t (X_s - \bar{X}_t)^2 + \sum_{s=t+1}^T (X_s - \tilde{X}_{T-t})^2 \right)$ , where $\bar{X}_t = t^{-1} \sum_{s=1}^t X_s$ and $\tilde{X}_{T-t} = (T-t)^{-1} \sum_{s=t+1}^T X_s$
stat_plot	Whether to create a plot of the values of the statistic at all potential change points
kernel	If character, the identifier of the kernel function as used in <b>cointReg</b> (see <a href="#">getLongRunVar</a> ); if function, the kernel function to be used for long-run variance estimation (default is the Bartlett kernel in <b>cointReg</b> )
bandwidth	If character, the identifier for how to compute the bandwidth as defined in <b>cointReg</b> (see <a href="#">getBandwidth</a> ); if function, a function to use for computing the bandwidth; if numeric, the bandwidth value to use (the default is to use Andrews' method, as used in <b>cointReg</b> )

**Value**

A htest-class object containing the results of the test

**References**

Rice G, Miller C, Horváth L (???). "A new class of change point test of Rényi type." in-press.

**Examples**

```
CUSUM.test(rnorm(1000))
CUSUM.test(rnorm(1000), use_kernel_var = TRUE, kernel = "bo",
            bandwidth = "nw")
```

---

DE.test

---

*Darling-Erdős Test*


---

**Description**

Performs the (univariate) Darling-Erdős test for change in mean, as described in (Rice et al. ). This is effectively an interface to [stat\\_de](#); see its documentation for more details. p-values are computed using [pdarling\\_erdos](#), which represents the limiting distribution of the test statistic under the null hypothesis when a and b are chosen appropriately. (Change those parameters at your own risk!)

**Usage**

```
DE.test(x, a = log, b = log, use_kernel_var = FALSE,
        stat_plot = FALSE, kernel = "ba", bandwidth = "and")
```

**Arguments**

x	Data to test for change in mean
a	The function that will be composed with $l(x) = (2 \log x)^{1/2}$
b	The function that will be composed with $u(x) = 2 \log x + \frac{1}{2} \log \log x - \frac{1}{2} \log \pi$
use_kernel_var	Set to TRUE to use kernel methods for long-run variance estimation (typically used when the data is believed to be correlated); if FALSE, then the long-run variance is estimated using $\hat{\sigma}_{T,t}^2 = T^{-1} \left( \sum_{s=1}^t (X_s - \bar{X}_t)^2 + \sum_{s=t+1}^T (X_s - \tilde{X}_{T-t})^2 \right)$ , where $\bar{X}_t = t^{-1} \sum_{s=1}^t X_s$ and $\tilde{X}_{T-t} = (T-t)^{-1} \sum_{s=t+1}^T X_s$
stat_plot	Whether to create a plot of the values of the statistic at all potential change points
kernel	If character, the identifier of the kernel function as used in <b>cointReg</b> (see <a href="#">getLongRunVar</a> ); if function, the kernel function to be used for long-run variance estimation (default is the Bartlett kernel in <b>cointReg</b> )
bandwidth	If character, the identifier for how to compute the bandwidth as defined in <b>cointReg</b> (see <a href="#">getBandwidth</a> ); if function, a function to use for computing the bandwidth; if numeric, the bandwidth value to use (the default is to use Andrews' method, as used in <b>cointReg</b> )

**Value**

A htest-class object containing the results of the test

**References**

Rice G, Miller C, Horváth L (???). "A new class of change point test of Rényi type." in-press.

**Examples**

```
DE.test(rnorm(1000))
DE.test(rnorm(1000), use_kernel_var = TRUE, kernel = "bo", bandwidth = "nw")
```

dZn

*Rényi-Type Statistic Limiting Distribution Density Function***Description**

Function for computing the value of the density function of the limiting distribution of the Rényi-type statistic.

**Usage**

```
dZn(x, summands = NULL)
```

**Arguments**

x	Point at which to evaluate the density function (note that this parameter is not vectorized)
summands	Number of summands to use in summation (the default should be machine accurate)



**Value**

Value of the density function at  $x$

**Examples**

CPAT:::dZn(1)

---

ff	<i>Fama-French Five Factors</i>
----	---------------------------------

---

**Description**

Data set containing the five factors described by Fama and French (2015), from the data library maintained by Kenneth French. Data ranges from July 1, 1963 to October 31, 2017.

**Usage**

ff

**Format**

A data frame with 13679 rows and 6 variables:

**Mkt.RF** Market excess returns

**RF** The risk-free rate of return

**SMB** The return on a diversified portfolio of small stocks minus return on a diversified portfolio of big stocks

**HML** The return of a portfolio of stocks with a high book-to-market (B/M) ratio minus the return of a portfolio of stocks with a low B/M ratio

**RMW** The return of a portfolio of stocks with robust profitability minus a portfolio of stocks with weak profitability

**CMA** The return of a portfolio of stocks with conservative investment minus the return of a portfolio of stocks with aggressive investment

Row names are dates in YYYYMMDD format.

**Source**

[http://mba.tuck.dartmouth.edu/pages/faculty/ken.french/data\\_library.html](http://mba.tuck.dartmouth.edu/pages/faculty/ken.french/data_library.html)

---

getLongRunWeights	<i>Weights for Long-Run Variance</i>
-------------------	--------------------------------------

---

### Description

Compute some weights for long-run variance. This code comes directly from the source code of **cointReg**; see [getLongRunWeights](#).

### Usage

```
getLongRunWeights(n, bandwidth, kernel = "ba")
```

### Arguments

n	Length of weights' vector
bandwidth	A number for the bandwidth
kernel	The kernel function; see <a href="#">getLongRunVar</a> for possible values

### Value

List with components w containing the vector of weights and upper, the index of the largest non-zero entry in w

### Examples

```
CPAT:::getLongRunWeights(10, 1)
```

---

get_lrv_vec	<i>Long-Run Variance Estimation With Possible Change Points</i>
-------------	---

---

### Description

Computes the estimates of the long-run variance in a change point context, as described in (Rice et al. ). By default it uses kernel and bandwidth selection as used in the package **cointReg**, though changing the parameters kernel and bandwidth can change this behavior. If **cointReg** is not installed, the Bartlett internal (defined internally) will be used and the bandwidth will be the square root of the sample size.

### Usage

```
get_lrv_vec(dat, kernel = "ba", bandwidth = "and")
```

### Arguments

dat	The data vector
kernel	If character, the identifier of the kernel function as used in <b>cointReg</b> (see <a href="#">getLongRunVar</a> ); if function, the kernel function to be used for long-run variance estimation (default is the Bartlett kernel in <b>cointReg</b> )
bandwidth	If character, the identifier for how to compute the bandwidth as defined in <b>cointReg</b> (see <a href="#">getBandwidth</a> ); if function, a function to use for computing the bandwidth; if numeric, the bandwidth value to use (the default is to use Andrews' method, as used in <b>cointReg</b> )

**Value**

A vector of estimates of the long-run variance

**References**

Rice G, Miller C, Horváth L (????). “A new class of change point test of Rényi type.” in-press.

**Examples**

```
x <- rnorm(1000)
CPAT:::get_lrv_vec(x)
CPAT:::get_lrv_vec(x, kernel = "pa", bandwidth = "nw")
```

---

HR.test	<i>Rényi-Type Test</i>
---------	------------------------

---

**Description**

Performs the (univariate) Rényi-type test for change in mean, as described in (Rice et al. ). This is effectively an interface to [stat\\_Zn](#); see its documentation for more details. p-values are computed using [pZn](#), which represents the limiting distribution of the test statistic under the null hypothesis, which represents the limiting distribution of the test statistic under the null hypothesis when  $kn$  represents a sequence  $t_T$  satisfying  $t_T \rightarrow \infty$  and  $t_T/T \rightarrow 0$  as  $T \rightarrow \infty$ . ([log](#) and [sqrt](#) should be good choices.)

**Usage**

```
HR.test(x, kn = log, use_kernel_var = FALSE, stat_plot = FALSE,
        kernel = "ba", bandwidth = "and")
```

**Arguments**

x	Data to test for change in mean
kn	A function corresponding to the trimming parameter $t_T$ ; by default, the square root function
use_kernel_var	Set to TRUE to use kernel methods for long-run variance estimation (typically used when the data is believed to be correlated); if FALSE, then the long-run variance is estimated using $\hat{\sigma}_{T,t}^2 = T^{-1} \left( \sum_{s=1}^t (X_s - \bar{X}_t)^2 + \sum_{s=t+1}^T (X_s - \tilde{X}_{T-t})^2 \right)$ , where $\bar{X}_t = t^{-1} \sum_{s=1}^t X_s$ and $\tilde{X}_{T-t} = (T-t)^{-1} \sum_{s=t+1}^T X_s$ ; if <code>custom_var</code> is not NULL, this argument is ignored
stat_plot	Whether to create a plot of the values of the statistic at all potential change points
kernel	If character, the identifier of the kernel function as used in <b>cointReg</b> (see <a href="#">getLongRunVar</a> ); if function, the kernel function to be used for long-run variance estimation (default is the Bartlett kernel in <b>cointReg</b> )
bandwidth	If character, the identifier for how to compute the bandwidth as defined in <b>cointReg</b> (see <a href="#">getBandwidth</a> ); if function, a function to use for computing the bandwidth; if numeric, the bandwidth value to use (the default is to use Andrews' method, as used in <b>cointReg</b> )

**Value**

A htest-class object containing the results of the test

**References**

Rice G, Miller C, Horváth L (????). “A new class of change point test of Rényi type.” in-press.

**Examples**

```
HR.test(rnorm(1000))
HR.test(rnorm(1000), use_kernel_var = TRUE, kernel = "bo", bandwidth = "nw")
```

---

HS.test	<i>Hidalgo-Seo Test</i>
---------	-------------------------

---

**Description**

Performs the (univariate) Hidalgo-Seo test for change in mean, as described in (Rice et al. ). This is effectively an interface to [stat\\_hs](#); see its documentation for more details. p-values are computed using [phidalgo\\_seo](#), which represents the limiting distribution of the test statistic when the null hypothesis is true.

**Usage**

```
HS.test(x, corr = TRUE, stat_plot = FALSE)
```

**Arguments**

x	Data to test for change in mean
corr	If TRUE, the long-run variance will be computed under the assumption of correlated residuals; ignored if custom_var is not NULL or use_kernel_var is TRUE
stat_plot	Whether to create a plot of the values of the statistic at all potential change points

**Value**

A htest-class object containing the results of the test

**References**

Rice G, Miller C, Horváth L (????). “A new class of change point test of Rényi type.” in-press.

**Examples**

```
HS.test(rnorm(1000))
HS.test(rnorm(1000), corr = FALSE)
```

---

pdarling_erdos	<i>Darling-Erdős Statistic CDF</i>
----------------	------------------------------------

---

### Description

CDF for the limiting distribution of the Darling-Erdős statistic.

### Usage

```
pdarling_erdos(q)
```

### Arguments

q	Quantile input to CDF
---	-----------------------

### Value

If  $Z$  is the random variable with this distribution, the quantity  $P(Z \leq q)$

### Examples

```
CPAT:::pdarling_erdos(0.1)
```

---

phidalgo_seo	<i>Hidalgo-Seo Statistic CDF</i>
--------------	----------------------------------

---

### Description

CDF of the limiting distribution of the Hidalgo-Seo statistic

### Usage

```
phidalgo_seo(q)
```

### Arguments

q	Quantile input to CDF
---	-----------------------

### Value

If  $Z$  is the random variable following the limiting distribution, the quantity  $P(Z \leq q)$

### Examples

```
CPAT:::phidalgo_seo(0.1)
```

---

pkolmogorov	<i>Kolmogorov CDF</i>
-------------	-----------------------

---

**Description**

CDF of the Kolmogorov distribution.

**Usage**

```
pkolmogorov(q, summands = ceiling(q * sqrt(72) + 3/2))
```

**Arguments**

q	Quantile input to CDF
summands	Number of summands for infinite sum (the default should have machine accuracy)

**Value**

If  $Z$  is the random variable following the Kolmogorov distribution, the quantity  $P(Z \leq q)$

**Examples**

```
CPAT::pkolmogorov(0.1)
```

---

pZn	<i>Rényi-Type Statistic CDF</i>
-----	---------------------------------

---

**Description**

CDF for the limiting distribution of the Rényi-type statistic.

**Usage**

```
pZn(q, summands = NULL)
```

**Arguments**

q	Quantile input to CDF
summands	Number of summands for infinite sum; if NULL, automatically determined

**Value**

If  $Z$  is the random variable following the limiting distribution, the quantity  $P(Z \leq q)$

**Examples**

```
CPAT::pZn(0.1)
```

---

`qdarling_erdos`*Darling-Erdős Statistic Limiting Distribution Quantile Function*

---

**Description**

Quantile function for the limiting distribution of the Darling-Erdős statistic.

**Usage**

```
qdarling_erdos(p)
```

**Arguments**

`p` The probability associated with the desired quantile

**Value**

The quantile associated with `p`

**Examples**

```
CPAT:::qdarling_erdos(0.5)
```

---

`qhidalgo_seo`*Hidalgo-Seo Statistic Limiting Distribution Quantile Function*

---

**Description**

Quantile function for the limiting distribution of the Hidalgo-Seo statistic

**Usage**

```
qhidalgo_seo(p)
```

**Arguments**

`p` The probability associated with the desired quantile

**Value**

A The quantile associated with `p`

**Examples**

```
CPAT:::qhidalgo_seo(0.5)
```

---

qkolmogorov

*Kolmogorov Distribution Quantile Function*


---

### Description

Quantile function for the Kolmogorov distribution.

### Usage

```
qkolmogorov(p, summands = 500, interval = c(0, 100),
  tol = .Machine$double.eps, ...)
```

### Arguments

p	Value of the CDF at the quantile
summands	Number of summands for infinite sum
interval, tol, ...	Arguments to be passed to <a href="#">uniroot</a>

### Details

This function uses [uniroot](#) for finding this quantity, and many of the the accepted parameters are arguments for that function; see its documentation for more details.

### Value

The quantile associated with p

### Examples

```
CPAT:::qkolmogorov(0.5)
```

---

qZn

*Rènyi-Type Statistic Quantile Function*


---

### Description

Quantile function for the limiting distribution of the Rènyi-type statistic.

### Usage

```
qZn(p, summands = 500, interval = c(0, 100),
  tol = .Machine$double.eps, ...)
```

### Arguments

p	Value of the CDF at the quantile
summands	Number of summands for infinite sum
interval, tol, ...	Arguments to be passed to <a href="#">uniroot</a>



**Details**

This function uses [uniroot](#) for finding this quantity, and many of the the accepted parameters are arguments for that function; see its documentation for more details.

**Value**

The quantile associated with p

**Examples**

```
CPAT:::qZn(0.5)
```

---

rchangepoint

*Simulate Univariate Data With a Single Change Point*


---

**Description**

This function simulates univariate data with a structural change.

**Usage**

```
rchangepoint(n, changepoint = NULL, mean1 = 0, mean2 = 0,
             dist = rnorm, meanparam = "mean", ...)
```

**Arguments**

n	An integer for the data set's sample size
changepoint	An integer for where the change point occurs
mean1	The mean prior to the change point
mean2	The mean after the change point
dist	The function with which random data will be generated
meanparam	A string for the parameter in dist representing the mean
...	Other arguments to be passed to dist

**Details**

This function generates artificial change point data, where up to the specified change point the data has one mean, and after the point it has a different mean. By default, the function simulates standard Normal data with no change. If changepoint is NULL, then by default the change point will be at about the middle of the data.

**Value**

A vector of the simulated data

**Examples**

```
CPAT:::rchangepoint(500)
CPAT:::rchangepoint(500, changepoint = 10, mean2 = 2, sd = 2)
CPAT:::rchangepoint(500, changepoint = 250, dist = rexp, meanparam = "rate",
                    mean1 = 1, mean2 = 2)
```

sim\_de\_stat

*Darling-Erdős Statistic Simulation***Description**

Simulates multiple realizations of the Darling-Erdős statistic.

**Usage**

```
sim_de_stat(size, a = log, b = log, use_kernel_var = FALSE,
            kernel = "ba", bandwidth = "and", n = 500, gen_func = rnorm,
            args = NULL, parallel = FALSE)
```

**Arguments**

size	Number of realizations to simulate
a	The function that will be composed with $l(x) = (2 \log(x))^{1/2}$
b	The function that will be composed with $u(x) = 2 \log(x) + \frac{1}{2} \log(\log(x)) - \frac{1}{2} \log(\pi)$
use_kernel_var	Set to TRUE to use kernel-based long-run variance estimation (FALSE means this is not employed)
kernel	If character, the identifier of the kernel function as used in the <b>cointReg</b> (see documentation for <code>cointReg::getLongRunVar</code> ); if function, the kernel function to be used for long-run variance estimation (default is the Bartlett kernel in <b>cointReg</b> ); this parameter has no effect if <code>use_kernel_var</code> is FALSE
bandwidth	If character, the identifier of how to compute the bandwidth as defined in the <b>cointReg</b> package (see documentation for <code>cointReg::getLongRunVar</code> ); if function, a function to use for computing the bandwidth; if numeric, the bandwidth to use (the default behavior is to use the Andrews (1991) method, as used in <b>cointReg</b> ); this parameter has no effect if <code>use_kernel_var</code> is FALSE
n	The sample size for each realization
gen_func	The function generating the random sample from which the statistic is computed
args	A list of arguments to be passed to <code>gen_func</code>
parallel	Whether to use the <b>foreach</b> and <b>doParallel</b> packages to parallelize simulation (which needs to be initialized in the global namespace before use)

**Details**

If `use_kernel_var` is set to TRUE, long-run variance estimation using kernel-based techniques will be employed; otherwise, a technique resembling standard variance estimation will be employed. Any technique employed, though, will account for the potential break points, as described in Rice et al. (). See the documentation for [stat\\_de](#) for more details.

The parameters `kernel` and `bandwidth` control parameters for long-run variance estimation using kernel methods. These parameters will be passed directly to [stat\\_de](#).

**Value**

A vector of simulated realizations of the Darling-Erdős statistic

## References

- Andrews DWK (1991). “Heteroskedasticity and Autocorrelation Consistent Covariance Matrix Estimation.” *Econometrica*, **59**(3), 817-858.
- Rice G, Miller C, Horváth L (????). “A new class of change point test of Rényi type.” in-press.

## Examples

```
CPAT:::sim_de_stat(100)
CPAT:::sim_de_stat(100, use_kernel_var = TRUE,
  gen_func = CPAT:::rchangeoint,
  args = list(changeoint = 250, mean2 = 1))
```

---

sim\_hs\_stat

Hidalgo-Seo Statistic Simulation

---

## Description

Simulates multiple realizations of the Hidalgo-Seo statistic.

## Usage

```
sim_hs_stat(size, corr = TRUE, gen_func = rnorm, args = NULL,
  n = 500, parallel = FALSE, use_kernel_var = FALSE, kernel = "ba",
  bandwidth = "and")
```

## Arguments

size	Number of realizations to simulate
corr	Whether long-run variance should be computed under the assumption of correlated residuals
gen_func	The function generating the random sample from which the statistic is computed
args	A list of arguments to be passed to gen_func
n	The sample size for each realization
parallel	Whether to use the <b>foreach</b> and <b>doParallel</b> packages to parallelize simulation (which needs to be initialized in the global namespace before use)
use_kernel_var	Set to TRUE to use kernel-based long-run variance estimation (FALSE means this is not employed); <i>TODO: NOT CURRENTLY IMPLEMENTED</i>
kernel	If character, the identifier of the kernel function as used in the <b>cointReg</b> (see documentation for <code>cointReg::getLongRunVar</code> ); if function, the kernel function to be used for long-run variance estimation (default is the Bartlett kernel in <b>cointReg</b> ); this parameter has no effect if use_kernel_var is FALSE; <i>TODO: NOT CURRENTLY IMPLEMENTED</i>
bandwidth	If character, the identifier of how to compute the bandwidth as defined in the <b>cointReg</b> package (see documentation for <code>cointReg::getLongRunVar</code> ); if function, a function to use for computing the bandwidth; if numeric, the bandwidth to use (the default behavior is to use the Andrews (1991) method, as used in <b>cointReg</b> ); this parameter has no effect if use_kernel_var is FALSE; <i>TODO: NOT CURRENTLY IMPLEMENTED</i>

## Details

If `corr` is `TRUE`, then the residuals of the data-generating process are assumed to be correlated and the test accounts for this in long-run variance estimation; see the documentation for `stat_hs` for more details. Otherwise, the sample variance is the estimate for the long-run variance, as described in Hidalgo and Seo (2013).

## Value

A vector of simulated realizations of the Hidalgo-Seo statistic

## References

Andrews DWK (1991). “Heteroskedasticity and Autocorrelation Consistent Covariance Matrix Estimation.” *Econometrica*, **59**(3), 817-858.

Hidalgo J, Seo MH (2013). “Testing for structural stability in the whole sample.” *Journal of Econometrics*, **175**(2), 84 - 93. ISSN 0304-4076, doi: [10.1016/j.jeconom.2013.02.008](https://doi.org/10.1016/j.jeconom.2013.02.008), <http://www.sciencedirect.com/science/article/pii/S0304407613000626>.

## Examples

```
CPAT:::sim_hs_stat(100)
CPAT:::sim_hs_stat(100, gen_func = CPAT:::rchangepoint,
  args = list(changepoint = 250, mean2 = 1))
```

---

sim_Vn	<i>CUSUM Statistic Simulation (Assuming Variance)</i>
--------	---

---

## Description

Simulates multiple realizations of the CUSUM statistic when the long-run variance of the data is known.

## Usage

```
sim_Vn(size, n = 500, gen_func = rnorm, sd = 1, args = NULL)
```

## Arguments

<code>size</code>	Number of realizations to simulate
<code>n</code>	The sample size for each realization
<code>gen_func</code>	The function generating the random sample from which the statistic is computed
<code>sd</code>	The square root of the second moment of the data
<code>args</code>	A list of arguments to be passed to <code>gen_func</code>

## Value

A vector of simulated realizations of the CUSUM statistic

## Examples

```
CPAT::sim_Vn(100)
CPAT::sim_Vn(100, gen_func = CPAT::rchangeoint,
  args = list(changeoint = 250, mean2 = 1))
```

---

sim_Vn_stat	<i>CUSUM Statistic Simulation</i>
-------------	-----------------------------------

---

## Description

Simulates multiple realizations of the CUSUM statistic.

## Usage

```
sim_Vn_stat(size, kn = function(n) { 1 }, tau = 0,
  use_kernel_var = FALSE, kernel = "ba", bandwidth = "and",
  n = 500, gen_func = rnorm, args = NULL, parallel = FALSE)
```

## Arguments

size	Number of realizations to simulate
kn	A function returning a positive integer that is used in the definition of the trimmed CUSUM statistic effectively setting the bounds over which the maximum is taken
tau	The weighting parameter for the weighted CUSUM statistic (defaults to zero for no weighting)
use_kernel_var	Set to TRUE to use kernel-based long-run variance estimation (FALSE means this is not employed)
kernel	If character, the identifier of the kernel function as used in the <b>cointReg</b> (see documentation for <code>cointReg::getLongRunVar</code> ); if function, the kernel function to be used for long-run variance estimation (default is the Bartlett kernel in <b>cointReg</b> ); this parameter has no effect if <code>use_kernel_var</code> is FALSE
bandwidth	If character, the identifier of how to compute the bandwidth as defined in the <b>cointReg</b> package (see documentation for <code>cointReg::getLongRunVar</code> ); if function, a function to use for computing the bandwidth; if numeric, the bandwidth to use (the default behavior is to use the method described in (Andrews 1991), as used in <b>cointReg</b> ); this parameter has no effect if <code>use_kernel_var</code> is FALSE
n	The sample size for each realization
gen_func	The function generating the random sample from which the statistic is computed
args	A list of arguments to be passed to <code>gen_func</code>
parallel	Whether to use the <b>foreach</b> and <b>doParallel</b> packages to parallelize simulation (which needs to be initialized in the global namespace before use)

Details

This differs from `sim_Vn()` in that the long-run variance is estimated with this function, while `sim_Vn()` assumes the long-run variance is known. Estimation can be done in a variety of ways. If `use_kernel_var` is set to `TRUE`, long-run variance estimation using kernel-based techniques will be employed; otherwise, a technique resembling standard variance estimation will be employed. Any technique employed, though, will account for the potential break points, as described in Rice et al. (). See the documentation for `stat_Vn` for more details.

The parameters `kernel` and `bandwidth` control parameters for long-run variance estimation using kernel methods. These parameters will be passed directly to `stat_Vn`.

Versions of the CUSUM statistic, such as the weighted or trimmed statistics, can be simulated with the function by passing values to `kn` and `tau`; again, see the documentation for `stat_Vn`.

Value

A vector of simulated realizations of the CUSUM statistic

References

Andrews DWK (1991). “Heteroskedasticity and Autocorrelation Consistent Covariance Matrix Estimation.” *Econometrica*, **59**(3), 817-858.

Rice G, Miller C, Horváth L (????). “A new class of change point test of Rényi type.” in-press.

Examples

```
CPAT:::sim_Vn_stat(100)
CPAT:::sim_Vn_stat(100, kn = function(n) {floor(0.1 * n)}), tau = 1/3,
  use_kernel_var = TRUE, gen_func = CPAT:::rchangeoint,
  args = list(changeoint = 250, mean2 = 1))
```

---

sim_Zn	<i>Rényi-Type Statistic Simulation (Assuming Variance)</i>
--------	--

---

Description

Simulates multiple realizations of the Rényi-type statistic when the long-run variance of the data is known.

Usage

```
sim_Zn(size, kn, n = 500, gen_func = rnorm, args = NULL, sd = 1)
```

Arguments

- size            Number of realizations to simulate
- kn             A function returning a positive integer that is used in the definition of the Rényi-type statistic effectively setting the bounds over which the maximum is taken
- n              The sample size for each realization
- gen\_func       The function generating the random sample from which the statistic is computed
- args           A list of arguments to be passed to `gen_func`
- sd             The square root of the second moment of the data

**Value**

A vector of simulated realizations of the R nyi-type statistic

**Examples**

```
CPAT::sim_Zn(100, kn = function(n) {floor(log(n))})
CPAT::sim_Zn(100, kn = function(n) {floor(log(n))},
  gen_func = CPAT::rchangepoint, args = list(changepoint = 250,
                                             mean2 = 1))
```

---

sim_Zn_stat	<i>R�nyi-Type Statistic Simulation</i>
-------------	--

---

**Description**

Simulates multiple realizations of the R nyi-type statistic.

**Usage**

```
sim_Zn_stat(size, kn = function(n) { floor(sqrt(n)) },
  use_kernel_var = FALSE, kernel = "ba", bandwidth = "and",
  n = 500, gen_func = rnorm, args = NULL, parallel = FALSE)
```

**Arguments**

size	Number of realizations to simulate
kn	A function returning a positive integer that is used in the definition of the R�nyi-type statistic effectively setting the bounds over which the maximum is taken
use_kernel_var	Set to TRUE to use kernel-based long-run variance estimation (FALSE means this is not employed)
kernel	If character, the identifier of the kernel function as used in the <b>cointReg</b> (see documentation for <code>cointReg::getLongRunVar</code> ); if function, the kernel function to be used for long-run variance estimation (default is the Bartlett kernel in <b>cointReg</b> ); this parameter has no effect if <code>use_kernel_var</code> is FALSE
bandwidth	If character, the identifier of how to compute the bandwidth as defined in the <b>cointReg</b> package (see documentation for <code>cointReg::getLongRunVar</code> ); if function, a function to use for computing the bandwidth; if numeric, the bandwidth to use (the default behavior is to use the Andrews (1991) method, as used in <b>cointReg</b> ); this parameter has no effect if <code>use_kernel_var</code> is FALSE
n	The sample size for each realization
gen_func	The function generating the random sample from which the statistic is computed
args	A list of arguments to be passed to <code>gen_func</code>
parallel	Whether to use the <b>foreach</b> and <b>doParallel</b> packages to parallelize simulation (which needs to be initialized in the global namespace before use)

## Details

This differs from `sim_Zn()` in that the long-run variance is estimated with this function, while `sim_Zn()` assumes the long-run variance is known. Estimation can be done in a variety of ways. If `use_kernel_var` is set to `TRUE`, long-run variance estimation using kernel-based techniques will be employed; otherwise, a technique resembling standard variance estimation will be employed. Any technique employed, though, will account for the potential break points, as described in Rice et al. (). See the documentation for `stat_Zn` for more details.

The parameters `kernel` and `bandwidth` control parameters for long-run variance estimation using kernel methods. These parameters will be passed directly to `stat_Zn`.

## Value

A vector of simulated realizations of the R nyi-type statistic

## References

Andrews DWK (1991). ‘‘Heteroskedasticity and Autocorrelation Consistent Covariance Matrix Estimation.’’ *Econometrica*, **59**(3), 817-858.

Rice G, Miller C, Horv th L (????). ‘‘A new class of change point test of R nyi type.’’ in-press.

## Examples

```
CPAT:::sim_Zn_stat(100)
CPAT:::sim_Zn_stat(100, kn = function(n) {floor(log(n))},
  use_kernel_var = TRUE, gen_func = CPAT:::rchangepoint,
  args = list(changepoint = 250, mean2 = 1))
```

---

stat\_de

---

*Compute the Darling-Erd s Statistic*


---

## Description

This function computes the Darling-Erd s statistic.

## Usage

```
stat_de(dat, a = log, b = log, estimate = FALSE,
  use_kernel_var = FALSE, custom_var = NULL, kernel = "ba",
  bandwidth = "and", get_all_vals = FALSE)
```

## Arguments

<code>dat</code>	The data vector
<code>a</code>	The function that will be composed with $l(x) = (2 \log x)^{1/2}$
<code>b</code>	The function that will be composed with $u(x) = 2 \log x + \frac{1}{2} \log \log x - \frac{1}{2} \log \pi$
<code>estimate</code>	Set to <code>TRUE</code> to return the estimated location of the change point
<code>use_kernel_var</code>	Set to <code>TRUE</code> to use kernel methods for long-run variance estimation (typically used when the data is believed to be correlated); if <code>FALSE</code> , then the long-run variance is estimated using $\hat{\sigma}_{T,t}^2 = T^{-1} \left( \sum_{s=1}^t (X_s - \bar{X}_t)^2 + \sum_{s=t+1}^T (X_s - \tilde{X}_{T-t})^2 \right)$ , where $\bar{X}_t = t^{-1} \sum_{s=1}^t X_s$ and $\tilde{X}_{T-t} = (T-t)^{-1} \sum_{s=t+1}^T X_s$



custom_var	Can be a vector the same length as dat consisting of variance-like numbers at each potential change point (so each entry of the vector would be the "best estimate" of the long-run variance if that location were where the change point occurred) or a function taking two parameters x and k that can be used to generate this vector, with x representing the data vector and k the position of a potential change point; if NULL, this argument is ignored
kernel	If character, the identifier of the kernel function as used in <b>cointReg</b> (see <a href="#">getLongRunVar</a> ); if function, the kernel function to be used for long-run variance estimation (default is the Bartlett kernel in <b>cointReg</b> )
bandwidth	If character, the identifier for how to compute the bandwidth as defined in <b>cointReg</b> (see <a href="#">getBandwidth</a> ); if function, a function to use for computing the bandwidth; if numeric, the bandwidth value to use (the default is to use Andrews' method, as used in <b>cointReg</b> )
get_all_vals	If TRUE, return all values for the statistic at every tested point in the data set

### Details

If  $\bar{A}_T(\tau, t_T)$  is the weighted and trimmed CUSUM statistic with weighting parameter  $\tau$  and trimming parameter  $t_T$  (see [stat\\_Vn](#)), then the Darling-Erdős statistic is

$$l(a_T)\bar{A}_T(1/2, 1) - u(b_T)$$

with  $l(x) = \sqrt{2\log x}$  and  $u(x) = 2\log x + \frac{1}{2}\log\log x - \frac{1}{2}\log\pi$  ( $\log x$  is the natural logarithm of  $x$ ). The parameter  $a$  corresponds to  $a_T$  and  $b$  to  $b_T$ ; these are both `log` by default.

See (Rice et al. ) to learn more.

### Value

If both `estimate` and `get_all_vals` are FALSE, the value of the test statistic; otherwise, a list that contains the test statistic and the other values requested (if both are TRUE, the test statistic is in the first position and the estimated changg point in the second)

### References

Rice G, Miller C, Horváth L (????). "A new class of change point test of Rényi type." in-press.

### Examples

```
CPAT:::stat_de(rnorm(1000))
CPAT:::stat_de(rnorm(1000), use_kernel_var = TRUE, bandwidth = "nw", kernel = "bo")
```

---

stat\_hs

---

*Compute the Hidalgo-Seo Statistic*


---

### Description

This function computes the Hidalgo-Seo statistic for a change in mean model.

## Usage

```
stat_hs(dat, estimate = FALSE, corr = TRUE, get_all_vals = FALSE,
        custom_var = NULL, use_kernel_var = FALSE, kernel = "ba",
        bandwidth = "and")
```

## Arguments

dat	The data vector
estimate	Set to TRUE to return the estimated location of the change point
corr	If TRUE, the long-run variance will be computed under the assumption of correlated residuals; ignored if custom_var is not NULL or use_kernel_var is TRUE
get_all_vals	If TRUE, return all values for the statistic at every tested point in the data set
custom_var	Can be a vector the same length as dat consisting of variance-like numbers at each potential change point (so each entry of the vector would be the "best estimate" of the long-run variance if that location were where the change point occurred) or a function taking two parameters x and k that can be used to generate this vector, with x representing the data vector and k the position of a potential change point; if NULL, this argument is ignored
use_kernel_var	Set to TRUE to use kernel methods for long-run variance estimation (typically used when the data is believed to be correlated); if FALSE, then the long-run variance is estimated using $\hat{\sigma}_{T,t}^2 = T^{-1} \left( \sum_{s=1}^t (X_s - \bar{X}_t)^2 + \sum_{s=t+1}^T (X_s - \tilde{X}_{T-t})^2 \right)$ , where $\bar{X}_t = t^{-1} \sum_{s=1}^t X_s$ and $\tilde{X}_{T-t} = (T-t)^{-1} \sum_{s=t+1}^T X_s$ ; if custom_var is not NULL, this argument is ignored
kernel	If character, the identifier of the kernel function as used in <b>cointReg</b> (see <a href="#">getLongRunVar</a> ); if function, the kernel function to be used for long-run variance estimation (default is the Bartlett kernel in <b>cointReg</b> )
bandwidth	If character, the identifier for how to compute the bandwidth as defined in <b>cointReg</b> (see <a href="#">getBandwidth</a> ); if function, a function to use for computing the bandwidth; if numeric, the bandwidth value to use (the default is to use Andrews' method, as used in <b>cointReg</b> )

## Details

For a data set  $x_t$  with  $n$  observations, the test statistic is

$$\max_{1 \leq s \leq n-1} (\mathcal{LM}(s) - B_n) / A_n$$

where  $\hat{u}_t = x_t - \bar{x}$  ( $\bar{x}$  is the sample mean),  $a_n = (2 \log \log n)^{1/2}$ ,  $b_n = a_n^2 - \frac{1}{2} \log \log \log n - \log \Gamma(1/2)$ ,  $A_n = b_n / a_n^2$ ,  $B_n = b_n^2 / a_n^2$ ,  $\hat{\Delta} = \hat{\sigma}^2 = n^{-1} \sum_{t=1}^n \hat{u}_t^2$ , and  $\mathcal{LM}(s) = n(n-s)^{-1} s^{-1} \hat{\Delta}^{-1} \left( \sum_{t=1}^s \hat{u}_t \right)^2$ .

If corr is FALSE, then the residuals are assumed to be uncorrelated. Otherwise, the residuals are assumed to be correlated and  $\hat{\Delta} = \hat{\gamma}(0) + 2 \sum_{j=1}^{\lfloor \sqrt{n} \rfloor} \left(1 - \frac{j}{\sqrt{n}}\right) \hat{\gamma}(j)$  with  $\hat{\gamma}(j) = \frac{1}{n} \sum_{t=1}^{n-j} \hat{u}_t \hat{u}_{t+j}$ .

This statistic was presented in (Hidalgo and Seo 2013).

## Value

If both estimate and get\_all\_vals are FALSE, the value of the test statistic; otherwise, a list that contains the test statistic and the other values requested (if both are TRUE, the test statistic is in the first position and the estimated change point in the second)

## References

Hidalgo J, Seo MH (2013). “Testing for structural stability in the whole sample.” *Journal of Econometrics*, **175**(2), 84 - 93. ISSN 0304-4076, doi: [10.1016/j.jeconom.2013.02.008](https://doi.org/10.1016/j.jeconom.2013.02.008), <http://www.sciencedirect.com/science/article/pii/S0304407613000626>.

## Examples

```
CPAT:::stat_hs(rnorm(1000))
CPAT:::stat_hs(rnorm(1000), corr = FALSE)
```

---

stat_Vn	<i>Compute the CUSUM Statistic</i>
---------	------------------------------------

---

## Description

This function computes the CUSUM statistic (and can compute weighted/trimmed variants, depending on the values of kn and tau).

## Usage

```
stat_Vn(dat, kn = function(n) { 1 }, tau = 0, estimate = FALSE,
        use_kernel_var = FALSE, custom_var = NULL, kernel = "ba",
        bandwidth = "and", get_all_vals = FALSE)
```

## Arguments

dat	The data vector
kn	A function corresponding to the trimming parameter $t_T$ in the trimmed CUSUM variant; by default, is a function returning 1 (for no trimming)
tau	The weighting parameter $\tau$ for the weighted CUSUM statistic; by default, is 0 (for no weighting)
estimate	Set to TRUE to return the estimated location of the change point
use_kernel_var	Set to TRUE to use kernel methods for long-run variance estimation (typically used when the data is believed to be correlated); if FALSE, then the long-run variance is estimated using $\hat{\sigma}_{T,t}^2 = T^{-1} \left( \sum_{s=1}^t (X_s - \bar{X}_t)^2 + \sum_{s=t+1}^T (X_s - \tilde{X}_{T-t})^2 \right)$ , where $\bar{X}_t = t^{-1} \sum_{s=1}^t X_s$ and $\tilde{X}_{T-t} = (T-t)^{-1} \sum_{s=t+1}^T X_s$
custom_var	Can be a vector the same length as dat consisting of variance-like numbers at each potential change point (so each entry of the vector would be the "best estimate" of the long-run variance if that location were where the change point occurred) or a function taking two parameters x and k that can be used to generate this vector, with x representing the data vector and k the position of a potential change point; if NULL, this argument is ignored
kernel	If character, the identifier of the kernel function as used in <b>cointReg</b> (see <a href="#">getLongRunVar</a> ); if function, the kernel function to be used for long-run variance estimation (default is the Bartlett kernel in <b>cointReg</b> )
bandwidth	If character, the identifier for how to compute the bandwidth as defined in <b>cointReg</b> (see <a href="#">getBandwidth</a> ); if function, a function to use for computing the bandwidth; if numeric, the bandwidth value to use (the default is to use Andrews' method, as used in <b>cointReg</b> )
get_all_vals	If TRUE, return all values for the statistic at every tested point in the data set

## Details

The definition of the statistic is

$$T^{-1/2} \max_{1 \leq t \leq T} \hat{\sigma}_{t,T}^{-1} \left| \sum_{s=1}^t X_s - \frac{t}{T} \sum_{s=1}^T X_s \right|$$

A more general version is

$$T^{-1/2} \max_{t_T \leq t \leq T-t_T} \hat{\sigma}_{t,T}^{-1} \left( \frac{t}{T} \left( \frac{T-t}{T} \right) \right)^{\tau} \left| \sum_{s=1}^t X_s - \frac{t}{T} \sum_{s=1}^T X_s \right|$$

The parameter `kn` corresponds to the trimming parameter  $t_T$  and the parameter `tau` corresponds to  $\tau$ .

See (Rice et al. ) for more details.

## Value

If both `estimate` and `get_all_vals` are `FALSE`, the value of the test statistic; otherwise, a list that contains the test statistic and the other values requested (if both are `TRUE`, the test statistic is in the first position and the estimated change point in the second)

## References

Rice G, Miller C, Horváth L (???). “A new class of change point test of Rényi type.” in-press.

## Examples

```
CPAT:::stat_Vn(rnorm(1000))
CPAT:::stat_Vn(rnorm(1000), kn = function(n) {0.1 * n}, tau = 1/2)
CPAT:::stat_Vn(rnorm(1000), use_kernel_var = TRUE, bandwidth = "nw", kernel = "bo")
```

---

stat\_Zn

---

*Compute the Rényi-Type Statistic*


---

## Description

This function computes the Rényi-type statistic.

## Usage

```
stat_Zn(dat, kn = function(n) { floor(sqrt(n)) }, estimate = FALSE,
  use_kernel_var = FALSE, custom_var = NULL, kernel = "ba",
  bandwidth = "and", get_all_vals = FALSE)
```

## Arguments

dat	The data vector
kn	A function corresponding to the trimming parameter $t_T$ ; by default, the square root function
estimate	Set to TRUE to return the estimated location of the change point
use_kernel_var	Set to TRUE to use kernel methods for long-run variance estimation (typically used when the data is believed to be correlated); if FALSE, then the long-run variance is estimated using $\hat{\sigma}_{T,t}^2 = T^{-1} \left( \sum_{s=1}^t (X_s - \bar{X}_t)^2 + \sum_{s=t+1}^T (X_s - \tilde{X}_{T-t})^2 \right)$ , where $\bar{X}_t = t^{-1} \sum_{s=1}^t X_s$ and $\tilde{X}_{T-t} = (T-t)^{-1} \sum_{s=t+1}^T X_s$ ; if custom_var is not NULL, this argument is ignored
custom_var	Can be a vector the same length as dat consisting of variance-like numbers at each potential change point (so each entry of the vector would be the "best estimate" of the long-run variance if that location were where the change point occurred) or a function taking two parameters x and k that can be used to generate this vector, with x representing the data vector and k the position of a potential change point; if NULL, this argument is ignored
kernel	If character, the identifier of the kernel function as used in <b>cointReg</b> (see <a href="#">getLongRunVar</a> ); if function, the kernel function to be used for long-run variance estimation (default is the Bartlett kernel in <b>cointReg</b> )
bandwidth	If character, the identifier for how to compute the bandwidth as defined in <b>cointReg</b> (see <a href="#">getBandwidth</a> ); if function, a function to use for computing the bandwidth; if numeric, the bandwidth value to use (the default is to use Andrews' method, as used in <b>cointReg</b> )
get_all_vals	If TRUE, return all values for the statistic at every tested point in the data set

## Details

The definition of the statistic is

$$\max_{t_T \leq t \leq T-t_T} \hat{\sigma}_{t,T}^{-1} \left| t^{-1} \sum_{s=1}^t X_s - (T-t)^{-1} \sum_{s=t+1}^T X_s \right|$$

The parameter kn corresponds to the trimming parameter  $t_T$ .

## Value

If both estimate and get\_all\_vals are FALSE, the value of the test statistic; otherwise, a list that contains the test statistic and the other values requested (if both are TRUE, the test statistic is in the first position and the estimated change point in the second)

## Examples

```
CPAT:::stat_Zn(rnorm(1000))
CPAT:::stat_Zn(rnorm(1000), kn = function(n) {floor(log(n))})
CPAT:::stat_Zn(rnorm(1000), use_kernel_var = TRUE, bandwidth = "nw",
               kernel = "bo")
```

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%s%	Concatenate (With Space)
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---

**Description**  
Concatenate and form strings (with space separation)

**Usage**  
x %s% y

**Arguments**  
x                    One object  
y                    Another object

**Value**  
A string combining x and y with a space separating them

**Examples**  

```
`%s%` <- CPAT:::`%s%`  
"Hello" %s% "world"
```

---

%s0%	Concatenate (Without Space)
------	-----------------------------

---

**Description**  
Concatenate and form strings (no space separation)

**Usage**  
x %s0% y

**Arguments**  
x                    One object  
y                    Another object

**Value**  
A string combining x and y

**Examples**  

```
`%s0%` <- CPAT:::`%s0%`  
"Hello" %s0% "world"
```

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