# Package 'CPAT'

September 24, 2018

**Title** Change Point Analysis Tests

**Version** 0.0.0.9000

**Description** Implements several statistical tests for structural change in R.

**Depends** R (>= 3.2)

**Suggests** cointReg (>= 0.2), foreach (>= 1.4), doParallel (>= 1.0), ggplot2 (>= 2.2), dplyr (>= 0.7), tikzDevice (>= 0.12), testthat (>= 2.0)

**Imports** stats (>= 3.2), utils (>= 3.2), grDevices (>= 3.2), Rdpack (>= 0.9), Rcpp (>= 0.12), purrr (>= 0.2)

**RdMacros** Rdpack

**SystemRequirements** GNU make

**License** MIT + file LICENSE

**Encoding** UTF-8

**LazyData** true

**LinkingTo** Rcpp, RcppArmadillo

**RoxygenNote** 6.1.0

**NeedsCompilation** yes

**Author** Curtis Miller [aut, cre]

**Maintainer** Curtis Miller <cmiller@math.utah.edu>

## R topics documented:

---

`.onAttach` *Package Attach Hook Function*

---

## Description

Hook triggered when package attached

## Usage

```
.onAttach(lib, pkg)
```

## Arguments

| | |
|---|---|
| `lib` | a character string giving the library directory where the package defining the namespace was found |
| `pkg` | a character string giving the name of the package |

## Examples

```
CPAT:::.onAttach(.libPaths()[1], "CPAT")
```

---

`Andrews.test` *Andrews' Test for End-of-Sample Structural Change*

---

## Description

Performs Andrews' test for end-of-sample structural change, as described in (Andrews 2003). This function works for both univariate and multivariate data depending on the nature of `x` and whether `formula` is specified. This function is thus an interface to `andrews_test` and `andrews_test_reg`; see the documentation of those functions for more details.

## Usage

```
Andrews.test(x, M, formula = NULL)
```

## Arguments

| | |
|---|---|
| `x` | Data to test for change in mean (either a vector or `data.frame`) |
| `M` | Numeric index of the location of the first potential change point |
| `formula` | The regression formula, which will be passed to `lm` |

## Value

A `htest`-class object containing the results of the test

## References

Andrews DWK (2003). "End-of-Sample Instability Tests." *Econometrica*, **71**(6), 1661–1694. ISSN 00129682, 14680262, https://www.jstor.org/stable/1555535.

## Examples

```
Andrews.test(rnorm(1000), M = 900)
x <- rnorm(1000)
y <- 1 + 2 * x + rnorm(1000)
df <- data.frame(x, y)
Andrews.test(df, y ~ x, M = 900)
```

## andrews_test *Univariate Andrews Test for End-of-Sample Structural Change*

### Description

This implements Andrews' test for end-of-sample change, as described by Andrews (2003). This test was derived for detecting a change in univariate data. See (Andrews 2003) for a description of the test.

### Usage

```
andrews_test(x, M, pval = TRUE, stat = TRUE)
```

### Arguments

| | |
|---|---|
| x | Vector of the data to test |
| M | Numeric index of the location of the first potential change point |
| pval | If TRUE, return a p-value |
| stat | If TRUE, return a test statistic |

### Value

If both pval and stat are TRUE, a list containing both; otherwise, a number for one or the other, depending on which is TRUE

### References

Andrews DWK (2003). "End-of-Sample Instability Tests." *Econometrica*, **71**(6), 1661–1694. ISSN 00129682, 14680262, https://www.jstor.org/stable/1555535.

### Examples

```
CPAT:::andrews_test(rnorm(1000), M = 900)
```

## andrews_test_reg *Multivariate Andrews' Test for End-of-Sample Structural Change*

### Description

This implements Andrews' test for end-of-sample change, as described by Andrews (2003). This test was derived for detecting a change in multivarate data, aso originally described. See (Andrews 2003) for a description of the test.

### Usage

```
andrews_test_reg(formula, data, M, pval = TRUE, stat = TRUE)
```

### Arguments

| | |
|---|---|
| formula | The regression formula, which will be passed to lm |
| data | data.frame containing the data |
| M | Numeric index of the location of the first potential change point |
| pval | If TRUE, return a p-value |
| stat | If TRUE, return a test statistic |

### Value

If both pval and stat are TRUE, a list containing both; otherwise, a number for one or the other, depending on which is TRUE

### References

Andrews DWK (2003). "End-of-Sample Instability Tests." *Econometrica*, **71**(6), 1661–1694. ISSN 00129682, 14680262, https://www.jstor.org/stable/1555535.

### Examples

```
x <- rnorm(1000)
y <- 1 + 2 * x + rnorm(1000)
df <- data.frame(x, y)
CPAT:::andrews_test_reg(y ~ x, data = df, M = 900)
```

---

## banks *Bank Portfolio Returns*

---

### Description

Data set representing the returns of an industry portfolio representing the banking industry based on company four-digit SIC codes, obtained from the data library maintained by Kenneth French. Data ranges from July 1, 1926 to October 31, 2017.

### Usage

```
banks
```

### Format

A data frame with 24099 rows and 1 variable:

**Banks** The return of a portfolio representing the banking industry

Row names are dates in YYYY-MM-DD format.

### Source

http://mba.tuck.dartmouth.edu/pages/faculty/ken.french/data_library.html

## bind_power_sim_objs *Power Result Data Frame Creation*

### Description

Creates a data.frame containing power simulation results. Effectively a better, higher-level interface to power_sim_Zn_to_df and power_sim_Vn_to_df.

### Usage

```
bind_power_sim_objs(files, crit_value, conv_func, stat_name)
```

### Arguments

| | |
|---|---|
| files | A character vector of file names |
| crit_value | The critical value against which to compare a test statistic |
| conv_func | The function responsible for converting a list containing simulated statistic values under different conditions to a data.frame |
| stat_name | The label of the statistic |

### Value

A data.frame containing power levels

### Examples

```
## Not run:
filenames <- c("powerSimulations_sdest_norm_DE.rda",
               "powerSimulations_sdest_ar1_0.5_DE.rda")
bind_power_sim_objs(filenames, crit_value = qdarling_erdos(.95),
                    conv_func = power_sim_Vn_to_df, stat_name = "de")

## End(Not run)
```

## CPAT_startup_message *Create Package Startup Message*

### Description

Makes package startup message.

### Usage

```
CPAT_startup_message()
```

### Examples

```
CPAT:::CPAT_startup_message()
```

## cpt_consistent_var *Variance Estimation Consistent Under Change*

### Description

Estimate the variance (using the sum of squared errors) with an estimator that is consistent when the mean changes at a known point.

### Usage

```
cpt_consistent_var(x, k)
```

### Arguments

| | |
|---|---|
| x | A numeric vector for the data set |
| k | The potential change point at which the data set is split |

### Details

This is the estimator

$$\hat{\sigma}^2_{T,t} = T^{-1}\left(\sum_{s=1}^{t}\left(X_s - \bar{X}_t\right)^2 + \sum_{s=t+1}^{T}\left(X_s - \tilde{X}_{T-t}\right)^2\right)$$

where $\bar{X}_t = t^{-1}\sum_{s=1}^{t} X_s$ and $\tilde{X}_{T-t} = (T-t)^{-1}\sum_{s=t+1}^{T} X_s$. In this implementation, $T$ is computed automatically as `length(x)` and `k` corresponds to $t$, a potential change point.

### Value

The estimated change-consistent variance

### Examples

```
CPAT:::cpt_consistent_var(c(rnorm(500, mean = 0), rnorm(500, mean = 1)), k = 500)
```

## CUSUM.test *CUSUM Test*

### Description

Performs the (univariate) CUSUM test for change in mean, as described in (Rice et al. ). This is effectively an interface to `stat_Vn`; see its documentation for more details. p-values are computed using `pkolmogorov`, which represents the limiting distribution of the statistic under the null hypothesis.

### Usage

```
CUSUM.test(x, use_kernel_var = FALSE, stat_plot = FALSE,
  kernel = "ba", bandwidth = "and")
```

### Arguments

| | |
|---|---|
| x | Data to test for change in mean |
| use_kernel_var | Set to TRUE to use kernel methods for long-run variance estimation (typically used when the data is believed to be correlated); if FALSE, then the long-run variance is estimated using $\hat{\sigma}^2_{T,t} = T^{-1}\left(\sum_{s=1}^{t}\left(X_s - \bar{X}_t\right)^2 + \sum_{s=t+1}^{T}\left(X_s - \tilde{X}_{T-t}\right)^2\right)$, where $\bar{X}_t = t^{-1}\sum_{s=1}^{t} X_s$ and $\tilde{X}_{T-t} = (T-t)^{-1}\sum_{s=t+1}^{T} X_s$ |
| stat_plot | Whether to create a plot of the values of the statistic at all potential change points |
| kernel | If character, the identifier of the kernel function as used in **cointReg** (see getLongRunVar); if function, the kernel function to be used for long-run variance estimation (default is the Bartlett kernel in **cointReg**) |
| bandwidth | If character, the identifier for how to compute the bandwidth as defined in **cointReg** (see getBandwidth); if function, a function to use for computing the bandwidth; if numeric, the bandwidth value to use (the default is to use Andrews' method, as used in **cointReg**) |

### Value

A htest-class object containing the results of the test

### References

Rice G, Miller C, Horváth L (????). "A new class of change point test of Rényi type." submitted.

### Examples

```
CUSUM.test(rnorm(1000))
CUSUM.test(rnorm(1000), use_kernel_var = TRUE, kernel = "bo",
           bandwidth = "nw")
```

---

## DE.test *Darling-Erdös Test*

---

### Description

Performs the (univariate) Darling-Erdös test for change in mean, as described in (Rice et al. ). This is effectively an interface to stat_de; see its documentation for more details. p-values are computed using pdarling_erdos, which represents the limiting distribution of the test statistic under the null hypothesis when a and b are chosen appropriately. (Change those parameters at your own risk!)

### Usage

```
DE.test(x, a = log, b = log, use_kernel_var = FALSE,
  stat_plot = FALSE, kernel = "ba", bandwidth = "and")
```

### Arguments

| | |
|---|---|
| x | Data to test for change in mean |
| a | The function that will be composed with $l(x) = (2 \log x)^{1/2}$ |
| b | The function that will be composed with $u(x) = 2 \log x + \frac{1}{2} \log \log x - \frac{1}{2} \log \pi$ |
| use_kernel_var | Set to TRUE to use kernel methods for long-run variance estimation (typically used when the data is believed to be correlated); if FALSE, then the long-run variance is estimated using $\hat{\sigma}^2_{T,t} = T^{-1} \left( \sum_{s=1}^{t} \left( X_s - \bar{X}_t \right)^2 + \sum_{s=t+1}^{T} \left( X_s - \tilde{X}_{T-t} \right)^2 \right)$, where $\bar{X}_t = t^{-1} \sum_{s=1}^{t} X_s$ and $\tilde{X}_{T-t} = (T-t)^{-1} \sum_{s=t+1}^{T} X_s$ |
| stat_plot | Whether to create a plot of the values of the statistic at all potential change points |
| kernel | If character, the identifier of the kernel function as used in **cointReg** (see getLongRunVar); if function, the kernel function to be used for long-run variance estimation (default is the Bartlett kernel in **cointReg**) |
| bandwidth | If character, the identifier for how to compute the bandwidth as defined in **cointReg** (see getBandwidth); if function, a function to use for computing the bandwidth; if numeric, the bandwidth value to use (the default is to use Andrews' method, as used in **cointReg**) |

### Value

A htest-class object containing the results of the test

### References

Rice G, Miller C, Horváth L (????). "A new class of change point test of Rényi type." submitted.

### Examples

```
DE.test(rnorm(1000))
DE.test(rnorm(1000), use_kernel_var = TRUE, kernel = "bo", bandwidth = "nw")
```

---

## dist_conv_plot_tikz *Create Tikz Plot Demonstrating Rényi-Type Statistic's Convergence in Distribution*

---

### Description

Create a Tikz file containing a plot demonstrating that the Rényi-type statistic converges in distribution. Optionally, create a PDF as well.

### Usage

```
dist_conv_plot_tikz(obj, dist, trim, size, title = "", width = 4,
  height = 3, filename = NULL, makePDF = TRUE, verbose = TRUE)
```

### Arguments

| | |
|---|---|
| obj | The list containing the simulations |
| dist | The identifier of the data-generating process that generated the datasets on which the Rényi-type statistic was computed |
| trim | The identifier of the trimming parameter of the Rényi-type statistic |
| size | The sample size of the simulated data sets |
| title | The title of the plot |
| width | The width of the plot |
| height | The height of the plot |
| filename | The name of the output file (without extensions; .tex and maybe .pdf files will be created); if NULL, the name will automatically be determined (of the form dist_conv_dist_nsize_trim) |
| makePDF | Automatically compile the resulting .tex file |
| verbose | Print updates about progress (via link[base]{cat}) |

### Examples

```
## Not run:
ZnSimulations <- list(
  "norm" = list(
    "log" = list(
      "n500" = c(3.206, 1.32, 0.776, 1.262, 0.676)
    )
  )
)
dist_conv_plot_tikz(ZnSimulations, "norm", "log", 500)

## End(Not run)
```

---

## dZn *Rényi-Type Statistic Limiting Distribution Density Function*

---

### Description

Function for computing the value of the density function of the limiting distribution of the Rényi-type statistic.

### Usage

```
dZn(x, summands = NULL)
```

### Arguments

| | |
|---|---|
| x | Point at which to evaluate the density function (note that this parameter is not vectorized) |
| summands | Number of summands to use in summation (the default should be machine accurate) |

## Value

Value of the density function at $x$

## Examples

```
CPAT:::dZn(1)
```

---

`ff` *Fama-French Five Factors*

---

## Description

Data set containing the five factors described by Fama and French (2015), from the data library maintained by Kenneth French. Data ranges from July 1, 1963 to October 31, 2017.

## Usage

```
ff
```

## Format

A data frame with 13679 rows and 6 variables:

**Mkt.RF** Market excess returns

**RF** The risk-free rate of return

**SMB** The return on a diversified portfolio of small stocks minus return on a diversified portfolio of big stocks

**HML** The return of a portfolio of stocks with a high book-to-market (B/M) ratio minus the return of a portfolio of stocks with a low B/M ratio

**RMW** The return of a portfolio of stocks with robust profitability minus a portfolio of stocks with weak profitability

**CMA** The return of a portfolio of stocks with conservative investment minus the return of a portfolio of stocks with aggressive investment

Row names are dates in YYYYMMDD format.

## Source

http://mba.tuck.dartmouth.edu/pages/faculty/ken.french/data_library.html

## getLongRunWeights *Weights for Long-Run Variance*

### Description

Compute some weights for long-run variance. This code comes directly from the source code of **cointReg**; see getLongRunWeights.

### Usage

```
getLongRunWeights(n, bandwidth, kernel = "ba")
```

### Arguments

| | |
|---|---|
| n | Length of weights' vector |
| bandwidth | A number for the bandwidth |
| kernel | The kernel function; see getLongRunVar for possible values |

### Value

List with components w containing the vector of weights and upper, the index of the largest non-zero entry in w

### Examples

```
CPAT:::getLongRunWeights(10, 1)
```

## get_expanding_window_pvals *Expanding Window p-Values*

### Description

Gets p-values for the CUSUM, Darling-Erdös, Hidalgo-Seo, Andrews, and Rényi-type tests when applied to an expanding window of data.

### Usage

```
get_expanding_window_pvals(dat, m = Inf)
```

### Arguments

| | |
|---|---|
| dat | The dataset for which to test for change in mean |
| m | The location of the first potential change point for Andrews' test |

### Value

A matrix containing p-values for an expanding sample size, with each row corresponding to one observation larger; columns are labeled for each statistic

## Examples

```
if (require("foreach") & require("doParallel")) {
  CPAT:::get_expanding_window_pvals(rnorm(1000), m = 900)
}
```

---

`get_expanding_window_pvals_reg` *Expanding Window p-Values for Regression Models*

---

## Description

Gets p-values for the CUSUM, Darling-Erdös, Hidalgo-Seo, Andrews, and Rényi-type tests when applied to an expanding window of data for a regression model.

## Usage

```
get_expanding_window_pvals_reg(formula, data, min_n = 3, m = Inf,
  verbose = FALSE)
```

## Arguments

| | |
|---|---|
| `formula` | The regression model formula, which will be passed to `lm` |
| `data` | A `data.frame`, the dataset for which to test for structural change |
| `min_n` | An integer; the minimum sample size |
| `m` | The location of the first potential change point for Andrews' test |
| `verbose` | If `TRUE`, send messages to output |

## Value

A matrix containing p-values for an expanding sample size, with each row corresponding to one observation larger; columns are labeled for each statistic

## Examples

```
x <- rnorm(1000)
y <- 1 + 2 * x + rnorm(1000)
df <- data.frame(x, y)
if (require("foreach") & require("doParallel")) {
  CPAT:::get_expanding_window_pvals_reg(y ~ x, data = df, min_n = 4, m = 900)
}
```

## get_lrv_vec *Long-Run Variance Estimation With Possible Change Points*

### Description

Computes the estimates of the long-run variance in a change point context, as described in (Rice et al. ). By default it uses kernel and bandwidth selection as used in the package **cointReg**, though changing the parameters `kernel` and `bandwidth` can change this behavior. If **cointReg** is not installed, the Bartlett internal (defined internally) will be used and the bandwidth will be the square root of the sample size.

### Usage

```
get_lrv_vec(dat, kernel = "ba", bandwidth = "and")
```

### Arguments

| | |
|---|---|
| `dat` | The data vector |
| `kernel` | If character, the identifier of the kernel function as used in **cointReg** (see `getLongRunVar`); if function, the kernel function to be used for long-run variance estimation (default is the Bartlett kernel in **cointReg**) |
| `bandwidth` | If character, the identifier for how to compute the bandwidth as defined in **cointReg** (see `getBandwidth`); if function, a function to use for computing the bandwidth; if numeric, the bandwidth value to use (the default is to use Andrews' method, as used in **cointReg**) |

### Value

A vector of estimates of the long-run variance

### References

Rice G, Miller C, Horváth L (????). "A new class of change point test of Rényi type." submitted.

### Examples

```
x <- rnorm(1000)
CPAT:::get_lrv_vec(x)
CPAT:::get_lrv_vec(x, kernel = "pa", bandwidth = "nw")
```

## HR.test *Rényi-Type Test*

### Description

Performs the (univariate) Rényi-type test for change in mean, as described in (Rice et al. ). This is effectively an interface to `stat_Zn`; see its documentation for more details. p-values are computed using `pZn`, which represents the limiting distribution of the test statistic under the null hypothesis, which represents the limiting distribution of the test statistic under the null hypothesis when `kn` represents a sequence $t_T$ satisfying $t_T \to \infty$ and $t_T/T \to 0$ as $T \to \infty$. (`log` and `sqrt` should be good choices.)

### Usage

```
HR.test(x, kn = log, use_kernel_var = FALSE, stat_plot = FALSE,
  kernel = "ba", bandwidth = "and")
```

### Arguments

| | |
|---|---|
| x | Data to test for change in mean |
| kn | A function corresponding to the trimming parameter $t_T$; by default, the square root function |
| use_kernel_var | Set to TRUE to use kernel methods for long-run variance estimation (typically used when the data is believed to be correlated); if FALSE, then the long-run variance is estimated using $\hat{\sigma}^2_{T,t} = T^{-1}\left(\sum_{s=1}^{t}\left(X_s - \bar{X}_t\right)^2 + \sum_{s=t+1}^{T}\left(X_s - \tilde{X}_{T-t}\right)^2\right)$, where $\bar{X}_t = t^{-1}\sum_{s=1}^{t} X_s$ and $\tilde{X}_{T-t} = (T-t)^{-1}\sum_{s=t+1}^{T} X_s$; if custom_var is not NULL, this argument is ignored |
| stat_plot | Whether to create a plot of the values of the statistic at all potential change points |
| kernel | If character, the identifier of the kernel function as used in **cointReg** (see getLongRunVar); if function, the kernel function to be used for long-run variance estimation (default is the Bartlett kernel in **cointReg**) |
| bandwidth | If character, the identifier for how to compute the bandwidth as defined in **cointReg** (see getBandwidth); if function, a function to use for computing the bandwidth; if numeric, the bandwidth value to use (the default is to use Andrews' method, as used in **cointReg**) |

### Value

A htest-class object containing the results of the test

### References

Rice G, Miller C, Horváth L (????). "A new class of change point test of Rényi type." submitted.

### Examples

```
HR.test(rnorm(1000))
HR.test(rnorm(1000), use_kernel_var = TRUE, kernel = "bo", bandwidth = "nw")
```

---

## HS.test *Hidalgo-Seo Test*

---

### Description

Performs the (univariate) Hidalgo-Seo test for change in mean, as described in (Rice et al. ). This is effectively an interface to stat_hs; see its documentation for more details. p-values are computed using phidalgo_seo, which represents the limiting distribution of the test statistic when the null hypothesis is true.

### Usage

```
HS.test(x, corr = TRUE, stat_plot = FALSE)
```

### Arguments

| | |
|---|---|
| x | Data to test for change in mean |
| corr | If TRUE, the long-run variance will be computed under the assumption of correlated residuals; ignored if custom_var is not NULL or use_kernel_var is TRUE |
| stat_plot | Whether to create a plot of the values of the statistic at all potential change points |

### Value

A htest-class object containing the results of the test

### References

Rice G, Miller C, Horváth L (????). "A new class of change point test of Rényi type." submitted.

### Examples

```
HS.test(rnorm(1000))
HS.test(rnorm(1000), corr = FALSE)
```

---

## lrv_plot_tikz *Long-Run Variance Estimation Simulations Plot*

---

### Description

Create a Tikz plot of the estimated distribution of LRV estimators

### Usage

```
lrv_plot_tikz(data, n, ker_name, true_lrv, phi = NULL, xrange = NULL,
  width = 4.5, height = 3.5, filename = NULL, verbose = FALSE,
  makePDF = TRUE)
```

### Arguments

| | |
|---|---|
| data | A data.frame containing the data to plot |
| n | The sample size of simulated data sets for which to plot an estimated distribution |
| ker_name | The name of the kernel function used in the LRV estimator |
| true_lrv | The value of the true long-run variance |
| phi | The autocorrelation parameter of the simulated data sets to plot; if NULL, the data is assumed to have been generated with a GARCH(1,1) process |
| xrange | The limits of the horizontal axis of the plot |
| width | The width of the plot |
| height | The height of the plot |
| filename | The name of the file to save output (without stems; files with this string appended with .tex and maybe .pdf will be created); if NULL, a file name will automatically be chosen (of the form lrv_est_plot_ker_name_phi) |
| verbose | Print updates about progress (via link[base]{cat}) |
| makePDF | Automatically compile the resulting .tex file |

## Examples

```
## Not run:
plotlist <- data.frame(val = c(0.649, 0.965, 0.905),
                       n   = c(50,    50,    50),
                       phi = c(0,     0,     0))
lrv_plot_tikz(plotlist, 50, ker_name = "bartlett", true_lrv = 1)

## End(Not run)
```

---

# pdarling_erdos *Darling-Erdös Statistic CDF*

---

## Description

CDF for the limiting distribution of the Darling-Erdös statistic.

## Usage

```
pdarling_erdos(q)
```

## Arguments

| | |
|---|---|
| q | Quantile input to CDF |

## Value

If $Z$ is the random variable with this distribution, the quantity $P(Z \leq q)$

## Examples

```
CPAT:::pdarling_erdos(0.1)
```

---

# phidalgo_seo *Hidalgo-Seo Statistic CDF*

---

## Description

CDF of the limiting distribution of the Hidalgo-Seo statistic

## Usage

```
phidalgo_seo(q)
```

## Arguments

| | |
|---|---|
| q | Quantile input to CDF |

## Value

If $Z$ is the random variable following the limiting distribution, the quantity $P(Z \leq q)$

## Examples

```
CPAT:::phidalgo_seo(0.1)
```

---

pkolmogorov *Kolmogorov CDF*

---

## Description

CDF of the Kolmogorov distribution.

## Usage

```
pkolmogorov(q, summands = ceiling(q * sqrt(72) + 3/2))
```

## Arguments

| | |
|---|---|
| q | Quantile input to CDF |
| summands | Number of summands for infinite sum (the default should have machine accuracy) |

## Value

If $Z$ is the random variable following the Kolmogorov distribution, the quantity $P(Z \leq q)$

## Examples

```
CPAT:::pkolmogorov(0.1)
```

---

power_plot_tikz *Power Curve Plot (By Statistic)*

---

## Description

Create a Tikz plot of the power curves of a statistic, with each sample size having its own curve.

## Usage

```
power_plot_tikz(data, d, t, c, s, title = "", legend_pos = "none",
  width = 4.5, height = 3.5, filename = NULL, verbose = FALSE,
  makePDF = TRUE)
```

### Arguments

| | |
|---|---|
| data | A data.frame containing the data to plot |
| d | Label for data-generating process used to simulate the data on which the statistics were computed |
| t | Label for the trimming parameter of the Rényi-type statistic |
| c | Label for the process that computes the location of change points |
| s | The statistic for which to plot a power curve |
| title | The title of the plot |
| legend_pos | A string to be passed to link[ggplot2]{theme} (the legend.position argument) identifying where to place the legend |
| width | The width of the plot |
| height | The height of the plot |
| filename | The name of the file to save output (without stems; files with this string appended with .tex and maybe .pdf will be created); if NULL, the name will be automatically determined |
| verbose | Print updates about progress (via link[base]{cat}) |
| makePDF | Automatically compile the resulting .tex file |

### Examples

```
## Not run:
pdat <- data.frame(power = c(0.8926, 0.8714, 0.8296, 0.7936),
                   stat  = c("de",   "de",   "de",   "de"),
                   dist  = c("norm", "norm", "norm", "norm"),
                   kn    = c("log",  "log",  "log",  "log"),
                   n     = c(50,     50,     50,     50),
                   cpt   = c("c4rt", "c4rt", "c4rt", "c4rt"),
                   delta = c(-2.0,   -1.9,   -1.8,   -1.7))
power_plot_tikz(pdat, "norm", "log", "c4rt", "de")

## End(Not run)
```

---

## power_plot_tikz_by_n *Power Curve Plot*

---

### Description

Create a Tikz plot of the power curves of simulated statistics.

### Usage

```
power_plot_tikz_by_n(data, d, t, c, N, statlines, title = "",
  legend_pos = "none", width = 4.5, height = 3.5, filename = NULL,
  verbose = FALSE, makePDF = TRUE)
```

### Arguments

| | |
|---|---|
| data | A data.frame containing the data to plot |
| d | Label for data-generating process used to simulate the data on which the statistics were computed |
| t | Label for the trimming parameter of the Rényi-type statistic |
| c | Label for the process that computes the location of change points |
| N | The sample size of the simulated data sets on which the statistics were computed |
| statlines | A character vector where the names of the entries are the labels of the statistics in the stat column of data and the entries define the line types used by the values entry of scale_linetype_manual |
| title | The title of the plot |
| legend_pos | A string to be passed to link[ggplot2]{theme} (the legend.position argument) identifying where to place the legend |
| width | The width of the plot |
| height | The height of the plot |
| filename | The name of the file to save output (without stems; files with this string appended with .tex and maybe .pdf will be created); if NULL, the name will be automatically determined |
| verbose | Print updates about progress (via link[base]{cat}) |
| makePDF | Automatically compile the resulting .tex file |

### Examples

```
## Not run:
pdat <- data.frame(power = c(0.8926, 0.8714, 0.8296, 0.7936),
                   stat  = c("de",   "de",   "de",   "de"),
                   dist  = c("norm", "norm", "norm", "norm"),
                   kn    = c("log",  "log",  "log",  "log"),
                   n     = c(50,     50,     50,     50),
                   cpt   = c("c4rt", "c4rt", "c4rt", "c4rt"),
                   delta = c(-2.0,   -1.9,   -1.8,   -1.7))
power_plot_tikz_by_n(pdat, "norm", "log", "c4rt", 50, c("de" = "solid"))

## End(Not run)
```

---

## power_sim_stat_df_creator

*Create Power Simulation Results Data Frame*

---

### Description

Creates a data.frame that contains power simulation results from files containing power simulations. This function should automate the use of power_sim_Zn_to_df and power_sim_Vn_to_df for collecting power simulation data. It takes two CSV files, one passed (as a character string) to file_meta and the other to stat_meta, describing how the files (named and described in file_meta) should be handled.

### Usage

```
power_sim_stat_df_creator(file_meta, stat_meta, prefix = "",
  alpha = 0.05)
```

### Arguments

| | |
|---|---|
| file_meta | The location of a CSV file that contains file names and the statistics that those files correspond to |
| stat_meta | The location of a CSV file that contains statistic (stat) labels (used in file_meta). the name of the variable for the statistic, and the name of the function that converts a file (mentioned in file_meta) to a data.frame of power data |
| prefix | Character string representing a prefix for file names mentioned in file_meta; could be used for adding path information to those names, in case the files are not in the working directory and there is no desire to edit file_meta's data |
| alpha | Numeric for level of significance used in power calculations |

### Value

A data frame containing the power simulation data

### Examples

```
## Not run:
power_sim_stat_df_creator("FileStatMeta.csv", "StatMeta.csv")

## End(Not run)
```

---

## power_sim_Vn_to_df *Convert CUSUM-Type Statistic Power Simulation Save List to Data Frame*

---

### Description

This function will convert the power simulation data generated in a list in our simulation scripts to a data.frame. Given such a list and a critical value to determine whether the null hypothesis should be rejected, the function will return a data.frame with columns power, stat, dist, n, cpt, and delta, which correspond to: the empirical power of the statistic; the identifier of the statistic; the generating distribution of the statistic was computed on; the identifier of how change points were computed; and the size of the change.

### Usage

```
power_sim_Vn_to_df(obj, crit)
```

### Arguments

| | |
|---|---|
| obj | A list containing simulated statistic values |
| crit | The critical value determining whether a statistic should lead to the rejection of the null hypothesis |

## Value

A `data.frame` summarizing the results of the data stored in `obj`

## Examples

```
saveobj <- list("norm" = list(
                  "n50" = list(
                    "c4rt" = list(
                      "d_0" = c(1.551, 1.276, 1.348, 1.982, 1.423)
))))
CPAT:::power_sim_Vn_to_df(saveobj, CPAT:::qkolmogorov(.95))
```

---

`power_sim_Zn_to_df` *Convert Rényi-Type Statistic Power Simulation Save List to Data Frame*

---

## Description

This function will convert the power simulation data generated in a list in our simulation scripts to a `data.frame`. Given such a list and a critical value to determine whether the null hypothesis should be rejected, the function will return a `data.frame` with columns `power`, `stat`, `dist`, `kn`, `n`, `cpt`, and `delta`, which correspond to: the empirical power of the statistic; the identifier of the statistic; the generating distribution of the statistic was computed on; the `kn` parameter; the identifier of how change points were computed; and the size of the change.

## Usage

```
power_sim_Zn_to_df(obj, crit)
```

## Arguments

| | |
|---|---|
| `obj` | A list containing simulated statistic values |
| `crit` | The critical value determining whether a statistic should lead to the rejection of the null hypothesis |

## Value

A `data.frame` summarizing the results of the data stored in `obj`

## Examples

```
saveobj <- list("norm" = list(
                  "log" = list(
                    "n50" = list(
                      "c4rt" = list(
                        "d_0" = c(1.551, 1.276, 1.348, 1.982, 1.423)
)))))
CPAT:::power_sim_Zn_to_df(saveobj, CPAT:::qZn(.95))
```

## pZn *Rènyi-Type Statistic CDF*

### Description

CDF for the limiting distribution of the Rènyi-type statistic.

### Usage

```
pZn(q, summands = NULL)
```

### Arguments

| | |
|---|---|
| q | Quantile input to CDF |
| summands | Number of summands for infinite sum; if NULL, automatically determined |

### Value

If $Z$ is the random variable following the limiting distribution, the quantity $P(Z \leq q)$

### Examples

```
CPAT:::pZn(0.1)
```

## qdarling_erdos *Darling-Erdös Statistic Limiting Distribution Quantile Function*

### Description

Quantile function for the limiting distribution of the Darling-Erdös statistic.

### Usage

```
qdarling_erdos(p)
```

### Arguments

| | |
|---|---|
| p | The probability associated with the desired quantile |

### Value

The quantile associated with p

### Examples

```
CPAT:::qdarling_erdos(0.5)
```

## qhidalgo_seo *Hidalgo-Seo Statistic Limiting Distribution Quantile Function*

### Description

Quantile function for the limiting distribution of the Hidalgo-Seo statistic

### Usage

```
qhidalgo_seo(p)
```

### Arguments

| | |
|---|---|
| p | The probability associated with the desired quantile |

### Value

A The quantile associated with p

### Examples

```
CPAT:::qhidalgo_seo(0.5)
```

## qkolmogorov *Kolmogorov Distribution Quantile Function*

### Description

Quantile function for the Kolmogorov distribution.

### Usage

```
qkolmogorov(p, summands = 500, interval = c(0, 100),
  tol = .Machine$double.eps, ...)
```

### Arguments

| | |
|---|---|
| p | Value of the CDF at the quantile |
| summands | Number of summands for infinite sum |
| interval, tol, ... | Arguments to be passed to uniroot |

### Details

This function uses uniroot for finding this quantity, and many of the the accepted parameters are arguments for that function; see its documentation for more details.

### Value

The quantile associated with p

## Examples

```
CPAT:::qkolmogorov(0.5)
```

---

qZn *Rènyi-Type Statistic Quantile Function*

---

## Description

Quantile function for the limiting distribution of the Rènyi-type statistic.

## Usage

```
qZn(p, summands = 500, interval = c(0, 100),
  tol = .Machine$double.eps, ...)
```

## Arguments

| | |
|---|---|
| p | Value of the CDF at the quantile |
| summands | Number of summands for infinite sum |
| interval, tol, ... | Arguments to be passed to uniroot |

## Details

This function uses uniroot for finding this quantity, and many of the the accepted parameters are arguments for that function; see its documentation for more details.

## Value

The quantile associated with p

## Examples

```
CPAT:::qZn(0.5)
```

---

rchangepoint *Simulate Univariate Data With a Single Change Point*

---

## Description

This function simulates univariate data with a structural change.

## Usage

```
rchangepoint(n, changepoint = NULL, mean1 = 0, mean2 = 0,
  dist = rnorm, meanparam = "mean", ...)
```

### Arguments

| | |
|---|---|
| n | An integer for the data set's sample size |
| changepoint | An integer for where the change point occurs |
| mean1 | The mean prior to the change point |
| mean2 | The mean after the change point |
| dist | The function with which random data will be generated |
| meanparam | A string for the parameter in dist representing the mean |
| ... | Other arguments to be passed to dist |

### Details

This function generates artificial change point data, where up to the specified change point the data has one mean, and after the point it has a different mean. By default, the function simulates standard Normal data with no change. If changepoint is NULL, then by default the change point will be at about the middle of the data.

### Value

A vector of the simulated data

### Examples

```
CPAT:::rchangepoint(500)
CPAT:::rchangepoint(500, changepoint = 10, mean2 = 2, sd = 2)
CPAT:::rchangepoint(500, changepoint = 250, dist = rexp, meanparam = "rate",
                    mean1 = 1, mean2 = 2)
```

---

## sim_de_stat *Darling-Erdös Statistic Simulation*

---

### Description

Simulates multiple realizations of the Darling-Erdös statistic.

### Usage

```
sim_de_stat(size, a = log, b = log, use_kernel_var = FALSE,
  kernel = "ba", bandwidth = "and", n = 500, gen_func = rnorm,
  args = NULL, parallel = FALSE)
```

### Arguments

| | |
|---|---|
| size | Number of realizations to simulate |
| a | The function that will be composed wit $l(x) = (2\log(x))^{1/2}$ |
| b | The function that will be composed with $u(x) = 2\log(x) + \frac{1}{2}\log(\log(x)) - \frac{1}{2}\log(pi)$ |
| use_kernel_var | Set to TRUE to use kernel-based long-run variance estimation (FALSE means this is not employed) |

| | |
|---|---|
| kernel | If character, the identifier of the kernel function as used in the **cointReg** (see documentation for cointReg::getLongRunVar); if function, the kernel function to be used for long-run variance estimation (default is the Bartlett kernel in **cointReg**); this parameter has no effect if use_kernel_var is FALSE |
| bandwidth | If character, the identifier of how to compute the bandwidth as defined in the **cointReg** package (see documentation for cointReg::getLongRunVar); if function, a function to use for computing the bandwidth; if numeric, the bandwidth to use (the default behavior is to use the Andrews (1991) method, as used in **cointReg**); this parameter has no effect if use_kernel_var is FALSE |
| n | The sample size for each realization |
| gen_func | The function generating the random sample from which the statistic is computed |
| args | A list of arguments to be passed to gen_func |
| parallel | Whether to use the **foreach** and **doParallel** packages to parallelize simulation (which needs to be initialized in the global namespace before use) |

## Details

If use_kernel_var is set to TRUE, long-run variance estimation using kernel-based techniques will be employed; otherwise, a technique resembling standard variance estimation will be employed. Any technique employed, though, will account for the potential break points, as described in Rice et al. (). See the documentation for stat_de for more details.

The parameters kernel and bandwidth control parameters for long-run variance estimation using kernel methods. These parameters will be passed directly to stat_de.

## Value

A vector of simulated realizations of the Darling-Erdös statistic

## References

Andrews DWK (1991). "Heteroskedasticity and Autocorrelation Consistent Covariance Matrix Estimation." *Econometrica*, **59**(3), 817-858.

Rice G, Miller C, Horváth L (????). "A new class of change point test of Rényi type." submitted.

## Examples

```
CPAT:::sim_de_stat(100)
CPAT:::sim_de_stat(100, use_kernel_var = TRUE,
                   gen_func = CPAT:::rchangepoint,
                   args = list(changepoint = 250, mean2 = 1))
```

---

# sim_hs_stat *Hidalgo-Seo Statistic Simulation*

---

## Description

Simulates multiple realizations of the Hidalgo-Seo statistic.

## Usage

```
sim_hs_stat(size, corr = TRUE, gen_func = rnorm, args = NULL,
  n = 500, parallel = FALSE, use_kernel_var = FALSE, kernel = "ba",
  bandwidth = "and")
```

## Arguments

| | |
|---|---|
| size | Number of realizations to simulate |
| corr | Whether long-run variance should be computed under the assumption of correlated residuals |
| gen_func | The function generating the random sample from which the statistic is computed |
| args | A list of arguments to be passed to gen_func |
| n | The sample size for each realization |
| parallel | Whether to use the **foreach** and **doParallel** packages to parallelize simulation (which needs to be initialized in the global namespace before use) |
| use_kernel_var | Set to TRUE to use kernel-based long-run variance estimation (FALSE means this is not employed); *TODO: NOT CURRENTLY IMPLEMENTED* |
| kernel | If character, the identifier of the kernel function as used in the **cointReg** (see documentation for cointReg::getLongRunVar); if function, the kernel function to be used for long-run variance estimation (default is the Bartlett kernel in **cointReg**); this parameter has no effect if use_kernel_var is FALSE; *TODO: NOT CURRENTLY IMPLEMENTED* |
| bandwidth | If character, the identifier of how to compute the bandwidth as defined in the **cointReg** package (see documentation for cointReg::getLongRunVar); if function, a function to use for computing the bandwidth; if numeric, the bandwidth to use (the default behavior is to use the Andrews (1991) method, as used in **cointReg**); this parameter has no effect if use_kernel_var is FALSE; *TODO: NOT CURRENTLY IMPLEMENTED* |

## Details

If corr is TRUE, then the residuals of the data-generating process are assumed to be correlated and the test accounts for this in long-run variance estimation; see the documentation for stat_hs for more details. Otherwise, the sample variance is the estimate for the long-run variance, as described in Hidalgo and Seo (2013).

## Value

A vector of simulated realizations of the Hidalgo-Seo statistic

## References

Andrews DWK (1991). "Heteroskedasticity and Autocorrelation Consistent Covariance Matrix Estimation." *Econometrica*, **59**(3), 817-858.

Hidalgo J, Seo MH (2013). "Testing for structural stability in the whole sample." *Journal of Econometrics*, **175**(2), 84 - 93. ISSN 0304-4076, doi: 10.1016/j.jeconom.2013.02.008, http://www.sciencedirect.com/science/article/pii/S0304407613000626.

### Examples

```
CPAT:::sim_hs_stat(100)
CPAT:::sim_hs_stat(100, gen_func = CPAT:::rchangepoint,
                   args = list(changepoint = 250, mean2 = 1))
```

---

## sim_Vn *CUSUM Statistic Simulation (Assuming Variance)*

---

### Description

Simulates multiple realizations of the CUSUM statistic when the long-run variance of the data is known.

### Usage

```
sim_Vn(size, n = 500, gen_func = rnorm, sd = 1, args = NULL)
```

### Arguments

| | |
|---|---|
| size | Number of realizations to simulate |
| n | The sample size for each realization |
| gen_func | The function generating the random sample from which the statistic is computed |
| sd | The square root of the second moment of the data |
| args | A list of arguments to be passed to gen_func |

### Value

A vector of simulated realizations of the CUSUM statistic

### Examples

```
CPAT:::sim_Vn(100)
CPAT:::sim_Vn(100, gen_func = CPAT:::rchangepoint,
              args = list(changepoint = 250, mean2 = 1))
```

---

## sim_Vn_stat *CUSUM Statistic Simulation*

---

### Description

Simulates multiple realizations of the CUSUM statistic.

### Usage

```
sim_Vn_stat(size, kn = function(n) {     1 }, tau = 0,
  use_kernel_var = FALSE, kernel = "ba", bandwidth = "and",
  n = 500, gen_func = rnorm, args = NULL, parallel = FALSE)
```

## Arguments

| | |
|---|---|
| size | Number of realizations to simulate |
| kn | A function returning a positive integer that is used in the definition of the trimmed CUSUSM statistic effectively setting the bounds over which the maximum is taken |
| tau | The weighting parameter for the weighted CUSUM statistic (defaults to zero for no weighting) |
| use_kernel_var | Set to TRUE to use kernel-based long-run variance estimation (FALSE means this is not employed) |
| kernel | If character, the identifier of the kernel function as used in the **cointReg** (see documentation for cointReg::getLongRunVar); if function, the kernel function to be used for long-run variance estimation (default is the Bartlett kernel in **cointReg**); this parameter has no effect if use_kernel_var is FALSE |
| bandwidth | If character, the identifier of how to compute the bandwidth as defined in the **cointReg** package (see documentation for cointReg::getLongRunVar); if function, a function to use for computing the bandwidth; if numeric, the bandwidth to use (the default behavior is to use the method described in (Andrews 1991), as used in **cointReg**); this parameter has no effect if use_kernel_var is FALSE |
| n | The sample size for each realization |
| gen_func | The function generating the random sample from which the statistic is computed |
| args | A list of arguments to be passed to gen_func |
| parallel | Whether to use the **foreach** and **doParallel** packages to parallelize simulation (which needs to be initialized in the global namespace before use) |

## Details

This differs from sim_Vn() in that the long-run variance is estimated with this function, while sim_Vn() assumes the long-run variance is known. Estimation can be done in a variety of ways. If use_kernel_var is set to TRUE, long-run variance estimation using kernel-based techniques will be employed; otherwise, a technique resembling standard variance estimation will be employed. Any technique employed, though, will account for the potential break points, as described in Rice et al. (). See the documentation for stat_Vn for more details.

The parameters kernel and bandwidth control parameters for long-run variance estimation using kernel methods. These parameters will be passed directly to stat_Vn.

Versions of the CUSUM statistic, such as the weighted or trimmed statistics, can be simulated with the function by passing values to kn and tau; again, see the documentation for stat_Vn.

## Value

A vector of simulated realizations of the CUSUM statistic

## References

Andrews DWK (1991). "Heteroskedasticity and Autocorrelation Consistent Covariance Matrix Estimation." *Econometrica*, **59**(3), 817-858.

Rice G, Miller C, Horváth L (????). "A new class of change point test of Rényi type." submitted.

## Examples

```
CPAT:::sim_Vn_stat(100)
CPAT:::sim_Vn_stat(100, kn = function(n) {floor(0.1 * n)}, tau = 1/3,
                   use_kernel_var = TRUE, gen_func = CPAT:::rchangepoint,
                   args = list(changepoint = 250, mean2 = 1))
```

---

`sim_Zn` *Rènyi-Type Statistic Simulation (Assuming Variance)*

---

## Description

Simulates multiple realizations of the Rènyi-type statistic when the long-run variance of the data is known.

## Usage

```
sim_Zn(size, kn, n = 500, gen_func = rnorm, args = NULL, sd = 1)
```

## Arguments

| | |
|---|---|
| `size` | Number of realizations to simulate |
| `kn` | A function returning a positive integer that is used in the definition of the Rènyi-type statistic effectively setting the bounds over which the maximum is taken |
| `n` | The sample size for each realization |
| `gen_func` | The function generating the random sample from which the statistic is computed |
| `args` | A list of arguments to be passed to `gen_func` |
| `sd` | The square root of the second moment of the data |

## Value

A vector of simulated realizations of the Rènyi-type statistic

## Examples

```
CPAT:::sim_Zn(100, kn = function(n) {floor(log(n))})
CPAT:::sim_Zn(100, kn = function(n) {floor(log(n))},
              gen_func = CPAT:::rchangepoint, args = list(changepoint = 250,
                                                          mean2 = 1))
```

`sim_Zn_stat` *Rènyi-Type Statistic Simulation*

## Description

Simulates multiple realizations of the Rènyi-type statistic.

## Usage

```
sim_Zn_stat(size, kn = function(n) {     floor(sqrt(n)) },
  use_kernel_var = FALSE, kernel = "ba", bandwidth = "and",
  n = 500, gen_func = rnorm, args = NULL, parallel = FALSE)
```

## Arguments

| | |
|---|---|
| `size` | Number of realizations to simulate |
| `kn` | A function returning a positive integer that is used in the definition of the Rènyi-type statistic effectively setting the bounds over which the maximum is taken |
| `use_kernel_var` | Set to `TRUE` to use kernel-based long-run variance estimation (`FALSE` means this is not employed) |
| `kernel` | If character, the identifier of the kernel function as used in the **cointReg** (see documentation for `cointReg::getLongRunVar`); if function, the kernel function to be used for long-run variance estimation (default is the Bartlett kernel in **cointReg**); this parameter has no effect if `use_kernel_var` is `FALSE` |
| `bandwidth` | If character, the identifier of how to compute the bandwidth as defined in the **cointReg** package (see documentation for `cointReg::getLongRunVar`); if function, a function to use for computing the bandwidth; if numeric, the bandwidth to use (the default behavior is to use the Andrews (1991) method, as used in **cointReg**); this parameter has no effect if `use_kernel_var` is `FALSE` |
| `n` | The sample size for each realization |
| `gen_func` | The function generating the random sample from which the statistic is computed |
| `args` | A list of arguments to be passed to `gen_func` |
| `parallel` | Whether to use the **foreach** and **doParallel** packages to parallelize simulation (which needs to be initialized in the global namespace before use) |

## Details

This differs from `sim_Zn()` in that the long-run variance is estimated with this function, while `sim_Zn()` assumes the long-run variance is known. Estimation can be done in a variety of ways. If `use_kernel_var` is set to `TRUE`, long-run variance estimation using kernel-based techniques will be employed; otherwise, a technique resembling standard variance estimation will be employed. Any technique employed, though, will account for the potential break points, as described in Rice et al. (). See the documentation for `stat_Zn` for more details.

The parameters `kernel` and `bandwidth` control parameters for long-run variance estimation using kernel methods. These parameters will be passed directly to `stat_Zn`.

## Value

A vector of simulated realizations of the Rènyi-type statistic

## References

Andrews DWK (1991). "Heteroskedasticity and Autocorrelation Consistent Covariance Matrix Estimation." *Econometrica*, **59**(3), 817-858.

Rice G, Miller C, Horváth L (????). "A new class of change point test of Rényi type." submitted.

## Examples

```
CPAT:::sim_Zn_stat(100)
CPAT:::sim_Zn_stat(100, kn = function(n) {floor(log(n))},
            use_kernel_var = TRUE, gen_func = CPAT:::rchangepoint,
            args = list(changepoint = 250, mean2 = 1))
```

---

`stat_de` *Compute the Darling-Erdös Statistic*

---

## Description

This function computes the Darling-Erdös statistic.

## Usage

```
stat_de(dat, a = log, b = log, estimate = FALSE,
  use_kernel_var = FALSE, custom_var = NULL, kernel = "ba",
  bandwidth = "and", get_all_vals = FALSE)
```

## Arguments

| | |
|---|---|
| `dat` | The data vector |
| `a` | The function that will be composed with $l(x) = (2 \log x)^{1/2}$ |
| `b` | The function that will be composed with $u(x) = 2 \log x + \frac{1}{2} \log \log x - \frac{1}{2} \log \pi$ |
| `estimate` | Set to `TRUE` to return the estimated location of the change point |
| `use_kernel_var` | Set to `TRUE` to use kernel methods for long-run variance estimation (typically used when the data is believed to be correlated); if `FALSE`, then the long-run variance is estimated using $\hat{\sigma}^2_{T,t} = T^{-1} \left( \sum_{s=1}^{t} \left( X_s - \bar{X}_t \right)^2 + \sum_{s=t+1}^{T} \left( X_s - \tilde{X}_{T-t} \right)^2 \right)$, where $\bar{X}_t = t^{-1} \sum_{s=1}^{t} X_s$ and $\tilde{X}_{T-t} = (T-t)^{-1} \sum_{s=t+1}^{T} X_s$ |
| `custom_var` | Can be a vector the same length as `dat` consisting of variance-like numbers at each potential change point (so each entry of the vector would be the "best estimate" of the long-run variance if that location were where the change point occured) or a function taking two parameters `x` and `k` that can be used to generate this vector, with `x` representing the data vector and `k` the position of a potential change point; if `NULL`, this argument is ignored |
| `kernel` | If character, the identifier of the kernel function as used in **cointReg** (see `getLongRunVar`); if function, the kernel function to be used for long-run variance estimation (default is the Bartlett kernel in **cointReg**) |
| `bandwidth` | If character, the identifier for how to compute the bandwidth as defined in **cointReg** (see `getBandwidth`); if function, a function to use for computing the bandwidth; if numeric, the bandwidth value to use (the default is to use Andrews' method, as used in **cointReg**) |
| `get_all_vals` | If `TRUE`, return all values for the statistic at every tested point in the data set |

## Details

If $\bar{A}_T(\tau, t_T)$ is the weighted and trimmed CUSUM statistic with weighting parameter $\tau$ and trimming parameter $t_T$ (see `stat_Vn`), then the Darling-Erdös statistic is

$$l(a_T)\bar{A}_T(1/2, 1) - u(b_T)$$

with $l(x) = \sqrt{2 \log x}$ and $u(x) = 2 \log x + \frac{1}{2} \log \log x - \frac{1}{2} \log \pi$ ($\log x$ is the natural logarithm of $x$). The parameter `a` corresponds to $a_T$ and `b` to $b_T$; these are both `log` by default.

See (Rice et al. ) to learn more.

## Value

If both `estimate` and `get_all_vals` are `FALSE`, the value of the test statistic; otherwise, a list that contains the test statistic and the other values requested (if both are `TRUE`, the test statistic is in the first position and the estimated changg point in the second)

## References

Rice G, Miller C, Horváth L (????). "A new class of change point test of Rényi type." submitted.

## Examples

```
CPAT:::stat_de(rnorm(1000))
CPAT:::stat_de(rnorm(1000), use_kernel_var = TRUE, bandwidth = "nw", kernel = "bo")
```

---

# stat_hs *Compute the Hidalgo-Seo Statistic*

---

## Description

This function computes the Hidalgo-Seo statistic for a change in mean model.

## Usage

```
stat_hs(dat, estimate = FALSE, corr = TRUE, get_all_vals = FALSE,
  custom_var = NULL, use_kernel_var = FALSE, kernel = "ba",
  bandwidth = "and")
```

## Arguments

| | |
|---|---|
| `dat` | The data vector |
| `estimate` | Set to `TRUE` to return the estimated location of the change point |
| `corr` | If `TRUE`, the long-run variance will be computed under the assumption of correlated residuals; ignored if `custom_var` is not `NULL` or `use_kernel_var` is `TRUE` |
| `get_all_vals` | If `TRUE`, return all values for the statistic at every tested point in the data set |
| `custom_var` | Can be a vector the same length as `dat` consisting of variance-like numbers at each potential change point (so each entry of the vector would be the "best estimate" of the long-run variance if that location were where the change point occured) or a function taking two parameters `x` and `k` that can be used to generate this vector, with `x` representing the data vector and `k` the position of a potential change point; if `NULL`, this argument is ignored |

`use_kernel_var` Set to `TRUE` to use kernel methods for long-run variance estimation (typically used when the data is believed to be correlated); if `FALSE`, then the long-run variance is estimated using $\hat{sigma}^2_{T,t} = T^{-1}\left(\sum_{s=1}^{t}\left(X_s - \bar{X}_t\right)^2 + \sum_{s=t+1}^{T}\left(X_s - \tilde{X}_{T-t}\right)^2\right)$, where $\bar{X}_t = t^{-1}\sum_{s=1}^{t} X_s$ and $\tilde{X}_{T-t} = (T-t)^{-1}\sum_{s=t+1}^{T} X_s$; if `custom_var` is not `NULL`, this argument is ignored

`kernel` If character, the identifier of the kernel function as used in **cointReg** (see `getLongRunVar`); if function, the kernel function to be used for long-run variance estimation (default is the Bartlett kernel in **cointReg**)

`bandwidth` If character, the identifier for how to compute the bandwidth as defined in **cointReg** (see `getBandwidth`); if function, a function to use for computing the bandwidth; if numeric, the bandwidth value to use (the default is to use Andrews' method, as used in **cointReg**)

## Details

For a data set $x_t$ with $n$ observations, the test statistic is

$$\max_{1 \leq s \leq n-1} (\mathcal{LM}(s) - B_n)/A_n$$

where $\hat{u}_t = x_t - \bar{x}$ ($\bar{x}$ is the sample mean), $a_n = (2\log\log n)^{1/2}$, $b_n = a_n^2 - \frac{1}{2}\log\log\log n - \log\Gamma(1/2)$, $A_n = b_n/a_n^2$, $B_n = b_n^2/a_n^2$, $\hat{\Delta} = \hat{\sigma}^2 = n^{-1}\sum_{t=1}^{n}\hat{u}_t^2$, and $\mathcal{LM}(s) = n(n-s)^{-1}s^{-1}\hat{\Delta}^{-1}\left(\sum_{t=1}^{s}\hat{u}_t\right)^2$.

If `corr` is `FALSE`, then the residuals are assumed to be uncorrelated. Otherwise, the residuals are assumed to be correlated and $\hat{\Delta} = \hat{\gamma}(0) + 2\sum_{j=1}^{\lfloor\sqrt{n}\rfloor}(1 - \frac{j}{\sqrt{n}})\hat{\gamma}(j)$ with $\hat{\gamma}(j) = \frac{1}{n}\sum_{t=1}^{n-j}\hat{u}_t\hat{u}_{t+j}$.

This statistic was presented in (Hidalgo and Seo 2013).

## Value

If both `estimate` and `get_all_vals` are `FALSE`, the value of the test statistic; otherwise, a list that contains the test statistic and the other values requested (if both are `TRUE`, the test statistic is in the first position and the estimated change point in the second)

## References

Hidalgo J, Seo MH (2013). "Testing for structural stability in the whole sample." *Journal of Econometrics*, **175**(2), 84 - 93. ISSN 0304-4076, doi: 10.1016/j.jeconom.2013.02.008, http://www.sciencedirect.com/science/article/pii/S0304407613000626.

## Examples

```
CPAT:::stat_hs(rnorm(1000))
CPAT:::stat_hs(rnorm(1000), corr = FALSE)
```

stat_Vn *Compute the CUSUM Statistic*

## Description

This function computes the CUSUM statistic (and can compute weighted/trimmed variants, depending on the values of kn and tau).

## Usage

```
stat_Vn(dat, kn = function(n) {     1 }, tau = 0, estimate = FALSE,
  use_kernel_var = FALSE, custom_var = NULL, kernel = "ba",
  bandwidth = "and", get_all_vals = FALSE)
```

## Arguments

| | |
|---|---|
| dat | The data vector |
| kn | A function corresponding to the trimming parameter $t_T$ in the trimmed CUSUM variant; by default, is a function returning 1 (for no trimming) |
| tau | The weighting parameter $\tau$ for the weighted CUSUM statistic; by default, is 0 (for no weighting) |
| estimate | Set to TRUE to return the estimated location of the change point |
| use_kernel_var | Set to TRUE to use kernel methods for long-run variance estimation (typically used when the data is believed to be correlated); if FALSE, then the long-run variance is estimated using $\hat{\sigma}^2_{T,t} = T^{-1}\left(\sum_{s=1}^{t}\left(X_s - \bar{X}_t\right)^2 + \sum_{s=t+1}^{T}\left(X_s - \tilde{X}_{T-t}\right)^2\right)$, where $\bar{X}_t = t^{-1}\sum_{s=1}^{t} X_s$ and $\tilde{X}_{T-t} = (T-t)^{-1}\sum_{s=t+1}^{T} X_s$ |
| custom_var | Can be a vector the same length as dat consisting of variance-like numbers at each potential change point (so each entry of the vector would be the "best estimate" of the long-run variance if that location were where the change point occured) or a function taking two parameters x and k that can be used to generate this vector, with x representing the data vector and k the position of a potential change point; if NULL, this argument is ignored |
| kernel | If character, the identifier of the kernel function as used in **cointReg** (see getLongRunVar); if function, the kernel function to be used for long-run variance estimation (default is the Bartlett kernel in **cointReg**) |
| bandwidth | If character, the identifier for how to compute the bandwidth as defined in **cointReg** (see getBandwidth); if function, a function to use for computing the bandwidth; if numeric, the bandwidth value to use (the default is to use Andrews' method, as used in **cointReg**) |
| get_all_vals | If TRUE, return all values for the statistic at every tested point in the data set |

## Details

The definition of the statistic is

$$T^{-1/2}\max_{1\le t\le T}\hat{\sigma}^{-1}_{t,T}\left|\sum_{s=1}^{t}X_s - \frac{t}{T}\sum_{s=1}^{T}\right|$$

A more general version is

$$T^{-1/2} \max_{t_T \le t \le T - t_T} \hat{\sigma}_{t,T}^{-1} \left( \frac{t}{T} \left( \frac{T-t}{T} \right) \right)^{\tau} \left| \sum_{s=1}^{t} X_s - \frac{t}{T} \sum_{s=1}^{T} \right|$$

The parameter `kn` corresponds to the trimming parameter $t_T$ and the parameter `tau` corresponds to $\tau$.

See (Rice et al. ) for more details.

## Value

If both `estimate` and `get_all_vals` are `FALSE`, the value of the test statistic; otherwise, a list that contains the test statistic and the other values requested (if both are `TRUE`, the test statistic is in the first position and the estimated change point in the second)

## References

Rice G, Miller C, Horváth L (????). "A new class of change point test of Rényi type." submitted.

## Examples

```
CPAT:::stat_Vn(rnorm(1000))
CPAT:::stat_Vn(rnorm(1000), kn = function(n) {0.1 * n}, tau = 1/2)
CPAT:::stat_Vn(rnorm(1000), use_kernel_var = TRUE, bandwidth = "nw", kernel = "bo")
```

---

`stat_Zn` *Compute the Rényi-Type Statistic*

---

## Description

This function computes the Rényi-type statistic.

## Usage

```
stat_Zn(dat, kn = function(n) {     floor(sqrt(n)) }, estimate = FALSE,
  use_kernel_var = FALSE, custom_var = NULL, kernel = "ba",
  bandwidth = "and", get_all_vals = FALSE)
```

## Arguments

| | |
|---|---|
| `dat` | The data vector |
| `kn` | A function corresponding to the trimming parameter $t_T$; by default, the square root function |
| `estimate` | Set to `TRUE` to return the estimated location of the change point |
| `use_kernel_var` | Set to `TRUE` to use kernel methods for long-run variance estimation (typically used when the data is believed to be correlated); if `FALSE`, then the long-run variance is estimated using $\hat{\sigma}^2_{T,t} = T^{-1} \left( \sum_{s=1}^{t} \left( X_s - \bar{X}_t \right)^2 + \sum_{s=t+1}^{T} \left( X_s - \tilde{X}_{T-t} \right)^2 \right)$, where $\bar{X}_t = t^{-1} \sum_{s=1}^{t} X_s$ and $\tilde{X}_{T-t} = (T-t)^{-1} \sum_{s=t+1}^{T} X_s$; if `custom_var` is not `NULL`, this argument is ignored |

| | |
|---|---|
| custom_var | Can be a vector the same length as dat consisting of variance-like numbers at each potential change point (so each entry of the vector would be the "best estimate" of the long-run variance if that location were where the change point occured) or a function taking two parameters x and k that can be used to generate this vector, with x representing the data vector and k the position of a potential change point; if NULL, this argument is ignored |
| kernel | If character, the identifier of the kernel function as used in **cointReg** (see getLongRunVar); if function, the kernel function to be used for long-run variance estimation (default is the Bartlett kernel in **cointReg**) |
| bandwidth | If character, the identifier for how to compute the bandwidth as defined in **cointReg** (see getBandwidth); if function, a function to use for computing the bandwidth; if numeric, the bandwidth value to use (the default is to use Andrews' method, as used in **cointReg**) |
| get_all_vals | If TRUE, return all values for the statistic at every tested point in the data set |

## Details

The definition of the statistic is

$$\max_{t_T \leq t \leq T - t_T} \hat{\sigma}_{t,T}^{-1} \left| t^{-1} \sum_{s=1}^{t} X_s - (T-t)^{-1} \sum_{s=t+1}^{T} X_s \right|$$

The parameter kn corresponds to the trimming parameter $t_T$.

## Value

If both estimate and get_all_vals are FALSE, the value of the test statistic; otherwise, a list that contains the test statistic and the other values requested (if both are TRUE, the test statistic is in the first position and the estimated change point in the second)

## Examples

```
CPAT:::stat_Zn(rnorm(1000))
CPAT:::stat_Zn(rnorm(1000), kn = function(n) {floor(log(n))})
CPAT:::stat_Zn(rnorm(1000), use_kernel_var = TRUE, bandwidth = "nw",
               kernel = "bo")
```

---

# %s% *Concatenate (With Space)*

---

## Description

Concatenate and form strings (with space separation)

## Usage

```
x %s% y
```

## Arguments

| | |
|---|---|
| x | One object |
| y | Another object |

### Value

A string combining x and y with a space separating them

### Examples

```
`%s%` <- CPAT:::`%s%`
"Hello" %s% "world"
```

---

## %s0% *Concatenate (Without Space)*

---

### Description

Concatenate and form strings (no space separation)

### Usage

```
x %s0% y
```

### Arguments

| | |
|---|---|
| x | One object |
| y | Another object |

### Value

A string combining x and y

### Examples

```
`%s0%` <- CPAT:::`%s0%`
"Hello" %s0% "world"
```

# Index