$$Cov(y) = (1 - \theta)^2 S + \frac{\theta}{2}(1 - \frac{\theta}{2})I$$