

Problem Set # 6

Given: Mon., Oct. 22 **Recommended Completion Date:** Mon., Oct. 29

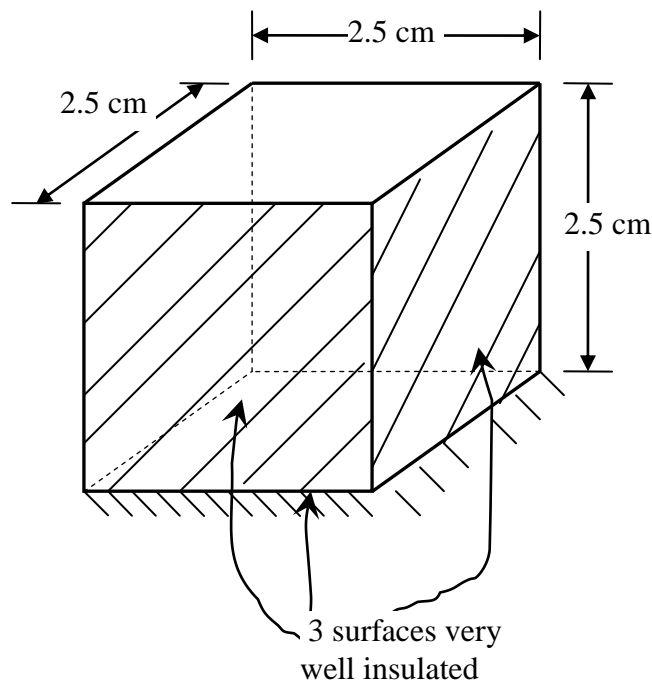
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Problem 1: A plate of stainless steel ($\rho = 7817 \text{ kg/m}^3$; $c = 460 \text{ J/kg-}^\circ\text{C}$; $k = 19 \text{ W/m-}^\circ\text{C}$) has thickness of 3 cm and is initially at a uniform temperature of $T_i = 500^\circ\text{C}$. The plate is suddenly exposed to same convection cooling environment on sides characterized by $T_\infty = 40^\circ\text{C}$ and $h = 150 \text{ W/m}^2\text{-}^\circ\text{C}$. Calculate the times for the center and face temperatures of the plate to reach 100°C .

Ans.: center: $t = 787.76 \text{ s}$; face: $t = 766.46 \text{ s}$ (Heisler Charts were used, please check these with one-term app.)

Problem 2: A slab of metal ($\rho = 8000 \text{ kg/m}^3$; $c = 1000 \text{ J/kg-}^\circ\text{C}$; $k = 25 \text{ W/m-}^\circ\text{C}$), in the shape of a rectangular parallelepiped and at a uniform temperature of $T_i = 520^\circ\text{C}$, has three of its surfaces very well insulated (essentially adiabatic), as shown in the figure. At time $t = 0 \text{ s}$ it is suddenly exposed to convective cooling: $T_\infty = 20^\circ\text{C}$ and $h = 1000 \text{ W/m}^2\text{-}^\circ\text{C}$.

- At $t = 200 \text{ s}$ into the cooling process, what are the maximum and minimum temperature inside the slab?
- If at this time, the cube is wrapped completely in excellent insulation (all surfaces essentially adiabatic) what would be its final equilibrium temperature?



Ans.: a) $T_{max} = 96.08^\circ\text{C}$, $T_{min} = 41.11^\circ\text{C}$; b) $T_{final} = 72.05^\circ\text{C}$