

Sell \$100

Price for <\$30

the company

injection
moulding

electronic

inj. moulding

metal chassis

metal sheet
metal forming

electronic

plastic

thermo forming

extrusion
3D printing

(injection
moulding)

machining

inj. m.

metal extrusion

injection moulding

the edges is

the rollers

the edges

Process Selection:

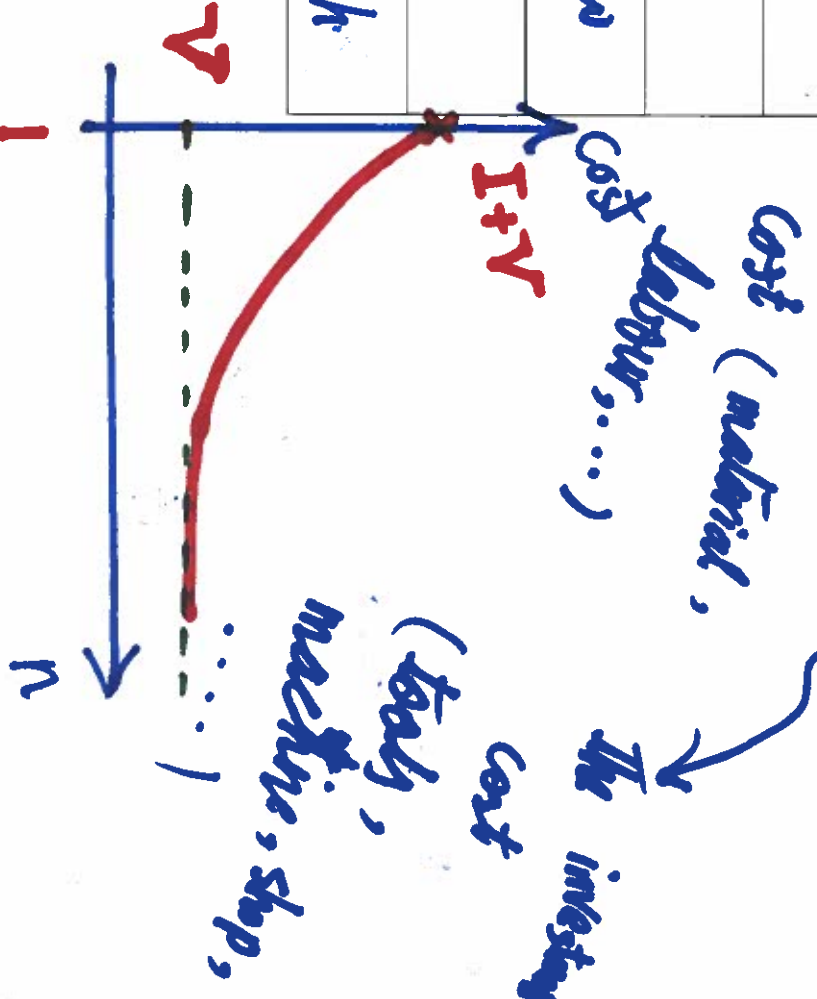
The 4 Main Attributes of each manufacturing process: Cost, Rate, Quality, and Flexibility

Process \ Attribute	Cost	Rate	Quality	Flexibility
Machining	high		high	mid
Sheet Metal Forming				
Thermoforming				
Injection molding		high		low
Casting			surface low	
3D Printing		low		high

How much? → How fast?

$C = V + I$

need to change the shape?



if we make n parts ⇒

$C = V + \frac{I}{n}$

Course Modules:

~~metal~~

1. Machining

→ { Turning
Milling

2. Sheet Metal Forming

→ { cutting
bending

~~plastic~~

3. Injection Molding

4. Thermoforming

5. Casting → { sand
die
investment

6. Additive Manufacturing (3D printing)

7. Quality and Monitoring

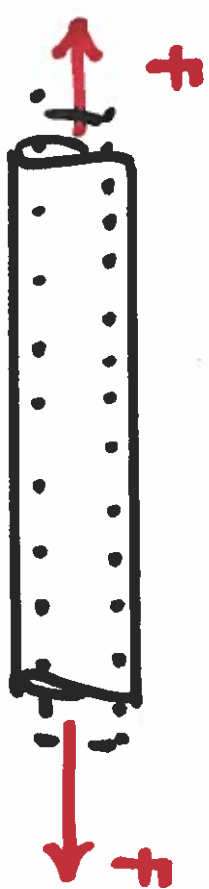
~~~~~ ✓

~~8. Forging~~

~~9. Automation~~

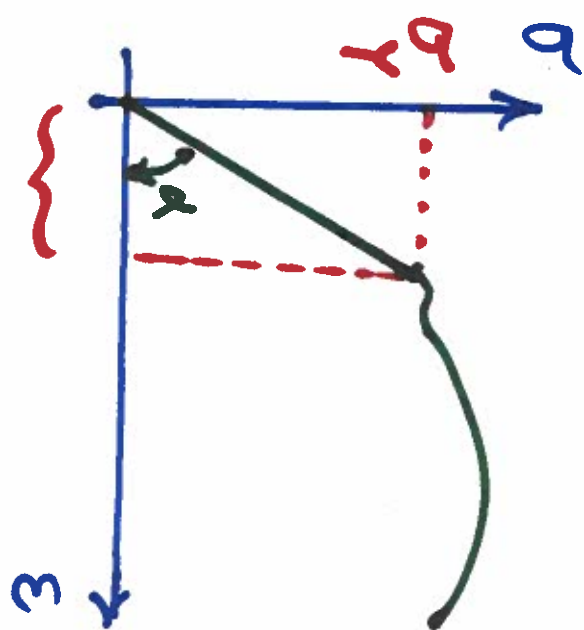
~~10.~~

# A Brief Review



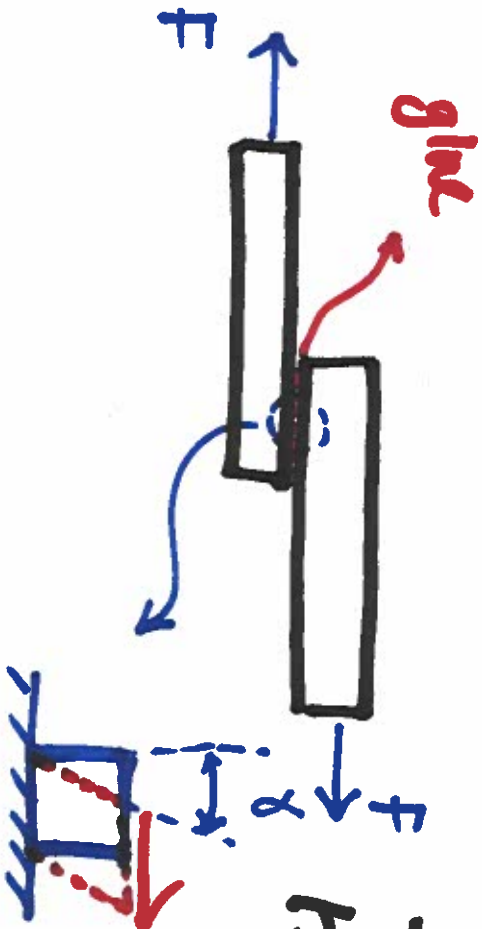
$$\sigma = \frac{F}{A}$$

$$\epsilon = \frac{\delta}{L}$$



$$\text{lateral strain} = -\nu \epsilon$$

Poisson ratio



Hooke's law

$$\left| \frac{\sigma}{\epsilon} = E \right|$$

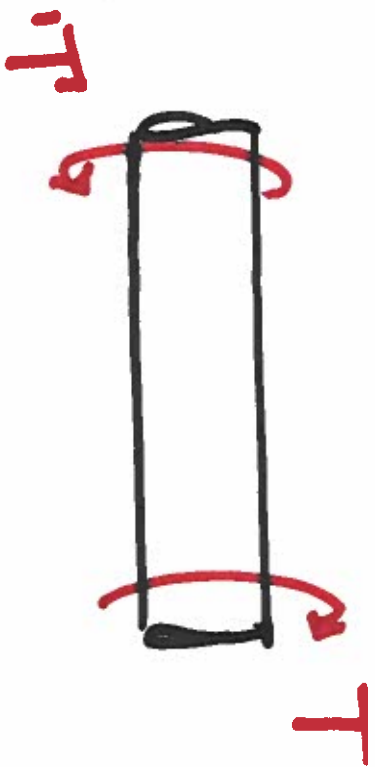
modulus of elasticity

$$\tau = \frac{F}{A}$$

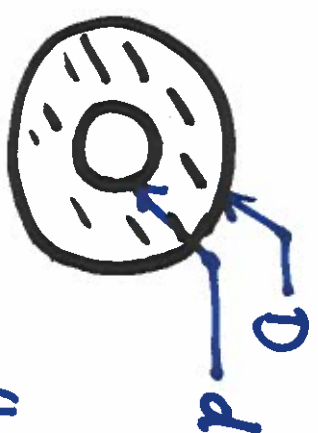
$$\left| G = \frac{E}{2(1+\nu)} \right|$$

$$\gamma = \phi$$

Shear angle  
Shear Modulus of elasticity



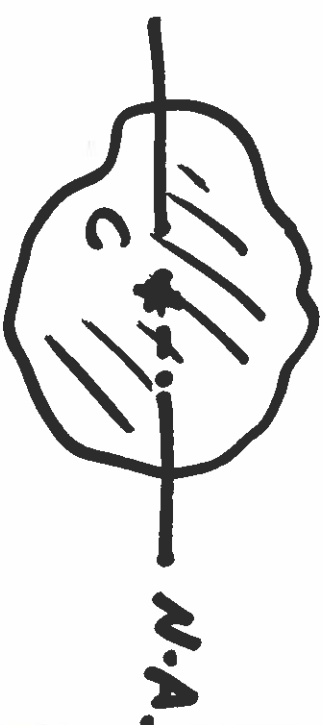
$$\gamma = \frac{TC}{J} \rightarrow \text{radians}$$



$$J = \frac{\pi}{32} (D^4 - d^4)$$

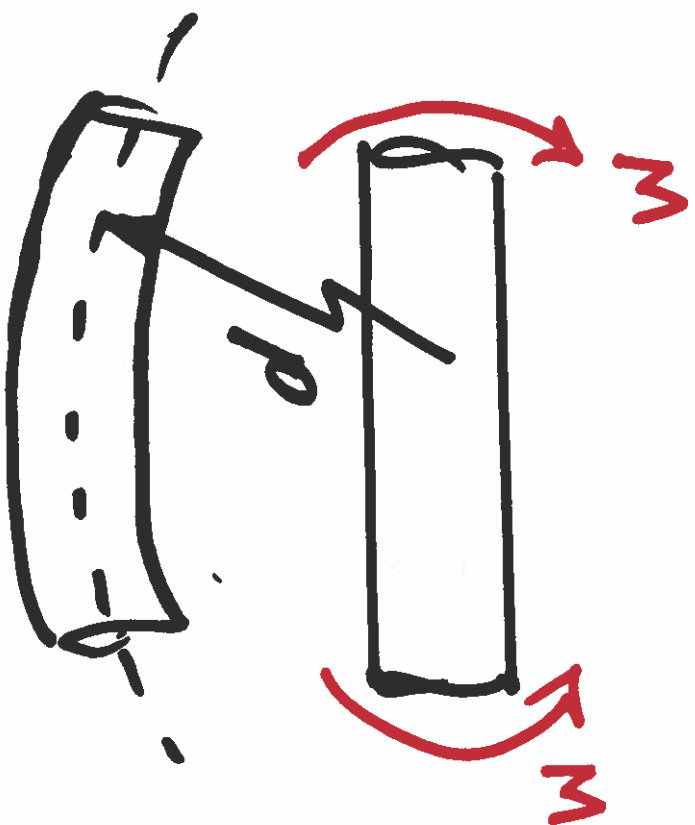
$$\phi = \frac{TL}{GJ}$$

$$\tau = \frac{Mc}{I}$$

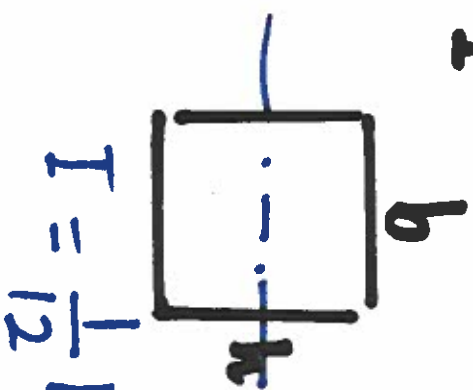


cross-section

I about N.A.



$$\frac{1}{\rho} = \frac{M}{EI}$$

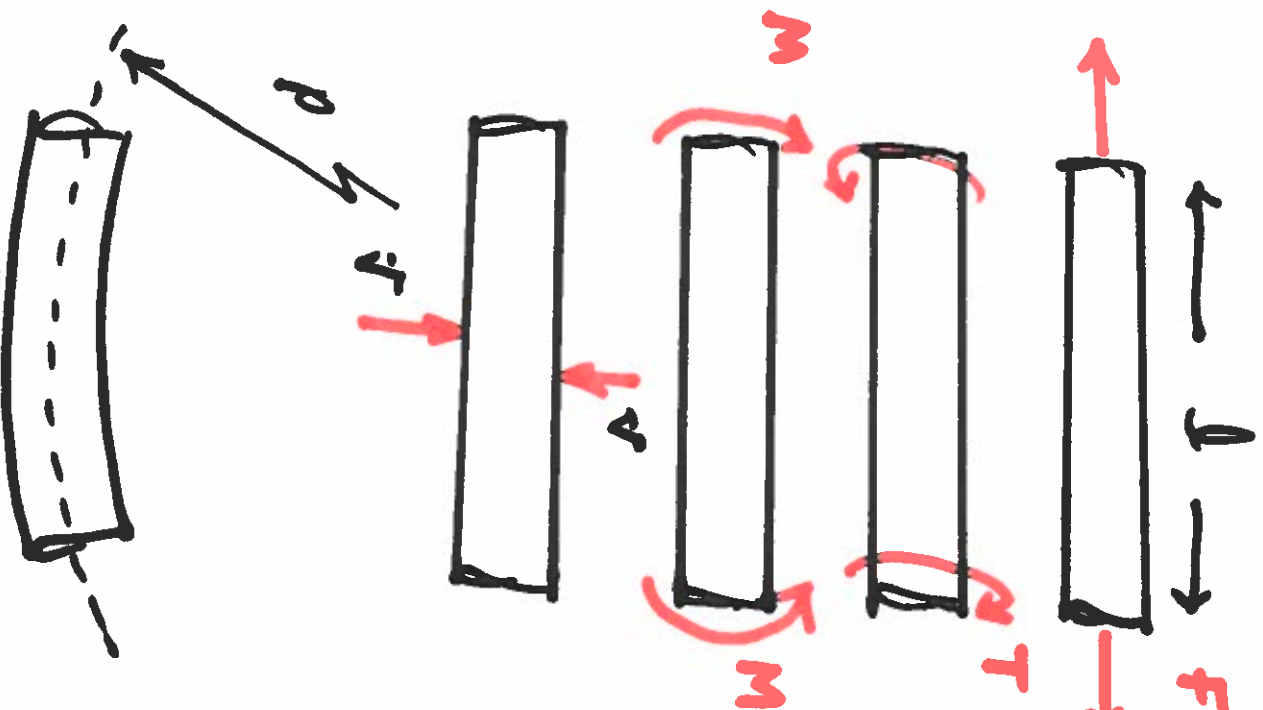


$$I = \frac{1}{12} bh^3$$

1 2 3



# A Brief Review



Stress

$$\sigma = \frac{F}{A}$$

$$\tau = \frac{TC}{J}$$

$$\sigma = \frac{MC}{I}$$

$$\tau = \frac{VQ}{It}$$

$$Q = A \cdot L$$

page  
(5.5)

Deformation

$$\delta = \frac{FL}{AE}$$

$$\tau = \frac{\pi}{32} (D^4 - d^4)$$

$$I = \frac{\pi}{64} D^4$$

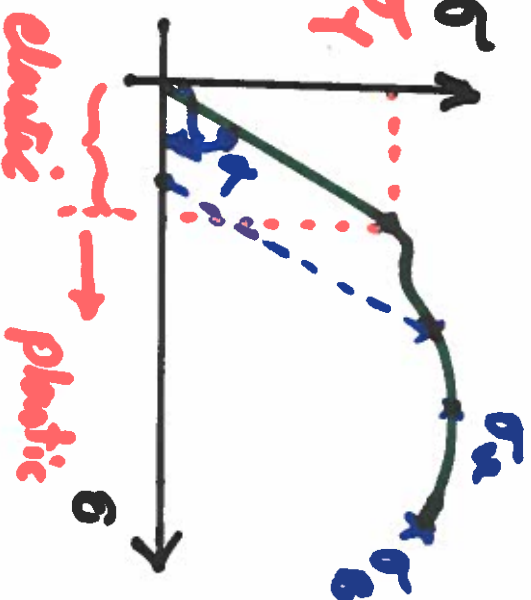
$$I = \frac{\pi}{64} D^4$$

$$\frac{1}{\rho} = \frac{M}{EI}$$

$$I = \frac{bh^3}{12}$$

$$f_{max} = \epsilon$$

$$\sigma = \epsilon E$$



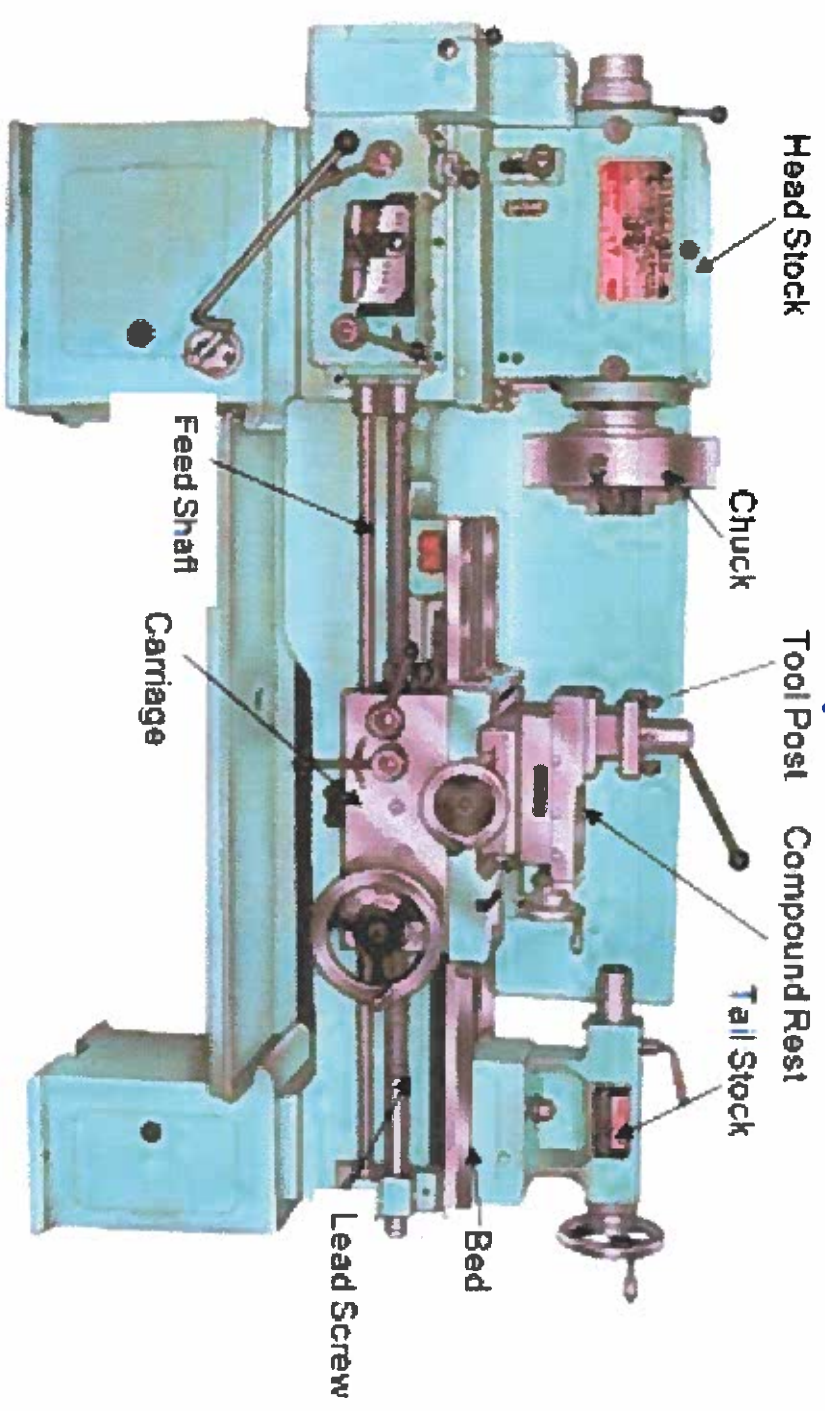
# Module 1. Machining

metals ✓  
wood

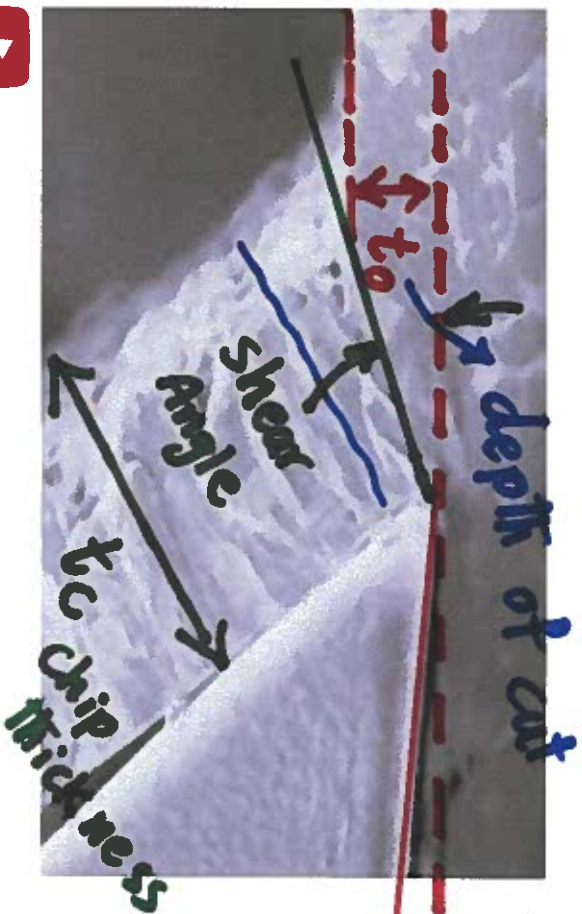
*workpiece is fixed*  
*tool rotates*  
milling, drilling, boring, turning, facing, tapping, threading, and cut-off.

*tool is fixed*  
*workpiece rotates*

Turning:



The mechanism of material removal:



Relief Angle

$$r = \frac{t_0}{t_c}$$

$$\tan \phi = \frac{r \cos \alpha}{1 - r \sin \alpha}$$

$$\phi = \frac{\pi}{4} + \frac{\alpha}{2} - \frac{\beta}{2}$$

$\tan^{-1}(\mu)$

Friction  
coef.

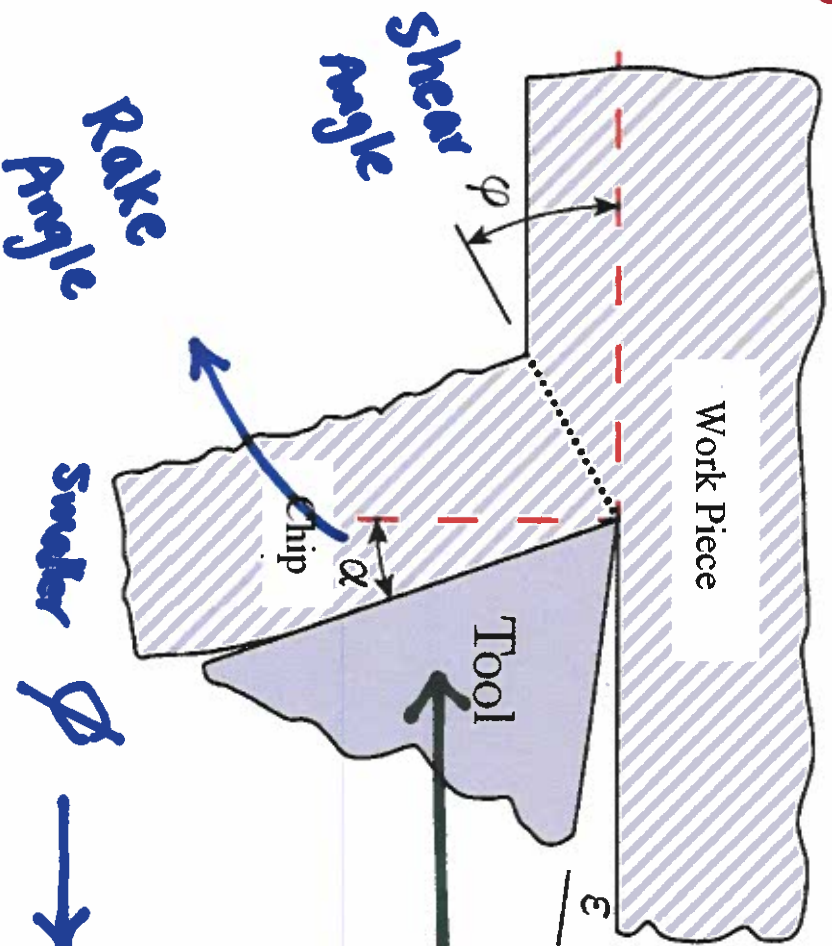
$$\tau = G \delta$$

Cut

Shear strain

$$\delta = \phi + \tan(\phi - \alpha)$$

shear



Shear  
Angle

Rake  
Angle

chip

Tool

Work Piece

$F_c$

Cutting  
Force

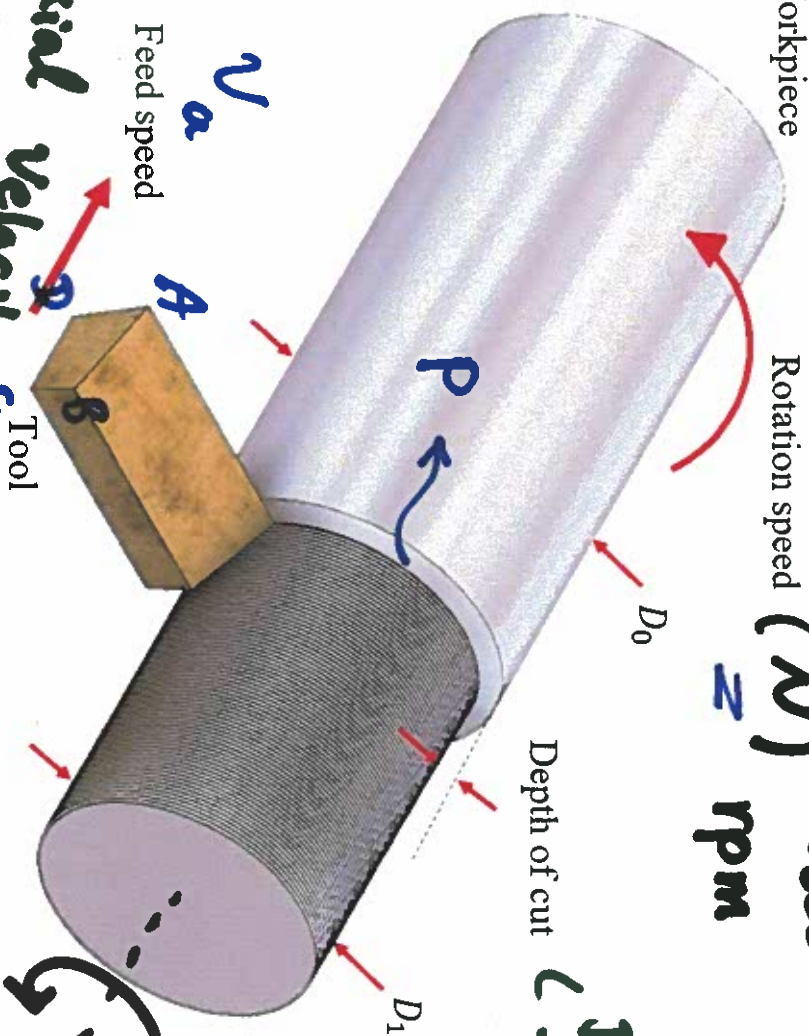


# Material Removal Rate (MRR):

Workpiece

Rotation speed ( $N$ )  $\frac{\text{rev}}{\text{sec}}$

$\approx \text{rpm}$



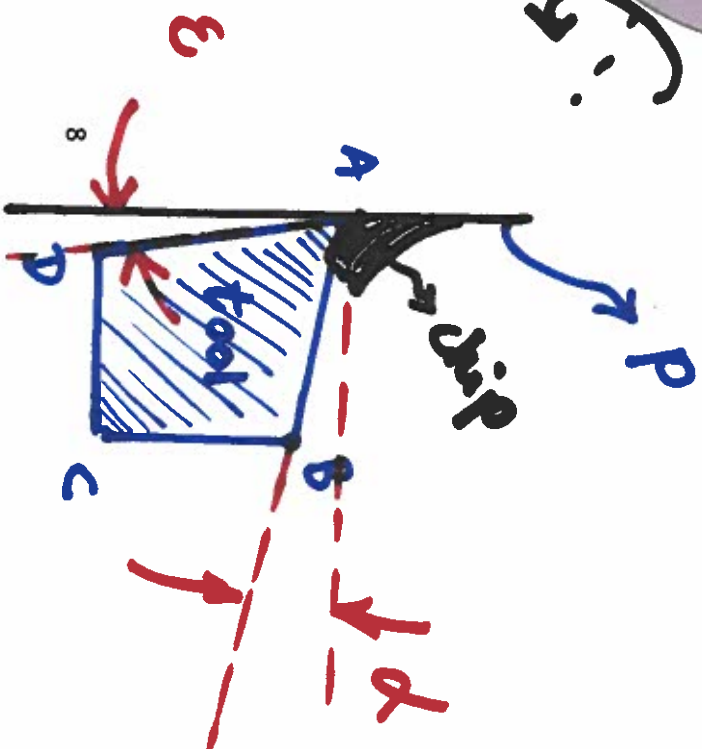
axial velocity of the tool  $c_{\text{Tool}}$

$\frac{\text{mm}}{\text{sec}}$ ,  $\frac{\text{mm}}{\text{rev}}$   $\times N$

$$\left( \frac{D_0 - D_1}{2} \right)$$



$$MRR = N \pi D_0 \times V_a \times \frac{D_0 - D_1}{2}$$



How much power we need to cut?

**Example 1)** On a lathe the operator is machining an Aluminum rod. The initial diameter of the rod is 2.0cm, and he set up the tool for a depth of cut 0.2cm. If the rotation speed is N= 500 RPM, and the tool axial velocity is 0.4 mm/min, what is the material removal rate?

$$\text{Feed} = 0.4 \frac{\text{mm}}{\text{rev}} \quad \text{rev.}$$

$$\begin{aligned} MRR &= \pi D N (\text{Feed}) (\text{depth of cut}) \\ &= \pi \times 20 \times \frac{500}{60} \times 0.4 \times 2 = 418 \frac{\text{mm}^3}{\text{Sec}} \end{aligned}$$

## Experimental Test:

Measuring the cutting forces during cutting:

- |                                | Cutting Force |
|--------------------------------|---------------|
| 1- Feed increase →             | increase ↑    |
| 2- Smaller Rake angle →        | increase ↑    |
| 3- Spindle rpm increase →      | no change —   |
| 4- Depth of cut increase →     | increase ↑    |
| 5- Smaller diameter of stock → | no change     |



Conclusion:

Feed speed affects the cutting force, but rotation speed does not. The cutting force depends on Rake angle and the depth of cut.

## Merchant's Relation:

Shearing Stress during machining and the chip formation:

$$\tau = G(\cot(\phi) + \tan(\phi - \alpha))$$

if  $\phi \downarrow \Rightarrow \tau \uparrow \rightarrow$  more required Power.

G: Shear Module of Elasticity

if  $\phi \downarrow \Rightarrow \left( \tan \phi = \frac{r \cos \alpha}{1 - r \sin \alpha} \right) \Rightarrow$  smaller  $r$   
(bigger  $t_c$ )

$\phi$  is called shear angle and can be calculated by Merchant's formula:

$$\phi = \frac{\pi}{4} - \frac{\beta}{2} + \frac{\alpha}{2}$$

$\beta$  friction angle

in general the bigger

the  $r = \frac{t_o}{t_c}$  means

better machining.



Merchant proved that smaller shear angle results in:

$\phi \downarrow \leftarrow$  (smaller  $\alpha$ )

1. Chip thickness increase  $t_c$
2. Energy dissipation via shear increase  $\leftarrow \tau \uparrow$
3. Heat generation and temperature increase

\* Heat & vibrations are the enemy of tools &

Machining

## Cutting Tools:

Steel 32 Rm

- HSS (High Speed Steel)
  - Carbide
- { 64 Rm  
77 Rm



increase ~~Feed~~ ~~Speed~~ <sup>I</sup>  $\Rightarrow$  Failure of the tool.  
(watch video; emailed link)

Observation from the demo (above video): with Carbide ~~he~~ he could cut at higher feed speed, but

Tools with different layers of coating: TiN, TiCN,  $Al_2O_3$



TiN  $\rightarrow$  less friction

eventually he had to stop because of

TiCN  $\rightarrow$  wear resistance

not enough Power.

$Al_2O_3$   $\rightarrow$  TBC  $\rightarrow$  Thermal Barrier Coating

$\rightarrow$  better Temperature stability

## Power Requirement:

Specific cutting energy (SCE) is the amount of energy required to cut a given volume of work material ( $W. Sec/mm^3$ ):

| Material         | SCE ( $W.s/mm^3$ ) |
|------------------|--------------------|
| Brass            | 0.7 ✓              |
| Aluminium alloy  | 0.8                |
| Stainless steels | 1.4                |
| Steel 1330       | 2.5                |
| Titanium         | 3 ✓                |

Required Power

$$P = MRR * SCE$$

$V = 2\pi \frac{D}{N} \downarrow$   $\frac{mm}{sec}$



cutting force

$$\pi D N$$

$P = (F_c) (\text{cutting speed})$

→ estimate  $F_c$

Example 2) Calculate the required power in Example 1? Aluminum specific cutting energy:

$$SCE = 0.82 \left( \frac{W \cdot s}{mm^3} \right) \rightarrow \frac{J \cdot s}{mm^3} = \frac{J}{mm^3} = \frac{N \cdot m}{mm^3}$$

$MRR = 418 \text{ mm/sec}$

$$P = (MRR)(SCE) = (418)(0.82) = \dots \text{ W}$$

Required time for removing volume material V:

$$MRR = \frac{\text{Volume}}{\text{time}} \rightarrow \text{time} = \checkmark$$

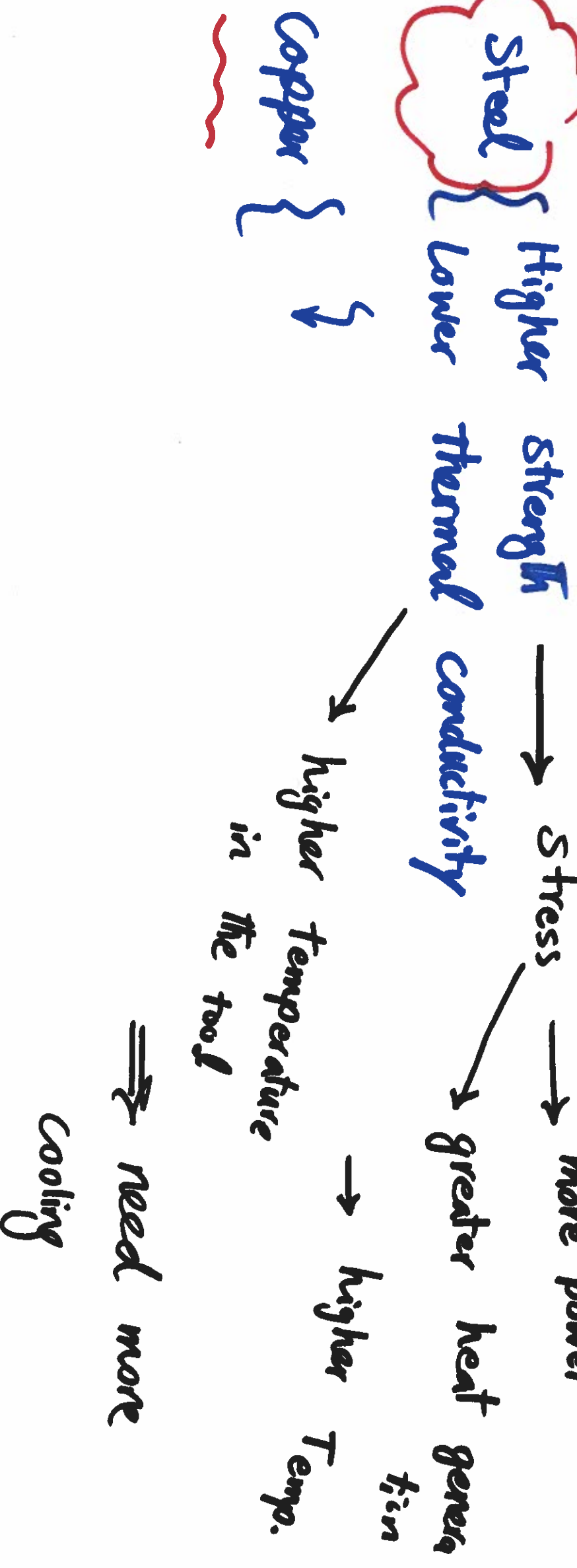
Example 3) What is the minimum time it would take to machine  $250 \text{ mm}^3$  of aluminum if your machine could provide  $0.4 \text{ kW}$  of power?

$$P = (MRR)(SCE) \rightarrow 400 = (MRR)(0.82) \rightarrow MRR = \dots$$

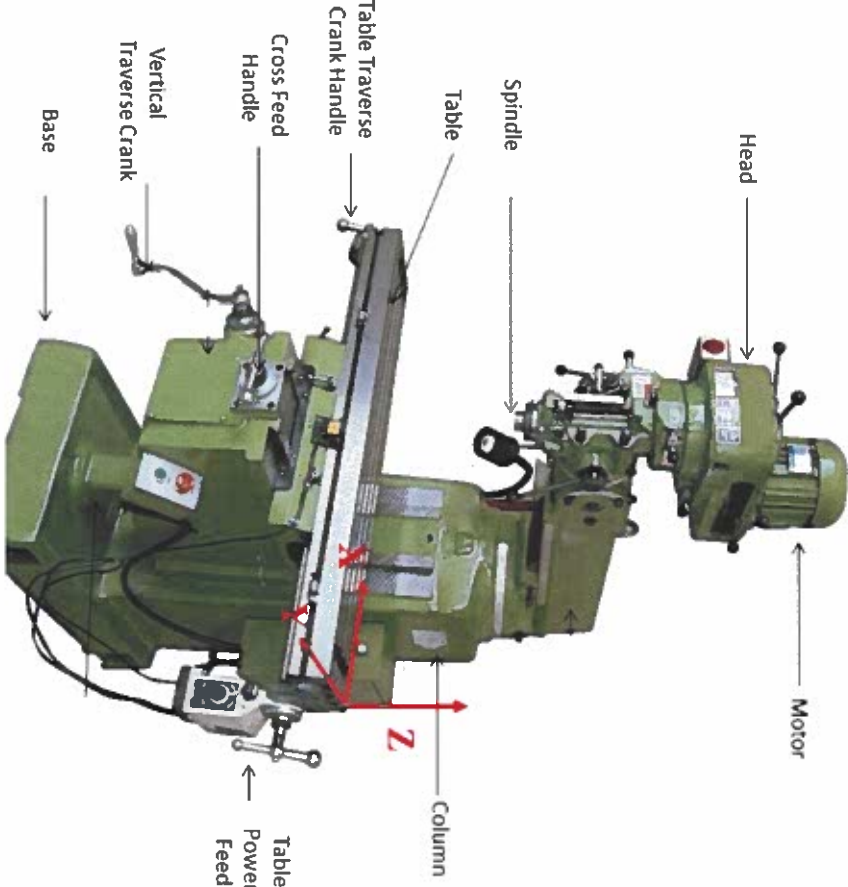
$$\text{time} = \frac{250}{MRR} = \dots$$



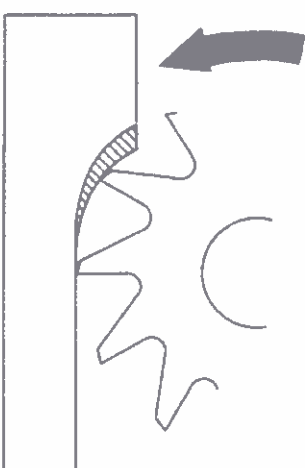
**Example 4)** Consider differences in machining two metals, an alloy of Steel (with module of elasticity 200GPa, and thermal conductivity of 50 W/m.K) and an alloy of Copper (with module of elasticity 115GPa, and thermal conductivity of 400 W/m.K). Compare machining of these two materials?



# Milling:

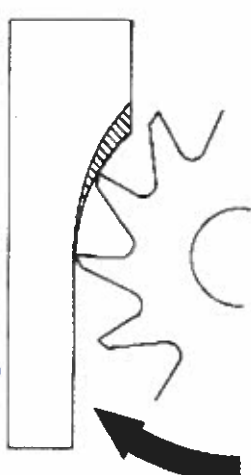


## Two modes of milling: *rotation*



**Climb cutting**  
(Direction of cutter rotation  
same as feed direction)

**Feed**



**Counter cutting**  
(Direction of cutter rotation  
oppose to feed direction)

**Feed**

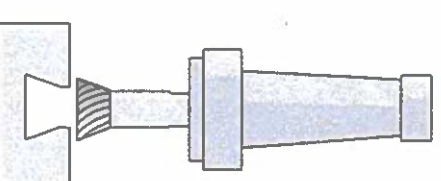
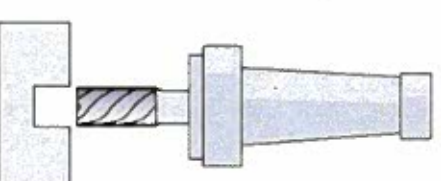
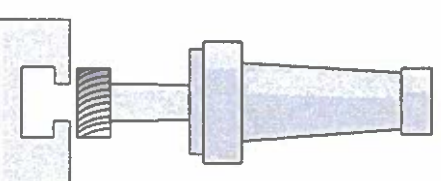
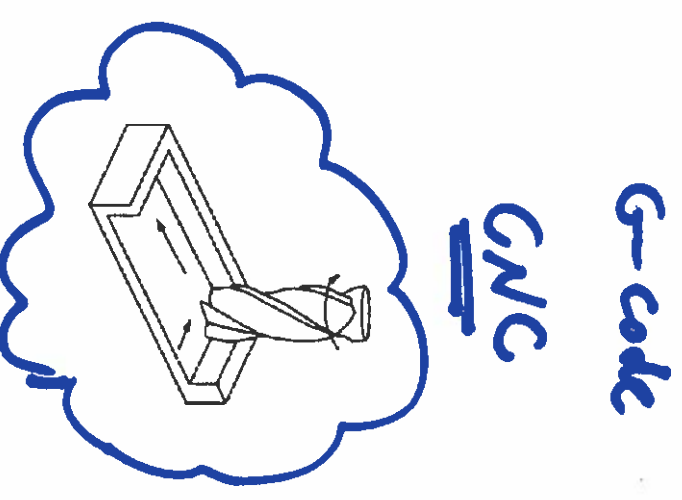
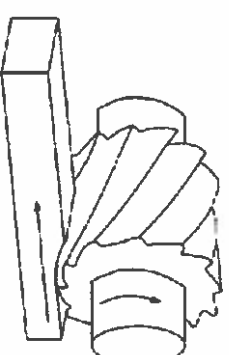
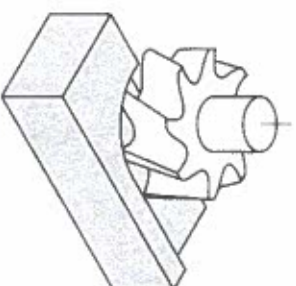
**- Safer**

**- higher force**

**to clamp**

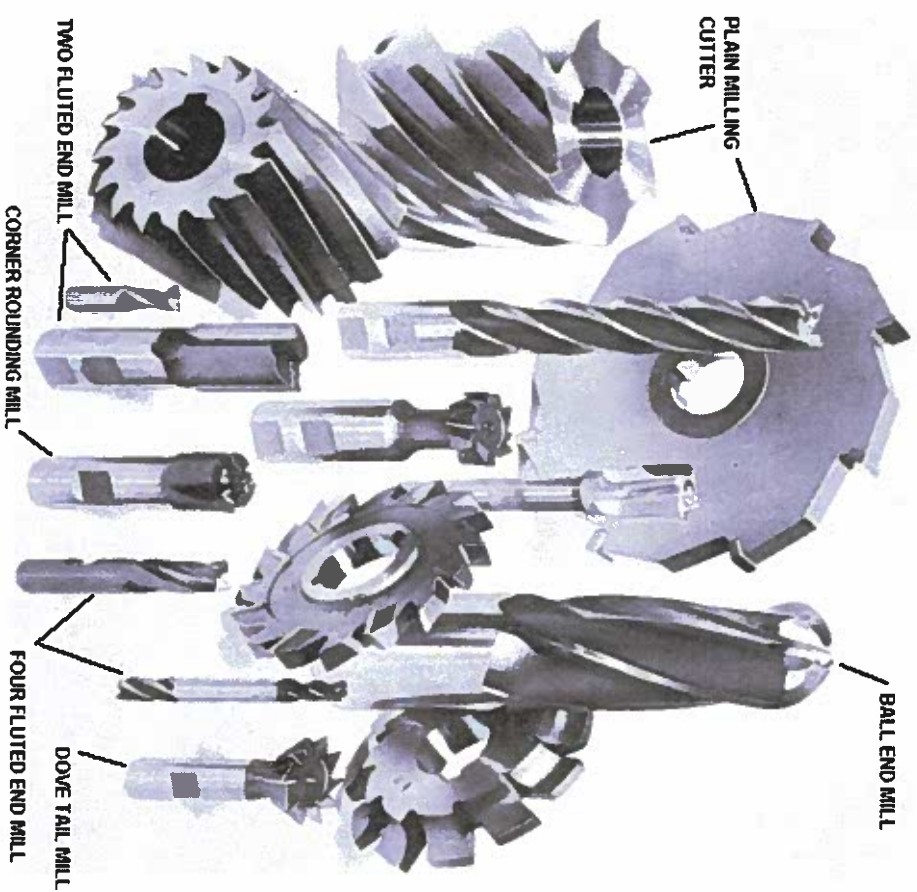
## Types of milling operations:

- Face milling
- Shoulder/side (end milling)
- Contour milling (complex surface curvature)
- Cutting slots and grooves
- Holes and taps



## Types of tools:

- Face mill
- End mill
- Peripheral/Side mill
- T-slot, Slot, Dovetail-slot mill





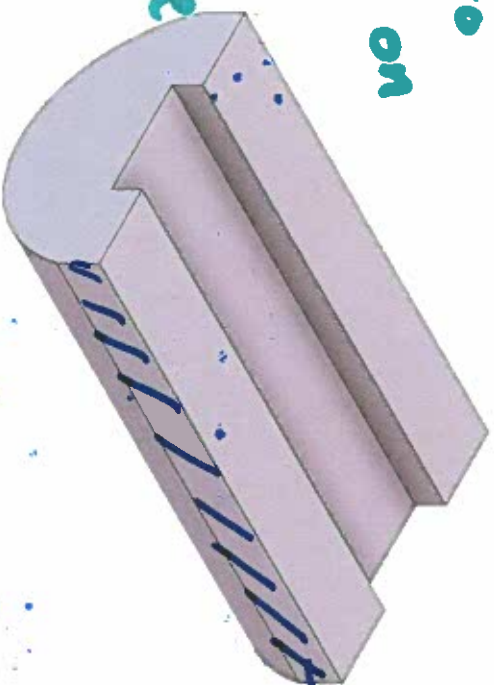
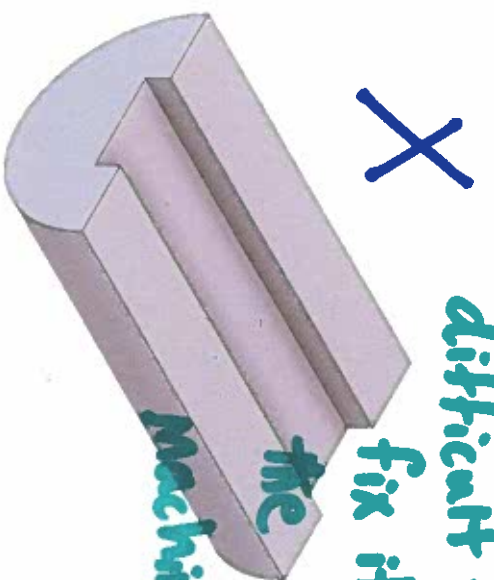
**Example 5)** In milling, what is the feed per tooth (in millimeters),  $f$ , if the tool velocity,  $v$  = 25 mm/s, the rotational speed,  $N$  = 1000 RPM, and the number of teeth,  $n$  = 4?

$$\text{Feed} = \frac{V}{N} = \frac{25}{\left(\frac{1000}{60}\right)} = 1.5 \text{ mm/rev.}$$

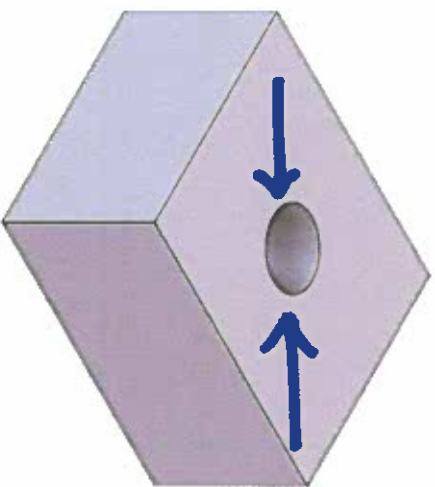
$$\text{Feed per tooth} = \frac{\text{Feed}}{n} = \frac{1.5}{4} = 0.375 \text{ mm/rev.}$$

## Design for Machining:

~~X~~ difficult to fix it on the machine



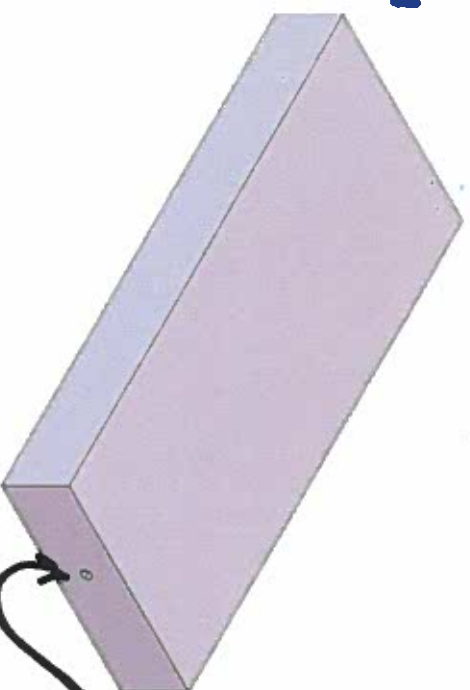
Flat surface  
(for clamping & fixing it on the machine)



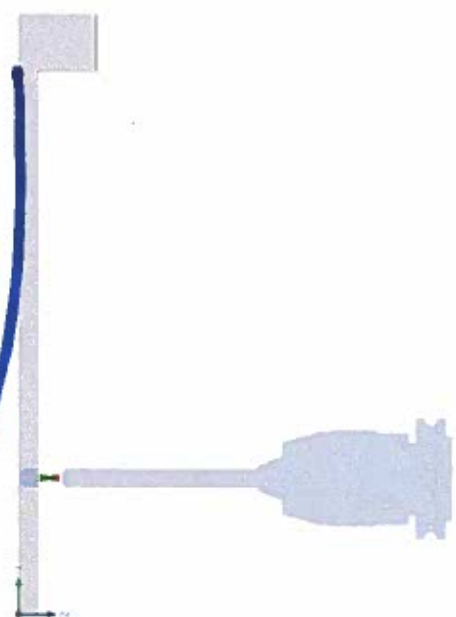
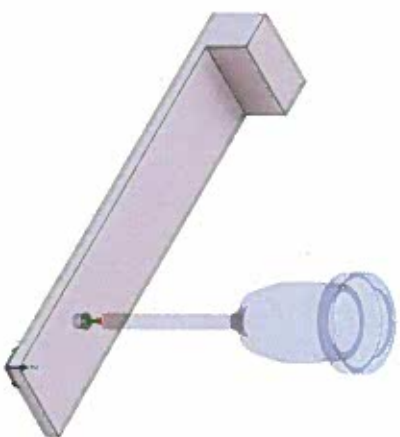
~~10.627~~ mm

10.625

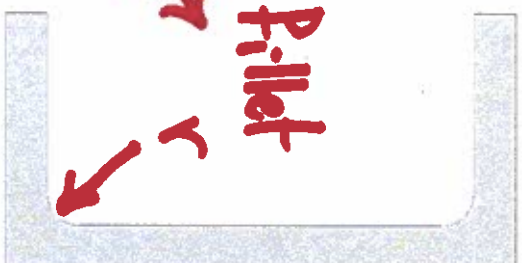
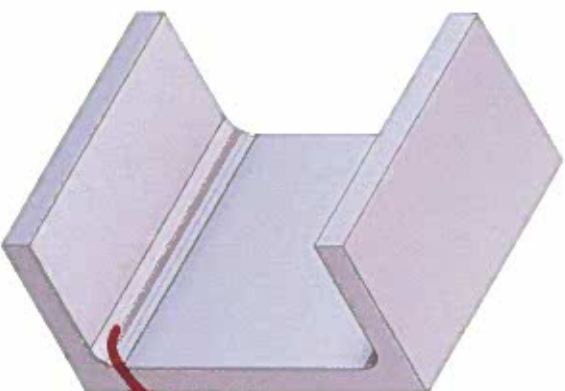
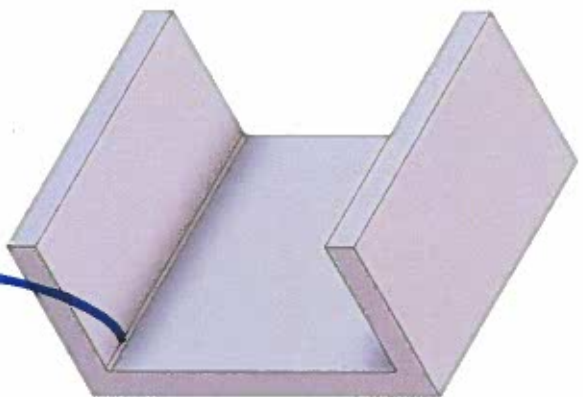
Standard size



avoid long, thin hole



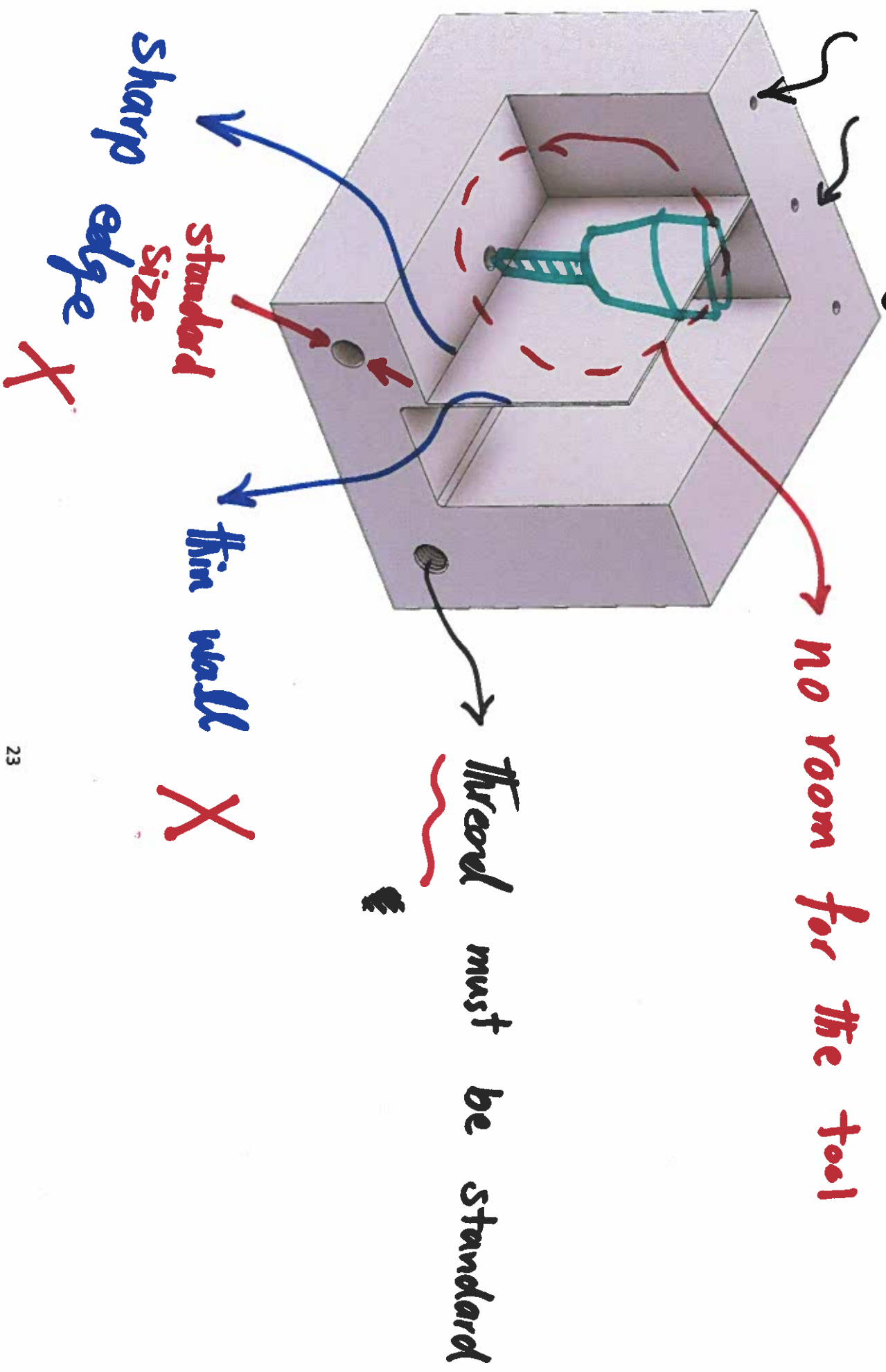
overhanged long  
workpiece  
⇒ results in large deflection



avoid sharp corner

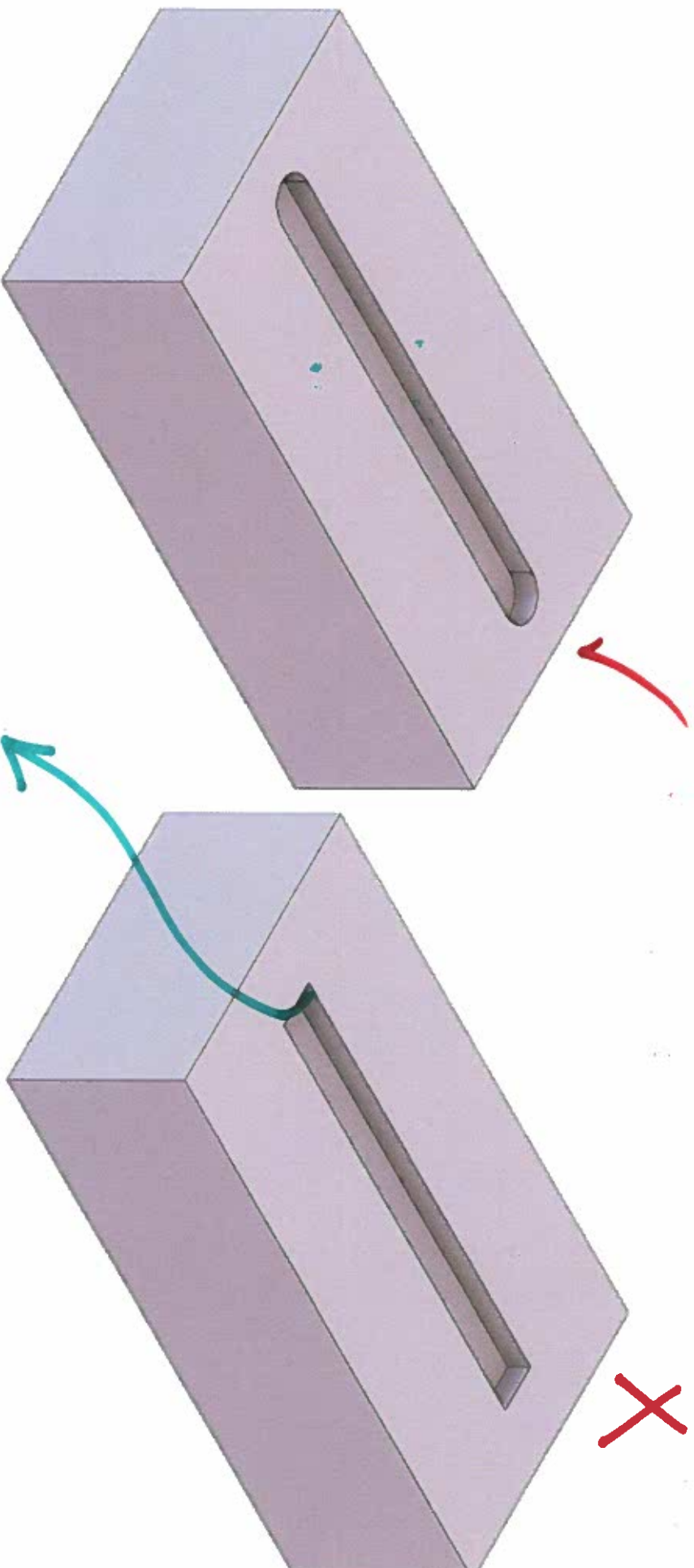
X

Example 6) What is wrong with machining this part?  
narrow & long hole





**Example 7)** You want to mill a pocket that is wide and narrow. Which of the following shapes should you pick from a Design for Machining perspective?



*difficult (impossible) to machine.*

**Example 8)** We need to make a thermoform mold that needs 0.05 inch-diameter holes to draw vacuum. Which of the following designs is optimized for manufacturability?

