

## Assignment#1 Solution

### Q1)

$$\text{Cutting Speed: } V_c = 165 \frac{\text{mm}}{\text{s}}$$

$$\text{Feed Speed: } \text{Feed} = 0.25 \frac{\text{mm}}{\text{rev}}$$

$$\text{Depth of cut: } d = 5 \text{ mm}$$

$$\text{Efficiency: } e = 0.85$$

$$\text{Specific Cutting Energy: } SCE = 1.6 \frac{\text{J}}{\text{mm}^3}$$

$$MRR = V_c \cdot \text{Feed} \cdot d = 206.25 \frac{\text{mm}^3}{\text{s}}$$

$$P = \frac{MRR \cdot SCE}{e} = 388.24 \text{ W}$$

### Q2)

$$\alpha = 10^\circ \quad \text{rake angle}$$

$$t_0 = 0.5 \text{ mm} \quad \text{chip thickness before the cut (depth of cut)}$$

$$t_c = 1.25 \text{ mm} \quad \text{chip thickness}$$

$$SCE = 0.7 \frac{\text{J}}{\text{mm}^3}$$

$$V_c = 120 \frac{\text{m}}{\text{min}}$$

$$F_c = 1550 \text{ N}$$

$$r = \frac{t_0}{t_c} = 0.4$$

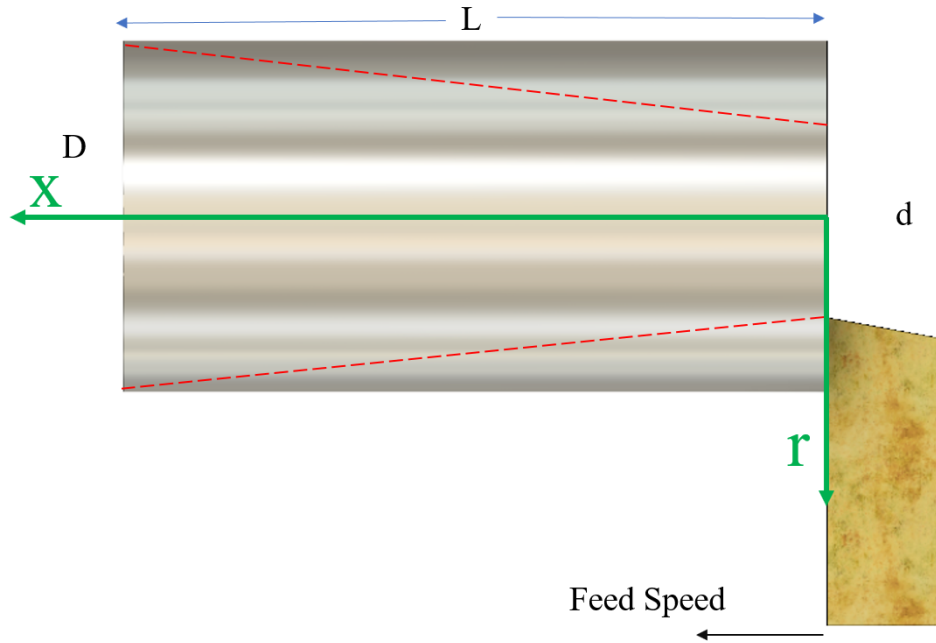
$$\text{Shear angle } \phi = \tan^{-1} \left( \frac{r \cos(\alpha)}{1 - r \sin(\alpha)} \right) = 22.94^\circ$$

$$\phi = \frac{\pi}{4} - \frac{\beta}{2} + \frac{\alpha}{2}, \quad 22.94 = 45 - \frac{\beta}{2} + 5, \quad \beta = 54.12^\circ$$

$$\mu = \tan \beta = 1.382$$

$$P = F_c \cdot V_c = 1550 \times \frac{120}{60} = 3100 \text{ W}$$

**Q3)**



$$MRR = V_c \cdot (Feed) \cdot (depth\ of\ cut)$$

$$r = \frac{D-d}{2L}x + \frac{d}{2} \quad (\text{the red dash-line})$$

$$Feed = \frac{V_a}{N}, \quad V_a \text{ is the axial tool speed (dis/sec)}$$

$$V_c = 2\pi \cdot r \cdot N$$

$$depth\ of\ cut = \frac{D}{2} - r$$

$$MRR = 2\pi \cdot r \cdot N \cdot \frac{V_a}{N} \cdot \left( \frac{D}{2} - r \right) = 2\pi V_a \left( \frac{D-d}{2L}x + \frac{d}{2} \right) \left( \frac{D}{2} - \frac{D-d}{2L}x - \frac{d}{2} \right) = 2\pi V_a \left( \frac{D-d}{2L}x + \frac{d}{2} \right) \left( \frac{D-d}{2} - \frac{D-d}{2L}x \right)$$

$$P = SCE \cdot MRR$$

$$\text{At } x=0, \quad P = SCE \cdot MRR = SCE \cdot 2\pi \frac{d}{2} \cdot V_a \cdot \left( \frac{D-d}{2} \right)$$

$$\text{At } x=L, \quad P = 0$$