

hw1\_1.py

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import matplotlib.pyplot as plt
import numpy as np
import sympy as sp

C = np.array([
    [ 158.    ,  5.64 ,  5.64 ,  0.    ,  0.    ,  0.    ],
    [   5.64 , 15.51 ,  7.21 ,  0.    ,  0.    ,  0.    ],
    [   5.64 ,  7.21 , 15.51 ,  0.    ,  0.    ,  0.    ],
    [   0.    ,  0.    ,  0.    ,  3.2   ,  0.    ,  0.    ],
    [   0.    ,  0.    ,  0.    ,  0.    ,  4.4   ,  0.    ],
    [   0.    ,  0.    ,  0.    ,  0.    ,  0.    ,  4.4 ]], np.float64) * 10**9

def Transform(theta):
    m = np.cos( np.deg2rad(theta) )
    n = np.sin( np.deg2rad(theta) )
    return np.array([
        [m**2, n**2, 2*m*n],
        [n**2, m**2, -2*m*n],
        [-m*n, m*n, m**2 - n**2]], np.float64)

S = np.linalg.inv(C)

s = np.zeros((3,3), np.float64)
s[:2,:2] = S[:2, :2]
s[-1, -1] = S[-1, -1]

theta = np.linspace(-90, 90, 100)

T = Transform(theta)
T_ = np.rollaxis(T, 2)

S_bar = np.einsum('...jk,kl,...lm->...jm', T.T, s, T_) #[S_bar] = [T.T][S][T]

Q_bar = np.linalg.inv(S_bar)

eps_xyz = np.array([[0,0,1]]).T

sigma_xyz = np.dot(Q_bar, eps_xyz).reshape(100, -1)

Q_bar /= 10**9

fig, ax = plt.subplots()

plt.plot(theta, Q_bar[:,0,2], 'k-', label=r'$\bar{Q}_{16}$')
plt.plot(theta, Q_bar[:,1,2], 'k--', label=r'$\bar{Q}_{26}$')
plt.plot(theta, Q_bar[:,2,2], 'k:', label=r'$\bar{Q}_{66}$')

plt.title(r'Stiffness factors relevant to $\gamma_{xy}$')
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plt.xlabel(r'$\theta^\circ$', fontsize=15)
plt.ylabel(r'$GPa$', fontsize=15)

legend = ax.legend(loc='upper right', shadow=True)
plt.xticks(np.linspace(-90, 90, 13))

plt.show()
```