

Discrete Structures

Assignment 02

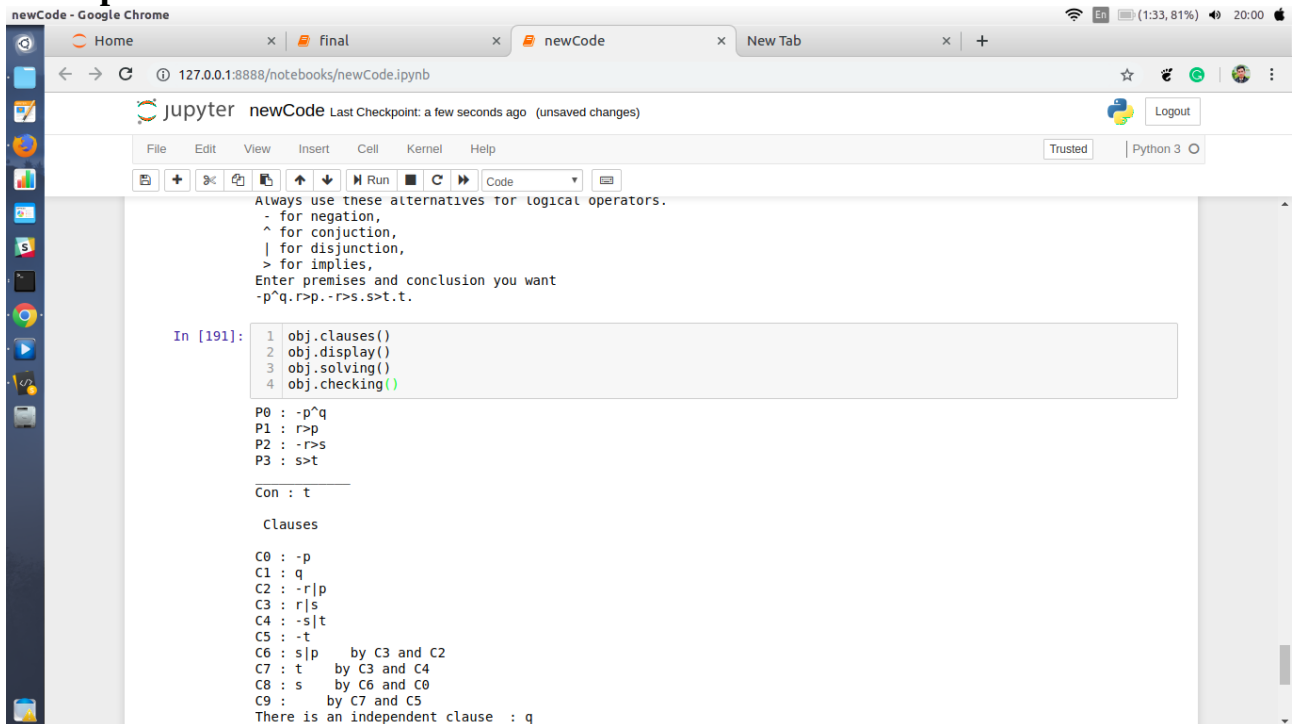
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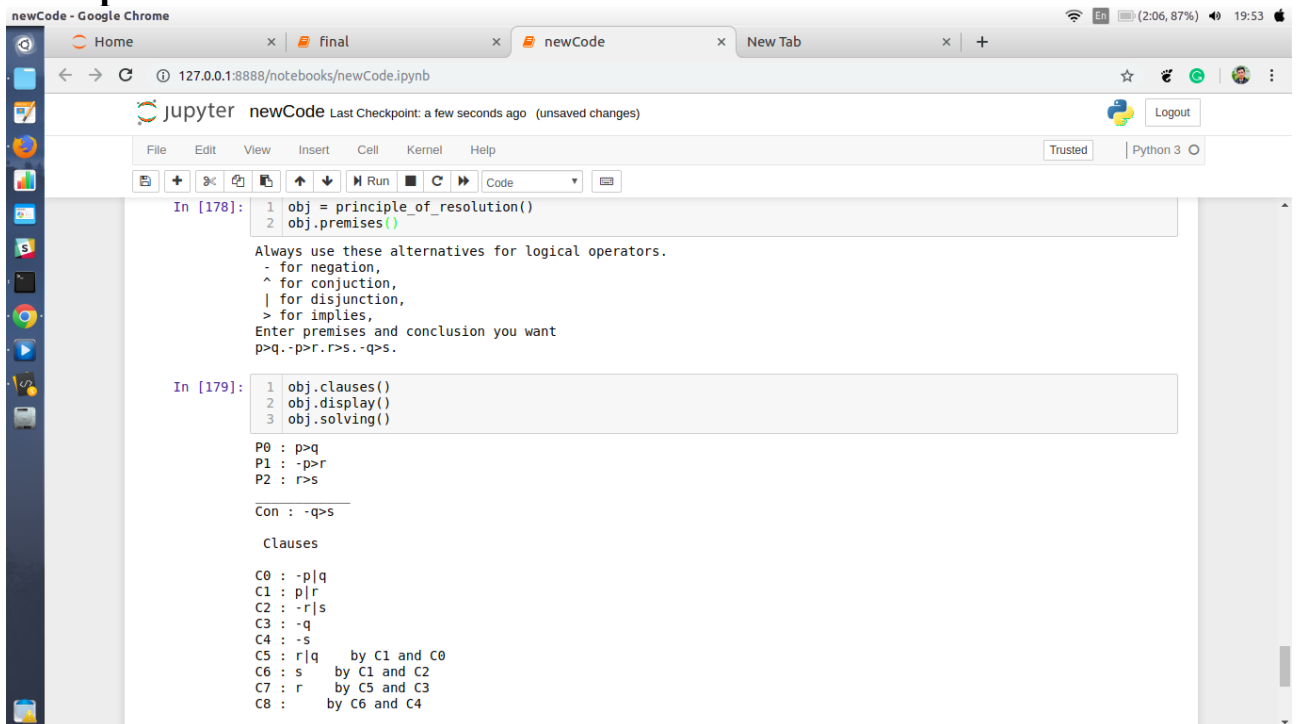
Example 6:



The screenshot shows a Jupyter Notebook interface in Google Chrome. The browser tabs include 'Home', 'final', 'newCode', and 'New Tab'. The address bar shows '127.0.0.1:8888/notebooks/newCode.ipynb'. The notebook title is 'newCode' with a status 'Last Checkpoint: a few seconds ago (unsaved changes)'. The interface includes a menu bar (File, Edit, View, Insert, Cell, Kernel, Help) and a toolbar with icons for file operations, cell navigation, and execution. The code cell contains the following text:

```
Always use these alternatives for logical operators.  
- for negation,  
^ for conjunction,  
| for disjunction,  
> for implies,  
Enter premises and conclusion you want  
-p^q.r>p.-r>s.s>t.t.  
  
In [191]:  
1 obj.clauses()  
2 obj.display()  
3 obj.solving()  
4 obj.checking()  
  
P0 : -p^q  
P1 : r>p  
P2 : -r>s  
P3 : s>t  
  
Con : t  
  
Clauses  
  
C0 : -p  
C1 : q  
C2 : -r|p  
C3 : r|s  
C4 : -s|t  
C5 : -t  
C6 : s|p by C3 and C2  
C7 : t by C3 and C4  
C8 : s by C6 and C0  
C9 : by C7 and C5  
There is an independent clause : q
```

Example 07:



The screenshot shows a Jupyter Notebook interface in Google Chrome. The browser tabs include 'Home', 'final', 'newCode', and 'New Tab'. The address bar shows '127.0.0.1:8888/notebooks/newCode.ipynb'. The notebook title is 'newCode' with a status 'Last Checkpoint: a few seconds ago (unsaved changes)'. The interface includes a menu bar (File, Edit, View, Insert, Cell, Kernel, Help) and a toolbar with icons for file operations, cell navigation, and execution. The code cell contains the following text:

```
In [178]:  
1 obj = principle_of_resolution()  
2 obj.premises()  
  
Always use these alternatives for logical operators.  
- for negation,  
^ for conjunction,  
| for disjunction,  
> for implies,  
Enter premises and conclusion you want  
p>q.-p>r.r>s.-q>s.  
  
In [179]:  
1 obj.clauses()  
2 obj.display()  
3 obj.solving()  
  
P0 : p>q  
P1 : -p>r  
P2 : r>s  
  
Con : -q>s  
  
Clauses  
  
C0 : -p|q  
C1 : p|r  
C2 : -r|s  
C3 : -q  
C4 : -s  
C5 : r|q by C1 and C0  
C6 : s by C1 and C2  
C7 : r by C5 and C3  
C8 : by C6 and C4
```

Example 09:

```
Always use these alternatives for logical operators.
- for negation,
^ for conjunction,
| for disjunction,
> for implies,
Enter premises and conclusion you want
L>A.E>-I.A>E.L>-I.

In [193]: 1 obj.clauses()
          2 obj.display()
          3 obj.solving()
          4 obj.checking()

P0 : L>A
P1 : E>-I
P2 : A>E

Con : L>-I

Clauses

C0 : -L|A
C1 : -E|-I
C2 : -A|E
C3 : L
C4 : I
C5 : A by C3 and C0
C6 : -E by C4 and C1
C7 : E by C5 and C2
C8 : by C7 and C6
```

Code:

class principle_of_resolution:

def __init__(self):

self.premiseList = []

self.clauseList = []

self.independentClause = []

self.preConclusion = "

self.conclusion = "

def __str__(self):

return str("Premises : "+str(self.premiseList)+ '\n'+ "Clauses : "+str(self.clauseList) +'\n'+ "conclusion : "+str(self.conclusion))

def display(self):

for i in range(len(self.premiseList)):

print("P"+str(i)+" : "+self.premiseList[i])

```
print("_____")
```

```
print("Con : "+self.preConclusion)
```

```
print("\n Clauses\n")
```

```
for i in range(len(self.clauseList)):
```

```
    print("C"+str(i)+" : "+self.clauseList[i])
```

```
#function to take input from user and convert it to premise and conclusion
```

```
def premises(self):
```

```
    print("Always use these alternatives for logical operators.\n - for negation, \n ^ for conjunction,\n | for  
disjunction, \n > for implies, ")
```

```
    print("Enter premises and conclusion you want ")
```

```
    n = input()[:-1]                #taking input
```

```
    self.premiseList = n.split('.')    #getting premises into list form
```

```
    self.preConclusion = self.premiseList[-1] #taking out conclusion from premises
```

```
    self.conclusion = "-" + self.preConclusion + ")"
```

```
    del self.premiseList[-1]          #delete the conclusion
```

```
#function that resolve the premises into clauses
```

```
def clauses(self):
```

```
    for i in self.premiseList:
```

```
        if ">" in i:
```

```
            prem = self.implies(i)
```

```
            self.clauseList.append(prem)
```

```
        elif "^" in i:
```

```
            self.conjunction(i)
```

```
        else:
```

```
            self.clauseList.append(prem)
```

```
    self.conclusion = self.negation(self.conclusion)
```

```
    if len(self.premiseList) != 0:
```

```
        if ">" in self.conclusion:
```

```
            prem = self.implies(self.conclusion)
```

```
            self.clauseList.append(prem)
```

```
        elif "^" in self.conclusion:
```

```

        self.conjunction(self.conclusion)
    else:
        self.clauseList.append(self.conclusion)
    else:
        return "you have no conclusion"

```

#function that applies the conjunction method

```

def conjunction(self, prem):
    self.clauseList += prem.split('^')

```

#function that applies the implication method

```

def implies(self, prem):
    if prem[0] == "-":
        prem = prem.replace('-', "", 1)
        prem = prem.replace('>', "|")
        return prem
    prem = '-' + prem.replace('>', "|")
    return prem

```

#function that take premise as input and find negation of this premise and output will be produced

```

def negation(self, prem):
    prem = prem.replace('-', "", 1)
    if '>' in prem:

```

#applying $p \rightarrow q = \neg p \vee q$

```

    if prem[prem.index('(')+1] == '-':
        prem = prem.replace('-', "", 1)
    elif prem[prem.index('(')+1] != '-':
        prem = self.insert_char(prem, prem.index('(')+1)
    prem = prem.replace('(', "")
    prem = prem.replace(')', "")
    prem = prem.replace('>', "|")

```

```

#applying demorgan Law in case of implies
if prem[0] == '-':
    prem = prem.replace('-', ",1)
elif prem[0] != '-':
    prem = self.insert_char(prem,0)
    prem = prem.replace('|','^')
if prem[prem.index('^')+1] == '-':
    prem = self.del_char(prem, prem.index("^")+1 )
elif prem[prem.index('^')+1] != '-':
    prem = self.insert_char(prem,prem.index('^')+1)
return prem

```

elif '^' in prem:

```

#applying demorgan Law in case of conjunction
if prem[(prem.index('(')+1)] == '-':
    prem = prem.replace('-', ",1)
elif prem[prem.index('(')+1] != '-':
    prem = self.insert_char(prem,prem.index('(')+1)
    prem = prem.replace('(','"')
    prem = prem.replace(')','"')
    prem = prem.replace('^','|')
if prem[(prem.index('|')+1)] == '-':
    prem = self.del_char(prem, prem.index("|")+1 )
elif prem[prem.index('|')+1] != '-':
    prem = self.insert_char(prem,prem.index('|')+1)
return prem

```

elif '|' in prem:

```

#applying demorgan Law in case of disjunction
if prem[prem.index('(')+1] == '-':
    prem =prem.replace('-', ", 1)
elif prem[prem.index('(')+1] != '-':

```

```

        prem = self.insert_char(prem,premier.index('(')+1)
    premier =premier.replace('(', '')
    premier =premier.replace(')', '')
    premier =premier.replace('|', '^')
    if premier[(premier.index('^')+1)] == '-':
        premier = self.del_char(premier, premier.index("^")+1 )
    elif premier[(premier.index('^')+1)] != '-':
        premier = self.insert_char(premier,premier.index('^')+1)

    return premier
else:
    premier = "-" + premier

    if "(" in premier:
        premier =premier.replace('(', '')
        premier =premier.replace(')', '')

    return premier

```

#function to insert a character in a string you have to give index and string in argument and character as well if you want by default function inserts hash('-')

```

def insert_char(self,string, index, char = '-'):
    return string[:index] + char + string[index:]

```

#function to delete a character from a string you have to give index and string as input in the function parameters it will return

```

def del_char(self,string, index):
    return string[:index] + string[index+1:]

```

```

def solving(self):
    counterClause = len(self.clauseList)
    for i in range(counterClause+3):
        lst = self.clauseList[i].split('|')
        for l in lst:
            if len(l) == 1:
                for j in range(len(self.clauseList)):

```

```

if i == j:
    continue
elif l in self.clauseList[j]:
    for k in range(len(self.clauseList[j])):
        if self.clauseList[j][k] == l:
            if k-1 >= 0 and self.clauseList[j][k-1] == '-':
                self.clauseList[j] = self.clauseList[j].replace(self.clauseList[j][k-1]+self.clauseList[j][k],")
            self.clauseList[i] = self.clauseList[i].replace(l,")
            if len(lst) == 2:
                if l == lst[0]:
                    clause = lst[1] + self.clauseList[j]
                    print('C'+str(counterClause)+" : "+clause + "   by C"+str(i)+" and C"+str(j))
                    self.clauseList[i] = self.clauseList[i].replace(self.clauseList[i],")
                    self.clauseList[j] = self.clauseList[j].replace(self.clauseList[j],")
                    self.clauseList.append(clause)
                    counterClause += 1

                lst = []
                break
            else:
                clause = lst[0] + self.clauseList[j]
                print('C'+str(counterClause)+" : "+clause + "   by C"+str(i)+" and C"+str(j))
                self.clauseList[i] = self.clauseList[i].replace(self.clauseList[i],")
                self.clauseList[j] = self.clauseList[j].replace(self.clauseList[j],")
                self.clauseList.append(clause)
                counterClause += 1

                lst = []
                break
        else:
            self.clauseList[j] = self.clauseList[j].replace('(',")
            clause = self.clauseList[j]
            print('C'+str(counterClause)+" : "+clause + "   by C"+str(i)+" and C"+str(j))
            self.clauseList[i] = self.clauseList[i].replace(self.clauseList[i],")
            self.clauseList[j] = self.clauseList[j].replace(self.clauseList[j],")
            self.clauseList.append(clause)

```



```
counterClause += 1
```

```
lst = []
```

```
break
```

```
else:
```

```
if len(self.clauseList[j]) == 1:
```

```
self.clauseList[i].replace(l,"")
```

```
if len(lst) == 2:
```

```
if l == lst[0]:
```

```
clause = lst[1] + "|" + self.clauseList[j]
```

```
print('C'+str(counterClause)+" : "+clause + " by C"+str(i)+" and C"+str(j))
```

```
self.clauseList[i] = self.clauseList[i].replace(self.clauseList[i],"")
```

```
self.clauseList[j] = self.clauseList[j].replace(self.clauseList[j],"")
```

```
self.clauseList.append(clause)
```

```
counterClause += 1
```

```
lst = []
```

```
break
```

```
else:
```

```
clause = lst[0] + "|" + self.clauseList[j]
```

```
print('C'+str(counterClause)+" : "+clause + " by C"+str(i)+" and C"+str(j))
```

```
self.clauseList[i] = self.clauseList[i].replace(self.clauseList[i],"")
```

```
self.clauseList[j] = self.clauseList[j].replace(self.clauseList[j],"")
```

```
self.clauseList.append(clause)
```

```
counterClause += 1
```

```
lst = []
```

```
break
```

```
else:
```

```
clause = self.clauseList[j]
```

```
print('C'+str(counterClause)+" : "+clause + " by C"+str(i)+" and C"+str(j))
```

```
self.clauseList[i] = self.clauseList[i].replace(self.clauseList[i],"")
```

```
self.clauseList[j] = self.clauseList[j].replace(self.clauseList[j],"")
```

```
self.clauseList.append(clause)
```

```
counterClause += 1
```

```
lst = []
```

```

        break
    elif len(self.clauseList[j]) > 2 and len(lst) == 2:
        lst = []
        break
    elif len(self.clauseList[j]) > 2 and len(lst) == 1:
        clause = self.clauseList[j]
        print('C'+str(counterClause)+" : "+clause + "   by C"+str(i)+" and C"+str(j))
        self.clauseList[i] = self.clauseList[i].replace(self.clauseList[i],")
        self.clauseList[j] = self.clauseList[j].replace(self.clauseList[j],")
        self.clauseList.append(clause)
        counterClause += 1
        lst = []

        break
    else:
        continue

elif len(l) == 2:
    for j in range(len(self.clauseList)):
        if i == j:
            continue
        elif l in self.clauseList[j]:
            for k in range(len(self.clauseList[j])):
                if self.clauseList[j][k] == l[1]:
                    if k-1 >= 0 and self.clauseList[j][k-1] == '-':
                        self.clauseList[i] = self.clauseList[i].replace(l,"")
                    if len(lst) == 1 and len(self.clauseList[j]) == 2:
                        clause = lst[0]
                        print('C'+str(counterClause)+" : "+clause + "   by C"+str(i)+" and C"+str(j))
                        self.clauseList[i] = self.clauseList[i].replace(self.clauseList[i],")
                        self.clauseList[j] = self.clauseList[j].replace(self.clauseList[j],")
                        self.clauseList.append(clause)
                        counterClause += 1
                        lst = []

```

```

        break

    elif len(lst) == 2 and len(self.clauseList[j]) == 2:

        clause = lst[0] +'|'+lst[1]

        print('C'+str(counterClause)+" : "+clause + "   by C"+str(i)+" and C"+str(j))

        self.clauseList[i] = self.clauseList[i].replace(self.clauseList[i],")
        self.clauseList[j] = self.clauseList[j].replace(self.clauseList[j],")

        self.clauseList.append(clause)

        counterClause += 1

        lst = []

        break

    else:

        lst = []

        break

else:

    if len(self.clauseList[j]) == 1:

        self.clauseList[i] = self.clauseList[i].replace(l,")

        if len(lst) == 2:

            if l == lst[0]:

                clause = lst[1]

                print(clause)

                print('C'+str(counterClause)+" : "+clause + "   by C"+str(i)+" and C"+str(j))

                self.clauseList[i] = self.clauseList[i].replace(self.clauseList[i],")

                self.clauseList[j] = self.clauseList[j].replace(self.clauseList[j],")

                self.clauseList.append(clause)

                counterClause += 1

                lst = []

                break

            else:

                clause = lst[0]

                print('C'+str(counterClause)+" : "+clause + "   by C"+str(i)+" and C"+str(j))

                self.clauseList[i] = self.clauseList[i].replace(self.clauseList[i],")

                self.clauseList[j] = self.clauseList[j].replace(self.clauseList[j],")

```

```

        self.clauseList.append(clause)

        counterClause += 1

        lst = []

        break
    else:
        clause = "

        print('C'+str(counterClause)+" : "+clause + "   by C"+str(i)+" and C"+str(j))

        self.clauseList[i] = self.clauseList[i].replace(self.clauseList[i],")
        self.clauseList[j] = self.clauseList[j].replace(self.clauseList[j],")

        self.clauseList.append(clause)

        counterClause += 1

        lst = []

        break
    elif len(self.clauseList[j]) > 2 and len(lst) == 2:
        self.clauseList[i] = self.clauseList[i].replace(l,")
        self.clauseList[j] = self.clauseList[j].replace(l[l[1],")
        self.clauseList[j] = self.clauseList[j].replace("|",")
        if l == lst[0]:
            clause = lst[1]+"|"+self.clauseList[j]

            print('C'+str(counterClause)+" : "+clause + "   by C"+str(i)+" and C"+str(j))

            self.clauseList[i] = self.clauseList[i].replace(self.clauseList[i],")
            self.clauseList.append(clause)

            counterClause += 1

            lst = []

            break
        else:
            clause = lst[0]+"|"+self.clauseList[j]

            print('C'+str(counterClause)+" : "+clause + "   by C"+str(i)+" and C"+str(j))

            self.clauseList[i] = self.clauseList[i].replace(self.clauseList[i],")
            self.clauseList[j] = self.clauseList[j].replace(self.clauseList[j],")

            self.clauseList.append(clause)

            counterClause += 1

```

```

        lst = []

        break

    elif len(self.clauseList[j]) > 2 and len(lst) == 1:

        clause = self.clauseList[j]

        print('C'+str(counterClause)+" : "+clause + "   by C"+str(i)+" and C"+str(j))

        self.clauseList[i] = self.clauseList[i].replace(self.clauseList[i],")

        self.clauseList[j] = self.clauseList[j].replace(self.clauseList[j],")

        self.clauseList.append(clause)

        counterClause += 1

        lst = []

        break

    else:

        continue

    break

else:

    continue

```

```

def checking(self):

    for i in self.clauseList:

        if i != "":

            print("There is an independent clause : "+i)

            break

```