

**The Most Comprehensive
Preparation App For All Exams**

CIRCLE DOUBT SESSION

Agenda :- Doubt Session (Circle)

→ 240 → 19 (done)

105 (left)

→ 450

Total 500 → Max 15

Practice Questions

Q13. ABCD is a cyclic quadrilateral AB and DC are produced to meet at P.

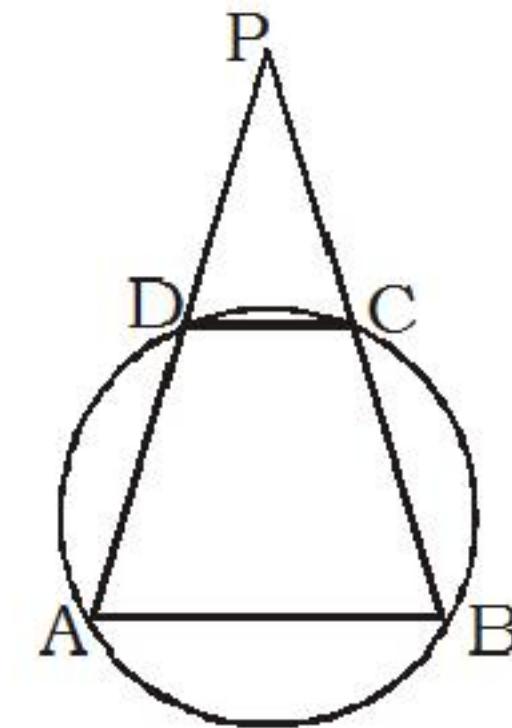
If $\angle ADC = 70^\circ$ and $\angle DAB = 60^\circ$, then the $\angle PBC + \angle PCB$ is:

- (a) 130°
- (b) 150°
- (c) 155°
- (d) 180°

Ans. (a)

Q14. In the figure given above, if $\angle BAD = 60^\circ$, $\angle ADC = 105^\circ$, then what is $\angle DPC$ equal to?

- (a) 40°
- (b) 45°
- (c) 50°
- (d) 60°



Ans. (b)

Q15. In the given figure, what is $\angle CBA$?

- (a) 30°
(b) 45°
(d) 50°
(c) 60°

$$\angle CQR = 45^\circ$$

$$\angle PQC = 135^\circ$$

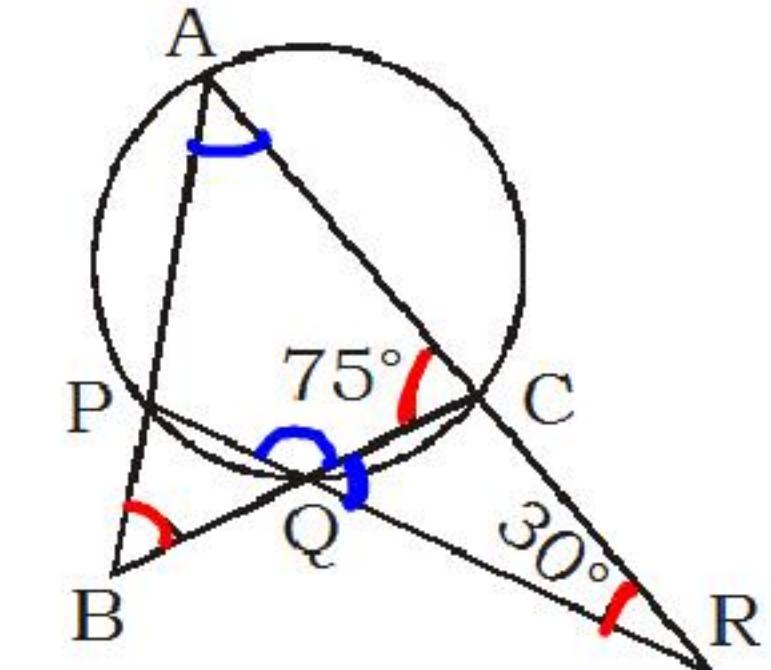
Cyclic Quad APQC

$\triangle ABC$

$$\angle A = 45^\circ$$

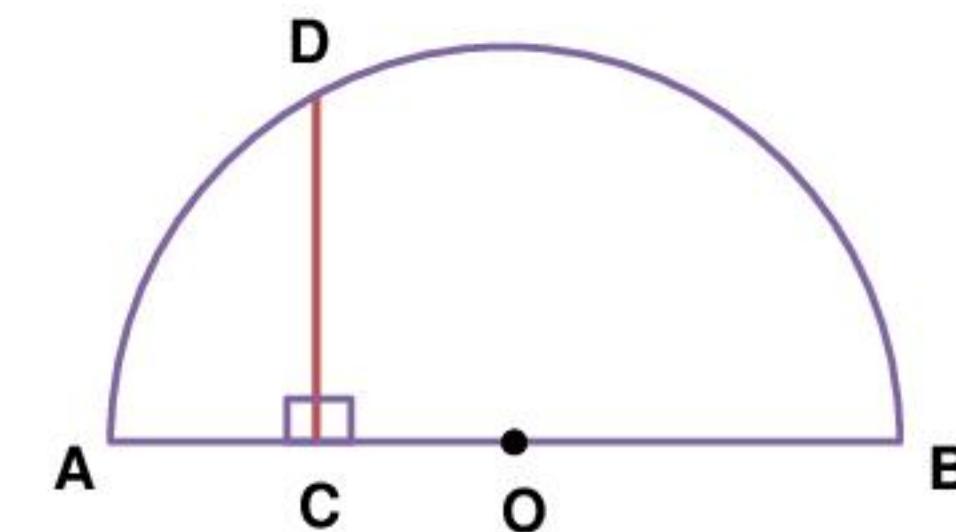
$$45 + 75 + \angle CBA = 180^\circ$$

$$\angle CBA = 60^\circ$$



Ans. (d)

Q20. If $AC = 3 \text{ cm}$, $CD = 9 \text{ cm}$
(O is centre of semicircle)
Find area of semi-circle.



Ans. $\frac{225\pi}{2}$

Q21. If $AB \parallel CD$

$$\angle CPB = 80^\circ$$

(O is centre of circle)

Find $\angle BCD$.

~~Ans~~

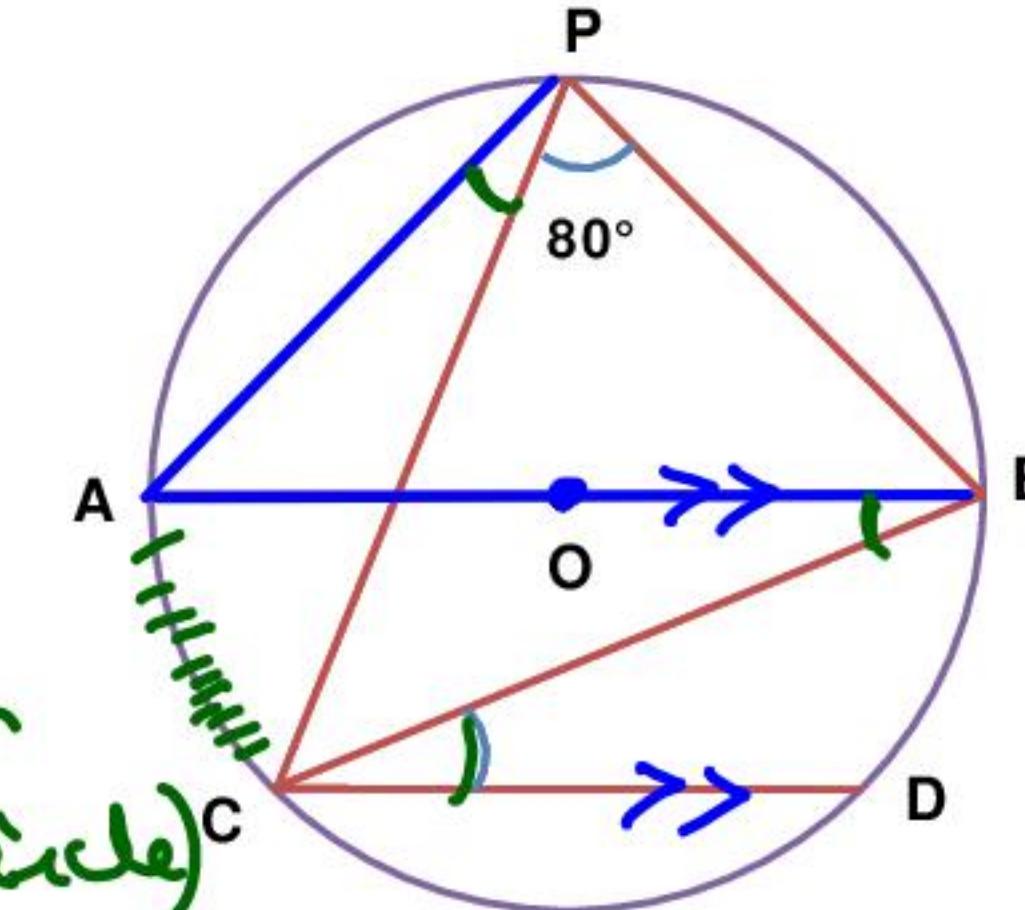
$$\angle APB = 90^\circ \quad (\text{Angle in a semi-circle})$$

$$\angle APC = 10^\circ$$

$$\angle ABC = 10^\circ \quad (\text{Angle in same segment})$$

$AB \parallel CD$

$$\angle BCD = 10^\circ$$



Ans. 10°

HOMEWORK

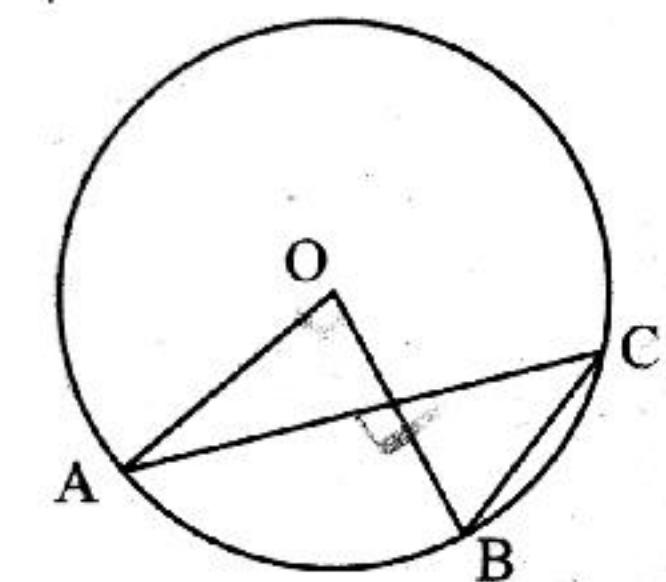
Q1. In the figure given above $\angle AOB = 46^\circ$, AC and OB intersect each other at right angles. What is the measure of $\angle OBC$ (where O is the centre of the circle)?

(a) 44°

(b) 46°

(c) 67°

(d) 78.5°



Ans. (c)

Q2. XY and XZ are tangent to a circle, ST is another tangent to the circle at the point R on the circle, which intersects XY and XZ at S and T respectively. If $XY = 15 \text{ cm}$ and $TX = 9 \text{ cm}$, then RT is

- (a) 4.5 cm
- (b) 7.5 cm
- (c) 6 cm
- (d) 3 cm

Ans. (c)

Q3. Diameter AOB of a circle is extended such that it intersect extended chord CD at E outside the circle. If $\angle AOC = 50^\circ$, $\angle AEC = 15^\circ$. Find $\angle BOD$. (O is the centre of the circle)

A. 10°

B. 20°

C. 40°

D. 5°

Ans. (B)

Q4. ABCD is a cyclic trapezium with $AB \parallel DC$ and AB = diameter of the circle. If $\angle CAB = 30^\circ$, then $\angle ADC$ is:

- (a) 60°
- (b) 120°
- (c) 150°
- (d) 30°

Ans. (b)

Q5. ABCD is a cyclic quadrilateral and O is the centre of the circle.

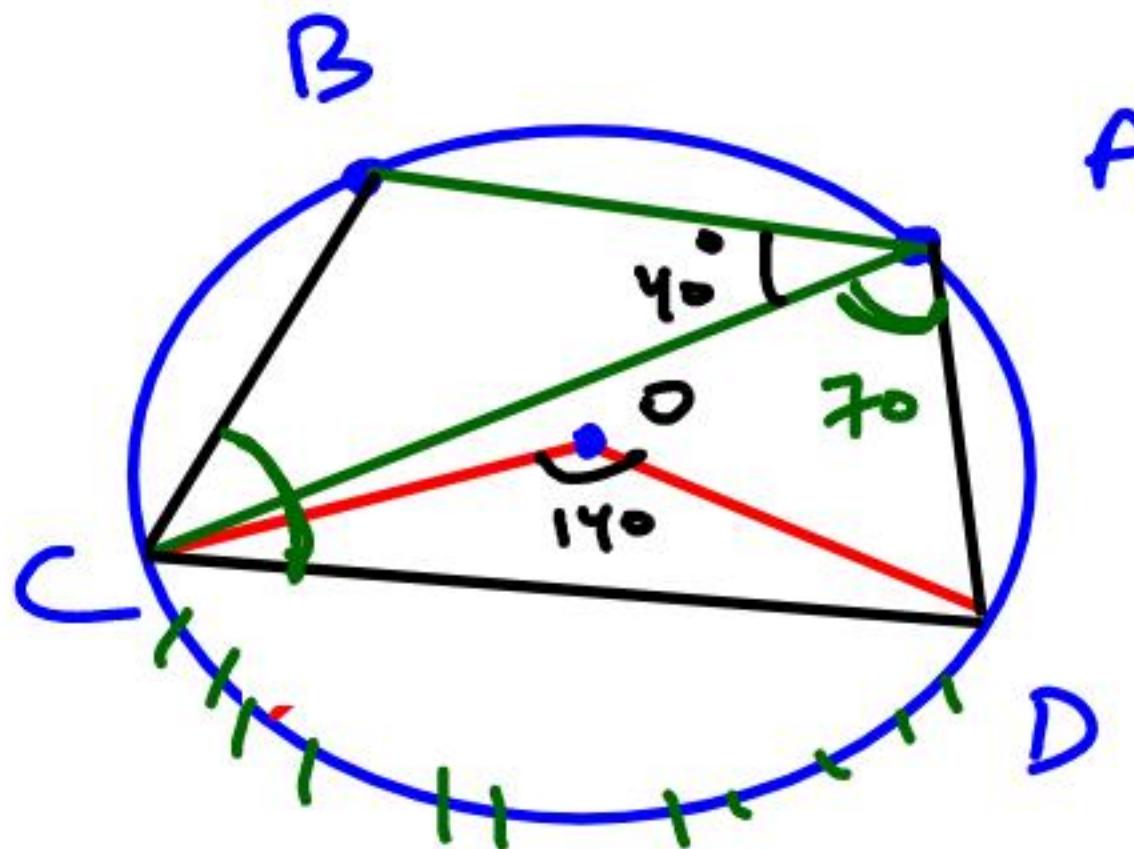
If $\angle COD = 140^\circ$ and $\angle BAC = 40^\circ$, then the value of $\angle BCD$ is equal to:

(a) 70°

(b) 90°

(c) 60°

(d) 80°



$$\angle CAD = 70^\circ$$

$$70 + 40 + \angle BCD = 180^\circ$$

$$\angle BCD = 70^\circ$$

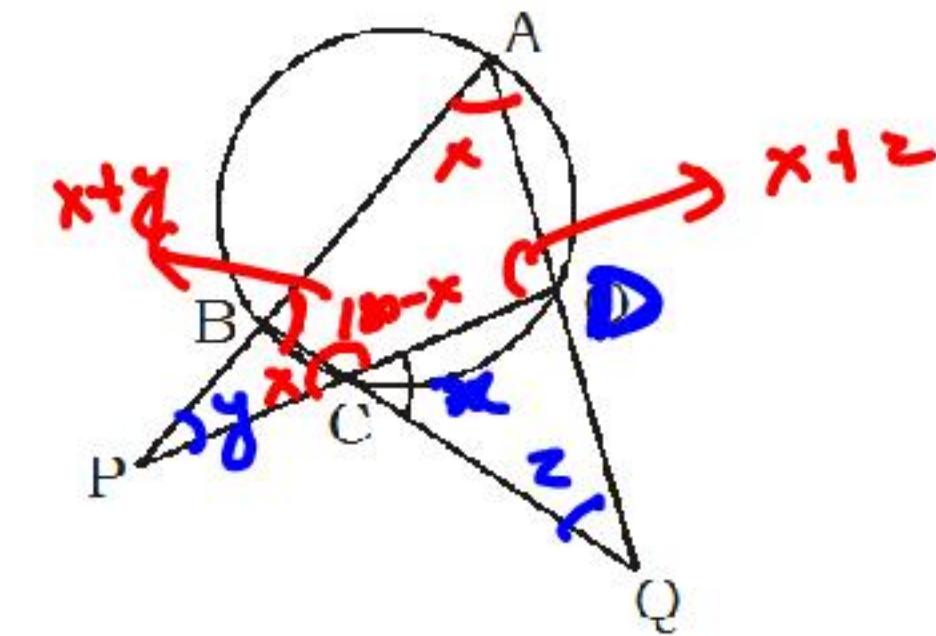
Ans. (a)

= K

Q6. In the given figure, if $x/3 = y/4 = z/5$, where $\angle DCQ = x$, $\angle BPC = y$ and $\angle DQC = z$, then what are the values of x, y and z respectively?

- (a) $30^\circ, 44^\circ$ and 55°
- ~~(b)~~ $36^\circ, 48^\circ$ and 60°
- (c) $39^\circ, 52^\circ$ and 65°
- (d) $42^\circ, 56^\circ$ and 70°

$$\begin{aligned}x &= \underline{3K} & (3\text{L}) \\y &= \underline{4K} & (4\text{L}) \\z &= \underline{5K} & (6\text{L})\end{aligned}$$



$$x+y+x+z = 180$$

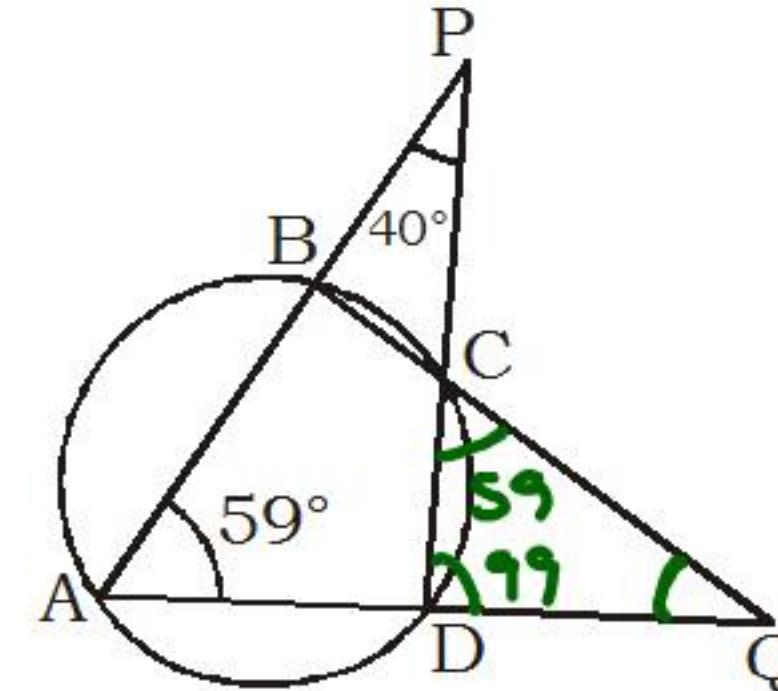
$$15K = 180$$

$$\underline{\underline{K=12}}$$

Ans. (b)

Q7. In the given figure, if $\angle PAQ = 59^\circ$,
 $\angle APD = 40^\circ$, then what is $\angle AQB$?

- (a) 19°
- (b) 20°
- (c) 22°
- (d) 27°



$$59 + 99 + \angle AQB = 180$$

$$\angle AQB = 22^\circ$$

Ans. (c)

Q8. Each of the circles of equal radii with centres A and B pass through the centre of each other circle they cut at C and D then $\angle DBC$ is equal to:

- (a) 60° (b) 100° (c) 120° (d) 140°

Ans. (c)

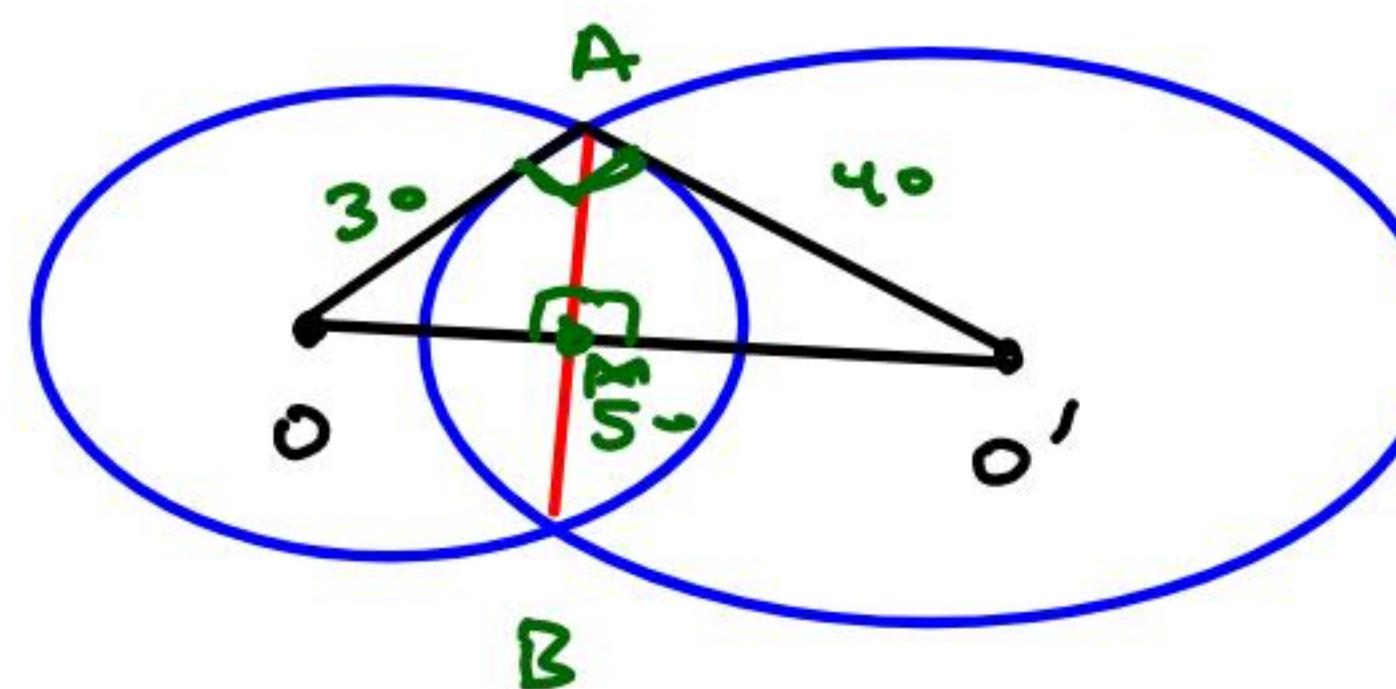
Q9. The length of the common chord of two circles of radii 30 cm and 40 cm whose centres are 50 cm apart, is (in cm)

(a) 12

(b) 24

(c) 36

~~(d) 48~~



$$\cancel{\frac{1}{2} \cdot 50 \cdot AM} = \cancel{\frac{1}{2} \cdot 30 \cdot 40}$$

$$AM = 24$$

$$AB = \underline{\underline{48}}$$

Ans. (d)

Q10. P and Q are centre of two circles with radii 9 cm and 2 cm respectively where $PQ = 17$ cm. R is the centre of another circle of radius x cm, which touches each of the above two circles externally. If $\angle PRQ = 90^\circ$, then the value of x is:

- (a) 4 cm (b) 6 cm (c) 7 cm (d) 8 cm

Ans. (b)

Q11. The radius of two concentric circles are 17 cm and 10 cm. A straight line ABCD intersects the larger circle at the point A and D and intersects the smaller circle at the points B and C. If BC = 12 cm, then the length of AD (in cm) is:

(a) 20

(b) 24

(c) 30

(d) 34

Ans. (c)

Q12. The distance between the centres of two circle having radii 4.5 cm and 3.5 cm respectively is 10 cm. What is the length of the transverse common tangent of these circles?

- (a) 8 cm
- (b) 7 cm
- (c) 6 cm
- (d) None of these

Ans. (c)

Q13. With A, B and C as centres, three circles are drawn such that they touch each other externally. If the sides of the $\triangle ABC$ are 4 cm, 6 cm and 8 cm then what is the sum of the radius of the circles?

- (a) 9 cm (b) 10 cm
 (c) 12 cm (d) 14 cm

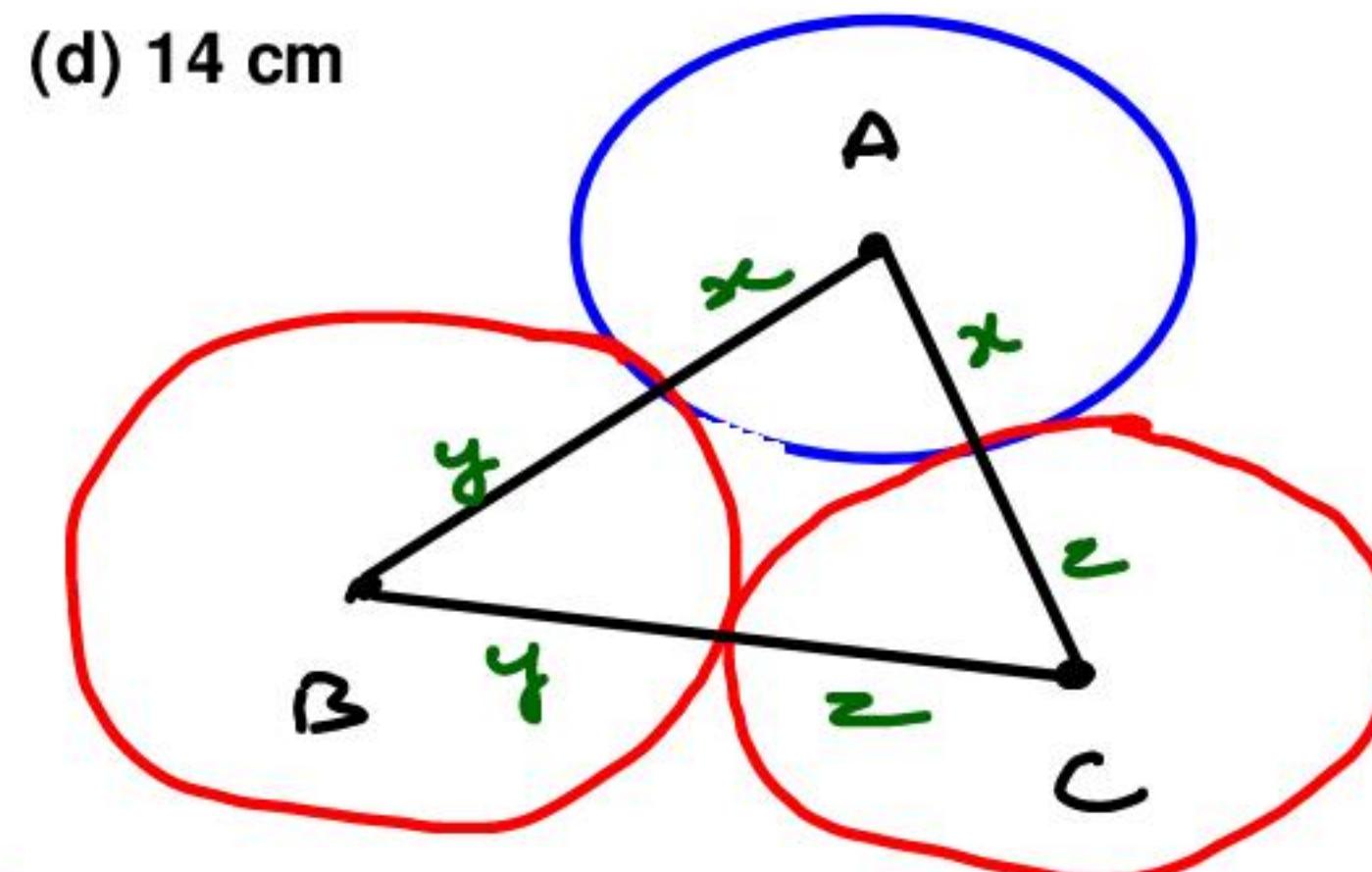
$$x+y=4$$

$$y + z = c$$

$$z + x = 8$$

$$2(x+y+z) = 18$$

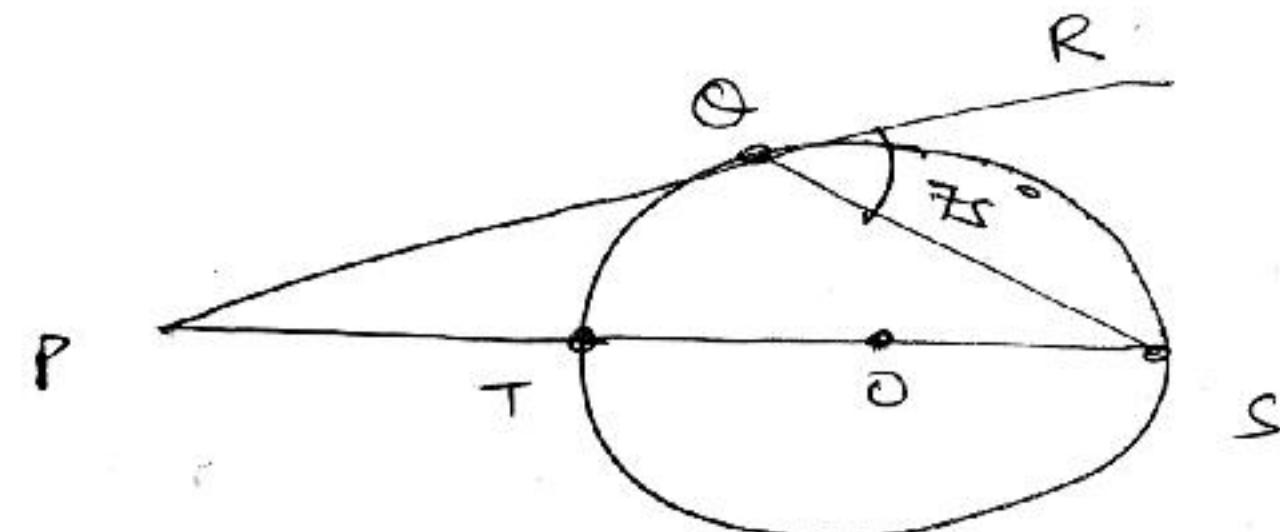
$$x+y+z = 0$$



Ans. (a)

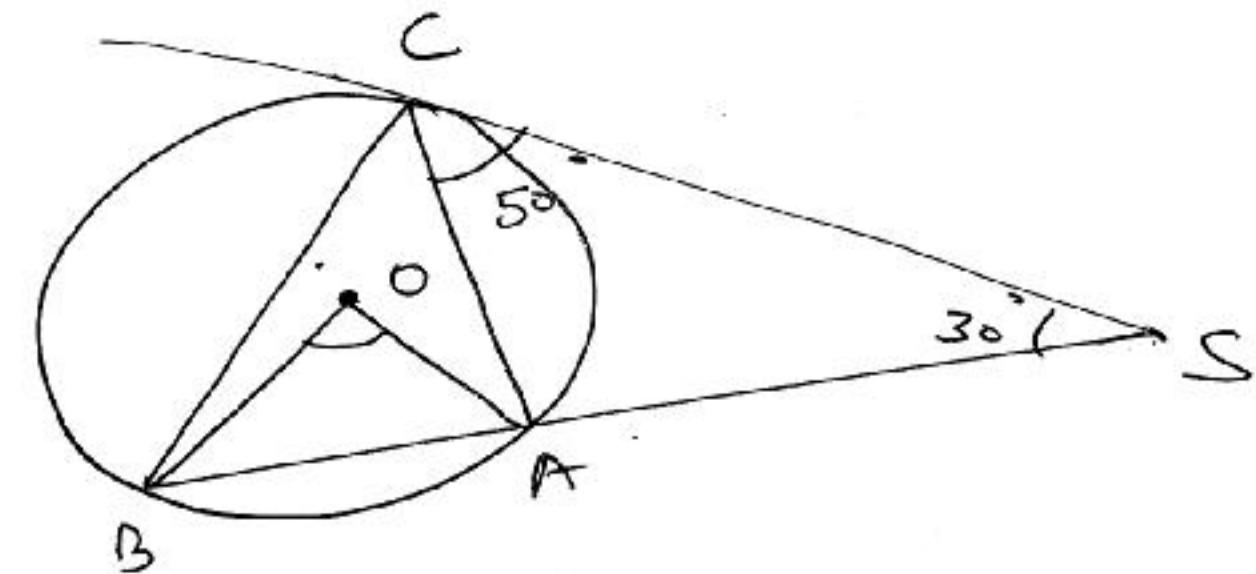
Q14. In the following figure PQR is a tangent to a circle with centre O.

If $\angle RQS = 75^\circ$, find $\angle QPS = ??$



Ans. $\angle QPS = 60^\circ$

Q15. In the figure, A, B and C are 3 points on a circle with centre O. The chord BA is extended to point S such that CS becomes a tangent to the circle at point C. If $\angle ASC = 30^\circ$, $\angle ACS = 50^\circ$; Find $\angle BOA = ??$

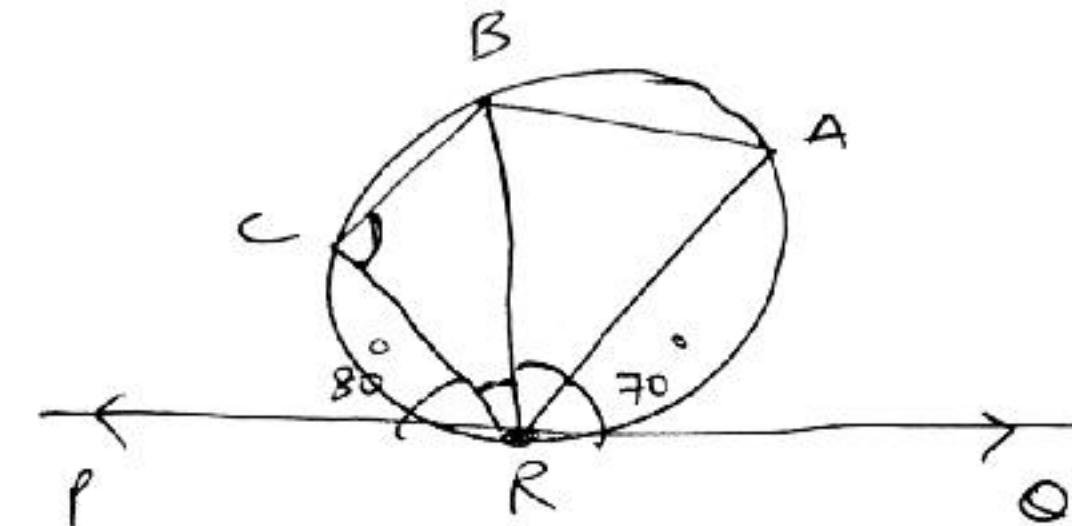


Ans. $\angle BOA = 100^\circ$

Q16. In the figure, PQ is a tangent touching the circle at point R.

$$\angle QRA = 70^\circ, \angle PRC = 80^\circ$$

If RB bisects $\angle CRA$. Find $\angle RCB$



Ans. $\angle RCB = 85^\circ$

Q17. A pentagon ABCDE is inscribed in a circle. From a point P outside the circle two tangents which touch the circle at B and C respectively are drawn.
If $\angle BCA = 36^\circ$, $\angle AEC = 78^\circ$; Find $\angle BPC = ??$

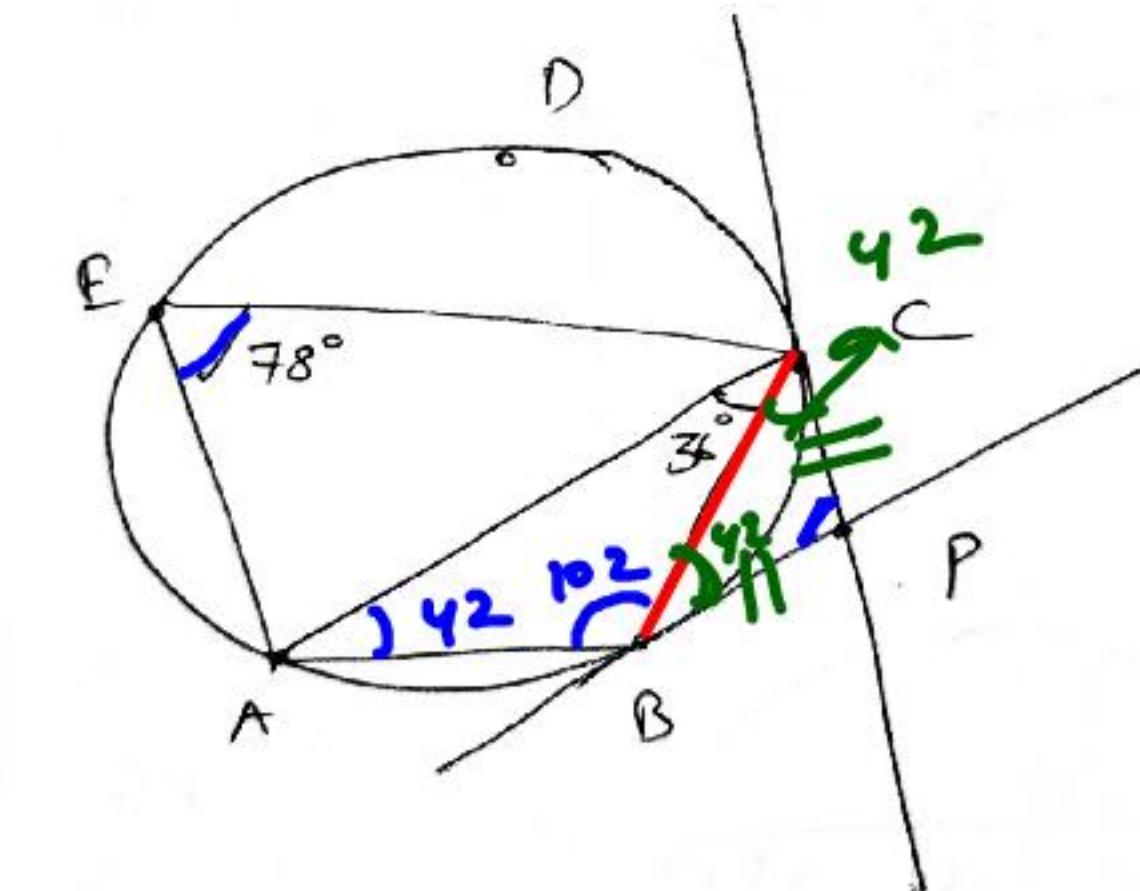
$$\angle ABC = 102^\circ$$

$$\angle BAC = 42^\circ$$

$\angle CBP = 42^\circ$ (Alternate segment)

$$42 + 42 + \angle BPC = 180^\circ$$

$$\angle BPC = 96^\circ$$



Ans. $\angle BPC = 96^\circ$



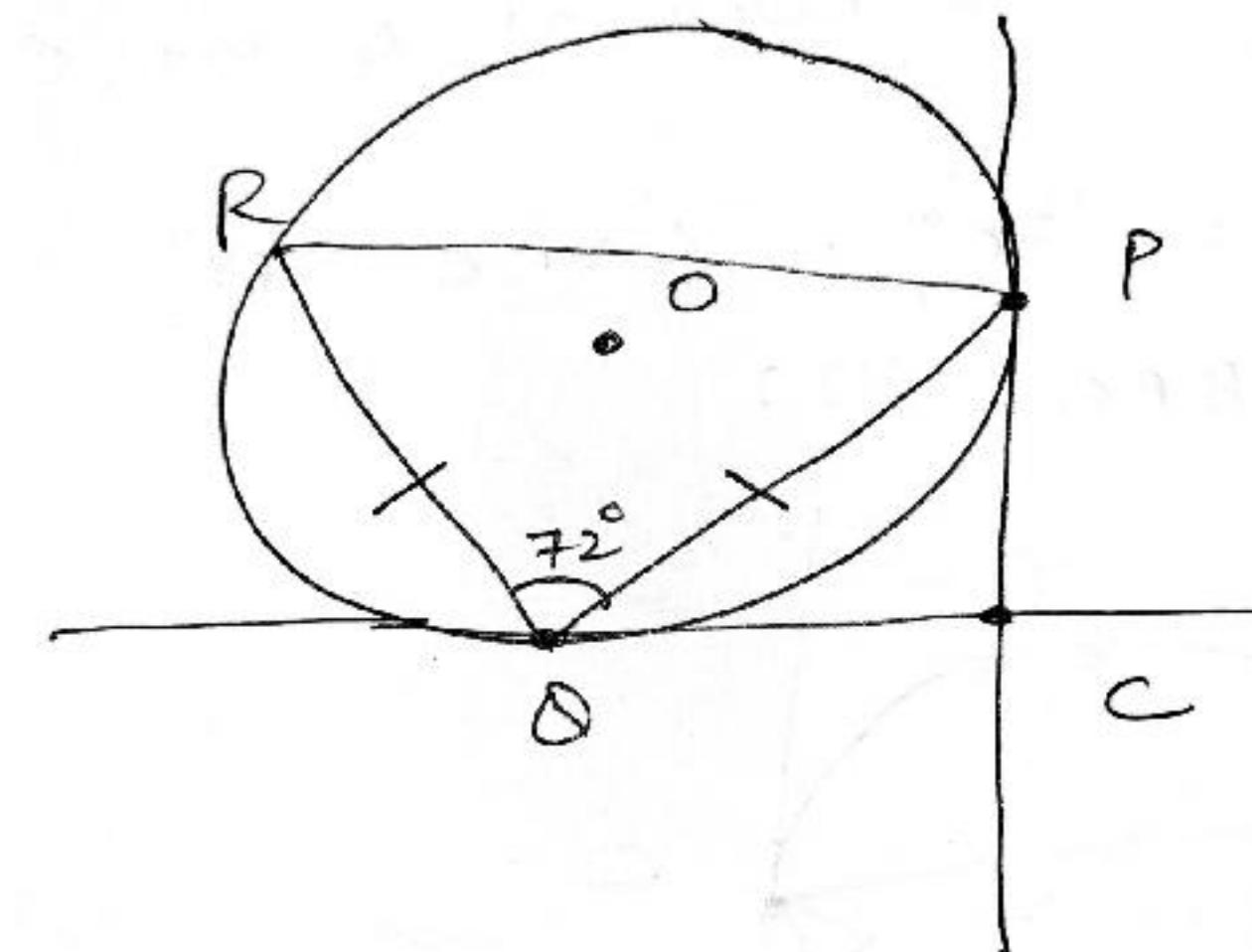
Q18. In the given figure,

$PQ = RQ$ and $\angle RQP = 72^\circ$

PC and QC are tangents

O is the centre.

Find $\angle PCQ = ??$



Ans. $\angle PCQ = 72^\circ$

Q19. PQ and PR are tangents drawn from external point.

If $\angle RPQ = 40^\circ$

Find $\angle PQS + \angle PRS = ??$

$$\underline{\underline{70}}$$

$PQOR \rightarrow \text{quad}$

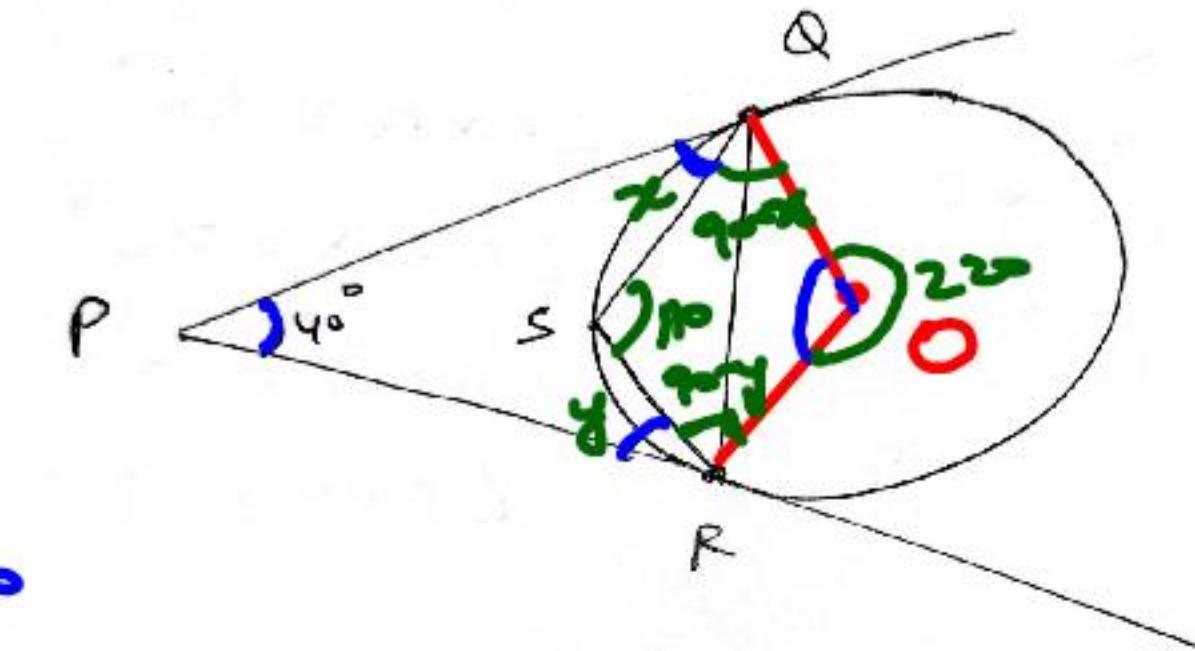
$$40^\circ + 90^\circ + 90^\circ + \angle POR = 360^\circ$$

$$\angle QOR = 140^\circ$$

$$\angle RSQ = 110^\circ$$

$$110^\circ + 140^\circ + 90^\circ - x + 90^\circ - y = 360^\circ$$

$$x + y = 70$$



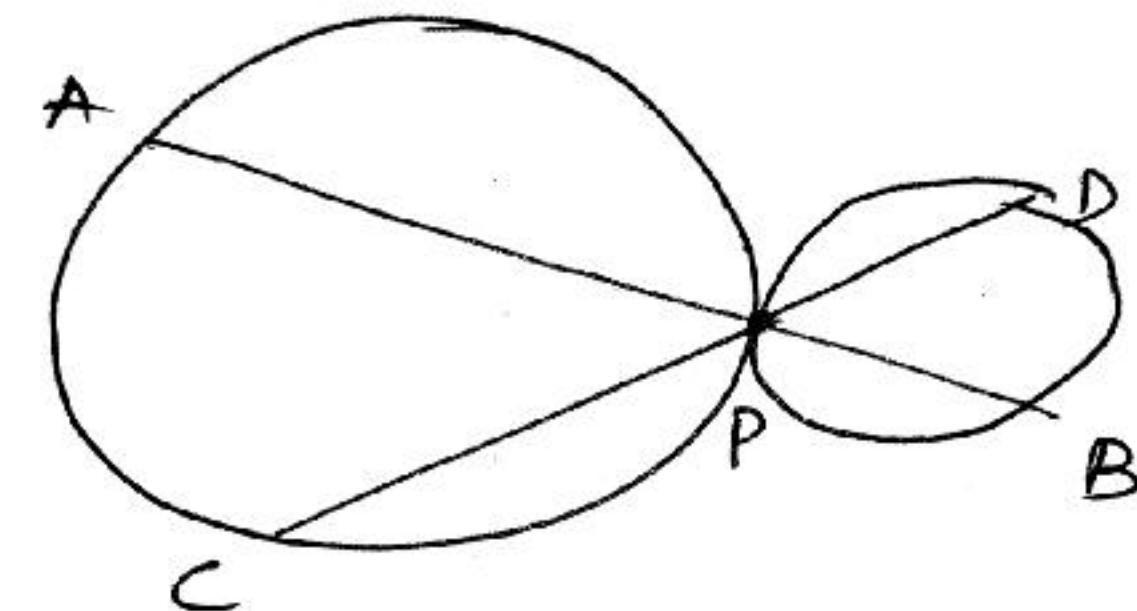
Ans. $\angle PQS + \angle PRS = 70^\circ$



Q20. Both circles are touching each other
there are two chords AB and CD which
pass through point of contact P.

If $AP = 12 \text{ cm}$, $PC = 4 \text{ cm}$, $PD = 6 \text{ cm}$

Find $PB = ??$

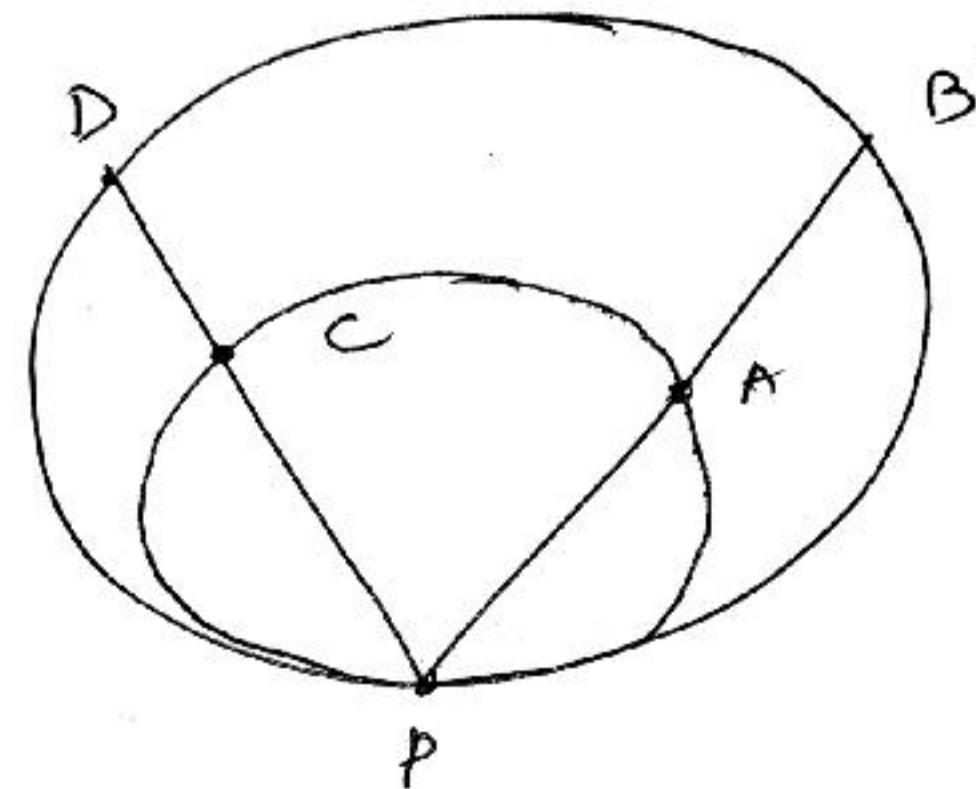


Ans. PB = 18 cm

Q21. Both circles are touching internally.

If $PA = 8 \text{ cm}$, $AB = 4 \text{ cm}$, $PC = 12 \text{ cm}$

Find $CD = ??$



Ans. CD = 6 cm

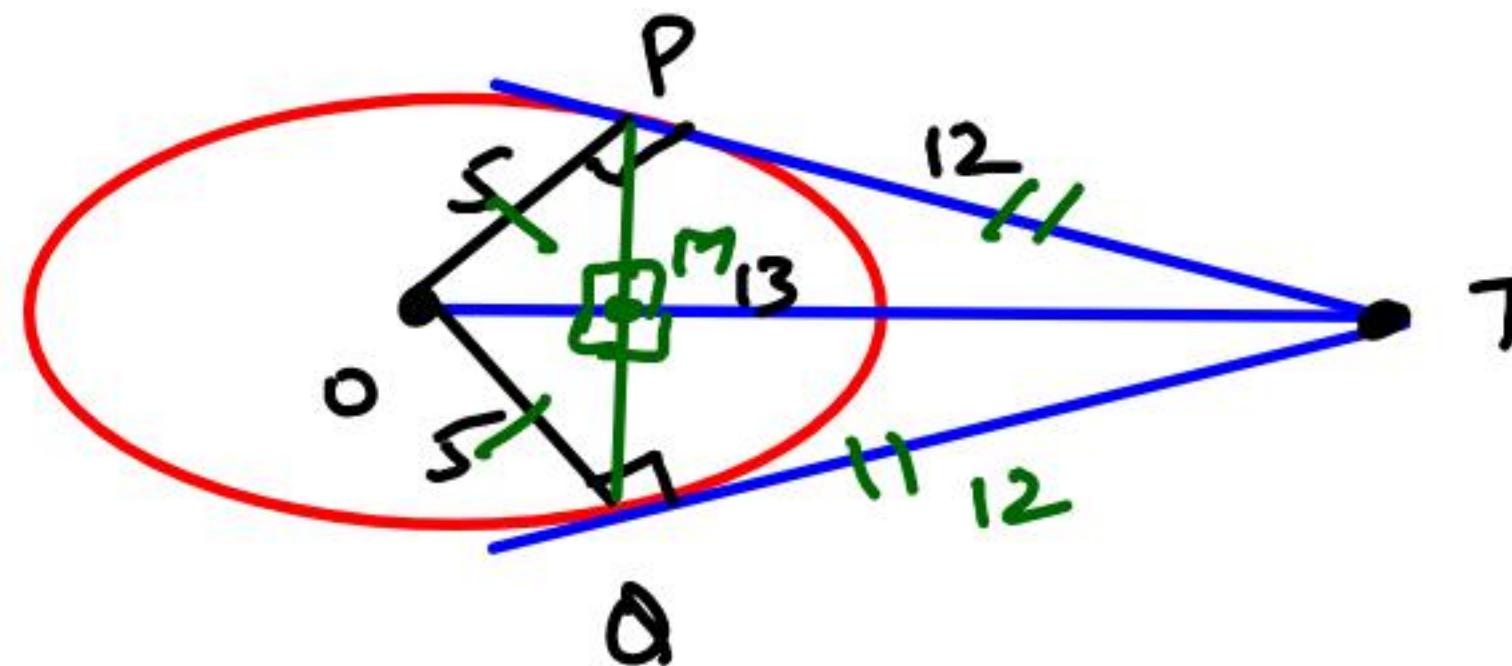
Q22. From an external point T, 13 cm away from the centre O of the circle of radius 5 cm, the two tangents PT and QT are drawn. What is the length of PQ?

$$(a) \frac{19}{3} \text{ cm}$$

$$(b) \frac{40}{13} \text{ cm}$$

$$(c) \frac{22}{3} \text{ cm}$$

$$(d) \frac{20}{3} \text{ cm}$$



$$5 \cdot 12 = 13 \cdot PM$$

$$PM = \frac{60}{13}$$

$$PQ = \frac{120}{13}$$

Ans. (d)

Q23. Two equal circles of radius 4 cm intersect each other such that each passes through the centre of the other. The length of the common chord is:

(a) $2\sqrt{3}$ cm

(c) $2\sqrt{2}$ cm

(b) $4\sqrt{3}$ cm

(d) 8 cm

Ans. (b)

Q24. If the radii of two circles be 6 cm and 3 cm and the length of the transverse common tangent be 8 cm, then the distance between the two centres is:

- (a) $\sqrt{145}$ cm
- (b) $\sqrt{140}$ cm
- (c) $\sqrt{150}$ cm
- (d) $\sqrt{135}$ cm

Ans. (a)

Q25. Two circles with radii 25 cm and 9 cm touch each other externally. The length of the direct common tangent is:

- (a) 34 cm
- (b) 30 cm
- (c) 26 cm
- (d) 32 cm

Ans. (b)

Q26. ABCD is a cyclic trapezium whose sides AD and BC are parallel to each other. If $\angle ABC = 75^\circ$ then the measure of $\angle BCD$ is:

- (a) 75°
- (b) 95°
- (c) 45°
- (d) 105°

Ans. (a)

Q27. In the figure given below $AO = CD$, where O is the centre of the circle. What is the value of $\angle APB$?

(a) 60°

(b) 50°

(c) 45°

(d) 30°

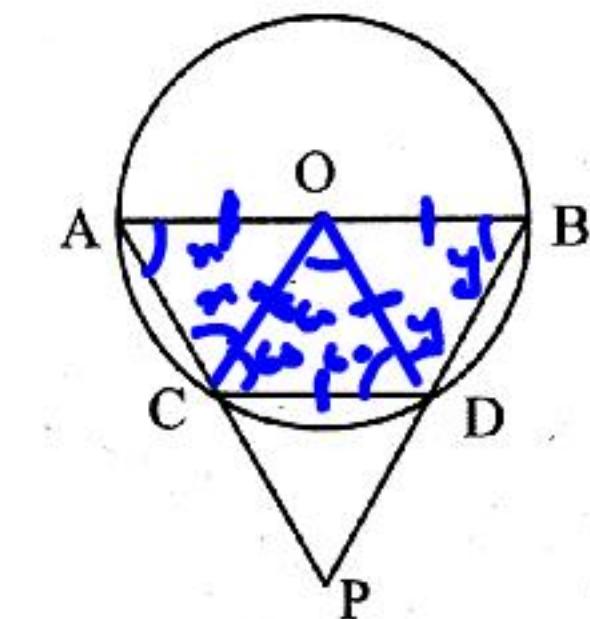
$$\angle AOC = 180 - 2x$$

$$\angle DOB = 180 - 2y$$

$$180 - 2x + 180 - 2y + 60 = 180$$

$$x + y = 120$$

$$\angle APB = 60^\circ$$



Ans. (a)

Q28. In the given fig., AT is a tangent of a circle of radius 6 cm. If A is at a distance of 10 cm from the centre O and AB = 5 cm, then what is the length of the chord BC?

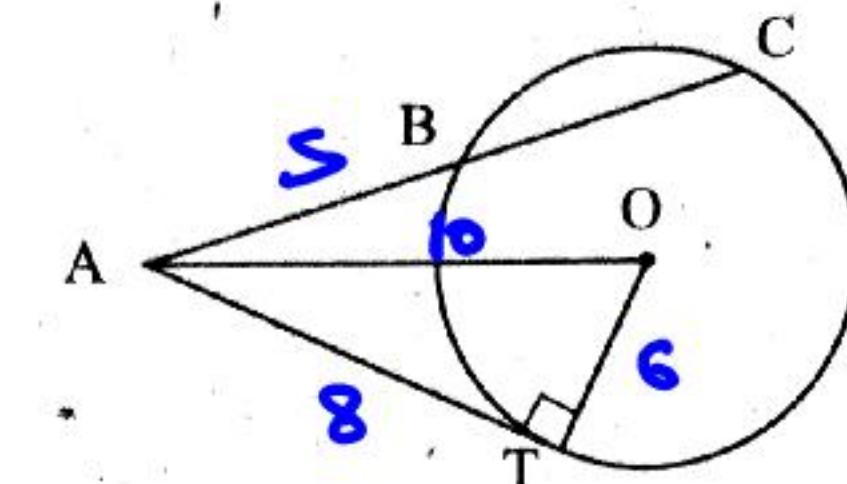
- (a) 7.8 cm
- (b) 8 cm
- (c) 8.4 cm
- (d) 9 cm

$$(TA)^2 = (AB)(AC)$$

$$8 \cdot 8 = 5 \cdot AC$$

$$AC = 12.8$$

$$BC = 12.8 - 5 = 7.8$$



Ans. (a)

Q29. In the given figure, O is the centre of the circle. The line UTV is a tangent to the circle at T, $\angle VTR = 52^\circ$ and ΔPTR is an isosceles triangle such that $TP = TR$. What is $\angle x + \angle y + \angle z$ equal to?

(a) 175°

~~(c) 218°~~

(b) 208°

(d) 250°

$x = 52^\circ$

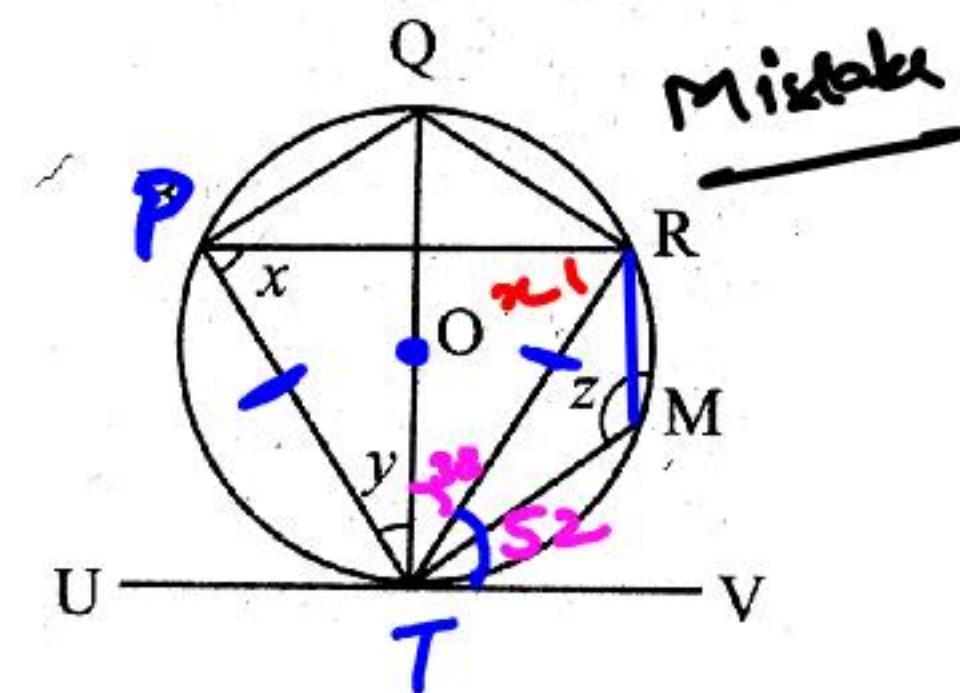
ΔPTR

$$52 + 52 + 38 + y = 180$$

$y = 38$

$x + z = 180$

$$52 + 38 + 138 = 218$$



Ans. (c)

Q30. The length of a chord of a circle is equal to the radius of the circle. The angle which this chord subtended in the major segment of the circle is equal to

- (a) 30°
- (b) 45°
- (c) 60°
- (d) 90°

Ans. (a)

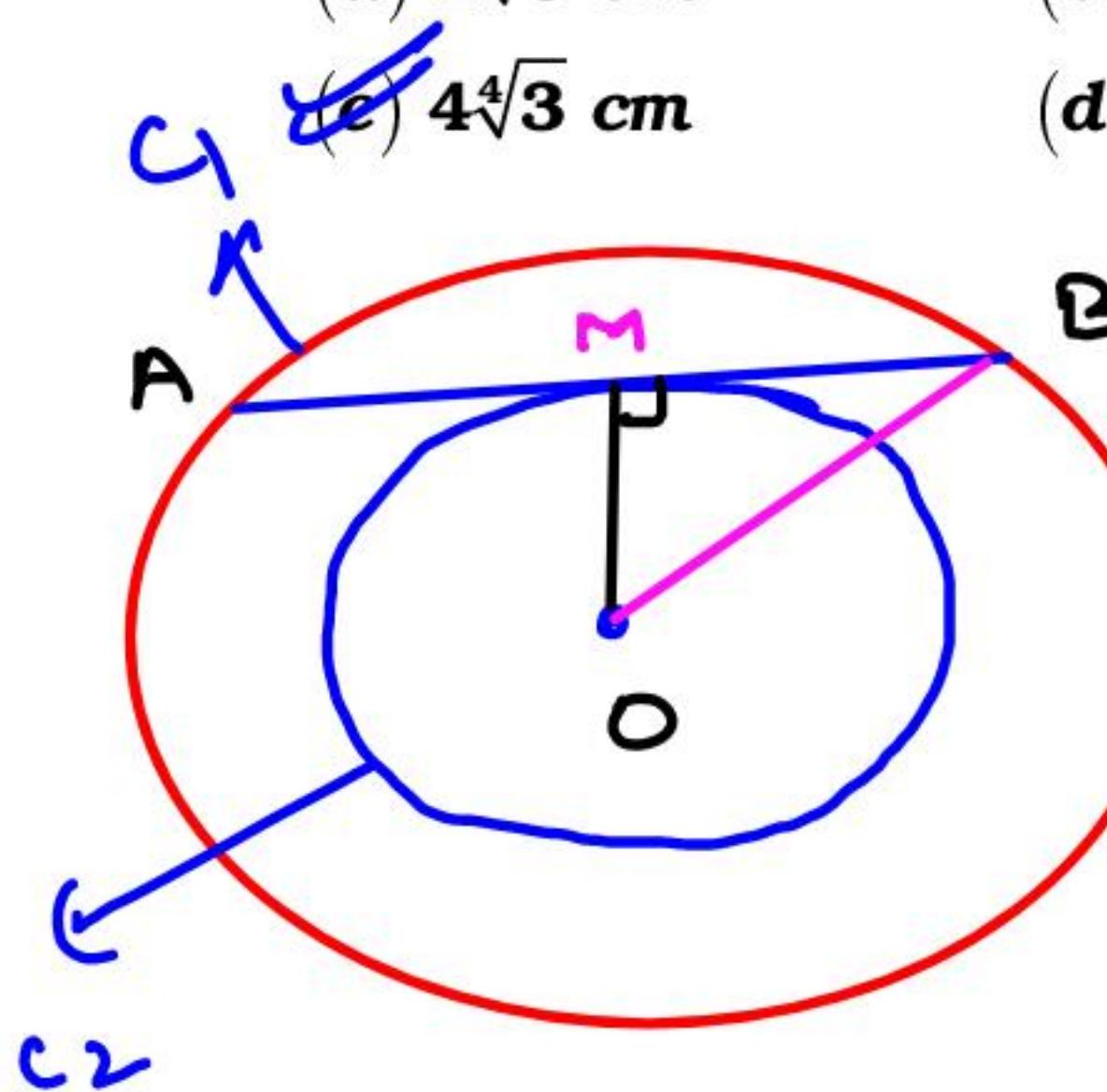
Q31. A chord AB of a circle C_1 of a radius $(\sqrt{3} + 1)$ cm touches a circle C_2 which is concentric to C_1 . If the radius of C_2 is $(\sqrt{3} - 1)$ cm, the length of AB is:

(a) $2\sqrt[4]{3}$ cm

(b) $8\sqrt{3}$ cm

~~(c) $4\sqrt[4]{3}$ cm~~

(d) $4\sqrt{3}$ cm



$\triangle OMB$

$$OM = \sqrt{3} - 1$$

$$OB = \sqrt{3} + 1$$

$$MB = \sqrt{(\sqrt{3}+1)^2 - (\sqrt{3}-1)^2}$$

$$MB = \sqrt{4\sqrt{3}}$$

$$MB = 2\frac{3}{4}$$

$$AB = 4 \cdot 2\frac{3}{4}$$

Ans. (c)

~~Ans~~

Q32. Chords AB and CD of a circle intersect at E and are perpendicular to each other. Segments AE, EB and ED are of lengths 2 cm, 6 cm and 3 cm respectively. Then the length of the diameter of the circle (in cm) is

(a) $\sqrt{65}$

(b) $\sqrt{62}$

(c) 65

(d) $\frac{65}{2}$

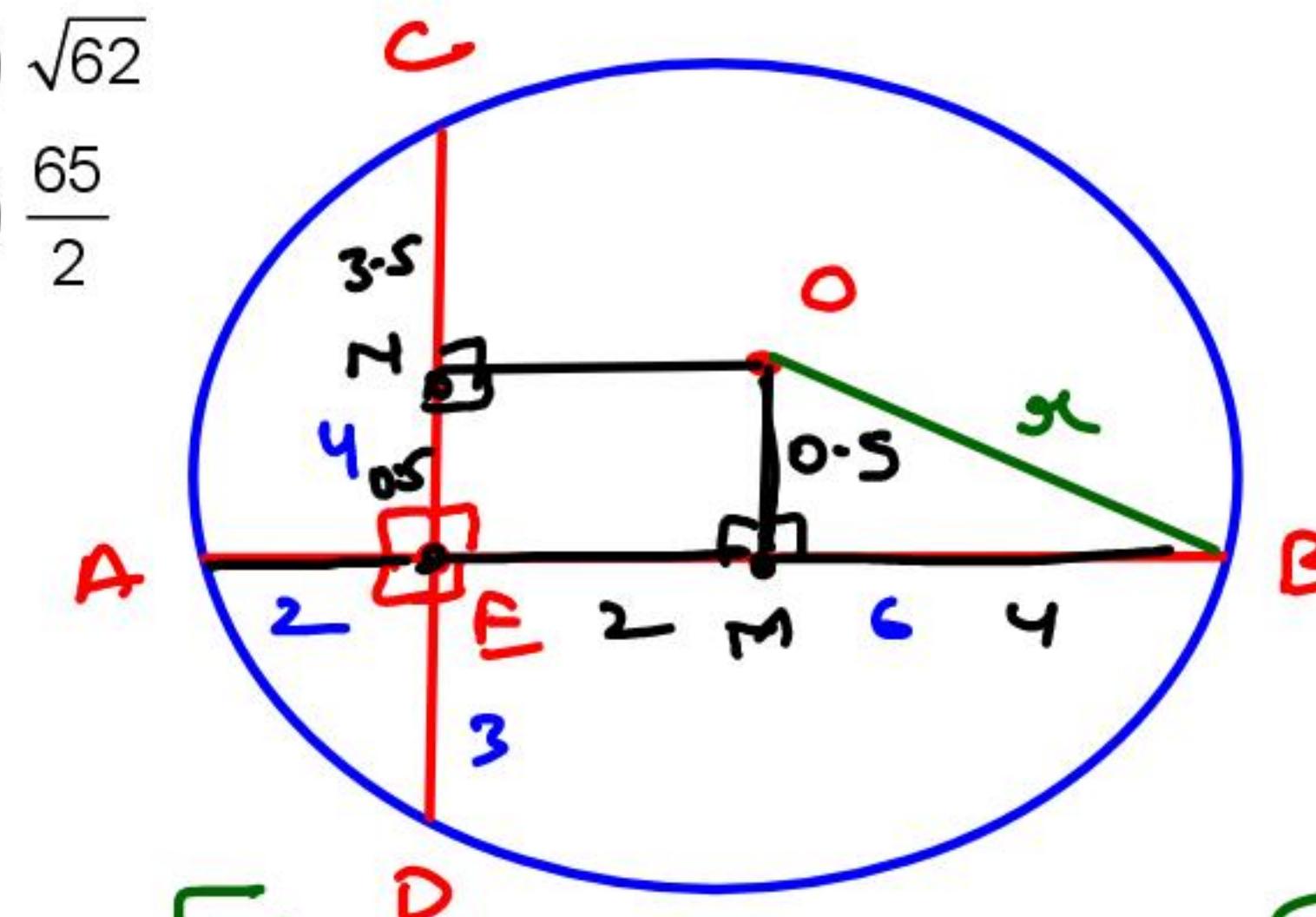
$$AE \times EB = DE \times CE$$

$$2 \times 6 = 3 \times CE$$

$$CE = 4$$

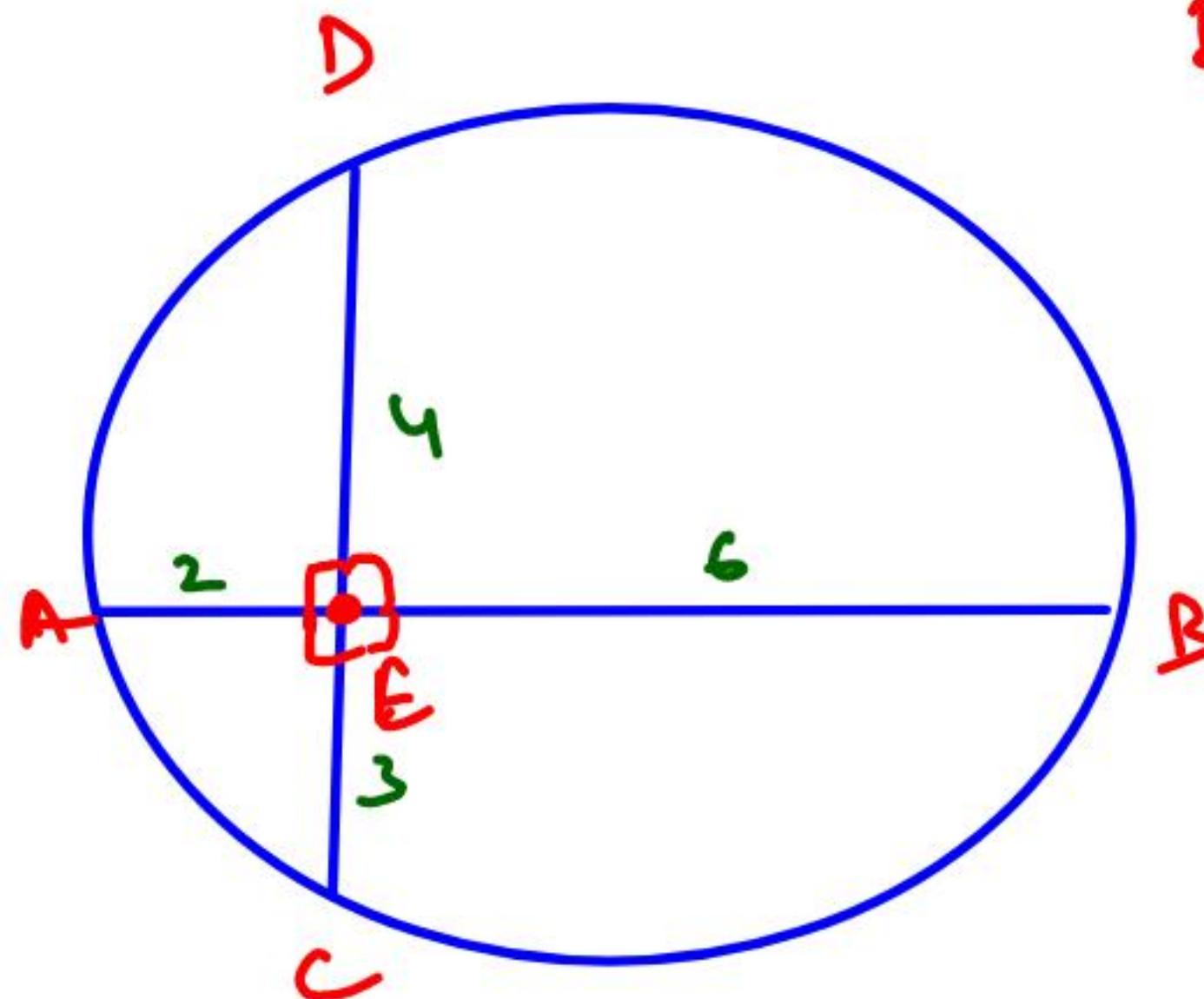
$$r^2 = 16 + \frac{1}{4}$$

$$r = \frac{\sqrt{65}}{2}$$



$$\text{Diameter} = \sqrt{65}$$

Ans. (a)



Diameter

$$= \sqrt{(AE)^2 + (BE)^2 + (CE)^2 + (DE)^2}$$

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Diameter

$$= \sqrt{2^2 + 6^2 + 3^2 + 4^2}$$

$$= \sqrt{65}$$

Q33. Two circles with centre P and Q intersect at B and C, A, D are points on the circle such that A, C, D are collinear. If $\angle APB = 130^\circ$, and $\angle BQD = x^\circ$, then the value of x is

- (a) 65 (b) 130 (c) 195 (d) 135

Ans. (b)

Q34. Two circles intersect each other at the points A and B. A straight line parallel to AB intersects the circles at C, D, E and F. If $CD = 4.5 \text{ cm}$, then the measure of EF is:

- (a) 1.50 cm
- (b) 2.25 cm
- (c) 4.50 cm
- (d) 9.00 cm

Ans. (c)

Q35. Two circles having radii 4 units intersect each other in such a way that each of them passes through the centre of the other. Then the length of their common chord is:

- (a) $\sqrt{2}$ r units
- (b) $\sqrt{3}$ r units
- (c) $\sqrt{5}$ r units
- (d) 4 units

Ans. (b)

Q36. The diagonals AC and BD of a cyclic quadrilateral ABCD intersect each other at the point P. Then, it is always true that:

- (a) $BP \times AB = CD \times CP$
- (b) $AP \times CP = BP \times DP$
- (c) $AP \times BP = CP \times DP$
- (d) $AP \times CD = AB \times CP$

Ans. (b)

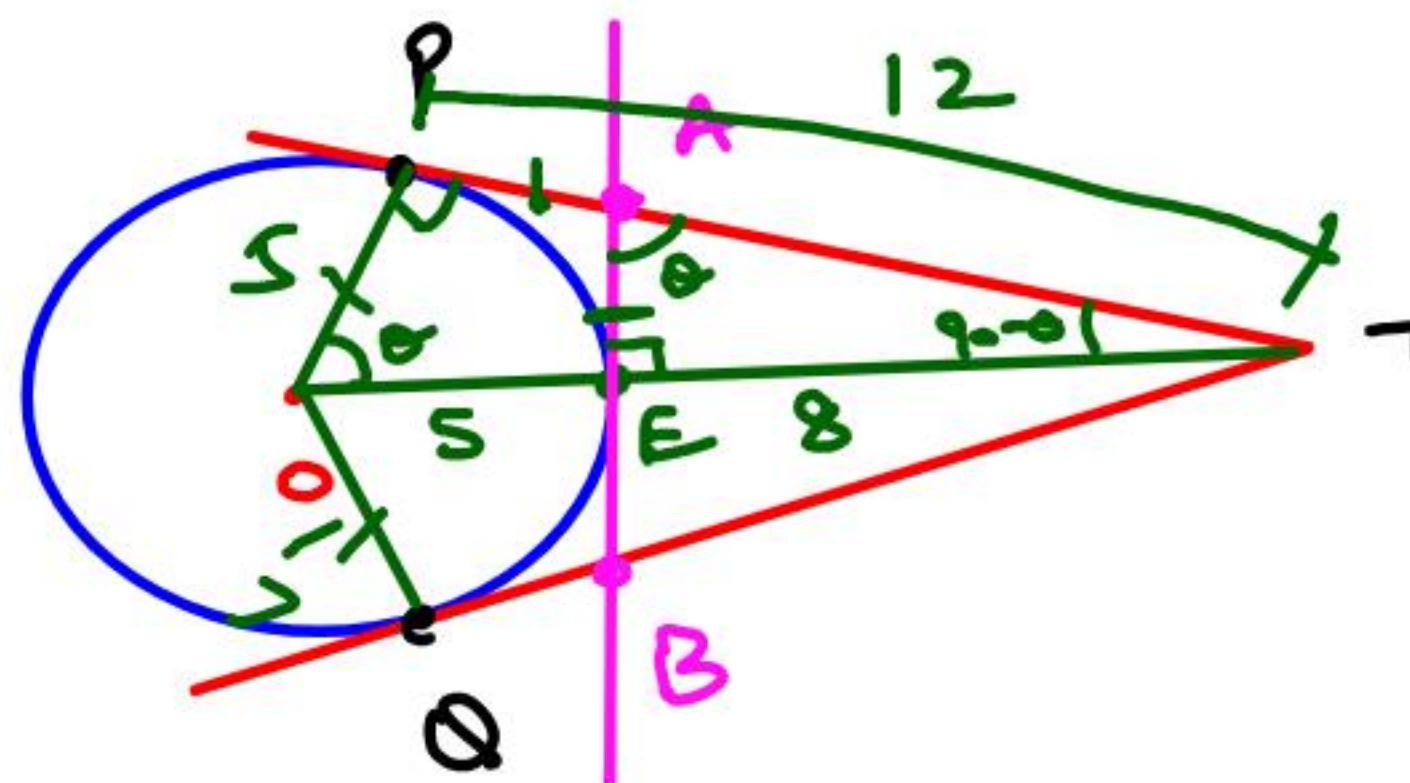
~~Q37.~~ A circular ring with centre O is kept in the vertical position by two weightless thin strings TP and TQ attached to the ring at P and Q. The line OT meets the ring at E where as a tangential string at E meets TP and TQ at A and B respectively. If the radius of the ring is 5 cm and $OT = 13 \text{ cm}$, then what is the length of AB?

(a) $10/3 \text{ cm}$

~~(b)~~ $20/3 \text{ cm}$

(c) 10 cm

(d) $40/3 \text{ cm}$



$$PT = 12 \text{ cm}$$

$$\triangle POT \sim \triangle EAT$$

$$\frac{OP}{EA} = \frac{OT}{AT} = \frac{13}{AT}$$

$$\frac{5}{EA} = \frac{13}{AT} = \frac{12}{8}$$

$$EA = \frac{10}{3} \text{ cm}$$

Ans. (b)

Q38. ABC is an equilateral triangle inscribed in a circle with AB = 5 cm. Let the bisector of the angle A meet BC in X and the circle in Y. What is the value of AX × AY?

(a) 16 cm^2

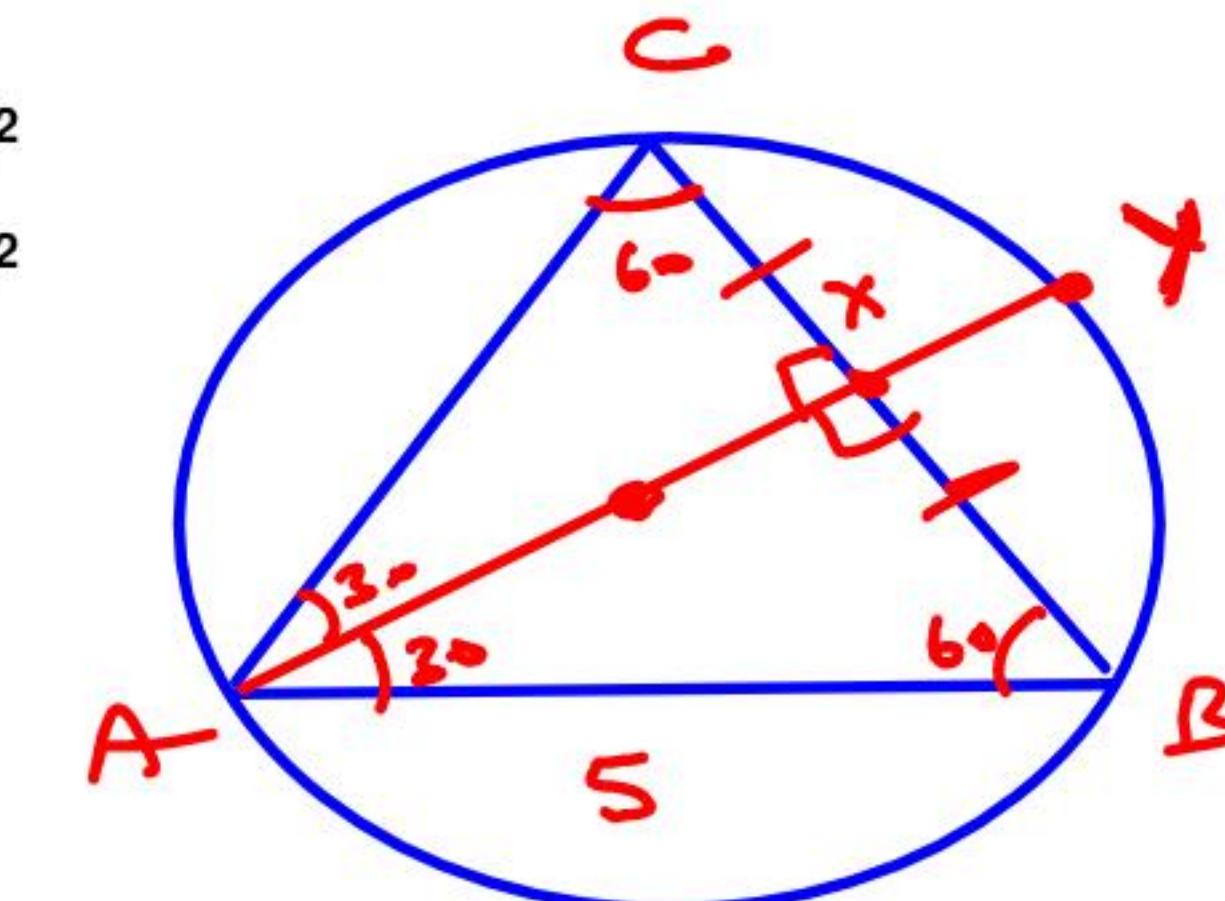
~~(c) 25 cm^2~~

(b) 20 cm^2

(d) 30 cm^2

$$AX = \frac{\sqrt{3}}{2} \cdot 5$$

$$AY = \frac{2 \cdot 5}{\sqrt{3}} = \frac{10}{\sqrt{3}}$$



$AX \cdot AY$

$$\frac{5\sqrt{3}}{2} \times \frac{10}{\sqrt{3}} = 25 \text{ cm}^2$$

Ans. (c)

Q39. In a ΔABC , $AB = AC$. A circle through B touches AC at D and intersects AB at P. If D is the mid point of AC, then which one of the following is correct?

- (a) $AB = 2AP$
- (b) $AB = 3AP$
- (c) $AB = 4AP$
- (d) $2AB = 5AP$

Ans. (c)

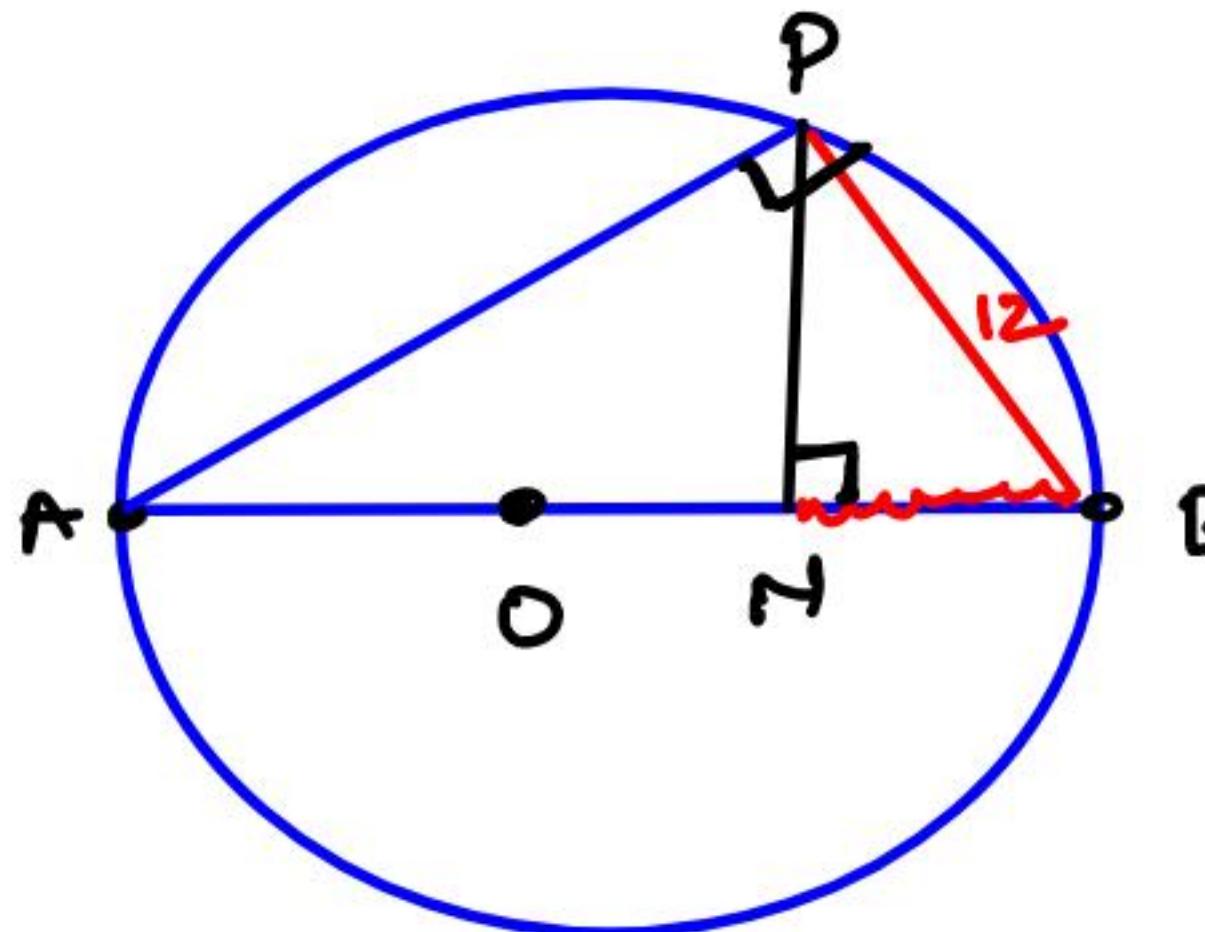
Q40. N is the foot of the perpendicular from a point P of a circle with radius 7 cm, on a diameter AB of the circle. If the length of the chord PB is 12 cm, the distance of the point N from the point B is:

(a) $6\frac{5}{7}$ cm

(b) $12\frac{2}{7}$ cm

(c) $3\frac{5}{7}$ cm

~~(d) $10\frac{2}{7}$ cm~~



$$AB = 14$$

$$(PB)^2 = BN \cdot BA$$

$$12 \cdot 12 = BN \cdot 14$$

$$BN = \frac{144}{14} = 10\frac{2}{7} \text{ cm}$$

Ans. (d)

~~Q41.~~ I and O are respectively the in-centre and circumcentre of a triangle ABC.

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The line AI produced intersects the circumcircle of ΔABC at the point D. If

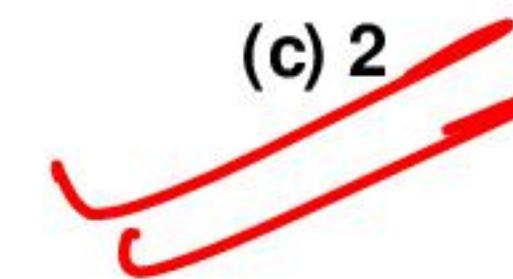
$$\angle ABC = x^\circ, \angle BID = y^\circ \text{ and } \angle BOD = z^\circ, \text{ then } \frac{z + x}{y} = ?$$

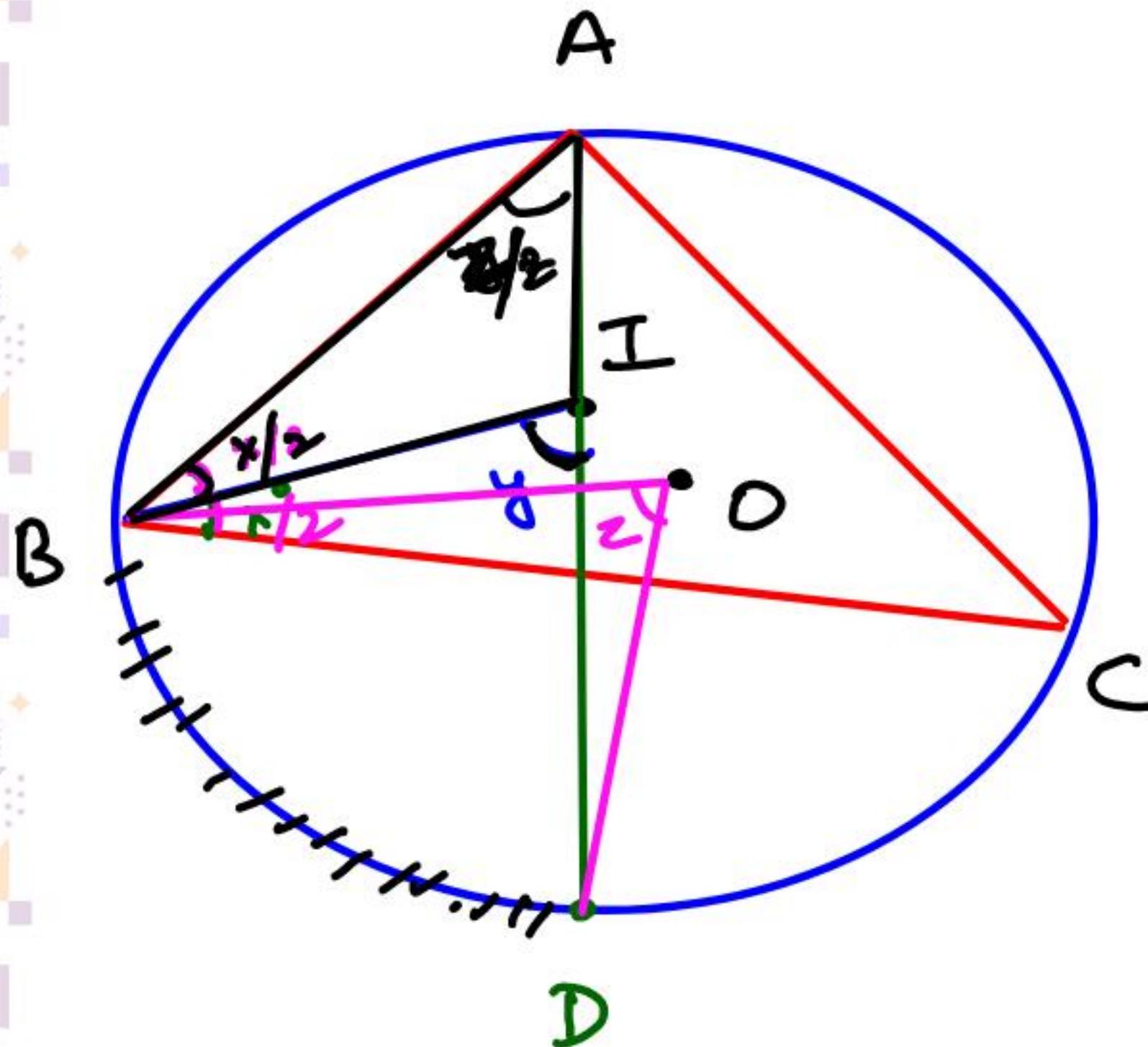
(a) 3

(b) 1

(c) 2

(d) 4




 $\triangle ABI$

$$\frac{x}{2} + \frac{z}{2} = y$$

$$\frac{x+z}{y} = 2$$

Ans. (c)

Q42. Two chords AB and CD of circle whose centre is O, meet at the point P and $\angle AOC = 50^\circ$, $\angle BOD = 40^\circ$. Then the value of $\angle BPD$ is:

- (a) 60°
- (b) 40°
- (c) 45°
- (d) 75°

Ans. (c)

Q43. Two chords AB, CD of a circle with centre O intersect each other at P.

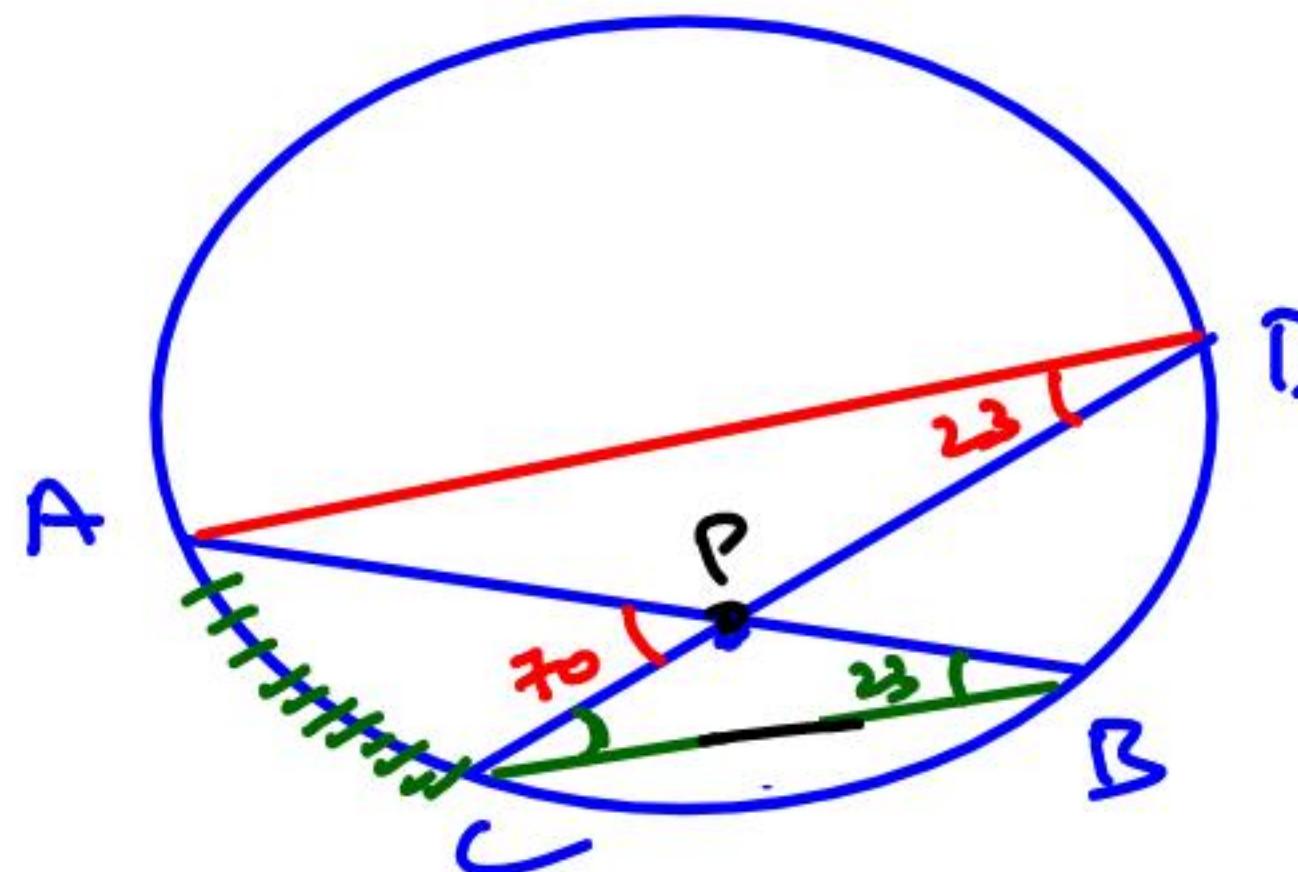
$\angle ADP = 23^\circ$ and $\angle APC = 70^\circ$, then $\angle BCD$ is:

(a) 45°

(b) 47°

(c) 57°

(d) 37°



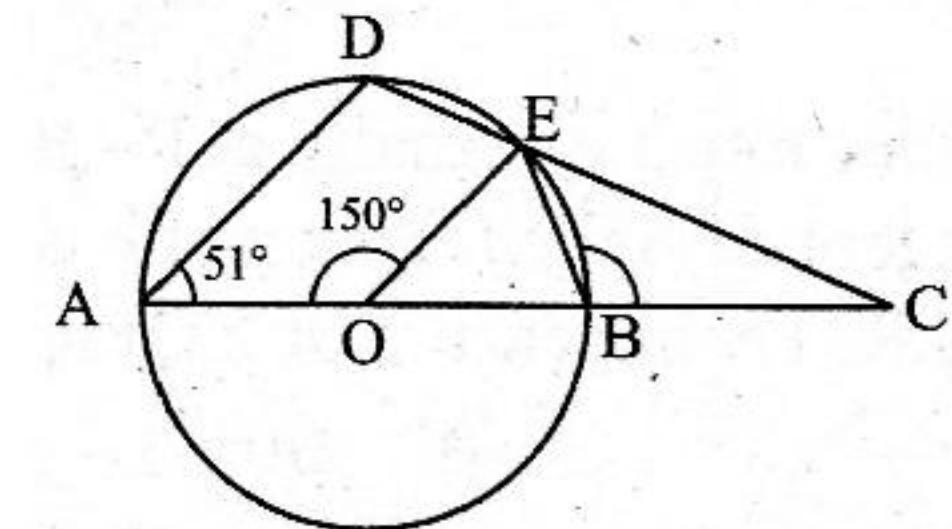
$$23 + \angle BCD = 70$$

$$\angle BCD = 47$$

Ans. (b)

Q44. In the following figure, AB be diameter of a circle whose centre is O, If $\angle AOE = 150^\circ$, $\angle DAO = 51^\circ$, then the measure of $\angle CBE$ is:

- (a) 115°
- (b) 110°
- (c) 105°
- (d) 120°



Ans. (c)

Q45. In the given figure, a circle is inscribed in a quadrilateral ABCD. Given that, $BC = 38 \text{ cm}$, $QB = 27 \text{ cm}$, $DC = 25 \text{ cm}$ and AD is perpendicular to DC . What is the radius of the circle?

- (a) 11 cm
- (b) 14 cm
- (c) 15 cm
- (d) 16 cm

~~(b) 14 cm~~
~~(d) 16 cm~~

