An Introduction to R for Quantitative Methods

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PREFACE

This ebook serves as a companion to the \dots

It pulls from many sources, including \dots

6 CONTENTS

Chapter 1

An Introduction

Getting Started in R with RStudio

\mathbf{R}

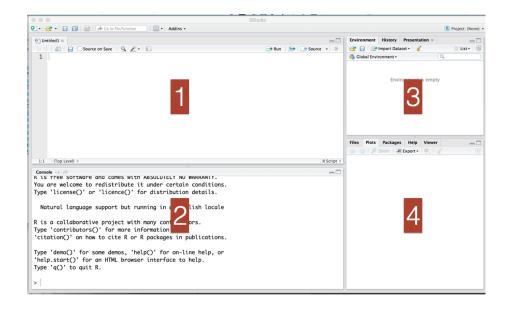
R, like the commercial S-Plus, is based on the statistical programming language S. Unlike S-Plus, it can be downloaded for free from www.r-project.org [Currently, to do so, choose: CRAN, then a mirror site in the US, then Download R for Windows, then base, then "Download R 3.4.0 for Windows"]. This page also has links to FAQs and other information about R.

RStudio

RStudio is an IDE (integrated development environment), and a convenient interface for R. Think of R as like a car's engine and RStudio as a car's dashboard. You can download and install Rstudio from the official Rstudio website.

Once you have both R and Rstudio installed, open Rstudio. You should now see four panels:

- (1) **Source editor**: Docking station for multiple files, Useful shortcuts ("Knit"), Highlighting/Tab-completion, Code-checking (R, HTML, JS), Debugging features
- (2) Console window: Highlighting/Tab-completion, Search recent com-
- (3) Environment pane: Tools for package development, git, etc
- (4) Other tabs/panes: Plots, R documentation, File system navigation/access



Executing code and R script files

You can start coding by typing commands in the Console panel. This window is also where the output will appear. Because this window is used for so many things it often fills up quickly — and so, if you are doing anything involving a large number of steps, it is often easiest to type them in a script first.

You can create a new script by clicking on the "File" menu and selecting "New File" then "R Script". A script is a collection of commands that you can save and run again later. To run a command, click in a given line or highlight the text and hit Ctrl+Enter, or click the "Run" button at the top of the script window. You can save your scripts for later use.

Also very useful are the fact that in the main R Console window, the up and down-arrow on the key-board can be used to scroll through previously entered lines in R, and that history() will open a window of previously entered commands (which we'll see below after entering some). If the font in this R Console is too small, or if you dislike the color or font, you can change it by selecting "Global Options" under the "Tools" menu and clicking on the "Appearance" tab in the pop up window.

RMarkdown

Markdown is a particular type of markup language. Markup languages are designed to produce documents from plain text. Some of you may be familiar with LaTeX, another (less human friendly) markup language for creating pdf documents. LaTeX gives you much greater control, but it is restricted to pdf and has a much greater learning curve.

Markdown is becoming a standard and many websites will generate HTML from Markdown (e.g. GitHub, Stack Overflow, reddit, ...). It is also relatively easy:

```
*italic*
**bold**
# Header 1
## Header 2
### Header 3
- List item 1
- List item 2
- item 2a
- item 2b
1. Numbered list item 1
1. Numbered list item 2
- item 2a
- item 2a
- item 2a
- item 2b
```

Have a look at RStudio's RMarkdown cheat sheet.

RMarkdown is an authoring format that enables easy creation of dynamic documents, presentations, and reports from R. It combines markdown syntax with embedded R code chunks that are run so their output can be included in the final document.





Figure 1.1: Artwork by allison horst

```
🖭 Untitled2 🗶

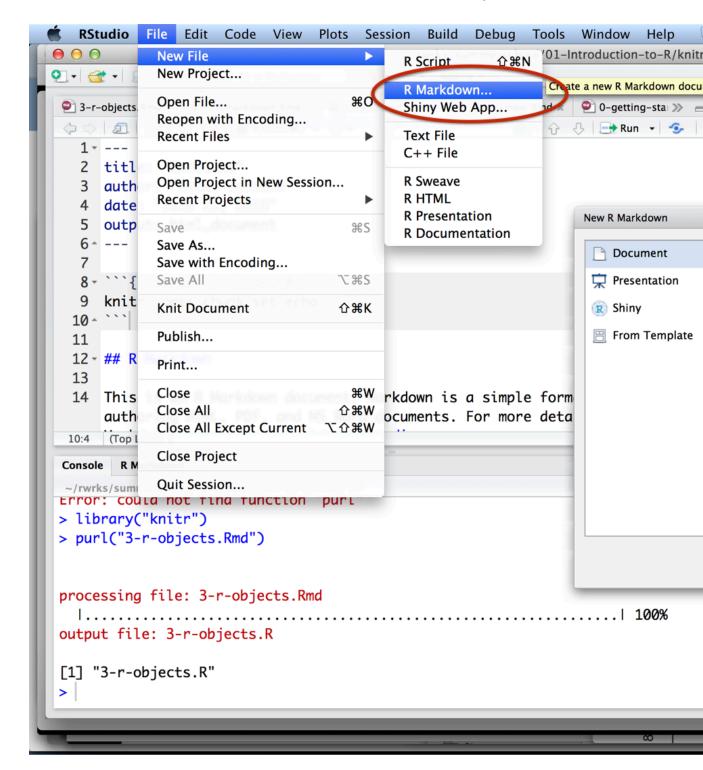
⟨⇒ ⇒ | ∑□ | □ | ABC | ✓ | ✓ Knit HTML ▼ (⊕ ▼)

  1 - ---
  2 title: "first markdown"
    author: "Heike Hofmann"
  3
  4 date: "September 8, 2016"
  5 output: html_document
  6 -
     ```{r setup, include=FALSE}
 knitr::opts_chunk$set(echo = TRUE)
 10 -
 12 - ## R Markdown
 13
 This is an R Markdown document. Markdown is a simple formatting
 14
 HTML, PDF, and MS Word documents. For more details on using R M
 <http://rmarkdown.rstudio.com>.
 15
 When you click the **Knit** button a document will be generated
 16
 content as well as the output of any embedded R code chunks wit
 embed an R code chunk like this:
 17
 18 - ```{r cars}
 19
 summary(cars)
 20 -
 22 - ## Including Plots
 23
 24 You can also embed plots, for example:
 25
14:192 📴 R Markdown 🕏
```

Most importantly, RMarkdown creates fully reproducible reports since each time you knit the analysis is run from the beginning, encouraging transparency. Collaborators (including your future self) will thank you for integrating your analysis and report.

Exercise: Create your first Rmarkdown.

- 1. Open RStudio, create a new project.
- 2. Create a new RMarkdown file and knit it.
- 3. Make changes to the markdown formatting and knit again (use the RMarkdown cheat sheet)
- 4. If you feel adventurous, change some of the R code and knit again.



## 1.1 Objects

At the heart of R are the various objects that you enter. An object could be data (in the form of a single value, a vector, a matrix, an array, a list, or a data frame) or a function that you created. Objects are created by assigning a value to the objects name using either <- or =. For example

```
x < -3
```

All R statements where you create objects, **assignment statements**, have the same form:

```
object_name <- value
```

When reading that code say "object name gets value" in your head.

You will make lots of assignments, and <- is a pain to type. You can save time with **RStudio's keyboard shortcut:** Alt + - (the minus sign). Notice that RStudio automatically surrounds <- with spaces, which is a good code formatting practice. Code is miserable to read on a good day, so giveyoureyesabreak and use spaces.

If you run x <-3 in your local console (at the > prompt), R will only give you another prompt. This is because you merely assigned the value; you didn't ask R to do anything with it. Typing

Х

## [1] 3

will now return the number 3, the value of x. R is case sensitive, so entering

```
X <- 5
X
```

## [1] 5

will create a separate object. If you reassign an object, say:

```
X <- 7
```

the original value is over-written. If you attempt to use the name of a built in function or constant (such as c(), t(), t.test(), or pi()) for one of your variable names, you will likely find that future work you are trying to do gives unexpected results. Notice in the name of t.test() that periods are allowed in names of objects. Other symbols (except numbers and letters) are not allowed.

### Your workspace

Note that the up-arrow and history() will now show us the commands we entered previously. This set of all of your created objects (your Workspace) is not saved when you exit R, and this is purposeful: Attachment to your workspace indicates that you have a non-reproducible workflow. Any individual R process

and the associated workspace is disposable and everything that really matters should be achieved through code that you save in your script.

### Data types in R

- logical: boolean values
  - ex. TRUE and FALSE
- double: floating point numerical values (default numerical type)
  - ex. 1.335 and 7
- integer: integer numerical values (indicated with an L)
  - ex. 7L and 1:3
- character: character string
  - ex. "hello"
- lists: 1d objects that can contain any combination of R objects
- & more, but we won't be focusing on those yet

### 1.2 Arithmetic and Parentheses

Using R can be a lot like using a calculator. All of the basic arithmetic operations work in R:

```
X - x
```

## [1] 4

7 - 3

## [1] 4

will both return the value 4, one by performing the arithmetic on the objects, and the other on the numbers. The other basic mathematical operators are:

- + addition
- - subtraction
- $\bullet$  \* multiplication
- / division
- ^ exponentiation
- %\*% matrix multiplication

R will often try to do the "common-sense" thing when using arithmetic arguments. For example, if Y is a vector or matrix of values, then Y + 4 will add 4 to each of the values in Y. (So the vector 3, 2, 5 would become 7, 6, 9).

Parentheses work as usual in mathematical statements, but they do not imply multiplication.

```
#X(x+5)
X*(x+5)
```



Figure 1.2: Image via Jenny Bryan's 'What They Forgot to Teach You About  ${\mathbb R}^{\prime}$ 

1.3. HELP! 17

```
[1] 56
```

Notice that the former returns an error about looking for a function called X, while the latter does the arithmetic to return the value 40.

The other use of parentheses in R are to indicate that you attempting to run a function, and, if the function has any options it will contain those. The command:

rnorm(10)

```
[1] -0.0525403 -0.2264235 -0.4853508 -1.1381637 1.7838127 -1.6505416
[7] 1.6124078 0.2315971 -0.8013489 -0.4000530
```

runs the function rnorm() with the argument 10. In this case it is generating a random sample of 10 values from a normal distribution.

## 1.3 Help!

To see this, we could run the help function on that command.

```
help(rnorm)
```

A shortcut, ?rnorm, would also work.

Every help file in R begins with a brief description of the function (or group of functions) in question, followed by all of the possible options (a.k.a. Arguments) that you can provide. In this case the value n (the number of observations) is required. Notice that all of the other options are shown as being = some value – this indicates the defaults those values take if you do not enter them. The sample we generated above thus has mean 0 and standard deviation 1.

Below the list of arguments are a brief summary of what the function does (called the *Details*), a list of the *Value* (or values) returned by running the function, the *Source* of the algorithm, and general *References* on the topic. *See Also* is often the most useful part of the help for a function as it provides a list of related functions. Finally, there are some *Examples* that you can cut and paste in to observe the function in action.

### 1.4 Functions

Functions are (most often) verbs, followed by what they will be applied to in parentheses:

```
do_this(to_this)
do_that(to_this, to_that, with_those)
```

It is always safest to enter the values of functions using the names of the arguments:

```
rnorm(10, sd = 4)
 [1] -3.9063761 2.2765973 3.0381877 -0.2588315 0.2878706 2.8585012
 [7] -3.8125093 2.7551731 0.4706417 -7.3545757
rather than trusting that the argument you want happens to be first in the list:
rnorm(10, 4)
 [1] 5.251843 5.547703 5.161922 3.330111 5.293310 4.962238 5.957459 4.872844
 [9] 4.063995 3.671120
Notice the former puts 4 in for the standard deviation, while the latter is putting
```

it in for the second overall argument, the mean (as seen in the help file).

Note that these values we generated have not been saved as an object, and exist solely on the screen. To save the values we could have assigned the output of our function to an object.

```
normal.sample <- rnorm(50)</pre>
normal.sample
 [1] -0.348060697 -0.317068368 -1.022448247 -1.487466210 -0.181647381
##
 [6] -1.674069034 2.013465437 -0.813361887 0.008619126 -1.815510241
 0.597348998 1.075861403 -2.089936716 -0.078590893 -0.030519305
[11]
1.230830390 2.060566337 -0.839316079 0.895362396 -0.735982900
[21]
[26] -0.652895987 -0.341271443 -0.981846480 -2.076386599 -0.200424411
[31] 0.025268773 -0.014000964 0.084182086 1.639351402 -1.622144863
[41]
 1.367258110 -1.044769132 1.807058627 -0.551201001 0.198072472
[46]
 0.139520538 -1.160104931 1.772887892 0.204862913 -0.132317639
```

#### Common statistical functions

A few common statistical functions include:

- mean() find the mean
- median() find the median
- sd() find the standard deviation
- var() find the variance
- quantile() find the quantiles (percentiles);
  - requires the data and the percentile you want
  - e.g. quantile(normal.sample, .5) is the median
- max() find the maximum
- min() find the minimum
- summary() find the 5-number summary
- hist() construct a histogram
- boxplot() construct a boxplot

- qqnorm() construct a normal quantile-quantile plot
- qqline() add the line to a normal quantile-quantile plot

Trying a few of these out (like mean(normal.sample)) will show us the descriptive statistics and basic graphs for a sample of size 50 from a normal population with mean 0 and standard deviation 1. (Using up arrow can make it quicker to try several in a row.)

As we will see in more detail later, it is possible to create your own functions by using the function function. This one creates a simple measure of skewness.

```
Skew <- function(x){
 (mean(x) - median(x))/sd(x)}</pre>
```

Note that braces { } in R are used to group several separate commands together, and also occur when using programming commands like loops or if-then statements. They work the same as parentheses in arithmetic expressions.

After entering or new function, it works like any built in function, except that it appears in our objects list.

```
Skew
Skew()
Skew(normal.sample)
```

## [1] 0.03193353

#### Common mathematical functions

There are also a number of mathematical functions as well. Ones common in statistical applications include:

- sqrt() square root
- exp() exponent (e to the power)
- log() the natural logarithm by default
- abs() absolute values
- floor() round down
- ceiling() round up
- round() round to the nearest (even if .5)

## 1.5 Vectors, Matrices, and Arrays

#### Vectors

The output from  ${\tt rnorm}()$  is different from the X and x we created as it contains more than just a single value - they are vectors. While we can think of them as vectors in the mathematical sense, we can also think of a vector as simply listing the values of a variable.

Vectors in R are created using the c() function (as in concatonate). Thus,

```
Y \leftarrow c(3, 2, 5)
[1] 3 2 5
Y + 4
[1] 7 6 9
Y * 2
[1]
 6 4 10
creates a vector of length three (and we can verify that arithmetic works on it
Z \leftarrow c(1, 2, 3)
```

componentwise). Given two vectors arithmetic is also done componentwise:

```
Y + Z
[1] 4 4 8
Y * Z
```

## [1] 3 4 15

Other functions are also evaluated component-wise (if possible):

```
sqrt(Z)
```

```
[1] 1.000000 1.414214 1.732051
```

Multiple vectors can be combined together by using the  ${\tt c}()$  function:

```
YandZ \leftarrow c(Y, Z)
YandZ
```

```
[1] 3 2 5 1 2 3
```

However, when asked to combine vectors of two different types, R will try to force them to be of the same type:

```
nums <- c(1, 2, 3)
nums
[1] 1 2 3
lttrs <- c("a", "b", "c")
lttrs
[1] "a" "b" "c"
c(nums, lttrs)
```

```
[1] "1" "2" "3" "a" "b" "c"
```

```
c(nums, lttrs) + 2
```

Once we have our desired vector, an element in the vector can be referred to by using square brackets:

```
YandZ[2]
[1] 2
YandZ[2:4]
[1] 2 5 1
YandZ[c(1, 4:6)]
[1] 3 1 2 3
```

By using the c() function, and the : to indicate a sequence of numbers, you can quickly refer to the particular portion of the data you are concerned with.

### Matrices and arrays

Matrices (two-dimensional) and arrays (more than two dimensions) work similarly - they use brackets to find particular values, and all the values in an array or matrix must be of the same type (e.g. numeric, character, or factor). In the case of matrices, the first values in the brackets indicates the desired rows, and the ones after the comma indicate the desired columns.

```
Xmat \leftarrow matrix(c(3, 2, 5, 1, 2, 3),
 ncol = 3, byrow = TRUE)
Xmat
##
 [,1] [,2] [,3]
[1,]
 3
 2
 5
 2
[2,]
 3
 1
Ymat <- rbind(Y, Z)</pre>
Ymat
##
 [,1] [,2] [,3]
Y
 2
 5
Z
 2
 3
 1
Xmat[1, 2:3]
[1] 2 5
Zmat <- cbind(nums, lttrs)</pre>
Zmat
##
 nums lttrs
[1,] "1" "a"
```

```
[2,] "2" "b"
[3,] "3" "c"
```

In the above code, matrix() is the function to form a vector into a matrix, rbind() places multiple vectors (or matrices) side-by-side as the rows of a new matrix (if the dimensions match), and cbind() does the same for columns.

## 1.6 Data Frames, Lists, and Attributes

### Data frames

In many cases the data set we wish to analyze will not have all of the rows or columns in the same format. This type of data is stored in R as a **data frame**. A data frame is a rectangular collection of variables (in the columns) and observations (in the rows).

scdata.txt is one such data set, and it can be found in the course materials (its description is found in scdata.pdf). The data can be read in using code similar to the below (assuming a similar file structure).

```
sctable <- readr::read_table("data/scdata.txt")

##
-- Column specification ------
cols(
.default = col_double(),
County = col_character(),
Region = col_character()
i Use `spec()` for the full column specifications.</pre>
```

### Inspecting objects

To inspect the data without needing to print out the entire data set, we can try out the following commands:

- head()
- tail()
- summary()
- str()
- dim()

For example, use head() and tail() to see the first and last rows. This lets you check the variable names as well as the number of observations successfully read in.

```
head(sctable)
```

```
A tibble: 6 x 27
```

```
##
 County Region Births Death InfMort Minor~1 Over65 PopChng PopDens Urban Income
 <dbl>
##
 <chr> <chr>
 <dbl> <dbl>
 <dbl>
 <dbl>
 <dbl>
 <dbl> <dbl>
1 Abbev~ Upsta~
 12.5
 10.3
 15.1
 14.7
 9.7
 51.5 23.4
 32635
 31.7
2 Aiken Midla~
 12.1
 9.8
 9.6
 28.6
 12.8
 17.8
 133.
 60.9
 37889
3 Allen~ LowCo~
 14.8
 12.1
 18.5
 72.6
 12.7
 -4.4
 27.5
 59
 20898
4 Ander~ Upsta~
 13
 10.7
 10.3
 18.4
 13.7
 14.2
 231.
 58.3
 36807
5 Bambe~ Midla~
 63.5
 42.4 45.7
 11.5
 9.9
 21.7
 13.9
 -1.4
 24007
6 Barnw~ Midla~
 14
 10.9
 21.4
 44.8
 12.6
 15.7
 42.8 14.9
 28591
... with 16 more variables: ConsInc <dbl>, FarmInc <dbl>, ManIncom <dbl>,
 RetInc <dbl>, FdStmps <dbl>, MoblHms <dbl>, NoCar <dbl>, PlumProb <dbl>,
 PoorChild <dbl>, Unemp <dbl>, Coll4 <dbl>, Crime <dbl>, HSGrad <dbl>,
#
 JuvDel <dbl>, MVDeath <dbl>, SchlSpnd <dbl>, and abbreviated variable name
#
 1: Minority
tail(sctable)
A tibble: 6 x 27
 County Region Births Death InfMort Minor~1 Over65 PopChng PopDens Urban Income
 <chr> <chr>
 <dbl>
##
 <dbl> <dbl>
 <dbl>
 <dbl>
 <dbl>
 <dbl> <dbl>
 <dbl>
1 Saluda Midla~
 11.2
 11.3
 4.7
 34.2
 14.5
 16.7
 42.5
 18.7
 35774
2 Spart~ Upsta~
 7.9
 24.9
 12.5
 64.8 37579
 13.1
 9.8
 11.9
 313.
3 Sumter Midla~
 15.6
 8.9
 8.5
 50
 11.2
 3.3
 157.
 62.1
4 Union Upsta~
 10.7
 13.2
 12.8
 32.2
 15.6
 -1.5
 58.1 35.7
 31441
5 Willi~ Peedee
 12.6
 11.8
 8.8
 67.3
 13
 1.1
 39.8
 15.1
 7.6
6 York
 Upsta~
 13.4
 7.7
 22.7
 10.4
 25.2
 241.
 64.3 44539
... with 16 more variables: ConsInc <dbl>, FarmInc <dbl>, ManIncom <dbl>,
 RetInc <dbl>, FdStmps <dbl>, MoblHms <dbl>, NoCar <dbl>, PlumProb <dbl>,
#
 PoorChild <dbl>, Unemp <dbl>, Coll4 <dbl>, Crime <dbl>, HSGrad <dbl>,
 JuvDel <dbl>, MVDeath <dbl>, SchlSpnd <dbl>, and abbreviated variable name
#
#
 1: Minority
```

#### Extracting parts of objects

For object x, we can extract parts in the following manner (rows and columns are vectors of indices):

```
x$variable
x[, "variable"]
x[rows, columns]
x[1:5, 2:3]
x[c(1,5,6), c("County", "Region")]
x$variable[rows]
```

Many of these extraction methods access the rows and columns of a data frame by treating it similarly to a matrix:

```
County1 <- sctable[1,]
Birth.Death <- sctable[, 3:4]</pre>
```

This simplicity sometimes causes trouble though. While Birth.Death may look on the screen like it is a matrix, it is still a data frame and many functions which use matrix operations (like matrix multiplication) will give an error. The attributes() function will show us the true status of our object (it returns NULL for a numeric vector and the dimensions if a matrix):

Birth.Death

```
A tibble: 46 x 2
##
 Births Death
##
 <dbl> <dbl>
 12.5 10.3
##
 1
##
 2
 12.1
 9.8
##
 14.8 12.1
 3
##
 4
 10.7
 13
##
 5
 11.5
 9.9
##
 6
 14
 10.9
##
 7
 15.8
 7.8
##
 8
 14.4
 6.6
##
 11.5 11.1
 9
10
 14.5
 8.5
... with 36 more rows
attributes(Birth.Death)
$names
[1] "Births" "Death"
$row.names
 [1] 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25
[26] 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46
$class
[1] "tbl_df"
 "tbl"
 "data.frame"
BD.matrix <- as.matrix(Birth.Death)</pre>
attributes(BD.matrix)
$dim
[1] 46 2
$dimnames
$dimnames[[1]]
NULL
##
$dimnames[[2]]
[1] "Births" "Death"
```

The \$ is used to access whatever corresponds to an entry in the names attribute:

#### Birth.Death\$Births

```
[1] 12.5 12.1 14.8 13.0 11.5 14.0 15.8 14.4 11.5 14.5 13.3 12.3 12.1 12.3 13.0 ## [16] 12.4 15.6 12.9 10.3 12.8 15.3 12.7 14.0 12.6 13.9 12.7 14.3 12.8 12.2 11.6 ## [31] 12.9 14.0 7.6 13.8 11.9 12.5 11.7 13.8 11.2 13.3 11.2 13.1 15.6 10.7 12.6 ## [46] 13.4
```

This is particularly useful when trying to access a portion of the output of a function for later use. For example, later we will see a method of doing statistical inference called the t-test. In R, this is performed by the function t.test() which can create a great deal of output on the screen.

#### t.test(normal.sample)

```
##
One Sample t-test
##
data: normal.sample
t = -0.44891, df = 49, p-value = 0.6555
alternative hypothesis: true mean is not equal to 0
95 percent confidence interval:
-0.3658978 0.2322749
sample estimates:
mean of x
-0.06681145
```

If you only want the part called the "p-value" for later use we can pull that out of the output.

```
t.out <- t.test(normal.sample)
attributes(t.out)</pre>
```

```
$names
[1] "statistic" "parameter" "p.value" "conf.int" "estimate"
[6] "null.value" "stderr" "alternative" "method" "data.name"
##
$class
[1] "htest"
t.out$p.value
```

### ## [1] 0.6554763

We could then save the resulting value as part of a vector or matrix of other p-values, for example.

The \$ is also used to access named parts of lists, which we will see can be used to store a variety of kinds of information in a single object.

## 1.7 Packages

The ability to "easily" write functions in R has lead to an explosion of procedures that researchers have written and made available to the public, typically as an R package. An R package is a collection of functions, data, and documentation that extends the capabilities of base R. Using packages is key to the successful use of R. For example, the **MASS** package contains all of the functions corresponding to the Springer text *Modern Applied Statistics with S* by Venables and Ripley.

While some of these are automatically included with the basic installation of R, most are not and can installed with the install.packages() function.

```
install.packages("package_name")
```

When you run the code to install a package on your own computer, R will download the packages from CRAN and install them on to your computer.

If you have problems installing, make sure that you are connected to the internet, and that https://cloud.r-project.org/ isn't blocked by your firewall or proxy.

You will not be able to use the functions, objects, and help files in a package until you load it with library().

```
library(package_name)
```

The command library() is used to activate a downloaded package and give access to all of its functions and must be done once per session.

```
help(fractions)
library(MASS)
help(fractions)
fractions(0.5)
```

```
[1] 1/2
```

fractions(pi)

```
[1] 4272943/1360120
```

4272943/1360120

```
[1] 3.141593
```

# Chapter 2

# Graphics

## Outline

### 1. Introduction to ggplot2

- setup
- $\bullet$  why ggplot2
- ullet the evolution of a ggplot
- create your first ggplot

### 2. ggplot2 concepts

- $\bullet$  the grammar of ggplot2
- geometrical layers
- statistical layers
- facets
- ggplots as objects

### 3. Advanced customization

- scales
- coordinates
- labels
- annotations
- $\bullet$  themes
- legends
- fonts

### 4. Extensions

- patchwork
- gganimate

- ggplotly ggiraph

### 2.1 Introduction

setup

intro to ggplot2

why ggplot2

the evolution of a ggplot

create your first ggplot

## 2.2 ggplot2 concepts

the grammar of ggplot2

aesthetic mapping

geometrical layers

geoms

Setting vs Mapping of Visual Properties

Local vs. Global Encoding

**Adding More Layers** 

The group Aesthetic

Overwrite Global Aesthetics

statistical layers

stat\_\*() and geom\_\*()

statistical summaries

facets

Store a ggplot as Object

inspect a ggplot Object

extend a ggplot Object

### 2.3 Advanced customization

scales

continuous vs. discrete

aesthetics + scales

coordinates

labels

annotations

themes

legends

fonts

# Chapter 3

# Transforming Data

## {dplyr} basics

The book R for Data Science is a *very* helpful reference guide. Chapter 5 covers many of the topics covered in this section, and may be useful as a resource later or to dive deeper into a topic.

### 3.1 Filter rows

- Comparisons
- Logical operators
- Missing values

## 3.2 Arrange rows

### 3.3 Select columns

## 3.4 Add new variables

## 3.5 Grouped summaries

- Combining multiple operations with the pipe
- Missing values
- Counts
- Useful summary functions
- Grouping by multiple variables
- Ungrouping

#### 3.6 Grouped mutates (and filters)

#### 3.7 An example

The following example ties several of the above ideas together. Imagine that we have a set of grades from a course that we would like to convert to letter grades using a particular weighting and letter-grade cut-offs.

```
students <- readr::read_table("data/CourseData.txt")[, -1]</pre>
head(students)
A tibble: 6 x 6
 E2
 E3
##
 College Year
 Hmwk
 E1
##
 <dbl> <dbl> <dbl>
 <dbl>
 <dbl>
1 NU
 83.8
 79
 89
 59
2 NU
 77.1
 60
 63
 1
 94.5
3 NU
 1
 83
 88
 69
4 NU
 84.3
 91
 77
 72
 1
5 NU
 1
 73.4
 68
 79
 76
6 NU
 94.7
 89
 96
 79
tail(students)
A tibble: 6 x 6
 E3
##
 College
 Year
 Hmwk
 E1
 E2
##
 <dbl> <dbl> <dbl>
 <dbl>
 <dbl>
1 MC
 2
 83.2
 69
 77
 93
```

95.8 In this particular case we want the weighting to be:

95.7

79.3

78.1

99.1

88

80

69

84

96

89

61

89

89

100

92

97

97

96

100

2

2

2

2

2

- 20% to Hmwk (col 3)
- 25% to E1 (col 4)

## 2 MC

## 3 MC

## 4 MC

## 5 MC

## 6 MC

- 25% to E2 (col 5)
- 30% to E3 (col 6)

But those weights could change later. A function can be written to take the data, and the weights and calculate the weighted average. We can then add that score to the students data frame, and add a final column with the actual letter grades on a 90-80-70-60 scale.

```
students <- students %>%
 mutate(Final = .2*Hmwk + .25*E1 + .25*E2 + .3*E3,
 Grade = case_when(
 Final < 60 \sim "F",
```

```
Final < 69 ~ "D",
 Final < 79 \sim "C",
 Final < 89 \sim "B",
 Final >= 90 ~ "A"))
head(students)
A tibble: 6 x 8
College Year Hmwk E1 E2
 E3 Final Grade
<chr> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
1 NU
 1 83.8 79 89 59 76.5 C
 1 77.1 60 97 63 73.6 C
1 94.5 83 88 69 82.4 B
1 84.3 91 77 72 80.5 B
2 NU
3 NU
4 NU
5 NU 1 73.4 68 79 76 74.2 C
6 NU 1 94.7 89 96 79 88.9 B
```

## 3.8 Extra: Working with factor variables

# Chapter 4

# Reshaping Data

## {tidyr} basics

The book R for Data Science is a *very* helpful reference guide. Chapter 12 covers many of the topics covered in this section, and may be useful as a resource later or to dive deeper into a topic.

- 4.1 Tidy data
- 4.2 Pivoting
- **4.2.1** Longer
- 4.2.2 Wider
- 4.3 Separate & unite

# Chapter 5

# Statistical Analysis

There are a huge variety of statistical tests built in to R for analyzing data. In many cases the same function will perform several different tests and confidence intervals, and produce a large amount of output. We provide examples of many of these functions below, including some that are part of other packages, and others that are custom written functions.

library(tidyverse)

#### Course Data

Most of the examples of the statistical methods in this section are carried out using the data set CourseData. The data is a stratified sample of 70 students from a large section course. The strata were based on the college the students belonged to (AS = Arts & Sciences, PM = Professional Management, MC = Mass Communications, and NU=Nursing) and their year in school (ranging from 1st to 3rd based on credit hours, and limited based on expectation of having at least 10 students from that college at that grade level). The response variables are their Hmwk = Homework Average and E1 to E3 = their grades on the first three exams.

If the data is read in using read\_table() from the readr package and called students, then table(students[, 1:2]) verifies the count of the students in each grouping.

```
students <- readr::read_table("data/CourseData.txt")[, -1]

verify grouping
students %>% dplyr::count(College, Year)
table(students[, 1:2])
```

```
Year

College 1 2 3

AS 10 10 10

MC 10 10 0

NU 10 0 0

PM 10 0 0
```

attach(students) allows you to reference the variables simply by College, Year, Hmwk, E1, E2, and E3.

```
attach(students)
```

If you have attached the dataset, some useful subsets of the data can be created to give the different types of scores by group. For example:

```
E1 for 1st year nursing students
E1.1NU <- E1[(College == "NU") & (Year == 1)]

E1 for 1st year arts & sciences students
E1.1AS <- E1[(College == "AS") & (Year == 1)]

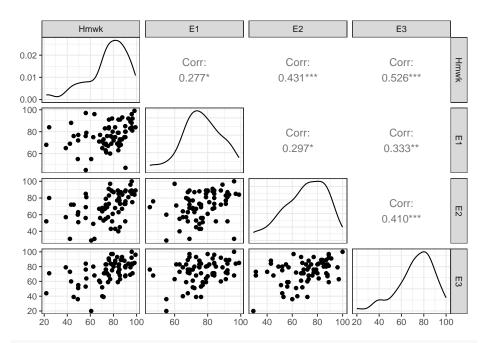
E3 for 1st year nursing students
E3.1NU <- E3[(College == "NU") & (Year == 1)]

Put Year and College together
grp <- as.factor(pasteO(Year, College))
students <- students %>%
 mutate(grp = as.factor(pasteO(Year, College)))
```

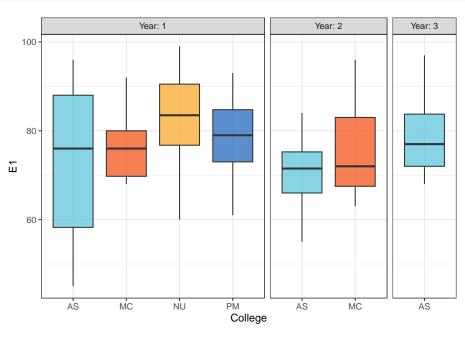
More detail on choosing subsets like this are covered in the upcoming section on Manipulating Data.

There are a variety of graphical tools we could use to get an overview of the data set, and we will see a number of them in the upcoming section on Graphics. Two of note include:

```
GGally::ggpairs(students[, 3:6])
```



ggplot(students, aes(College, E1)) +
 geom\_boxplot(aes(fill = stage(College, after\_scale = alpha(fill, 0.8))), show.legend = FALSE) +
 facet\_grid(~Year, scales = "free", space = "free\_x", labeller = labeller(Year = label\_both))



The coverage of the different methods below is divided into several sections:

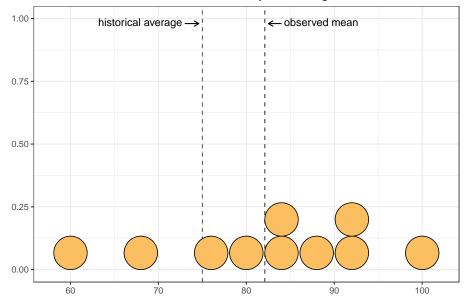
- 1. One-sample t-test
- 2. Other Basic Hypothesis Tests
- 3. One-way ANOVA and Multiple Comparisons
- 4. Regression, Factorial ANOVA, and ANCOVA
- 5. Other Methods

Each of them assumes you have created and attached the data frame students and created the objects E1.1NU, E1.1AS, E3.1NU, and grp.

### 5.1 One-sample t-test and interval

Test the null hypothesis that the mean score on E1 for 1st year nursing students is greater than the historical exam average of 75.

Distribution of scores on Exam 1 for 1st year nursing students



```
students %>%
 dplyr::filter(College == "NU") %>%
 infer::t_test(response = E1, mu = 75, alternative = "greater") %>%
 pander::pander()
```

statistic	$t_ddf$	$p\_value$	alternative	estimate	lower_ci	upper_ci
1.906	9	0.04452	greater	82.1	75.27	Inf

**Note** that this produces a one-sided confidence bound because of the alternative

selected. To get the standard 95% interval in the solutions, run it without the alternative = "greater" part (you don't need to specify "two-sided" because that is the default setting). The other option is "less".

Using help(t\_test) we can also see that the default null hypothesis is mu = 0, the function can perform the two-sample tests, and conf\_level controls the confidence level for the confidence intervals.

In some cases it is useful to be able to retrieve only part of the output from a test. For example, a simulation study might only want to use the p-values. Because infer::t\_test() returns a data frame, the values can easily be extracted.

```
students %>%
 dplyr::filter(College == "NU") %>%
 infer::t_test(response = E1, mu = 75, alternative = "greater") %>%
 pull(p_value)
```

```
[1] 0.04451704
```

If we save the output as an object, the values can be accessed using the \$. For example:

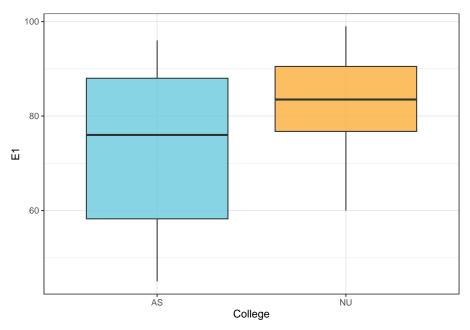
```
t.out <- students %>%
 dplyr::filter(College == "NU") %>%
 infer::t_test(response = E1, mu = 75, alternative = "greater")
t.out$p_value
```

```
[1] 0.04451704
```

## 5.2 Other Basic Hypothesis Tests

#### 5.2.1 Two-sample t-test and interval

Test the null hypothesis that the mean on E1 for 1st year students from arts and sciences is less than the mean for 1st year students from nursing.

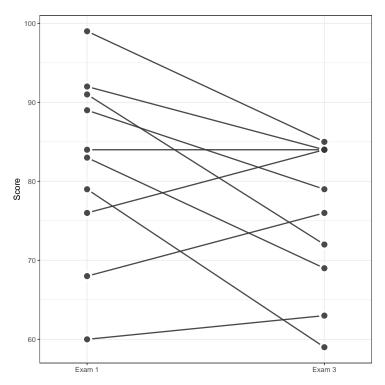


statistic	t_df	p_value	alternative	estimate	lower_ci	upper_ci
-1.385	18	0.09152	less	-9.6	-Inf	2.421

var.equal = TRUE specifies use of the equal variances assumption. The default
is variances not equal (or use var.equal = FALSE). Again, the confidence interval gotten using this code is the one-sided confidence bound. Use two-sided to
get the confidence interval.

#### 5.2.2 Paired t-test and confidence interval

Test that the mean for E3 is greater than the mean of E1 for first year nursing students.



```
students %>%
 dplyr::filter(College == "NU") %>%
 mutate(Change = E3 - E1) %>%
 infer::t_test(response = Change, alternative = "greater") %>%
 pander::pander()
```

statistic	$t_df$	p_value	alternative	estimate	lower_ci	upper_ci
-1.962	9	0.9593	greater	-6.6	-12.77	Inf

Another option for conducting a paired t-test is to use the t.test() function with paired = T. The output, of course, is the same as conducting the one-sample t test on the differences.

```
The correct paired test
t.test(E3.1NU, E1.1NU, alternative = "greater", paired = T)
##
```

```
Paired t-test
##
data: E3.1NU and E1.1NU
t = -1.962, df = 9, p-value = 0.9593
```

### 5.2.3 Chi-square test and interval for one variance

Test whether the standard deviation of E1 is greater than 10 for the first year nursing students.

R doesn't have this test built in (which isn't that horrible since we should probably never do it... but it does make it odd that they have the F-test for two variances then.) In any case its pretty easy to write a function to do it. To analyze the data, cut and paste the function in, and then run it on your data. Or, it can be read in using source("code/TWRfns.txt").

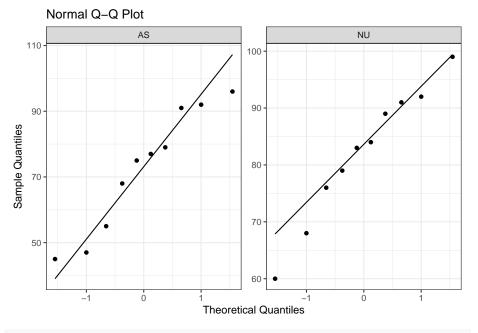
```
chisquare.var <- function(y, sigma2 = 1, alpha = 0.05) {</pre>
 n <- length(y)
 chisquare \leftarrow (n-1) * var(y) / sigma2
 pval.low <- pchisq(chisquare, df = n - 1)</pre>
 pval.hi <- 1 - pchisq(chisquare, df = n - 1)</pre>
 pval.not <- 2 * min(pval.low, pval.hi)</pre>
 cilow \leftarrow (n-1) * var(y) / gchisq(1 - alpha / 2, df = n - 1)
 cihi \leftarrow (n-1) * var(y) / qchisq(alpha / 2, df = n-1)
 list(
 chisquare = chisquare, pval.for.less.than = pval.low,
 pval.for.greater.than = pval.hi, pval.for.not.equal = pval.not,
 ci.for.variance = c(cilow, cihi), ci.for.sd = c(sqrt(cilow), sqrt(cihi))
}
chisquare.var(E1.1NU, sigma2 = 10^2)
$chisquare
[1] 12.489
##
$pval.for.less.than
[1] 0.8128762
$pval.for.greater.than
[1] 0.1871238
$pval.for.not.equal
[1] 0.3742476
##
```

```
$ci.for.variance
[1] 65.65291 462.48884
##
$ci.for.sd
[1] 8.102648 21.505554
```

Note that the confidence intervals here are sub-optimal in terms of length because they place an equal amount of area in each end.

#### 5.2.4 F test for two variances

Test whether the variance of E1 for the first year nursing students is equal to the variance of E1 for the first year arts and sciences students.



```
var.test(E1.1NU, E1.1AS)
```

```
##
F test to compare two variances
##
data: E1.1NU and E1.1AS
F = 0.40595, num df = 9, denom df = 9, p-value = 0.1954
alternative hypothesis: true ratio of variances is not equal to 1
95 percent confidence interval:
0.1008318 1.6343456
sample estimates:
ratio of variances
```

## 0.4059483

## -14.382926

## sample estimates: ## mean of x mean of y 8.9

#### 5.2.5Two-sample Modified Levene's Test

3.182926

14.5

Test of whether the variance of E1 for the first year nursing students is equal to the variance of E1 for the first year arts and sciences students.

R doesn't contain a built in function for the Modified Levene's test, but it can be carried out simply by running the two sample t.test on the right values.

```
##
##
 Two Sample t-test
##
data: abs(E1.1NU - median(E1.1NU)) and abs(E1.1AS - median(E1.1AS))
t = -1.3395, df = 18, p-value = 0.1971
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
```

t.test(abs(E1.1NU - median(E1.1NU)), abs(E1.1AS - median(E1.1AS)), var.equal = T)

Of course the means this is testing about are the means of the absolute deviation from the median. If that measure of spread is different between the two populations, then the variances should be different as well.

The packages car and lawstat have built in modified Levene's test functions, but they require having a response variable and a group variable (like in ANOVA). An easy function for the two sample case would be:

```
levene2 <- function(data1, data2) {</pre>
 print("p-value for testing null hypothesis of equal variances")
 t.test(abs(data1 - median(data1)), abs(data2 - median(data2)), var.equal = T)$p.value
levene2(E1.1NU, E1.1AS)
```

```
[1] "p-value for testing null hypothesis of equal variances"
[1] 0.1970608
```

#### One-way ANOVA and Multiple Compar-5.3 isons

#### 5.3.1 One-way ANOVA

Test whether the means of E1 are equal for the seven populations of students.

lm(E1 ~ grp)

The basic function for conducting an ANOVA (or any linear model) is lm():

```
##
Call:
lm(formula = E1 ~ grp)
Coefficients:
 (Intercept)
##
 grp1MC
 grp1NU
 grp1PM
 grp2MC
 grp2AS
##
 72.5
 3.8
 9.6
 5.6
 -1.8
 3.3
##
 grp3AS
##
```

The ~ indicates that you are specifying a model equation. The variable to the left of the tilde is the response variable, and the variable to the right is the predictor variable. (In multiple regression and more complicated ANOVA there can be multiple predictor variables).

Unfortunately the output from lm() seems pretty meager - it is just the estimates of the parameters in the model equation. Using:

```
attributes(lm(E1 ~ grp))
```

```
$names
 [1] "coefficients"
 "residuals"
 "effects"
 "rank"
 [5] "fitted.values" "assign"
 "qr"
 "df.residual"
 [9] "contrasts"
 "xlevels"
 "call"
 "terms"
[13] "model"
##
$class
[1] "lm"
```

shows that there is a lot more behind the scenes. The functions anova(), summary(), broom::glance(), and broom::augment() can be used to extract much of this information.

```
E1fit <- lm(E1 ~ grp)
anova(E1fit)

Analysis of Variance Table

##
Response: E1
Df Sum Sq Mean Sq F value Pr(>F)

grp 6 907.3 151.22 1.1563 0.341

Residuals 63 8239.0 130.78

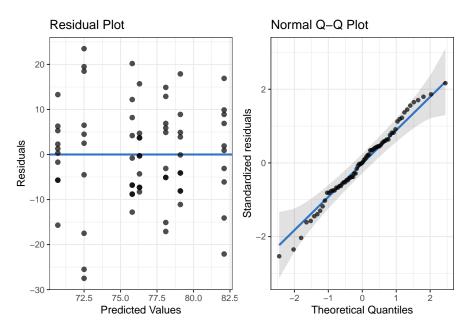
summary(E1fit)
```

## # A tibble: 70 x 8

```
Call:
lm(formula = E1 ~ grp)
##
Residuals:
 Min
 1Q Median
 3Q
 Max
-27.50 -6.80 0.10
 6.45 23.50
##
Coefficients:
 Estimate Std. Error t value Pr(>|t|)
##
(Intercept) 72.500
 3.616 20.048
 <2e-16 ***
 5.114 0.743
grp1MC
 3.800
 0.4602
grp1NU
 9.600
 5.114
 1.877
 0.0651 .
grp1PM
 5.600
 5.114
 1.095
 0.2777
grp2AS
 -1.800
 5.114 -0.352
 0.7260
grp2MC
 3.300
 5.114
 0.645
 0.5211
 6.600
 1.291
 0.2016
grp3AS
 5.114

Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Residual standard error: 11.44 on 63 degrees of freedom
Multiple R-squared: 0.0992, Adjusted R-squared: 0.01341
F-statistic: 1.156 on 6 and 63 DF, p-value: 0.341
broom::tidy(E1fit)
A tibble: 7 x 5
 term
 estimate std.error statistic p.value
##
 <chr>
 <dbl> <dbl> <dbl>
 <dbl>
1 (Intercept)
 72.5
 3.62
 20.0 4.87e-29
2 grp1MC
 5.11
 0.743 4.60e- 1
 3.8
3 grp1NU
 9.6
 5.11
 1.88 6.51e- 2
4 grp1PM
 5.60
 5.11
 1.09 2.78e- 1
5 grp2AS
 -1.80
 5.11
 -0.352 7.26e- 1
6 grp2MC
 3.30
 5.11
 0.645 5.21e- 1
 1.29 2.02e- 1
7 grp3AS
 6.60
 5.11
broom::glance(E1fit)
A tibble: 1 x 12
 r.squ~1 adj.r~2 sigma stati~3 p.value
 df logLik
 AIC
 BIC devia~4 df.re~5
 <dbl>
 <dbl> <dbl> <dbl>
##
 <dbl> <dbl> <dbl> <dbl> <dbl> <
 <dbl>
 <int>
1 0.0992 0.0134 11.4
 1.16
 0.341
 6 -266. 548. 566.
 8239
... with 1 more variable: nobs <int>, and abbreviated variable names
 1: r.squared, 2: adj.r.squared, 3: statistic, 4: deviance, 5: df.residual
broom::augment(E1fit)
```

```
##
 E1 grp
 .fitted .resid .hat .sigma .cooksd .std.resid
##
 <dbl> <fct>
 <dbl>
 <dbl> <dbl> <dbl>
 <dbl>
##
 79 1NU
 82.1 -3.10 0.100
 11.5 0.00130
 -0.286
 1
 60 1NU
 11.1 0.0659
##
 82.1 -22.1
 0.100
 -2.04
 83 1NU
3
 0.900 0.100
 11.5 0.000109
 82.1
 0.0830
4
 91 1NU
 82.1
 8.90 0.1
 11.5 0.0107
 0.820
5
 68 1NU
 82.1 -14.1
 0.1
 11.4 0.0268
 -1.30
 6.90 0.1
6
 89 1NU
 82.1
 11.5 0.00642
 0.636
7
 82.1 -6.10 0.1
 76 1NU
 11.5 0.00502
 -0.562
8
 92 1NU
 82.1
 9.90 0.1
 11.5 0.0132
 0.913
9
 84 1NU
 82.1
 1.90 0.1
 11.5 0.000487
 0.175
10
 99 1NU
 82.1 16.9
 0.1
 11.3 0.0385
 1.56
... with 60 more rows
\# par(mfrow = c(1, 2))
plot(E1fit, 1)
plot(E1fit, 2)
\# par(mfrow = c(1, 1))
E1fit_resids <- broom::augment(E1fit) %>%
 ggplot(aes(x = .fitted, y = .resid)) +
 geom_hline(yintercept = 0, color = "#3273c2", size = 1) +
 geom_point(size = 2, alpha = 0.7) + #shape = 1) +
 labs(title = "Residual Plot",
 x = "Predicted Values",
 y = "Residuals")
devtools::install_github("aloy/qqplotr")
E1fit_qqplot <- broom::augment(E1fit) %>%
 ggplot(aes(sample = .std.resid)) +
 qqplotr::geom_qq_band(fill = "#363636", alpha = 0.15) +
 stat qq line(color = "#3273c2", size = 1) +
 stat_qq(size = 1.5, alpha = .7) +
 labs(x = "Theoretical Quantiles",
 y = "Standardized residuals",
 title = "Normal Q-Q Plot")
library(patchwork)
E1fit_resids + E1fit_qqplot
```



The first is the residual vs. predicted plot, and the second is the qq-plot of the residuals.

In some cases it is necessary to enter the data on your own, and then it is important to be sure that the group variable is a "factor". For example, imagine that you had the vector E1 entered, but did not have the vector of group memberships yet. We know however that the test scores go with different groups in sets of 10 (observations 1-10 are 1NU, 11-20 are 1PM, etc...). One way we could do a set of labels is:

```
grplabs <- c(
 rep(1, 10), rep(2, 10), rep(3, 10),
 rep(4, 10), rep(5, 10), rep(6, 10), rep(7, 10)
)
grplabs</pre>
```

The rep repeats the value in the first spot the number of times indicated in the second. Trying

```
lm(E1 ~ grplabs)
```

```
##
Call:
lm(formula = E1 ~ grplabs)
##
```

```
Coefficients:
(Intercept) grplabs
78.6429 -0.5679
```

gives a very different result from before though. Because the predictor variable is numeric, by default it attempted to do a regression instead of an ANOVA. Using:

```
grplabs <- as.factor(grplabs)</pre>
lm(E1 ~ grplabs)
##
Call:
lm(formula = E1 ~ grplabs)
##
Coefficients:
(Intercept)
 grplabs2
 grplabs3
 grplabs4
 grplabs5
 grplabs6
##
 82.1
 -4.0
 -9.6
 -11.4
 -3.0
 -5.8
##
 grplabs7
##
 -6.3
```

solves that problem. If we had entered the names of the various groups in quotation marks, instead of 1-7, then the grplabs would have been characters instead of numeric, and it would have worked without being factors (although some other functions might give a warning message).

#### 5.3.2 Modified Levene Test

Test whether the variances of E2 are equal for the seven populations of students.

The modified Levene test is available in the package car, so if that package has been downloaded it could be conducted using.

#### 5.3.3 All Pairwise Comparisons - Tukey's HSD and Scheffe

Simultaneously construct confidence intervals around the differences in the mean of E2 between each pair of groups, or test the hypotheses of equality of the mean E2 score between each pair of groups.

R has a built in function TukeyHSD that will construct the intervals in the balanced case, and includes an adjustment for the slightly unbalanced cases.

```
TukeyHSD(aov(E2 ~ grp))
```

```
Tukey multiple comparisons of means
##
 95% family-wise confidence level
##
Fit: aov(formula = E2 ~ grp)
##
##
 $grp
##
 diff
 lwr
 upr
 p adj
1MC-1AS
 16.7
 -3.8321876 37.232188 0.1853530
 2.6678124 43.732188 0.0169654
1NU-1AS
 23.2
1PM-1AS
 6.5 -14.0321876 27.032188 0.9597899
2AS-1AS
 0.8 -19.7321876 21.332188 0.9999997
2MC-1AS
 19.8 -0.7321876 40.332188 0.0657667
 14.9
3AS-1AS
 -5.6321876 35.432188 0.3049582
 6.5 -14.0321876 27.032188 0.9597899
1NU-1MC
1PM-1MC -10.2 -30.7321876 10.332188 0.7360677
2AS-1MC -15.9 -36.4321876 4.632188 0.2336176
 3.1 -17.4321876 23.632188 0.9992362
2MC-1MC
3AS-1MC
 -1.8 -22.3321876 18.732188 0.9999677
1PM-1NU -16.7 -37.2321876 3.832188 0.1853530
2AS-1NU -22.4 -42.9321876 -1.867812 0.0237608
2MC-1NU
 -3.4 -23.9321876 17.132188 0.9987091
3AS-1NU
 -8.3 -28.8321876 12.232188 0.8792779
2AS-1PM -5.7 -26.2321876 14.832188 0.9789714
2MC-1PM
 13.3 -7.2321876 33.832188 0.4417963
 8.4 -12.1321876 28.932188 0.8731517
3AS-1PM
2MC-2AS
 19.0
 -1.5321876 39.532188 0.0876541
3AS-2AS
 14.1 -6.4321876 34.632188 0.3702996
3AS-2MC
 -4.9 -25.4321876 15.632188 0.9903950
```

The structure is a little inelegant (it uses aov, an alternate to anova on the original lm statement). The output is also not in the prettiest form... although that might be the only form that works if it is unbalanced.

As an alternative the function allpairs below will make the "prettier" display for either Tukey's HSD or Scheffe's method in the case where the different groups/treatments all have the same sample size. To run it, simply copy in the function as is, and then run it with the appropriate data.

```
The following function performs all pairwise comparisons using either Tukey's HSD (
The function only needs to be copied in once.
NOTE: This function requires that all treatments have # equal sample size.
allpairs <- function(y, treat, method = "Tukey", alpha = 0.05) {</pre>
```

```
dat.reord <- order(treat)</pre>
treat <- treat[dat.reord]</pre>
y <- y[dat.reord]</pre>
s2w \leftarrow anova(lm(y \sim treat))[2, 3]
t <- length(table(treat))
n <- length(y) / t
df \leftarrow n * t - t
qval <- qtukey(1 - alpha, t, df)
if (method == "Tukey") {
 stat <- qval * sqrt(s2w / n)</pre>
if (method == "Scheffe") {
 stat <-
 sqrt(2 * s2w / n * (t - 1) * qf(1 - alpha, t - 1, df))
}
chars <- c(
 "A ", "B ", "C ", "D ", "E ", "F ", "G ", "H ",
 "I", "J", "L", "M", "N", "O", "P", "Q"
means <- tapply(y, treat, mean)</pre>
ord.means <- order(-means)</pre>
treat <- treat[ord.means]</pre>
means <- means[ord.means]</pre>
grp <- 1
current <- 1
last <- 0
lastsofar <- 0
charmat <- NULL
while (last < t) {
 newchar <- rep(" ", t)</pre>
 for (i in current:t) {
 if (abs(means[current] - means[i]) < stat) {</pre>
 newchar[i] <- chars[grp]</pre>
 last <- i
 }
 }
 current <- current + 1</pre>
 if (last > lastsofar) {
 charmat <- cbind(charmat, newchar)</pre>
 grp <- grp + 1
 lastsofar <- last
 }
}
charmat <- apply(charmat, 1, "paste", sep = "", collapse = "")</pre>
list(
```

```
Method = paste(method, ", alpha=", as.character(alpha),
 sep = "", collapse = ""
),
 Critical.Val = stat,
 Display = data.frame(Grp = charmat, Mean = means)
}
allpairs(E2, grp)
$Method
[1] "Tukey, alpha=0.05"
$Critical.Val
[1] 20.53219
##
$Display
##
 Grp Mean
1NU A
 81.9
2MC A B 78.5
1MC A B 75.4
3AS A B 73.6
1PM A B 65.2
2AS
 B 59.5
1AS
 B 58.7
allpairs(E2, grp, method = "Scheffe")
$Method
[1] "Scheffe, alpha=0.05"
##
$Critical.Val
[1] 24.75036
##
$Display
##
 Grp Mean
1NU A 81.9
2MC A 78.5
1MC A 75.4
3AS A 73.6
1PM A 65.2
2AS A 59.5
1AS A 58.7
```

The built-in function pairwise.t.test will conduct all of the pairwise tests using

the step-wise Bonferonni procedure. In the balanced case that will be very suboptimal compared to Tukey's HSD. In the case where the decision to test is after examining the data then it won't have the protection of Scheffe.

#### 5.3.4 Comparison to a Control - Dunnett's method

Simultaneously construct confidence intervals around the differences for the E2 means between the 1st year nursing students (the control) and all of the others, or test the corresponding hypotheses of equality.

There are several packages in R that contain ways of doing Dunnett's method... but they are all rather opaque. The following function carries it out when the data is balanced. Again, simply copy the entire function in, and then run it on your data. The value for the control is which of the treatments/groups is the control (the order it occurs if you do levels() on the group variable).

The following function performs Dunnett's comparison with a control. The default alternative is the two-sided hypothesis, "greater" tests the alternate hypothesis that the other treatments have a larger mean than the control, and "less" tests for smaller means. The function only needs to be copied in once. Note that this function requires that all treatments have equal sample size.

```
library(MCPMod)
dunnett <- function(y, treat, control = 1, alternative = "two.sided", alpha = 0.05) {</pre>
 dat.reord <- order(treat)</pre>
 treat <- treat[dat.reord]</pre>
 y <- y[dat.reord]
 s2w <- anova(lm(y ~ treat))[2, 3]
 t <- length(table(treat))
 n <- length(y) / t</pre>
 if (alternative == "two.sided") {
 alt <- TRUE
 if (alternative != "two.sided") {
 alt <- FALSE
 }
 dval <- critVal(rbind(-1, diag(t - 1)), rep(n, t), alpha = alpha, twoSide = alt)</pre>
 D \leftarrow dval * sqrt(2 * s2w / n)
 comp <- NULL
 yimyc <- NULL
 sig <- NULL
 count <- 0
 for (i in ((1:t)[-control])) {
 count <- count + 1
 comp <- rbind(comp, paste(as.character(treat[i * n]), "-", as.character(treat[control * n])))</pre>
 yimyc <- rbind(yimyc, mean(y[treat == treat[i * n]]) -</pre>
 mean(y[treat == treat[control * n]]))
```

```
sigt <- ""
 if (((yimyc[count, 1]) >= D) & (alternative != "less")) {
 sigt <- "***"
 if (((yimyc[count, 1]) <= (-D)) & (alternative != "greater")) {</pre>
 sigt <- "***"
 sig <- rbind(sig, sigt)</pre>
 }
 out.order <- order(-yimyc)</pre>
 list(
 Method = paste("Dunnett, alternative=", alternative, ",", " alpha=",
 as.character(alpha),
 sep = "", collapse = ""
),
 Critical.D = D, Differences = data.frame(
 Comparison = comp[out.order],
 Observed.Diff = yimyc[out.order], Significant = sig[out.order]
)
)
}
notice that 1st year nursing students are the 3rd group
levels(grp)
[1] "1AS" "1MC" "1NU" "1PM" "2AS" "2MC" "3AS"
dunnett(E2, grp, control = 3)
$Method
[1] "Dunnett, alternative=two.sided, alpha=0.05"
$Critical.D
[1] 17.7856
##
$Differences
 Comparison Observed.Diff Significant
##
1 2MC - 1NU
 -3.4
2 1MC - 1NU
 -6.5
3 3AS - 1NU
 -8.3
4 1PM - 1NU
 -16.7
5 2AS - 1NU
 -22.4

6 1AS - 1NU
 -23.2

```

# 5.3.5 Specific Contrasts - Step-wise Bonferroni and Scheffe

Simultaneously test whether the mean E2 score of 1st year CAS students is different from the mean of the other 1st year students, whether the mean E2 score of 1st year CAS students is different from the mean score of the other years of CAS students, and whether the mean of E2 for the 1st year Mass Communication Students is different from the mean of the 1st year Professional Management Students

There are a number of (fairly opaque) functions in R to do contrasts. The function below works fairly nicely in the case where all the treatments are balanced. To run the function, simply copy it in once, and then enter the lines to test your particular set of contrasts.

```
The following function estimates specific contrasts and adjusts them by either using the step-
For the step-down Bonferroni the final p-value reported is already adjusted and just needs to
For Scheffe, both the final p-value and a confidence interval (default of 95%) are reported.
The contrast matrix must be entered in a specific format for the function to work (see the exa
The function only needs to be copied in once.
NOTE: This function requires that all treatments have equal sample size.
contrasts <- function(y, treat, control.mat, method = "StepBon", conf.level = 0.95, digits = 4)
 dat.reord <- order(treat)</pre>
 treat <- treat[dat.reord]</pre>
 y <- y[dat.reord]</pre>
 s2w <- anova(lm(y ~ treat))[2, 3]</pre>
 t <- length(table(treat))
 n <- length(y) / t
 ncontrasts <- nrow(control.mat)</pre>
 contrastmat <- matrix(as.numeric(control.mat[, 2:(t + 1)]),</pre>
 nrow = nrow(control.mat)
 colnames(contrastmat) <- levels(treat)</pre>
 divisors <- as.numeric(control.mat[, (t + 3)])</pre>
 contrastd <- contrastmat / divisors</pre>
 cnames <- control.mat[, 1]</pre>
 means <- tapply(y, treat, mean)</pre>
 L <- contrastd %*% means
 seL <- sqrt((s2w / n) * apply(contrastd^2, 1, sum))</pre>
 t.stat <- L / seL
 Unadj.p \leftarrow 2 * pt(-abs(t.stat), df = n * t - t)
 baseout <- data.frame(Contrast = cnames, contrastmat, Div = divisors)</pre>
 meth <- method
 if (method == "StepBon") {
 StepBon.p <- Unadj.p * rank(-Unadj.p)</pre>
 ord.un <- order(Unadj.p)</pre>
```

```
for (i in 2:ncontrasts) {
 if (StepBon.p[ord.un[i]] <= StepBon.p[ord.un[i - 1]]) {</pre>
 StepBon.p[ord.un[i]] <-</pre>
 StepBon.p[ord.un[i - 1]]
 if (StepBon.p[ord.un[i]] > 1) {
 StepBon.p[ord.un[i]] <- 1</pre>
 }
 out <- data.frame(</pre>
 Contrast = cnames, 1 = round(L, digits),
 se = round(seL, digits), t = round(t.stat, digits), raw.p = round(Unadj.p, digit
 stepBon.p = round(StepBon.p, digits)
 }
 if (method == "Scheffe") {
 S \leftarrow seL * sqrt((t-1) * qf(conf.level, t-1, n * t-t))
 Scheffe.p <-1 - pf((abs(L) / (seL * sqrt(t - 1)))^2, t - 1, n * t - t)
 CL.low <- L - S
 CL.hi <- L + S
 out <- data.frame(</pre>
 Contrast = cnames, 1 = round(L, digits),
 se = round(seL, digits), t = round(t.stat, digits), raw.p = round(Unadj.p, digits)
 Scheffe.p = round(Scheffe.p, digits), S = round(S, 4), CL.low = round(CL.low, 4)
 CL.hi = round(CL.hi, 4)
 meth <- paste(method, ", conf.level=", as.character(conf.level), sep = "", collaps</pre>
 }
 list(Method = meth, Definitions = baseout, Results = out)
Note the levels order is "1AS" "1MC" "1NU" "1PM" "2AS" "2MC" "3AS"
levels(grp)
[1] "1AS" "1MC" "1NU" "1PM" "2AS" "2MC" "3AS"
Setting up the matrix of contrasts
first line will always look like this
control.mat <- matrix(</pre>
 #' name of contrast', coefficient list, 'divisor=', divisor value,
 "1AS vs. 10ther", 3, -1, -1, -1, 0, 0, 0, "divisor=", 3,
 "1AS vs. 2+3AS2", 2, 0, 0, 0, -1, 0, -1, "divisor=", 2,
 "1MC vs. 1PM ", 0, 1, 0, -1, 0, 0, 0, "divisor=", 1
```

```
the end of the last row will always be this, although your nrow
 # needs to match the number of contrasts
 byrow = T, nrow = 3
)
contrasts(E2, grp, control.mat, method = "StepBon")
$Method
[1] "StepBon"
##
$Definitions
 Contrast X1AS X1MC X1NU X1PM X2AS X2MC X3AS Div
1 1AS vs. 10ther 3 -1
 -1
 -1
 0
2 1AS vs. 2+3AS2
 2
 0
 0
 0
 -1
 0
 -1
 2
3 1MC vs. 1PM
 0
 1
 0
 -1
 0
 0
 0
 1
##
$Results
 Contrast
 1
 t raw.p stepBon.p
 se
1 1AS vs. 10ther -15.4667 5.5045 -2.8098 0.0066
 0.0198
2 1AS vs. 2+3AS2 -7.8500 5.8384 -1.3446 0.1836
 0.2706
3 1MC vs. 1PM
 10.2000 6.7416 1.5130 0.1353
 0.2706
contrasts(E2, grp, control.mat, method = "Scheffe")
$Method
[1] "Scheffe, conf.level=0.95"
##
$Definitions
##
 Contrast X1AS X1MC X1NU X1PM X2AS X2MC X3AS Div
1 1AS vs. 10ther 3 -1
 -1
 -1
 0
 -1
 2
2 1AS vs. 2+3AS2
 2
 0
 0
 0
 0
 -1
3 1MC vs. 1PM
 0
 1
 0
 -1
 0
 0
 1
##
$Results
##
 Contrast
 1
 t raw.p Scheffe.p
 S CL.low
 se
1 1AS vs. 10ther -15.4667 5.5045 -2.8098 0.0066 0.2633 20.2086 -35.6753
2 1AS vs. 2+3AS2 -7.8500 5.8384 -1.3446 0.1836 0.9340 21.4344 -29.2844
 10.2000 6.7416 1.5130 0.1353 0.8881 24.7504 -14.5504
3 1MC vs. 1PM
##
 CL.hi
1 4.7419
2 13.5844
3 34.9504
```

##

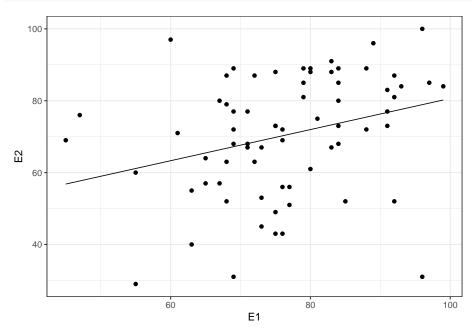
# 5.4 Regression, Factorial ANOVA, and AN-COVA:

### 5.4.1 Simple Linear Regression

Predict the E2 scores from the E1 scores.

R has a large number of functions for analyzing regression data, the most basic ones the same as those for one-way ANOVA.

```
scatterplot with fitted line
ggplot(students, aes(E1, E2)) +
 geom_point() +
 geom_smooth(method = "lm", se = FALSE, color = "black", linewidth = 0.4)
```

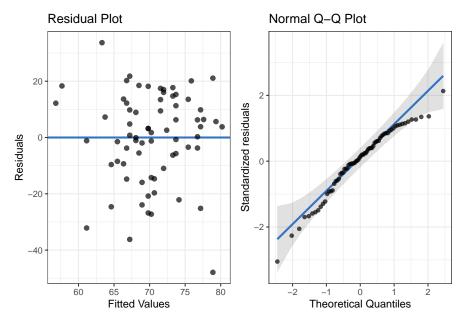


```
The basic output
Regfit <- lm(E2 ~ E1)
summary(Regfit)

##
Call:
lm(formula = E2 ~ E1)
##
Residuals:
Min 1Q Median 3Q Max
-47.904 -9.123 2.178 12.218 33.693</pre>
```

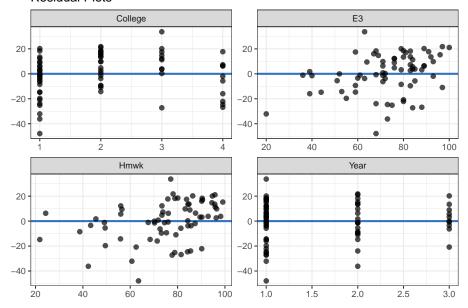
#### Residuals $\dots$

```
The two standard residual plots
\# par(mfrow = c(1, 2))
plot(Regfit, 1)
plot(Regfit, 2)
\# par(mfrow = c(1, 1))
Regfit_resids <- broom::augment(Regfit) %>%
 ggplot(aes(x = .fitted, y = .resid)) +
 geom_hline(yintercept = 0, color = "#3273c2", size = 1) +
 geom_point(size = 2, alpha = 0.7) + #shape = 1) +
 labs(title = "Residual Plot",
 x = "Fitted Values",
 y = "Residuals")
Regfit_qqplot <- broom::augment(Regfit) %>%
 ggplot(aes(sample = .std.resid)) +
 qqplotr::geom_qq_band(fill = "#363636", alpha = 0.15) +
 stat_qq_line(color = "#3273c2", size = 1) +
 stat_qq(size = 1.5, alpha = .7) +
 labs(x = "Theoretical Quantiles",
 y = "Standardized residuals",
 title = "Normal Q-Q Plot")
Regfit_resids + Regfit_qqplot
```



```
The plots of the residuals vs. other variables to check independence.
Looks like the errors might have some dependence due to college.
residuals <- Regfit$residuals</pre>
\# par(mfrow = c(2, 2))
plot(E3, residuals)
lines(c(-1e10, 1e10), c(0, 0))
plot(Hmwk, residuals)
lines(c(-1e10, 1e10), c(0, 0))
plot(as.numeric(as.factor(College)), residuals)
lines(c(-1e10, 1e10), c(0, 0))
plot(Year, residuals)
lines(c(-1e10, 1e10), c(0, 0))
\# par(mfrow = c(1, 1))
broom::augment(Regfit, data = students) %>%
 mutate(College = as.numeric(as.factor(College))) %>%
 gather(key = "key", value = "value", College:E3) %>%
 filter(key %in% c("E3", "Hmwk", "College", "Year")) %>%
 ggplot(aes(x = value, y = .resid)) +
 geom_hline(yintercept = 0, color = "#3273c2", size = 1) +
 geom_point(size = 2, alpha = 0.7) + #shape = 1) +
 facet_wrap(~key, scales = "free") +
 labs(title = "Residual Plots",
 x = NULL,
 y = NULL)
```

#### Residual Plots

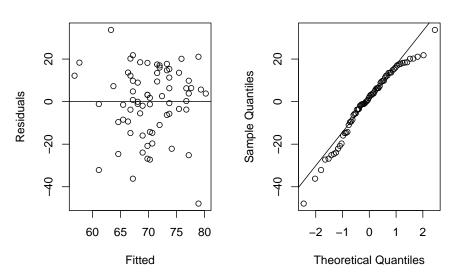


The function SASreg() below will produce output similar to SAS using just one function. It requires that you have loaded in and installed the car package. To use it, simply copy the function in once, and then apply it to your data set.

```
SASreg <- function(model) {</pre>
 regout <- lm(model)</pre>
 baseoutput <- anova(regout)</pre>
 k <- nrow(baseoutput) - 1</pre>
 Summary <- round(c(</pre>
 summary(lm(model))$sigma,
 summary(lm(model))$r.squared,
 summary(lm(model))$adj.r.squared
 names(Summary) <- c("Root MSE", "R square", "Adj R-Squ")</pre>
 ANOVA <- rbind(
 apply(baseoutput[1:k,], 2, sum),
 baseoutput[k + 1,],
 apply(baseoutput[1:(k + 1),], 2, sum)
 rownames(ANOVA) <- c("Model", "Error", "C Total")</pre>
 attributes(ANOVA)$heading <- attributes(ANOVA)$heading[1]</pre>
 ANOVA[1, 3] <- ANOVA[1, 2] / ANOVA[1, 1]
 ANOVA[1, 4] \leftarrow ANOVA[1, 3] / ANOVA[2, 3]
 ANOVA[1, 5] \leftarrow 1 - pf(ANOVA[1, 4], ANOVA[1, 1], ANOVA[2, 1])
 attributes(ANOVA)$heading <- NULL
```

```
TypeI <- baseoutput[1:k,]</pre>
 attributes(TypeI)$heading <- NULL</pre>
 TypeIII <- Anova(regout, type = 3)[2:(k + 1), c(2, 1, 3, 4)]
 attributes(TypeIII)$heading <- NULL
 if (k == 1) {
 vifs <- 1
 } else {
 vifs <- t(vif(regout))</pre>
 ParEsts <- round(cbind(summary(regout)$coefficients, c(0, vifs)), 4)
 colnames(ParEsts)[5] <- "VIF"</pre>
 par(mfrow = c(1, 2))
 plot(regout$fitted.values, regout$residuals, xlab = "Fitted", ylab = "Residuals")
 lines(c(min(regout$fitted.values) - 1, max(regout$fitted.values) + 1), c(0, 0))
 qqnorm(regout$residuals)
 qqline(regout$residuals)
 par(mfrow = c(1, 1))
 list(
 Model.Equation = model,
 Coefficients = regout$coefficients,
 Summary = Summary,
 Analysis.of.Variance = ANOVA,
 Type.I.Tests = TypeI,
 Type.III.Tests = TypeIII,
 Parameter.Estimates = ParEsts
}
SASreg(E2 ~ E1)
```

#### Normal Q-Q Plot



```
$Model.Equation
E2 ~ E1
##
$Coefficients
(Intercept)
 E1
 37.3125215
 0.4332442
##
##
$Summary
Root MSE R square Adj R-Squ
 16.1601
 0.0882
##
 0.0747
$Analysis.of.Variance
 Df Sum Sq Mean Sq F value Pr(>F)
 1 1716.8 1716.77
 6.574 0.01256 *
Model
Error
 68 17758.0 261.15
C Total 69 19474.8 1977.92
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
$Type.I.Tests
 Df Sum Sq Mean Sq F value Pr(>F)
E1 1 1716.8 1716.8 6.574 0.01256 *
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
```

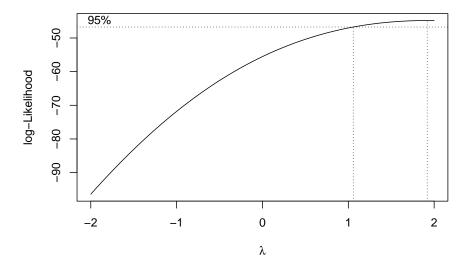
```
$Type.III.Tests
 Df Sum Sq F value Pr(>F)
##
E1 1 1716.8 6.574 0.01256 *
 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Signif. codes:
##
$Parameter.Estimates
##
 Estimate Std. Error t value Pr(>|t|) VIF
 37.3125
 2.8595
 0.0056
(Intercept)
 13.0485
 0
E1
 0.4332
 0.1690
 2.5640
 0.0126
 1
```

This output is perhaps a bit overkill for simple linear regression, but is very useful when performing multiple regression (or even ANCOVA or factorial ANOVA).

#### 5.4.2 Box-Cox Transformation

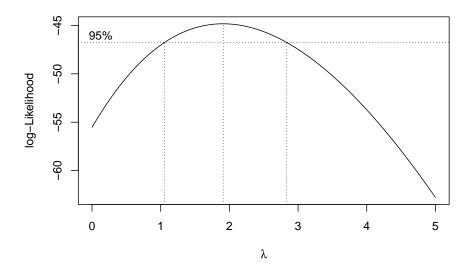
To get the Box-Cox transformation for this data set we could use the boxcox function from the MASS library (which is automatically included with R and just needs to have library(MASS) to install:

```
library(MASS)
boxcox(lm(E2 ~ E1))
```



This plot doesn't have the peak! So try from 0 to 5 with spacing every .01 to see if its better:

```
boxcox(lm(E2 \sim E1), lambda = seq(0, 5, .01))
```



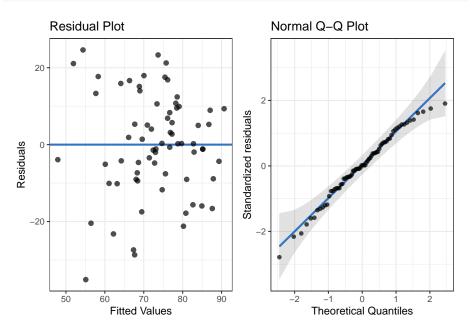
It looks like 1 is just outside the range, of the values that make the 95% cut-off, the one that is "nicest" and close to the peak is 2. So, the transformation y-squared is recommended.

#### 5.4.3 Multiple Linear Regression

Predict the performance on Exam3 from the performance of the first two exams and the homework.

This can be done by mimicking the procedure for simple linear regression. In this case the model statement must be of the form  $E3 \sim Hmwk + E1 + E2$ . An interaction could be added by something like + E2\*E3 if it were needed.

mlr\_fit <- lm(E3 ~ Hmwk + E1 + E2)

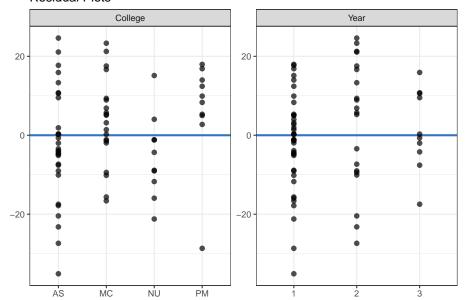


The plots to help assess independence (the residuals versus other variables not included in the model) and to check for needing higher order terms (the residual versus independent variables) could be generated as follows:

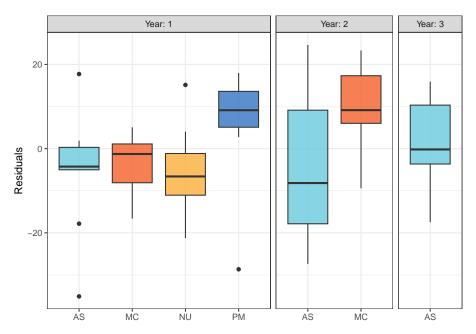
residuals <- lm(E3 ~ Hmwk + E1 + E2)\$residuals

```
y = NULL)
```

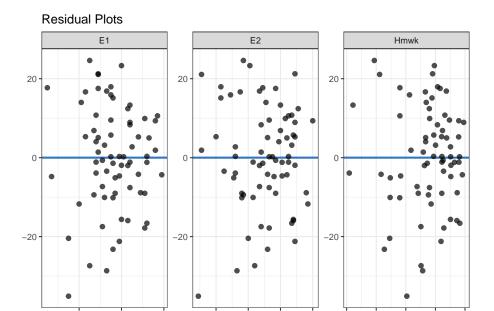
#### Residual Plots



```
Plotting against group might be better
plot(grp, residuals)
broom::augment(mlr_fit, data = students) %>%
 ggplot(aes(College, .resid)) +
 geom_boxplot(aes(fill = stage(College, after_scale = alpha(fill, 0.8))), show.legend = FALSE) +
 facet_grid(~Year, scales = "free", space = "free_x", labeller = labeller(Year = label_both)) +
 labs(x = NULL, y = "Residuals")
```



```
No signs of needing higher order terms
\# par(mfrow = c(2, 2))
plot(Hmwk, residuals)
plot(E1, residuals)
plot(E2, residuals)
\# par(mfrow = c(1, 1))
broom::augment(mlr_fit, data = students) %>%
 select(3:5, 8:13) %>%
 gather(key = "key", value = "value", Hmwk:E2) %>%
 ggplot(aes(x = value, y = .resid)) +
 geom_hline(yintercept = 0, color = "#3273c2", size = 1) +
 geom_point(size = 2, alpha = 0.7) + #shape = 1) +
 facet_wrap(~key, scales = "free") +
 labs(title = "Residual Plots",
 x = NULL,
 y = NULL)
```



#### 5.4.4 Variable Selection

Assuming we trusted the model fit, is there a subset of Hmwk, E1, and E2 that predicts E3 just as well as all three of them?

R has some packages that do all subsets variable selection, but the output is somewhat inelegant. The Cp function below is a bit prettier. It requires the leaps library, and that package must be installed for it to run It also requires that you put all of the predictor variables together in a matrix called X. To run it, be sure to load the **leaps** library and copy over the function, construct the X matrix using cbind(), and then run the function.

```
library(leaps)
Cp <- function(X, Y) {
 baseout <- summary(regsubsets(X, Y, nbest = 10))
 inmat <- baseout$which[, -1]
 n <- nrow(inmat)
 namemat <- matrix(rep(colnames(X), n), nrow = n, byrow = T)
 namemat[!inmat] <- ""
 namemat <- cbind(rep(" ", n), namemat)
 nvars <- apply(inmat, 1, sum)
 sets <- apply(namemat, 1, paste, collapse = " ")
 for (i in 1:ncol(X)) {
 sets <- gsub(" ", " ", sets)
 }
 out <- as.table(cbind()</pre>
```

```
sets, round(baseout$cp, 4),
 round(baseout$rsq, 4), round(baseout$adjr2, 4)
))
colnames(out) <- c("Variables", "Cp", "R square", "adj-R2")
rownames(out) <- nvars
out
}

X <- cbind(Hmwk, E1, E2)
Cp(X, E3)</pre>
```

```
R square adj-R2
 Variables
 Ср
1 Hmwk
 6.5697 0.277
 0.2664
1
 E2
 17.5215 0.1679
 0.1557
1 E1
 23.2662 0.1107
 0.0976
2 Hmwk E2
 4.4533 0.3181
 0.2977
2 Hmwk E1
 4.7743 0.3149
 0.2944
2
 E1 E2
 14.6179 0.2168
 0.1934
3 Hmwk E1 E2 4
 0.3425
 0.3126
```

It looks as if using Hmwk and just one of the other two exams just misses the general guideline for Mallow's Cp, and have slightly worse adjusted R-squared values.

#### 5.4.5 Outlier Diagnostics

Are there examinees that are either extreme in terms of their predictor variables, have E3 badly predicted by the model, or significantly change the model?

R has the built in functions hat values, rstudent, dffits, and cooks.distance to help with outlier diagns ostics. The function outlier below puts them into one a single matrix.

```
outlier <- function(model) {
 baseout <- lm(model)
 outs <- cbind(
 hatvalues(baseout), rstudent(baseout),
 dffits(baseout), cooks.distance(baseout)
)
 outs <- round(outs, 4)
 colnames(outs) <- c("hii", "ti", "DFFITS", "Cooks.D")
 outs
}

outlier(E3 ~ Hmwk + E1 + E2)</pre>
```

## hii ti DFFITS Cooks.D

```
1 0.0322 -1.6206 -0.2957 0.0213
2 0.1088 -0.9214 -0.3219
 0.0260
3 0.0382 -1.2109 -0.2413 0.0145
4 0.0382 -0.6809 -0.1357
 0.0046
5 0.0309 0.3026 0.0541 0.0007
6 0.0569 -0.6760 -0.1660
 0.0069
7 0.0672 1.1656 0.3127
 0.0243
8 0.0474 -0.0895 -0.0200 0.0001
9 0.0381 -0.0864 -0.0172
 0.0001
10 0.0798 -0.3335 -0.0982 0.0024
11 0.0308 -2.2243 -0.3966
 0.0371
12 0.1040 0.4138 0.1410
 0.0050
13 0.0747 0.2098 0.0596
 0.0009
14 0.0242 0.6225
 0.0980
 0.0024
15 0.0434 1.0629
 0.2264
 0.0128
16 0.0736 1.3942
 0.3930
 0.0381
17 0.0434 0.7501
 0.1598
 0.0064
18 0.0473 0.3777 0.0842 0.0018
19 0.0283 1.2757 0.2177
 0.0117
20 0.0418 0.9402 0.1962 0.0096
21 0.1257 -2.9432 -1.1158
 0.2789
22 0.1501 -0.3123 -0.1312 0.0044
23 0.0557 -0.3876 -0.0942 0.0022
24 0.0406 -1.3594 -0.2795
 0.0193
25 0.0533 -0.3513 -0.0833 0.0018
26 0.1857 0.1539 0.0735 0.0014
27 0.1523 -0.3838 -0.1627
 0.0067
28 0.0797 0.0249 0.0073 0.0000
29 0.1372 1.4264 0.5689
 0.0797
30 0.0276 0.0167 0.0028
 0.0000
31 0.0808 -1.6009 -0.4747
 0.0550
32 0.0286 -2.1151 -0.3627
 0.0312
33 0.0692 -1.8169 -0.4953
 0.0593
34 0.0464 -0.7640 -0.1685
 0.0071
35 0.0265 -0.6764 -0.1117
 0.0031
36 0.0189 -0.5461 -0.0758
 0.0015
37 0.0751 -0.2627 -0.0749
 0.0014
38 0.1081 1.6797 0.5848
 0.0832
39 0.2150 1.1177 0.5849
 0.0852
40 0.0805 1.9456 0.5756 0.0795
41 0.0179 -1.3160 -0.1775 0.0078
42 0.1048 -0.3283 -0.1123
 0.0032
43 0.0209 -0.5660 -0.0828
 0.0017
44 0.0218 -0.1487 -0.0222 0.0001
45 0.0265 -0.0504 -0.0083 0.0000
46 0.0397 1.2089 0.2459 0.0150
```

```
47 0.0257 0.0215
 0.0035
 0.0000
48 0.1169 0.8353
 0.3040
 0.0232
49 0.0263 0.7135
 0.0035
 0.1172
50 0.0477 0.8166 0.1828
 0.0084
51 0.0365 -0.7657 -0.1490
 0.0056
52 0.0333 -1.1846 -0.2197
 0.0120
53 0.0350 -0.0844 -0.0161
 0.0001
54 0.0203 0.1044 0.0150
 0.0001
55 0.0144 -0.1056 -0.0128
 0.0000
56 0.0535 -1.2735 -0.3029
 0.0227
57 0.0215 0.3788
 0.0562
 0.0008
58 0.0357 0.2372
 0.0456
 0.0005
59 0.0350 -0.1453 -0.0277
 0.0002
60 0.0369 0.0170 0.0033
 0.0000
61 0.0325 -0.7084 -0.1298
 0.0042
62 0.0424 1.2695
 0.2672
 0.0177
63 0.0384 0.5168
 0.1033
 0.0027
64 0.0336 0.4293
 0.0801
 0.0016
65 0.0288
 1.3285
 0.2288
 0.0129
66 0.0458 0.3970
 0.0869
 0.0019
67 0.0255
 1.7818
 0.2880
 0.0201
68 0.0474 1.6359
 0.3649 0.0325
69 0.0467 0.6765 0.1498 0.0057
70 0.0824 0.7212 0.2162 0.0118
```

### 5.4.6 Prediction Intervals and Confidence Intervals for the Regression Line

What is the confidence interval for the mean E3 scores for examinees with Hmwk=95, E1=70, and E2=85? What would the prediction interval be?

The prediction intervals and confidence intervals for the regression surface can be gotten using the built in predict function. The following give those intervals for data points matching the original data (again using the model we defined above):

```
predict(lm(E3~Hmwk+E1+E2),interval="confidence")
predict(lm(E3~Hmwk+E1+E2),interval="predict")
For Hmwk=95, E1=70, and E2=85:
predict(lm(E3~Hmwk+E1+E2),data.frame(Hmwk=95,E1=70,E2=85),interval="confidence")
predict(lm(E3~Hmwk+E1+E2),data.frame(Hmwk=95,E1=70,E2=85),interval="predict")
```

### 5.4.7 Factorial ANOVA

Conduct a 2-way ANOVA for Hmwk based on Year 1 vs. 2 and AS vs. MC.

The data for this problem can be constructed using:

```
HmwkA<-Hmwk[((College=="AS")|(College=="MC"))&((Year==1)|(Year==2))]
CollegeA<-College[((College=="AS")|(College=="MC"))&((Year==1)|(Year==2))]
CollegeA<-as.factor(as.character(CollegeA))
YearA<-Year[((College=="AS")|(College=="MC"))&((Year==1)|(Year==2))]
YearA<-as.factor(as.character(YearA))</pre>
```

The basic output can again be constructed either using the built in functions or SASreg. The interaction is added using a colon if the terms are listed separately, or all the terms will be crossed using an asterisk.

```
summary(lm(HmwkA~CollegeA+YearA+CollegeA:YearA))
par(mfrow=c(1,2))
plot(lm(HmwkA~CollegeA+YearA+CollegeA:YearA),1)
plot(lm(HmwkA~CollegeA+YearA+CollegeA:YearA),2)
par(mfrow=c(1,1))

SASreg(HmwkA~CollegeA+YearA+CollegeA:YearA)
SASreg(HmwkA~CollegeA*YearA)
```

Profile plots can be constructed using the built in function interaction.plot. The first argument is the variable on the x-axis, and the third is the response variable.

```
interaction.plot(CollegeA, YearA, HmwkA)
interaction.plot(YearA, CollegeA, HmwkA)
```

### 5.4.8 ANCOVA

Predict E3 from Hmwk using grp as a covariate.

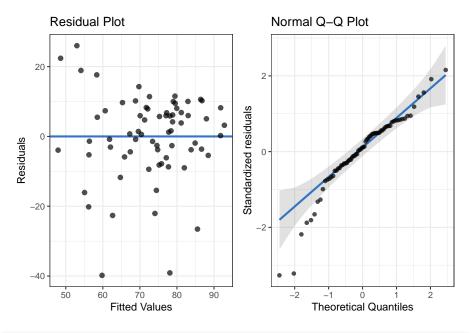
Again this can be performed using either the built in functions or SASreg.

```
ancova_fit <- lm(E3 ~ Hmwk + grp)
summary(ancova_fit)</pre>
```

```
##
Call:
lm(formula = E3 ~ Hmwk + grp)
Residuals:
##
 1Q Median
 3Q
 Min
 Max
-39.791 -5.051 1.322 7.752 25.999
##
Coefficients:
##
 Estimate Std. Error t value Pr(>|t|)
(Intercept) 41.28345 8.50894 4.852 8.6e-06 ***
Hmwk
 0.30491 0.11446 2.664 0.009829 **
 6.40928 6.03209 1.063 0.292116
grp1MC
```

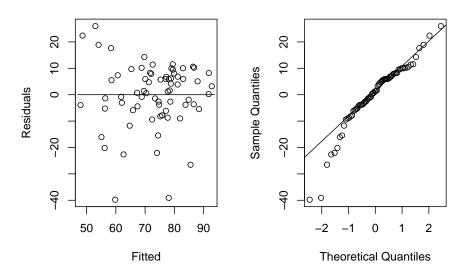
```
grp1NU
 7.61338
 6.27024 1.214 0.229273
grp1PM
 15.03430
 6.01798
 2.498 0.015147 *
 5.88744 -0.014 0.988934
grp2AS
 -0.08199
 21.30066
 6.14449 3.467 0.000963 ***
grp2MC
 5.80620 1.959 0.054554 .
 11.37722
grp3AS

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
Residual standard error: 12.85 on 62 degrees of freedom
Multiple R-squared: 0.4382, Adjusted R-squared: 0.3748
F-statistic: 6.909 on 7 and 62 DF, p-value: 4.48e-06
\# par(mfrow = c(1, 2))
plot(lm(E3 \sim Hmwk + grp), 1)
\# plot(lm(E3 ~ Hmwk + grp), 2)
\# par(mfrow = c(1, 1))
ancova_fit_resids <- broom::augment(ancova_fit) %>%
 ggplot(aes(x = .fitted, y = .resid)) +
 geom_hline(yintercept = 0, color = "#3273c2", size = 1) +
 geom_point(size = 2, alpha = 0.7) + #shape = 1) +
 labs(title = "Residual Plot",
 x = "Fitted Values",
 y = "Residuals")
ancova_fit_qqplot <- broom::augment(ancova_fit) %>%
 ggplot(aes(sample = .std.resid)) +
 qqplotr::geom_qq_band(fill = "#363636", alpha = 0.15) +
 stat_qq_line(color = "#3273c2", size = 1) +
 stat_qq(size = 1.5, alpha = .7) +
 labs(x = "Theoretical Quantiles",
 y = "Standardized residuals",
 title = "Normal Q-Q Plot")
ancova_fit_resids + ancova_fit_qqplot
```



SASreg(lm(E3 ~ Hmwk + grp))

### Normal Q-Q Plot



## \$Model.Equation

##

## Call:

```
lm(formula = E3 ~ Hmwk + grp)
Coefficients:
(Intercept)
 grp1MC
 grp1NU
 Hmwk
 grp1PM
 grp2AS
 0.30491
 6.40928
 7.61338
##
 41.28345
 15.03430
 -0.08199
##
 grp2MC
 grp3AS
##
 21.30066
 11.37722
##
##
$Coefficients
(Intercept)
 Hmwk
 grp1MC
 grp1NU
 grp1PM
grp2MC
 grp3AS
21.30066031 11.37722469
##
$Summary
Root MSE R square Adj R-Squ
##
 12.8483
 0.4382
 0.3748
##
$Analysis.of.Variance
 Df Sum Sq Mean Sq F value Pr(>F)
 7 7983.1 1140.4 6.9085 4.48e-06 ***
Model
Error 62 10234.9
 165.1
C Total 69 18218.0 5701.6
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
$Type.I.Tests
 Df Sum Sq Mean Sq F value
 Pr(>F)
Hmwk 1 5047.1 5047.1 30.5742 6.834e-07 ***
 6 2936.0
 489.3 2.9642
 0.0131 *
grp

Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
$Type.III.Tests
 Df Sum Sq F value Pr(>F)
Hmwk 1 1171.5 7.0968 0.009829 **
grp
 6 2936.0 2.9642 0.013097 *

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
$Parameter.Estimates
 Estimate Std. Error t value Pr(>|t|)
(Intercept) 41.2834 8.5089 4.8518 0.0000 0.0000
Hmwk
 0.3049
 0.1145 2.6640 0.0098 1.6736
 6.4093
 6.0321 1.0625 0.2921 1.0000
grp1MC
```

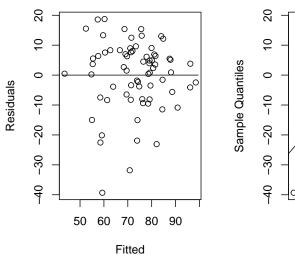
```
grp1NU
 7.6134
 6.2702
 1.2142
 0.2293 1.2937
grp1PM
 15.0343
 6.0180
 2.4982
 0.0151 1.6736
 -0.0820
 5.8874 -0.0139
grp2AS
 0.9889 6.0000
grp2MC
 21.3007
 6.1445
 3.4666
 0.0010 1.0438
grp3AS
 5.8062
 1.9595
 0.0546 0.0000
 11.3772
```

Note that the VIFs should not be part of the output in SASreg when categorical variables are present, and this is currently a bug.

Checking whether the lines are parallel can be done simply by checking the interaction Hmwk:grp.

```
SASreg(lm(E3 ~ Hmwk * grp))
```

### Normal Q-Q Plot



```
Sample Quantiles

Sample Quantiles

Theoretical Quantiles
```

```
$Model.Equation
##
Call:
lm(formula = E3 ~ Hmwk * grp)
##
Coefficients:
 (Intercept)
##
 Hmwk
 grp1MC
 grp1NU
 grp1PM
 grp2AS
 34.65972
##
 0.40631
 2.23406
 4.29217
 -39.95759
 32.07351
##
 grp2MC
 grp3AS
 Hmwk:grp1MC
 Hmwk:grp1NU
 Hmwk:grp1PM
 Hmwk:grp2AS
##
 -4.41607
 13.08221
 0.03133
 0.01258
 0.65975
 -0.57325
Hmwk:grp2MC
 Hmwk:grp3AS
 0.28205
 -0.03366
##
##
```

grp2AS

```
##
$Coefficients
 (Intercept)
 Hmwk
 grp1MC
 grp1NU
 grp1PM
##
 34.65972374 0.40631164
 2.23406485
 4.29216905 -39.95759295 32.07351063
 grp3AS Hmwk:grp1MC Hmwk:grp1NU Hmwk:grp1PM Hmwk:grp2AS
##
 grp2MC
##
 -4.41607393 13.08221050
 0.03132616
 0.01257784
 0.65975222 -0.57325369
 Hmwk:grp2MC Hmwk:grp3AS
 0.28204916 -0.03366234
##
##
$Summary
Root MSE R square Adj R-Squ
##
 12.7778
 0.4981
 0.3816
##
$Analysis.of.Variance
 Df Sum Sq Mean Sq F value
 13 9074.8
 698.1 4.2754 6.298e-05 ***
Model
Error 56 9143.2
 163.3
C Total 69 18218.0 5881.7
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
$Type.I.Tests
##
 Df Sum Sq Mean Sq F value Pr(>F)
 1 5047.1 5047.1 30.9125 7.81e-07 ***
Hmwk
 6 2936.0
 489.3 2.9970 0.01306 *
grp
Hmwk:grp 6 1091.6
 181.9 1.1143 0.36580
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
$Type.III.Tests
##
 Df Sum Sq F value Pr(>F)
Hmwk
 1 690.67 4.2302 0.04438 *
 6 714.43 0.7293 0.62795
grp
Hmwk:grp 6 1091.64 1.1143 0.36580

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
$Parameter.Estimates
 Estimate Std. Error t value Pr(>|t|)
##
 VTF
(Intercept) 34.6597 13.5219 2.5632 0.0131 0.000000e+00
Hmwk
 0.4063
 0.1976 2.0567 0.0444 5.041000e+00
 30.5272 0.0732 0.9419 1.000000e+00
grp1MC
 2.2341
 43.3093 0.0991 0.9214 2.245200e+00
grp1NU
 4.2922
 0.4732 9.571270e+09
grp1PM
 -39.9576
 55.3296 -0.7222
grp2AS
 32.0735 18.9058 1.6965 0.0953 6.000000e+00
grp2MC
 -4.4161 41.0984 -0.1075 0.9148 6.788100e+00
```

```
grp3AS
 13.0822
 24.9749 0.5238
 0.6025 1.132895e+10
Hmwk:grp1MC
 0.0313
 0.3869 0.0810
 0.9358 6.000000e+00
Hmwk:grp1NU
 0.0126
 0.5092 0.0247
 0.9804 6.884100e+00
Hmwk:grp1PM
 0.6598
 0.6898 0.9565
 0.3430 0.000000e+00
Hmwk:grp2AS
 0.3051 -1.8790
 0.0655 5.041000e+00
 -0.5733
Hmwk:grp2MC
 0.2820
 0.4985 0.5658
 0.5738 1.000000e+00
Hmwk:grp3AS
 -0.0337
 0.3458 -0.0974
 0.9228 2.245200e+00
```

### 5.5 Other Methods

Functions in base SAS for other commonly used methods include:

For Nonparametrics:

- wilcox.test()
- friedman.test()
- kruskal.test()

For Categorical Data:

- binom.test()
- chisq.test()
- glm( ,family=binomial("logit"))
- fisher.test()
- mantel.haen.test()

### Chapter 6

## Psychometric Packages

There are a number of packages that can be used for psychometric analysis. The following code uses a small sample of what is out there. A good reference with a list of numerous packages can be found at https://cran.r-project.org/web/views/Psychometrics.html. This section contains some examples from the CTT, psychometric, psych, difr, and mirt packages.

The first several examples use the data set samptest.txt. It also gives a chance to see how to score an exam using the CTT package. The next lines enter the answer key, format it for later use, and read in the data set.

```
sample test data with 36 items and 2 demographic variables (ethnicity and gender)
key <- "ADCABCACDCDCBBCBDCADADCABDBABADBCADB"
new.key <- unlist(strsplit(key, split = ""))</pre>
testdat <- read.fwf("data/samptest.txt", widths = c(rep(1, 38)))
dim(testdat)
[1] 102 38
head(testdat)
 V1 V2 V3 V4 V5 V6 V7 V8 V9 V10 V11 V12 V13 V14 V15 V16 V17 V18
 V19 V20
 С
 С
 С
 R
 C
 C
 C
 D
 D
 D
 В
 D
 С
 D
 С
 C
 С
 В
 В
 С
 Α
 D
 Α
 C
 С
 С
 C
 С
 С
 D
 Α
 В
 В
 Α
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 В
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 Α
 В
 C
 Α
 C
 Α
 В
 В
 D
 В
 D
 С
 Α
 D
 V23 V24 V25 V26 V27 V28 V29
 V30
 V31 V32 V33 V34 V35 V36 V37
 V38
1
 D
 В
 В
 Α
 D
 В
 C
 Α
 D
 В
 В
 F
 D
 Α
 Α
 В
 Α
 F
 D
 D
 В
 Α
 В
 В
 С
 Α
 D
 В
 D
 F
3
 Α
 Α
 Α
 В
 Α
 D
 Α
 В
 Α
 В
 В
 Α
 Α
 Α
 В
```

mid75

```
4
 D
 С
 В
 D
 В
 В
 D
 В
 C
 В
 В
 Μ
5
 В
 С
 В
 D
 В
 В
 D
 В
 С
 D
 В
 В
 F
 Α
 Α
 Α
 Α
 С
6
 В
 D
 С
 A
 В
 С
 D
 В
 D
 В
 D
 Α
 В
 В
 Μ
```

The CTT package contains basic data functions like distractorAnalysis(), and score() for scoring the data.

```
library(CTT)
distractorAnalysis(testdat[, 1:36], key = new.key)[[1]]
```

```
##
 pBis
 lower
 mid50
 correct key
 rspP
 discrim
A
 A 75 0.73529412 0.5149574 0.5806452 0.4193548 0.8571429 0.7692308
B
 7 0.06862745 -0.5289839 -0.2258065 0.2258065 0.0000000 0.0000000
 C 11 0.10784314 -0.2247585 -0.1612903 0.1612903 0.1428571 0.1153846
C
 9 0.08823529 -0.2920536 -0.1935484 0.1935484 0.0000000 0.1153846
D
P
 0 0.00000000
 ##
 upper
A
 1
B
 0
C
 0
D
 0
P
 0
score gives both the sum scores and the response matrix
scoredat <- score(testdat[, 1:36], new.key, output.scored = TRUE)</pre>
get 0/1 responses only
responses <- scoredat$scored
get the total scores only
sumscores <- scoredat$score</pre>
```

It also includes some basic classical analyses:

### itemAnalysis(responses)

```
##
##
 Number of Items
##
##
##
 Number of Examinees
##
 102
##
##
 Coefficient Alpha
##
 0.844
```

The **psychometric** and **psych** packages overlap some, but are both larger.

```
library(psychometric)
alpha(responses)
[1] 0.8441692
alpha.CI(alpha(responses), N = dim(responses)[1], k = dim(responses)[2])
##
 LCI.
 ALPHA
 UCI.
1 0.8057113 0.8441692 0.8787447
library(psych)
psych::polyserial(as.matrix(sumscores), as.matrix(responses[, 1]))
##
 [,1]
[1,] 0.7657925
It is important to check that the functions in each package actually do what you
want. In the case of measuring item discrimination using the biserial correlation
of the items with the rest score, it's necessary to check that the polyserial funcion
in the psych package is the one you want to agree with texts like Lord and Novick,
or Crocker and Algina.
biserials <- NULL
for (i in 1:ncol(responses)) {
 biserials <- c(biserials, polyserial(as.matrix(sumscores - responses[, i]), as.matrix(responses
biserials
 [1] 0.69400052 0.50200231 0.30618509 0.45158311 0.38036029 0.51107140
 [7] 0.26724319 0.37702310 0.58276455 0.68733895 0.55842935 0.70796675
[13] 0.30582385 0.08002487 0.46911103 0.11720900 0.64378754 0.46670904
[19] 0.26342658 0.70517564 0.50782867 0.59232271 0.41577996 0.57712603
[25] 0.52496694 0.52036168 0.47193436 0.27588499 0.25170829 0.40882539
[31] 0.40607968 0.67815832 0.47517826 0.52294511 0.42049977 0.55669711
Among the more specialized packages are those that do more specialized proce-
dures such as DIF detection in the difR package.
Looking at difR
library(difR)
difdat <- data.frame(responses, testdat[, 38])</pre>
dichoDif(difdat, group = 37, focal.name = "F", method = c("MH", "Logistic"), criterion = "Wald")
Comparison of DIF detection results using 2 methods
##
Methods used:
Mantel-Haenszel
Logistic regression
##
```

```
Matching variable: test score
No set of anchor items was provided
##
Parameters:
Significance level: 0.05
Mantel-Haenszel DIF statistic: Chi-square statistic
##
 Mantel-Haenszel continuity correction: Yes
##
 Type of Mantel-Haenszel test: asymptotic test
 Logistic regression DIF statistic: Wald statistic
##
 DIF effect(s) tested by logistic regression: both DIF effects
 Item purification: No
##
##
##
 No p-value adjustment for multiple comparisons
##
Comparison of DIF detection results:
##
 Logistic #DIF
##
 M-H
V1
 DIF NoDIF
 1/2
 NoDIF DIF
 1/2
V2
V3
 NoDIF NoDIF
 0/2
V4
 DIF NoDIF
 1/2
V5 NoDIF NoDIF
 0/2
V6
 NoDIF NoDIF
 0/2
V7
 NoDIF NoDIF
 0/2
V8 NoDIF NoDIF
 0/2
V9
 DIF NoDIF
 1/2
V10 NoDIF DIF
 1/2
V11 NoDIF NoDIF
 0/2
V12 NoDIF NoDIF
 0/2
V13 NoDIF NoDIF
 0/2
V14 NoDIF NoDIF
 0/2
V15 NoDIF NoDIF
 0/2
V16 NoDIF NoDIF
 0/2
V17 NoDIF NoDIF
 0/2
V18 NoDIF NoDIF
 0/2
V19 NoDIF NoDIF
 0/2
V20 NoDIF NoDIF
 0/2
V21 NoDIF DIF
 1/2
V22 NoDIF NoDIF
 0/2
V23 NoDIF NoDIF
 0/2
V24 NoDIF NoDIF
 0/2
V25 NoDIF NoDIF
 0/2
V26 NoDIF NoDIF
 0/2
V27 NoDIF NoDIF
 0/2
V28 NoDIF NoDIF
 0/2
```

```
V29 NoDIF DIF
 1/2
V30 NoDIF NoDIF
 0/2
V31 NoDIF NoDIF
 0/2
V32 NoDIF DIF
 1/2
V33 NoDIF NoDIF
 0/2
V34 NoDIF NoDIF
 0/2
V35 NoDIF NoDIF
 0/2
V36 NoDIF NoDIF
 0/2
##
##
 Output was not captured!
There are also packages for estimating IRT models, icluding the mirt package.
A larger data set is used for this example.
mdatab2 <- read.fwf("data/mdatab.txt", widths = rep(1, 32))</pre>
dim(mdatab2)
[1] 2642
 32
head(mdatab2)
 V1 V2 V3 V4 V5 V6 V7 V8 V9 V10 V11 V12 V13 V14 V15 V16 V17 V18
 V19 V20 V21
1
 1
 0
 1
 1
 1
 1
 1
 1
 0
 0
 0
 1
 1
 0
 0
 0
 0
 0
 0
 1
 0
 0
 0
 0
 1
 1
 1
 1
 0
 1
 1
 0
 0
 0
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 1
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 0
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 0
 0
 0
 0
 0
 1
 1
 1
 1
 0
 1
 0
 1
 0
 0
 0
 1
 1
 1
 1
 1
 1
 0
 0
5 1
 0
 0
 0
 0
 0
 1
 0
 0
 0
 0
 0
 1
 0
 0
 1
 0
 1
 0
 0
 0
 0
 1
 0
 0
 0
 0
 1
 0
 1
 1
 1
 1
 1
 1
 1
##
 V22 V23 V24 V25 V26 V27 V28 V29 V30 V31 V32
1
 0
 1
 1
 1
 0
 0
 0
 0
 0
2
 0
 0
 1
 0
 0
 0
 1
 0
 0
 0
 0
3
 0
 0
 0
 0
 0
4
 0
 0
 0
 0
 0
 0
 1
 0
 0
 1
 1
5
 0
 0
 0
 0
 0
 1
 0
 1
 0
 0
 0
6
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 1
mirt package
library(mirt)
estimating IRT model parameters
mod1.rasch <- mirt(mdatab2, 1, itemtype = "Rasch")</pre>
Iteration: 1, Log-Lik: -50361.109, Max-Change: 0.09008Iteration: 2, Log-Lik: -50349.088, Max-C
mod1.3PL <- mirt(mdatab2, 1, itemtype = "3PL")</pre>
Iteration: 1, Log-Lik: -50725.510, Max-Change: 3.35905Iteration: 2, Log-Lik: -50127.462, Max-Change: 3.35905Iteration: 3, Log-Lik: -50127.462, Max-Change: 3.35905Iteration: 3, Log-Lik: -50127.462, Max-Change: 3.35905Iteration: 3, Log-Lik: -50127.462, Max-Change: 3, Log-Lik: -50127.462, Max-Change
coef(mod1.rasch)
```

```
$V1
a1 dgu
par 1 0.462 0 1
$V2
a1 dgu
par 1 1.137 0 1
##
$V3
a1 dgu
par 1 0.797 0 1
##
$V4
a1 dgu
par 1 1.077 0 1
##
$V5
a1 dgu
par 1 1.827 0 1
##
$V6
a1 dgu
par 1 1.032 0 1
##
$V7
a1 dgu
par 1 -0.51 0 1
##
$V8
a1 dgu
par 1 0.482 0 1
##
$V9
a1 dgu
par 1 0.801 0 1
##
$V10
a1 dgu
par 1 0.575 0 1
##
$V11
a1 dgu
par 1 -0.262 0 1
##
$V12
a1 dgu
```

```
par 1 1.275 0 1
##
$V13
a1 dgu
par 1 -1.241 0 1
##
$V14
a1 dgu
par 1 1.232 0 1
##
$V15
a1 dgu
par 1 0.045 0 1
##
$V16
a1 dgu
par 1 -0.624 0 1
##
$V17
a1 dgu
par 1 0.251 0 1
##
$V18
a1 dgu
par 1 0.154 0 1
##
$V19
a1 dgu
par 1 0.733 0 1
##
$V20
a1 dgu
par 1 -0.021 0 1
##
$V21
a1 dgu
par 1 -0.342 0 1
##
$V22
a1 dgu
par 1 -0.473 0 1
##
$V23
a1 dgu
par 1 -0.259 0 1
##
```

```
$V24
a1 dgu
par 1 -0.471 0 1
$V25
a1 dgu
par 1 1.754 0 1
##
$V26
a1 dgu
par 1 -0.226 0 1
##
$V27
a1 dgu
par 1 -0.172 0 1
##
$V28
a1 dgu
par 1 -0.46 0 1
##
$V29
a1 dgu
par 1 -0.558 0 1
##
$V30
a1 dgu
par 1 -0.885 0 1
##
$V31
a1 dgu
par 1 -0.037 0 1
##
$V32
a1 dgu
par 1 -0.802 0 1
$GroupPars
MEAN_1 COV_11
par 0 0.849
coef(mod1.3PL)
$V1
a1 d gu
par 1.228 0.485 0.001 1
##
```

```
$V2
a1 d gu
par 0.936 0.264 0.379 1
$V3
 a1
 d gu
par 0.925 0.785 0.001 1
##
$V4
a1 d g u
par 1.565 1.283 0.001 1
$V5
a1 d gu
par 0.824 1.104 0.377 1
##
$V6
a1 d
par 0.94 1.027 0.001 1
##
$V7
a1 d g u
par 1.77 -2.628 0.29 1
##
$V8
a1 d gu
par 1.502 0.089 0.167 1
$V9
a1 d g u
par 2.333 -0.12 0.342 1
##
$V10
a1 d g u
par 2.533 -0.782 0.362 1
##
$V11
a1 d g u
par 1.72 -1.204 0.193 1
##
$V12
a1 d g u
par 0.954 1.272 0.005 1
##
$V13
##
 a1 d gu
```

```
par 1.437 -1.608 0.029 1
##
$V14
a1 d g u
par 1.148 1.304 0.001 1
##
$V15
a1 d gu
par 1.831 -1.387 0.307 1
##
$V16
a1 d g u
par 1.188 -0.93 0.065 1
##
$V17
a1 d gu
par 1.609 0.089 0.068 1
##
$V18
a1 d gu
par 1.735 -0.454 0.179 1
##
$V19
a1 d g u
par 1.368 0.79 0.013 1
$V20
a1 d gu
par 1.911 -1.065 0.233 1
$V21
a1 d gu
par 0.963 -1.208 0.219 1
##
$V22
a1 d gu
par 2.103 -2.177 0.239 1
##
$V23
a1 d gu
par 1.002 -0.286 0.003 1
$V24
a1 d gu
par 0.656 -0.558 0.038 1
##
```

```
$V25
##
 a1
 d
par 1.094 1.81 0.021 1
##
$V26
##
 a1
 d
 g u
par 1.587 -0.307 0.002 1
##
$V27
##
 a1
 d
 g u
par 1.004 -1.142 0.254 1
##
$V28
##
 d
 a1
 g u
par 1.414 -1.261 0.165 1
##
$V29
##
 d
 a1
par 1.115 -1.96 0.258 1
##
$V30
##
 d
 a1
 g u
par 1.641 -2.177 0.171 1
##
$V31
##
 g u
 a1
 d
par 1.809 -1.384 0.283 1
##
$V32
##
 a1
 d
 g u
par 1.259 -1.707 0.159 1
##
$GroupPars
##
 MEAN_1 COV_11
par
 0
```

The function has several different fitting methods, and allows specification of prior distributions. The package also has a simulate function for simulating item response data. As with the classical test theory item discrimination example above, it's necessary to check how the items are parameterized (do they use 1.7, for example).

## Chapter 7

# **Function Writing**

Chapter 8

Sample Simulations