

# ESM 204 HW 3 Appendix

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## Question 1

**‘Low’ income demand curve:**  $y = 11.6854836 - 6.6114372 \times 10^{-5}x$

**‘High’ income demand curve:**  $y = 15.803428 - 6.6114372 \times 10^{-5}x$

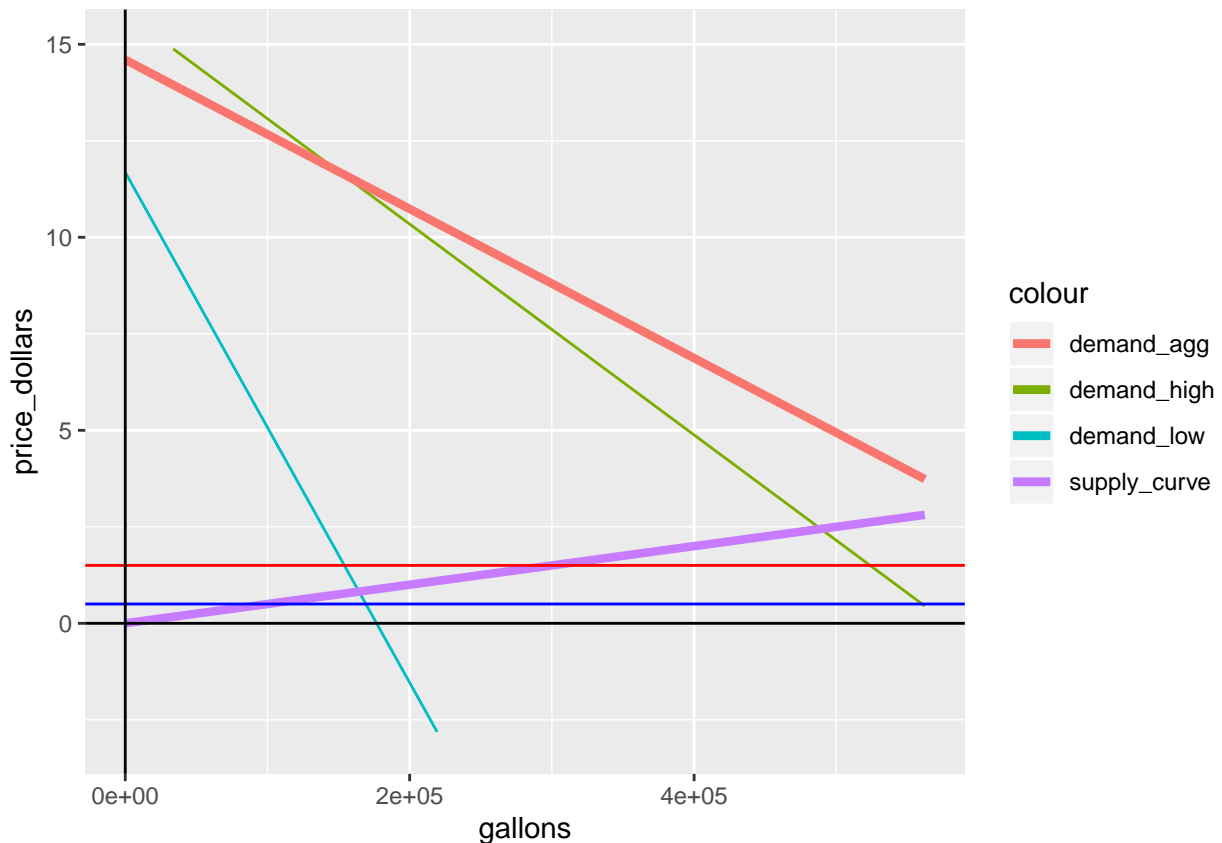
$$y_{low} = 11.68548 - 6.611437e-05x_{low} \quad x_{low} = (11.68548/6.611437e-05) + (1/-6.611437e-05)y_{low} \quad x_{low} = 176746.4 - 15125.3y_{low}$$

$$y_{high} = 15.80343 - 2.730926e-05x_{high} \quad x_{high} = (15.80343/2.730926e-05) + (1/-2.730926e-05)y_{high} \quad x_{high} = 578683.9 - 36617.62y_{high}$$

$$x_{agg} = (176746.4 + 578683.9) + ((1/-6.611437e-05) + (1/-2.730926e-05))y_{agg} \quad x_{agg} = 755430.3 - 51742.92y_{agg}$$

**Aggregate demand curve:**  $y_{agg} = 14.5996844 - 1.9326316 \times 10^{-5}x_{agg}$

**Supply curve:**  $y = (1/200,067)x$



## Consumer Benefit

The benefit to consumers under the status quo is the consumer surplus (the area under the demand curve, which we integrate when the price is \$3).

$$\$3 = 14.5996844 - 1.9326316 \times 10^{-5}x$$

$$x = 6.0020154 \times 10^5 \text{ gallons}$$

$$1.8006046 \times 10^6 = 3 \times 6.0020154 \times 10^5$$

$$5,284,660 - 1.8006046 \times 10^6 = 3,484,057$$

The consumer benefit is \$\_\_\_\_\_.

### **Producer Benefit**

The benefit to producers under the status quo is the producer surplus (the area under the demand curve, which we integrate when the price is \$3).

The producer benefit is \$\_\_\_\_\_.

### **Environmental Cost**

#### **Local**

The local environmental cost is  $9.0030231 \times 10^5$ . It is the area under the curve from 0 to 600201, so we integrate  $y = 1.50$  from 0 to 600201

#### **Rest of the world**

The rest of the world environmental cost is  $3.0010077 \times 10^5$ . It is the area under the curve from 0 to 600201, so we integrate  $y = 0.50$  from 0 to 600201

## **Question 2 - Individual Consumer Benefit**

### **Low Income**

$$x_{low} = (3 - 11.6854836) / -6.6114372 \times 10^{-5}$$

The quantity for the low income demand curve where the price is \$3 is  $1.3137058 \times 10^5$ . The consumer surplus is the area of a triangle.

$$5.7050852 \times 10^5 = 0.5 * (11.6854836 - 3) * 1.3137058 \times 10^5$$

The consumer benefit for low income consumers is  $5.7050852 \times 10^5$ .

### **High Income**

$$x_{high} = (3 - 15.803428) / -2.7309265 \times 10^{-5}$$

The quantity for the high income demand curve where the price is \$3 is  $4.6883093 \times 10^5$ .

$$5.7050852 \times 10^5 = 0.5 * (15.803428 - 3) * 4.6883093 \times 10^5$$

The consumer benefit for high income consumers is  $3.0013216 \times 10^6$ .

The aggregate benefit is  $3.5718301 \times 10^6$ .

### Question 3 - Effects from Gas Tax

**a) The amount of gasoline produced and consumed.**

\$1 will be subtracted from every gallon purchased.

The new supply curve is  $y - 1 = (1/200,067)x$ . Less gas would be produced and consumed. Setting this new supply curve equal to the aggregate demand curve, the new equilibrium quantity is  $5.5909096 \times 10^5$  gallons.

**b) Gas price**

The new gas price is 3.79/gallon at  $5.5909096 \times 10^5$  gallons.

**c) Welfare of 'high' income consumers**

$$4.5820286 \times 10^5 = (1 - 15.803428)/(-2.7309265 \times 10^{-5} - 4.9983211 \times 10^{-6})$$

The quantity where  $P = 3.79$  is  $4.5820286 \times 10^5$

$$2.7512589 \times 10^6 = 0.5 * (15.803428 - 3.7945161) * 4.5820286 \times 10^5$$

The welfare of high income customers after the tax is  $2.7512589 \times 10^6$ .

**d) Welfare of 'low' income consumers**

$$1.5026127 \times 10^5 = (1 - 11.6854836)/(-6.6114372 \times 10^{-5} - 4.9983211 \times 10^{-6})$$

The quantity where  $P = 3.79$  is  $1.5026127 \times 10^5$

$$5.928534 \times 10^5 = 0.5 * (11.6854836 - 3.7945161) * 1.5026127 \times 10^5$$

The welfare of low income customers after the tax is  $5.928534 \times 10^5$ .

**e) Welfare of gas producers**

The welfare of gas consumers is \$ \_\_\_\_.

**f) Local environmental damage**

A tax of \$1.00 doesn't cover all of local environmental damage, but it covers more than half of it, raising the tax to \$2.00.

**g) Rest of world environmental damage**

A tax of \$1.00 covers all of the world environmental damage and more. A socially optimum equilibrium is met at least with this externality. The MPC has captured the MEC value of this externality. The new supply curve with the tax is the MSC.

**h) Total revenue generated by the tax**

The total revenue generated by the tax is  $1.5623887 \times 10^6$ .

### Question 4

**a) overall welfare of 'High' income consumers**

**b) overall welfare of ‘Low’ income consumers**

The low income customers have to pay a higher tax because they have greater MECs. We assume that they will cover both the local externality and the ROW externality.

$$\text{Global externality} = \$1.50(\text{local}) + \$0.50(\text{ROW}) = \$2.00$$

They will need to pay a \$2 tax.

Maybe the ideal tax is \$1.25 because  $2 + .50 = 2.50$  which split between two groups is 1.25.

**c) gas producers**

**Question 5 - EV Technology**

**Note:** For the following calculations, we divided the y-intercept of each demand curve by half.

**a) gas consumption by ‘High’ income consumers**

The new consumption by high income consumers is  $2.4457767 \times 10^5$  gallons. Consumption decreases about 52.2%

**b) gas consumption by ‘Low’ income consumers**

The new consumption by high income consumers is  $8.2161728 \times 10^4$  gallons. Consumption decreases about 62.5%

**c) gas price**

The new gas price is \$1.5.

**d) local environmental damage from gasoline**

$$.5 * 1.50 * 300,101 = 225,075.75$$

**e) rest of world environmental damage from gasoline**

$$.5 * .50 * 300,101 = 75,025.25$$

**Question 6**

$$\tau = 7.3$$

**New supply curve with optimal tax:**  $y = 4.9983211 \times 10^{-6}x + 7.3$

A tax of \$7.3 makes the local environmental quality equal between the gas tax situation and the electric car situation.