

Demo: Counterpoint Analysis and Synthesis

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Abstract

We present *Music Tools*, an Agda library for analyzing and synthesizing music. The library uses dependent types to simplify encoding of music rules, thus improving existing approaches based on simply typed languages. As an application of the library, we demonstrate an implementation of first-species counterpoint, where we use dependent types to constrain the motion of two parallel voices.

Keywords: counterpoint, Haskell, SMT

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1 Introduction

We demonstrate work in progress on a tool to assist in the analysis of synthesis of musical counterpoint. Since the mid-18th century, the composition of counterpoint has been guided by principles enunciated in Fux’s *Gradus ad Parnassum* [Fux 1965]), first published in 1725. Fux presents an increasingly sophisticated series of “species” (one note against one note, two notes against one note, etc.) along with rules governing intervals between notes and motion between intervals designed to ensure consonance and independence of voices. It is well documented that great composers including Haydn, Mozart and Beethoven both studied and taught from this text, and its fundamentals continue to taught to music students today (for example [Aldwell and Cadwallader 2018; Kennan 1999]).

In previous work, Cong and Leo [Cong and Leo 2019] encode the

Cong [Cong 2022].

To analyze and synthesize tonal music, researchers have attempted to encode these rules into programming languages. Functional programming languages seem ideally suited for this task, and in particular, those with a static type system can further guarantee that *well-typed music does not sound wrong*. In the past decade, Haskell has been a popular choice for encoding the rules of harmony [De Haas et al. 2011, 2013; Koops et al. 2013; Magalhães and de Haas 2011; Magalhães and Koops 2014] as well as counterpoint [Szamozvancev and Gale 2017]. An interesting observation is that, many of the existing encodings rely on some form of *dependent types*, i.e.,

types that depend on terms. While Haskell is not a dependently typed language, it has various language extensions (such as GADTs [Cheney and Hinze 2002] and singleton types [Eisenberg and Weirich 2013]) for simulating dependent types, and as shown by previous studies, the extended type system is expressive enough for a wide class of music applications. On the other hand, the need for simulating dependent types can also result in code duplication, making the implementation less elegant [Monnier and Hagenauer 2010]. This motivates us to explore music programming in a language with intrinsic support for dependent types.

We present *Music Tools*¹, a library of small tools that can be combined functionally to help analyze and synthesize music. To allow simple and natural encoding of rules, we build our library in Agda [Norell 2007], a functional language with full dependent types. As an application of the library, we demonstrate an implementation of species counterpoint, based on the rules given by Fux [1965]. Thanks to Agda’s rich type system, we can express the rules in a straightforward manner, and thus ensure by construction that well-typed counterpoint satisfies all the required rules.

2 The Music Tools Library

The goal of *Music Tools* is to provide a core collection of types and functions that can be used to easily build applications to analyze and synthesize music. It is intended to evolve into a dependently-typed replacement for *Euterpea* [Hudak and Quick 2018], and borrows many ideas from that library. Currently, *Music Tools* is restricted to the chromatic scale for simplicity, and like *Euterpea* is designed to work well with MIDI.

The fundamental type for melody is *Pitch*, which is just a natural number with 0 representing the lowest expressible pitch (it is intended to correspond to MIDI note 0, but the interpretation can change depending upon the application). One can also express pitch as a pair of an octave and relative pitch within the octave, which is more convenient for some applications, and convert between this representation and absolute pitch. One can then prove that converting back and forth is the identity function.

For rhythm the fundamental type is *Duration*, also a natural number, which represents some unspecified unit of time (when the music is played the unit is then specified). A combination of a pitch and a duration gives a *Note*, and notes in

¹<https://github.com/halfaya/MusicTools>

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