# SSJ User's Guide

# Package simevents

Simulation Clock and Event List Management

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This package provides the simulation clock and tools to manage the future events list. These are the basic tools for discrete-event simulation. Several different implementations of the event list are offered. Some basic tools for continuous simulation (i.e., solving differential equations with respect to time) are also provided.

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### Overview

The scheduling part of discrete-event simulations is managed by the "chief-executive" class Simulator, which contains the simulation clock and the central monitor. The event list is taken from one of the implementations of the interface EventList, which provide different kinds of event list implementations. One can change the default SplayTree event list implementation via the method init. The class Event provides the facilities for creating and scheduling events in the simulation. Each type of event must be defined by extending the class Event. The class Continuous provides elementary tools for continuous simulation, where certain variables vary continuously in time according to ordinary differential equations.

The class LinkedListStat implements *doubly linked* lists, with tools for inserting, removing, and viewing objects in the list, and automatic statistical collection. These lists can contain any kind of Object.

# Sim

This static class contains the executive of a discrete-event simulation. It maintains the simulation clock and starts executing the events in the appropriate order. Its methods permit one to start, stop, and (re)initialize the simulation, and read the simulation clock.

Starting from SSJ-2.0, the Sim class now uses the default simulator returned by the getDefaultSimulator() method in the Simulator class. Although the Sim class is perfectly adequate for simple simulations, the Simulator class is more general and supports more functionnalities. For example, if one needs to have more than one simulation clock and event list, one will have to use the Simulator class instead of the simpler Sim class.

```
package umontreal.iro.lecuyer.simevents;
public final class Sim
```

#### Methods

```
public static double time()
```

Returns the current value of the simulation clock.

```
public static void init()
```

Reinitializes the simulation executive by clearing up the event list, and resetting the simulation clock to zero. This method must not be used to initialize process-driven simulation; SimProcess.init must be used instead.

```
public static void init (EventList evlist)
```

Same as init, but also chooses evlist as the event list to be used. For example, calling init(new DoublyLinked()) initializes the simulation with a doubly linked linear structure for the event list. This method must not be used to initialize process-driven simulation; umontreal.iro.lecuyer.simprocs.DSOLProcessSimulator (EventList) or umontreal.iro.lecuyer.simprocs.ThreadProcessSimulator (EventList) must be used

```
public static EventList getEventList()
```

Gets the currently used event list.

```
public static void start()
```

instead.

Starts the simulation executive. There must be at least one Event in the event list when this method is called.

```
public static void stop()
```

Tells the simulation executive to stop as soon as it takes control, and to return control to the program that called start. This program will then continue executing from the instructions right after its call to Sim.start. If an Event is currently executing (and this event has just called Sim.stop), the executive will take control when the event terminates its execution.

### Simulator

Represents the executive of a discrete-event simulator. This class maintains a simulation clock, an event list, and starts executing the events in the appropriate order. Its methods permit one to start, stop, and (re)initialize the simulation, and read the simulation clock.

Usually, a simulation program uses a single simulation clock which is represented by an instance of this class. For more convenience and compatibility, this class therefore provides a mechanism to construct and return a default simulator which is used when an event is constructed without an explicit reference to a simulator, and when the simulator is accessed through the Sim class.

Note that this class is NOT thread-safe. Consequently, if a simulation program uses multiple threads, it should acquire a lock on a simulator (using a synchronized block) before accessing its state. Note however, that one can launch many simulations in parallel with as many threads, as long as *each thread has its own* Simulator.

```
package umontreal.iro.lecuyer.simevents;
  import java.util.ListIterator;
public class Simulator
  public static Simulator defaultSimulator
```

Represents the default simulator being used by the class Sim, and the no-argument constructor of Event. This simulator is usually obtained with the getDefaultSimulator method, which initializes it if needed. But it might also be initialized differently, e.g., if process-driven simulation is required.

#### Constructors

```
public Simulator()
```

Constructs a new simulator using a splay tree for the event list.

```
public Simulator (EventList eventList)
```

Constructs a new simulator using eventList for the event list.

#### Methods

```
public double time()
```

Returns the current value of the simulation clock.

```
public void init()
```

Reinitializes the simulation executive by clearing up the event list, and resetting the simulation clock to zero.

#### public void init (EventList evlist)

Same as init, but also chooses evlist as the event list to be used. For example, init (new DoublyLinked()) initializes the simulation with a doubly linked linear structure for the event list. To initialize the current Simulator with a not empty eventList is also possible, but the events scheduled in the eventList will be linked with the current simulator only.

#### public EventList getEventList()

Gets the currently used event list.

#### public boolean isSimulating()

Determines if this simulator is currently running, i.e., executing scheduled events.

#### public boolean isStopped()

Determines if this simulator was stopped by an event. The simulator may still be processing the event which has called the stop method; in this case, isSimulating returns true.

#### protected Event removeFirstEvent()

Removes the first event from the event list and sets the simulation clock to its event time.

#### public void start ()

Starts the simulation executive. There must be at least one Event in the event list when this method is called.

#### public void stop()

Tells the simulation executive to stop as soon as it takes control, and to return control to the program that called start. This program will then continue executing from the instructions right after its call to start If an Event is currently executing (and this event has just called stop), the executive will take control when the event terminates its execution.

#### public ContinuousState continuousState()

Returns the current state of continuous variables being integrated during the simulation. This state is used by the Continuous class when performing simulation of continuous variables; it defaults to an empty state, which is initialized only when this method is called.

#### Static methods

#### public static Simulator getDefaultSimulator()

Returns the default simulator instance used by the deprecated class Sim. If this simulator does not exist yet, it is constructed using the no-argument constructor of this class. One can specify a different default simulator by setting the defaultSimulator field directly.

### **Event**

This abstract class provides event scheduling tools. Each type of event should be defined as a subclass of the class Event, and should provide an implementation of the method actions which is executed when an event of this type occurs. The instances of these subclasses are the actual events.

Each event is linked to a simulator represented by an instance of Simulator before it can be scheduled and processed. A default simulator, given by Simulator.getDefaultSimulator, is used if no simulator is linked explicitly with an event. When an event is constructed, it is not scheduled. It must be scheduled separately by calling one of the scheduling methods schedule, scheduleNext, scheduleBefore, etc. An event can also be cancelled before it occurs.

A scheduled event has an associated time at which it will happen and a priority, which can be queried using the methods time and priority, respectively. By default, events occur in ascending order of time, and have priority 1. Events with the same time occur in ascending order of priority. For example, if events e1 and e2 occur at the same time with priority 2 and 1 respectively, then e2 will occur before e1. Events with the same time and priority occur in the order they were scheduled.

```
package umontreal.iro.lecuyer.simevents;
public abstract class Event implements Comparable<Event>
```

#### Constructors

```
public Event()
```

Constructs a new event instance, which can be placed afterwards into the event list of the default simulator by calling one of the schedule... variants. For example, if Bang is an Event subclass, the statement "new Bang().scheduleNext();" creates a new Bang event and places it at the beginning of the event list.

```
public Event (Simulator sim)
```

Construct a new event instance associated with the given simulator.

#### Methods

```
public void schedule (double delay)
```

Schedules this event to happen in delay time units, i.e., at time sim.time() + delay, by inserting it in the event list. When two or more events are scheduled to happen at the same time and with the same priority, they are placed in the event list (and executed) in the same order as they have been scheduled. Note that the priority of this event should be adjusted using setPriority before it is scheduled.

#### public void scheduleNext()

Schedules this event as the *first* event in the event list, to be executed at the current time (as the next event).

#### public void scheduleBefore (Event other)

Schedules this event to happen just before, and at the same time, as the event other. For example, if Bing and Bang are Event subclasses, after the statements

```
Bang bigOne = new Bang().schedule(12.0);
new Bing().scheduleBefore(bigOne);
```

the event list contains two new events scheduled to happen in 12 units of time: a Bing event, followed by a Bang called bigOne.

#### public void scheduleAfter (Event other)

Schedules this event to happen just after, and at the same time, as the event other.

#### public void reschedule (double delay)

Cancels this event and reschedules it to happen in delay time units.

#### public boolean cancel()

Cancels this event before it occurs. Returns true if cancellation succeeds (this event was found in the event list), false otherwise.

#### public final boolean cancel (String type)

Finds the first occurrence of an event of class "type" in the event list, and cancels it. Returns true if cancellation succeeds, false otherwise.

#### public final Simulator simulator()

Returns the simulator linked to this event.

#### public final void setSimulator (Simulator sim)

Sets the simulator associated with this event to sim. This method should not be called while this event is in an event list.

#### public final double time()

Returns the (planned) time of occurrence of this event.

#### public final void setTime (double time)

Sets the (planned) time of occurrence of this event to time. This method should never be called after the event was scheduled, otherwise the events would not execute in ascending time order anymore.

#### public final double priority()

Returns the priority of this event.

#### public final void setPriority (double priority)

Sets the priority of this event to inPriority. This method should never be called after the event was scheduled, otherwise the events would not execute in ascending priority order anymore.

#### public int compareTo (Event e)

Compares this object with the specified object e for order. Returns -1 or +1 as this event occurs before or after the specified event e, respectively. If the two events occur at the same time, then returns -1, 0, or +1 as this event has a smaller, equal, or larger priority than event e.

#### public abstract void actions();

This is the method that is executed when this event occurs. Every subclass of Event that is to be instantiated must provide an implementation of this method.

# Continuous

Represents a variable in a continuous-time simulation. This abstract class provides the basic structures and tools for continuous-time simulation, where certain variables evolve continuously in time, according to differential equations. Such continuous variables can be mixed with events and processes.

Each type of continuous-time variable should be defined as a subclass of Continuous. The instances of these subclasses are the actual continuous-time variables. Each subclass must implement the method derivative which returns its derivative with respect to time. The trajectory of this variable is determined by integrating this derivative. The subclass may also reimplement the method afterEachStep, which is executed immediately after each integration step. By default (in the class Continuous), this method does nothing. This method could, for example, verify if the variable has reached a given threshold, or update a graphical illustration of the variable trajectory.

When creating a class representing a continuous variable, the **toString** method can be overridden to display information about the continuous variable. This information will be displayed when formating the event list as a string.

Each continuous variable has a linked simulator represented by an instance of the Simulator class. If no simulator is provided explicitly when constructing a variable, the default simulator returned by Simulator.getDefaultSimulator is used.

```
package umontreal.iro.lecuyer.simevents;
public abstract class Continuous
```

#### Constructors

```
public Continuous()
```

Constructs a new continuous-time variable linked to the default simulator, without initializing it.

```
public Continuous (Simulator sim)
```

Constructs a new continuous-time variable linked to the given simulator, without initializing it.

#### Methods

```
public void init (double val)
```

Initializes or reinitializes the continuous-time variable to val.

```
public double value()
```

Returns the current value of this continuous-time variable.

#### public Simulator simulator()

Returns the simulator linked to this continuous-time variable.

#### public void setSimulator(Simulator sim)

Sets the simulator linked to this continuous-time variable. This method should not be called while this variable is active.

#### public void startInteg()

Starts the integration process that will change the state of this variable at each integration step.

#### public void startInteg (double val)

Same as startInteg, after initializing the variable to val.

#### public void stopInteg()

Stops the integration process for this continuous variable. The variable keeps the value it took at the last integration step before calling stopInteg.

#### public abstract double derivative (double t);

This method should return the derivative of this variable with respect to time, at time t. Every subclass of Continuous that is to be instantiated must implement it. If the derivative does not depend explicitly on time, t becomes a dummy parameter. Internally, the method is used with t not necessarily equal to the current simulation time.

#### public void afterEachStep()

This method is executed after each integration step for this Continuous variable. Here, it does nothing, but every subclass of Continuous may reimplement it.

#### public static void selectEuler(double h)

Selects the Euler method as the integration method, with the integration step size h, in time units, for the default simulator. The non-static method selectEuler in ContinuousState can be used to set the integration method for any given simulator. This method appears here only to keep compatibility with older versions of SSJ; using a non-static Simulator instance rather than the default simulator is recommended.

#### public static void selectRungeKutta4(double h)

Selects a Runge-Kutta method of order 4 as the integration method to be used, with step size h. The non-static method selectRungeKutta4 in ContinuousState can be used to set the integration method for any given simulator. This method appears here only to keep compatibility with older versions of SSJ; using a non-static Simulator instance rather than the default simulator is recommended.

#### public static void selectRungeKutta2(double h)

Selects a Runge-Kutta method of order 2 as the integration method to be used, with step size h. The non-static method selectRungeKutta2 in ContinuousState can be used to set the integration method for any given simulator. This method appears here only to keep compatibility with older versions of SSJ; using a non-static Simulator instance rather than the default simulator is recommended.

### ContinuousState

Represents the portion of the simulator's state associated with continuous-time simulation. Any simulator, including the default static one, can have an associate continuous state which is obtained using the continuousState() method of the Simulator class. This state includes all active integration variables as well as the current integration method.

One of the methods selectEuler, selectRungeKutta2 or selectRungeKutta4 must be called before starting any integration. These methods permit one to select the numerical integration method and the step size h (in time units) that will be used for *all* continuous-time variables linked to the simulator. For all the methods, an integration step at time t changes the values of the variables from their old values at time t - h to their new values at time t.

Each integration step is scheduled as an event and added to the event list.

#### Constructor

```
protected ContinuousState (Simulator sim)
```

Creates a new ContinuousState object linked to the given simulator. Usually, the user should not call this constructor directly since a new object is created automatically by the continuousState() method of class Simulator.

#### Methods

```
public List<Continuous> getContinuousVariables()
```

Returns the list of continuous-time variables currently integrated by the simulator. The returned list is updated automatically as variables are added or removed, but it cannot be modified directly. One must instead use startInteg or stopInteg in class Continuous to add or remove variables.

```
public IntegMethod integMethod ()
```

Return an integer that represent the integration method in use.

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#### public void selectEuler (double h)

Selects the Euler method as the integration method, with the integration step size h, in time units.

### public void selectRungeKutta2 (double h)

Selects a Runge-Kutta method of order 2 as the integration method to be used, with step size h.

#### public void selectRungeKutta4 (double h)

Selects a Runge-Kutta method of order 4 as the integration method to be used, with step size h.

### ListWithStat

Implements a list with integrated statistical probes to provide automatic collection of statistics on the sojourn times of objects in the list and on the size of the list as a function of time given by a simulator. The automatic statistical collection can be enabled or disabled for each list, to reduce overhead. This class extends TransformingList and transforms elements into nodes associating insertion times with elements.

#### Constructors

```
public ListWithStat (List<Node<E>> nodeList)
```

Constructs a new list with internal data structure using the default simulator and implemented by nodeList. The given list is cleared for the constructed list to be initially empty.

```
public ListWithStat (Simulator inSim, List<Node<E>> nodeList)
```

Constructs a new list with internal data structure implemented by nodeList. The given list is cleared for the constructed list to be initially empty.

```
public ListWithStat (List<Node<E>> nodeList, Collection<? extends E> c)
```

Constructs a list containing the elements of the specified collection, whose elements are stored into nodeList and using the default simulator.

Constructs a list containing the elements of the specified collection, whose elements are stored into nodeList.

```
public ListWithStat (List<Node<E>> nodeList, String name)
```

Constructs a new list with name name, internal list nodeList, and using the default simulator. This name can be used to identify the list in traces and reports. The given list is cleared for the constructed list to be initially empty.

Constructs a new list with name name, and internal list nodeList. This name can be used to identify the list in traces and reports. The given list is cleared for the constructed list to be initially empty.

Constructs a new list containing the elements of the specified collection c, with name name, internal list nodeList, and using the default simulator. This name can be used to identify the list in traces and reports.

Constructs a new list containing the elements of the specified collection c, with name name, and internal list nodeList. This name can be used to identify the list in traces and reports.

#### Methods

```
public E convertFromInnerType (Node<E> node)
public Node<E> convertToInnerType (E element)
public Simulator simulator()
  Returns the simulator associated with this list.
public void setSimulator(Simulator sim)
```

Sets the simulator associated with this list. This list should be cleared after this method is called.

#### Statistic collection methods

```
public boolean getStatCollecting()
```

Returns true if the list collects statistics about its size and sojourn times of elements, and false otherwise. By default, statistical collecting is turned off.

```
public void setStatCollecting (boolean b)
```

Starts or stops collecting statistics on this list. If the statistical collection is turned ON, the method creates two statistical probes if they do not exist yet. The first one, of the class Accumulate, measures the evolution of the size of the list as a function of time. It can be accessed by the method statSize. The second one, of the class Tally and accessible via statSojourn, samples the sojourn times in the list of the objects removed during the observation period, i.e., between the last initialization time of this statistical probe and the current time. The method automatically calls initStat to initialize these two probes. When this method is used, it is normally invoked immediately after calling the constructor of the list.

```
public void initStat()
```

Reinitializes the two statistical probes created by setStatCollecting (true) and makes an update for the probe on the list size.

#### public double getInitTime()

Returns the last simulation time initStat was called.

```
public Accumulate statSize()
```

Returns the statistical probe on the evolution of the size of the list as a function of the simulation time. This probe exists only if setStatCollecting (true) has been called for this list.

```
public Tally statSojourn()
```

Returns the statistical probe on the sojourn times of the objects in the list. This probe exists only if setStatCollecting (true) has been called for this list.

```
public String report()
```

Returns a string containing a statistical report on the list, provided that setStatCollecting (true) has been called before for this list. Even If setStatCollecting was called with false afterward, the report will be made for the collected observations. If the probes do not exist, i.e., setStatCollecting was never called for this object, an illegal state exception will be thrown.

```
public String getName()
```

Returns the name associated to this list, or null if no name was assigned.

#### Inner class

```
public static class Node<E>
```

Represents a node that can be part of a list with statistical collecting.

#### Constructor

```
public Node (E element, double insertionTime)
```

Constructs a new node containing element element inserted into the list at time insertionTime.

#### Methods

```
public E getElement()
```

Returns the element stored into this node.

```
public double getInsertionTime()
```

Returns the insertion time of the element in this node.

## LinkedListStat

This class extends ListWithStat, and uses a linked list as the internal data structure.

package umontreal.iro.lecuyer.simevents;

public class LinkedListStat<E> extends ListWithStat<E>

#### Constructors

```
public LinkedListStat()
```

Constructs a new list, initially empty.

public LinkedListStat(Simulator inSim)

Constructs a new list, initially empty, and using the default simulator.

```
public LinkedListStat (Collection<? extends E> c)
```

Constructs a list containing the elements of the specified collection, using the default simulator.

```
public LinkedListStat (Simulator inSim, Collection<? extends E> c)
```

Constructs a list containing the elements of the specified collection.

```
public LinkedListStat (String name)
```

Constructs a new list with name name, using the default simulator. This name can be used to identify the list in traces and reports.

```
public LinkedListStat (Simulator inSim, String name)
```

Constructs a new list with name name. This name can be used to identify the list in traces and reports.

```
public LinkedListStat (Collection<? extends E> c, String name)
```

Constructs a new list containing the elements of the specified collection c and with name name, using the default simulator. This name can be used to identify the list in traces and reports.

Constructs a new list containing the elements of the specified collection c and with name name. This name can be used to identify the list in traces and reports.

#### LinkedList methods

See the JDK documentation for more information about these methods.

```
public void addFirst (E obj)
public void addLast (E obj)
public E getFirst()
public E getLast()
public E removeFirst()
public E removeLast()
```

### Accumulate

A subclass of StatProbe, for collecting statistics on a variable that evolves in simulation time, with a piecewise-constant trajectory. Each time the variable changes its value, the method update must be called to inform the probe of the new value. The probe can be reinitialized by init.

package umontreal.iro.lecuyer.simevents; public class Accumulate extends StatProbe implements Cloneable

#### Constructors

#### public Accumulate()

Constructs a new Accumulate statistical probe using the default simulator and initializes it by invoking init().

#### public Accumulate (Simulator inSim)

Constructs a new Accumulate statistical probe linked to the given simulator, and initializes it by invoking init().

#### public Accumulate (String name)

Construct and initializes a new Accumulate statistical probe with name name and initial time 0, using the default simulator.

```
public Accumulate (Simulator inSim, String name)
```

Construct and initializes a new Accumulate statistical probe with name name and initial time 0.

#### Methods

```
public void init()
```

Initializes the statistical collector and puts the current value of the corresponding variable to 0.

```
public void init (double x)
```

Same as init followed by update(x).

#### public void update()

Updates the accumulator using the last value passed to update.

```
public void update (double x)
```

Gives a new observation x to the statistical collector. If broadcasting to observers is activated for this object, this method will also transmit the new information to the registered observers by invoking the methods notifyListeners.

#### public double getInitTime()

Returns the initialization time for this object. This is the simulation time when init was called for the last time.

#### public double getLastTime()

Returns the last update time for this object. This is the simulation time of the last call to update or the initialization time if update was never called after init.

#### public double getLastValue()

Returns the value passed to this probe by the last call to its update method (or the initial value if update was never called after init).

#### public Simulator simulator()

Returns the simulator associated with this statistical probe.

#### public void setSimulator(Simulator sim)

Sets the simulator associated with this probe to sim. One should call init after this method to reset the statistical probe.

### public Accumulate clone()

Clone this object.

### **EventList**

An interface for implementations of event lists. Different implementations are provided in SSJ: doubly-linked list, splay tree, Henricksen's method, etc. The *events* in the event list are objects of the class Event. The method Sim.init permits one to select the actual implementation used in a simulation [2].

To allow the user to print the event list, the toString method from the Object class should be reimplemented in all EventList implementations. It will return a string in the following format: "Contents of the event list event list class:" for the first line and each subsequent line has format "scheduled event time, event priority: event string". The event string is obtained by calling the toString method of the event objects. The string should not end with the end-of-line character.

The following example is the event list of the bank example, printed at 10h30. See examples.pdf for more information.

```
Contents of the event list SplayTree:
```

```
10.51, 1 : BankEv$Arrival@cfb549

10.54, 1 : BankEv$Departure@8a7efd

11, 1 : BankEv$3@86d4c1

14, 1 : BankEv$4@f9f9d8

15, 1 : BankEv$5@820dda
```

```
package umontreal.iro.lecuyer.simevents.eventlist;
public interface EventList extends Iterable<Event>
   public boolean isEmpty();
    Returns true if and only if the event list is empty (no event is scheduled).

public void clear();
   Empties the event list, i.e., cancels all events.

public void add (Event ev);
   Adds a new event in the event list, according to the time of ev. If the event list contains events scheduled to happen at the same time as ev, ev must be added after all these events.

public void addFirst (Event ev);
```

public void addBefore (Event ev, Event other);

current simulation time.

Same as add, but adds the new event ev immediately before the event other in the list.

Adds a new event at the beginning of the event list. The given event ev will occur at the

#### public void addAfter (Event ev, Event other);

Same as add, but adds the new event ev immediately after the event other in the list.

#### public Event getFirst();

Returns the first event in the event list. If the event list is empty, returns null.

#### public Event getFirstOfClass (String cl);

Returns the first event of the class cl (a subclass of Event) in the event list. If no such event is found, returns null.

#### public <E extends Event> E getFirstOfClass (Class<E> cl);

Returns the first event of the class E (a subclass of Event) in the event list. If no such event is found, returns null.

#### public ListIterator<Event> listIterator();

Returns a list iterator over the elements of the class Event in this list.

#### public boolean remove (Event ev);

Removes the event ev from the event list (cancels this event). Returns true if and only if the event removal has succeeded.

#### public Event removeFirst();

Removes the first event from the event list (to cancel or execute this event). Returns the removed event. If the list is empty, then null is returned.

# DoublyLinked

An implementation of EventList using a doubly linked linear list. Each event is stored into a list node that contains a pointer to its following and preceding events. Adding an event requires a linear search to keep the event list sorted by event time and priority. Removing the first event is done in constant time because it simply removes the first list node. List nodes are recycled for increased memory management efficiency.

package umontreal.iro.lecuyer.simevents.eventlist; public class DoublyLinked implements EventList

# SplayTree

An implementation of EventList using a splay tree [4]. This tree is like a binary search tree except that when it is modified, the affected node is moved to the top. The rebalancing scheme is simpler than for a  $red\ black$  tree and can avoid the worst case of the linked list. This gives a  $O(\log(n))$  average time for adding or removing an event, where n is the size of the event list.

package umontreal.iro.lecuyer.simevents.eventlist; public class SplayTree implements EventList

# BinaryTree

An implementation of EventList using a binary search tree. Every event is stored into a tree node which has left and right children. Using the event time as a comparator the left child is always smaller than its parent whereas the right is greater or equal. This allows an average  $O(\log(n))$  time for adding an event and searching the first event, where n is the number of events in the structure. There is less overhead for adding and removing events than splay tree or red black tree. However, in the worst case, adding or removing could be done in time proportional to n because the binary search tree can be turned into a linked list.

package umontreal.iro.lecuyer.simevents.eventlist; public class BinaryTree implements EventList

# Henriksen

An implementation of EventList using the doubly-linked indexed list of Henriksen [3] (see also [1, p. 207]).

Events are stored in a normal doubly-linked list. An additionnal index array is added to the structure to allow quick access to the events.

package umontreal.iro.lecuyer.simevents.eventlist; public class Henriksen implements EventList

# RedblackTree

An implementation of EventList using a red black tree, which is similar to a binary search tree except that every node is colored red or black. When modifying the structure, the tree is reorganized for the colors to satisfy rules that give an average  $O(\log(n))$  time for removing the first event or inserting a new event, where n is the number of elements in the structure. However, adding or removing events imply reorganizing the tree and requires more overhead than a binary search tree.

The present implementation uses the Java 2 TreeMap class which implements a red black tree for general usage. This event list implementation is not efficient.

package umontreal.iro.lecuyer.simevents.eventlist; public class RedblackTree implements EventList

### References

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