



Support Vector Machines (SVM)

Session-11



SUMMARY of PREVIOUS CLASS

- KNN
- Selection of K: Elbow, Gridsearch
- Distance:
 - Euclidian
 - Manhattan
 - Minkowski
- Weights parameters
 - Uniform: Majority voting
 - Distance: Weighted majority voting
- Data Scaling is important

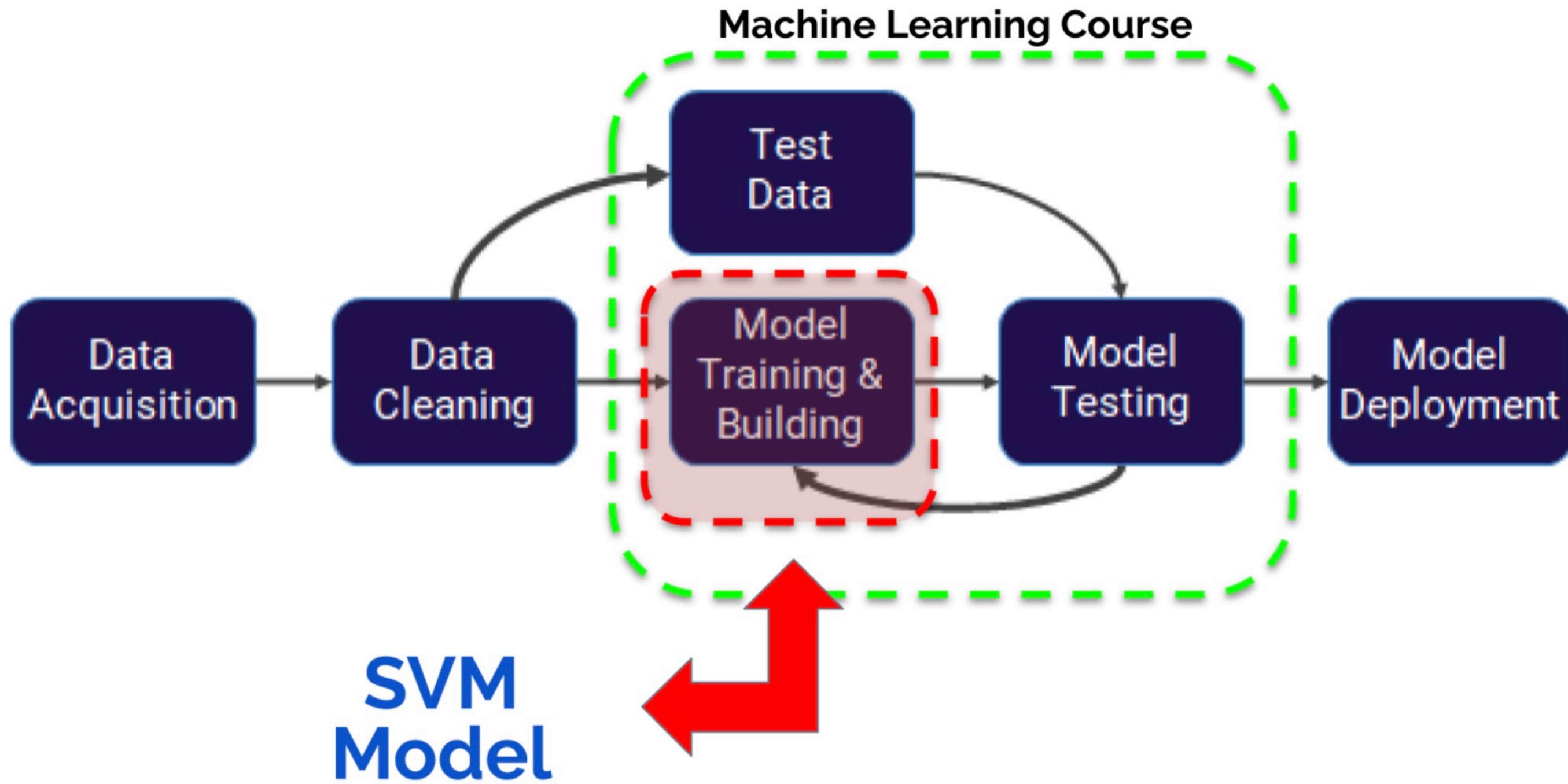


Support Vector Machines Theory

Support Vector Machines with Python



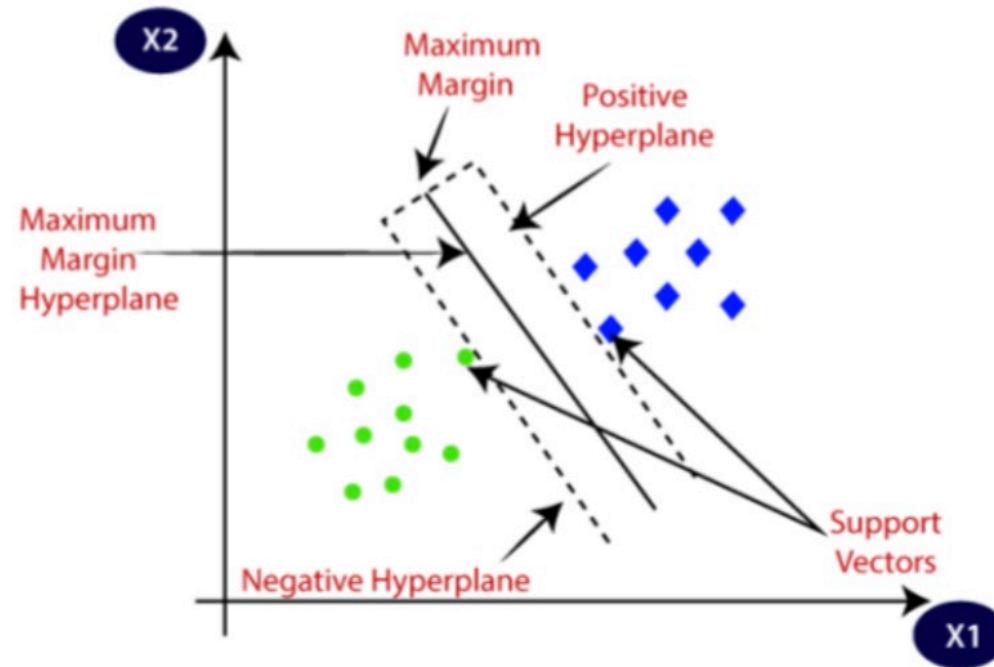
Where are we?



SVM Theory



Support Vector Machines are used especially in **classification problems** with **high accuracy** capacity.



Some usage areas of SVM classification problems:

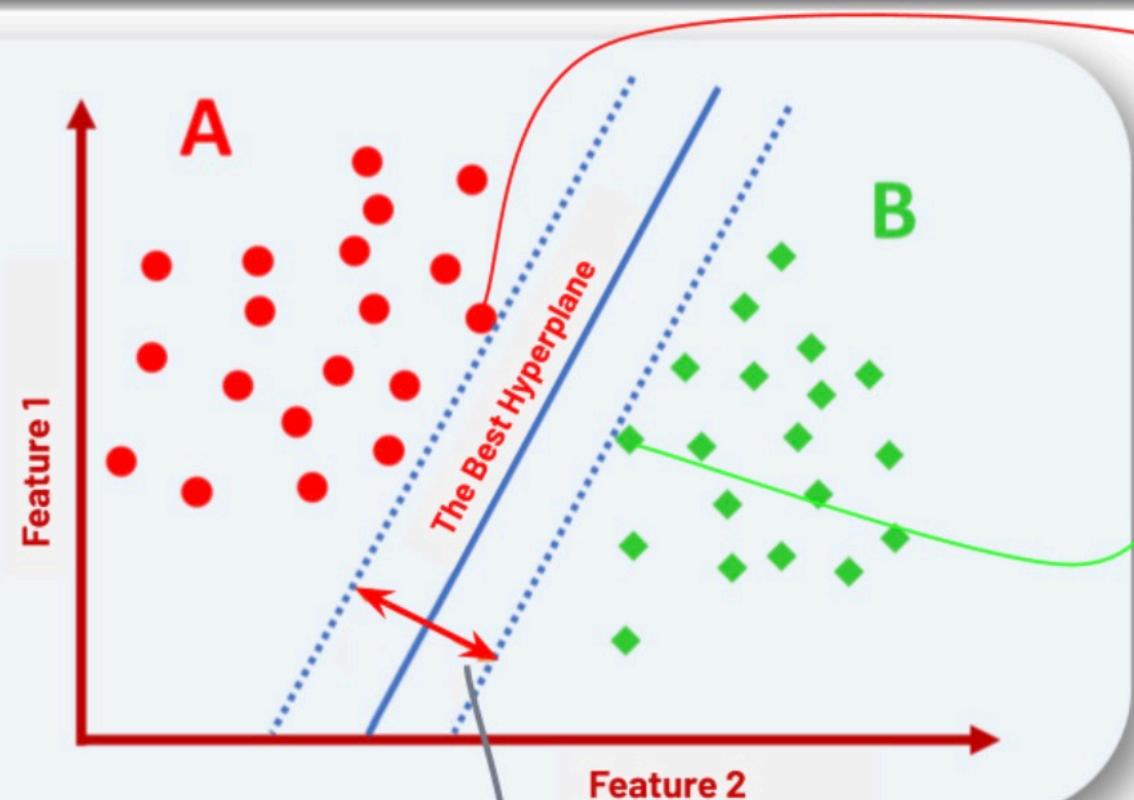
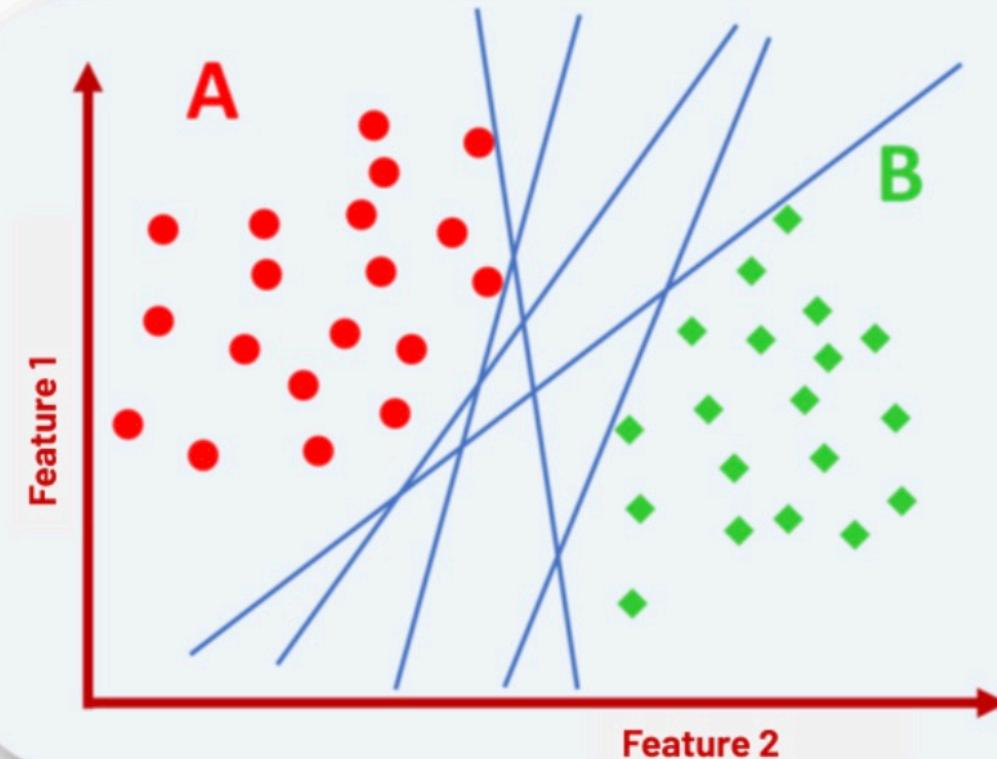
- * Text Classification,
- * Pattern Recognition,
- * Image-based Gender Detection etc.

SVM Theory



The main goal of the SVM algorithm is to find a hyperplane in the space of variables that perfectly separates classes.

2 Dimensional



SVM picks the best separating hyperplane based on the **maximum margin (Max. Margin Classification)**

SVM Theory

We can think of **hyperplanes** as decision boundaries founded using classification.

3 Dimensional

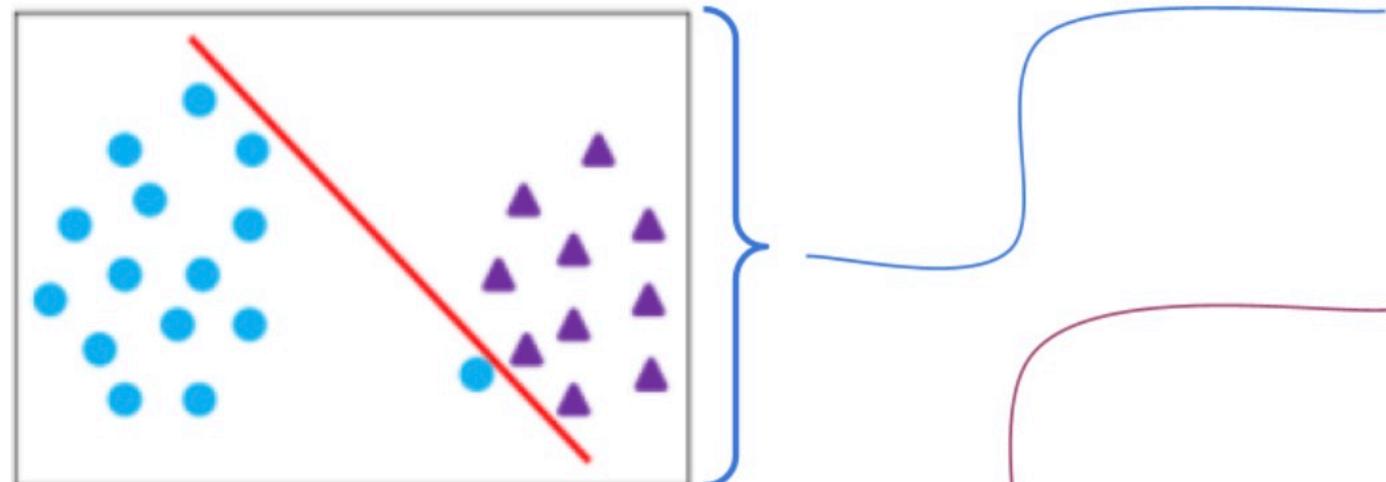
Since we have **two variables**, our hyperplane was **just one line**.

We see the **hyperplane** created for a **three variable dataset**.

However, when the number of variables exceeds three, we will not be able to show them visually.

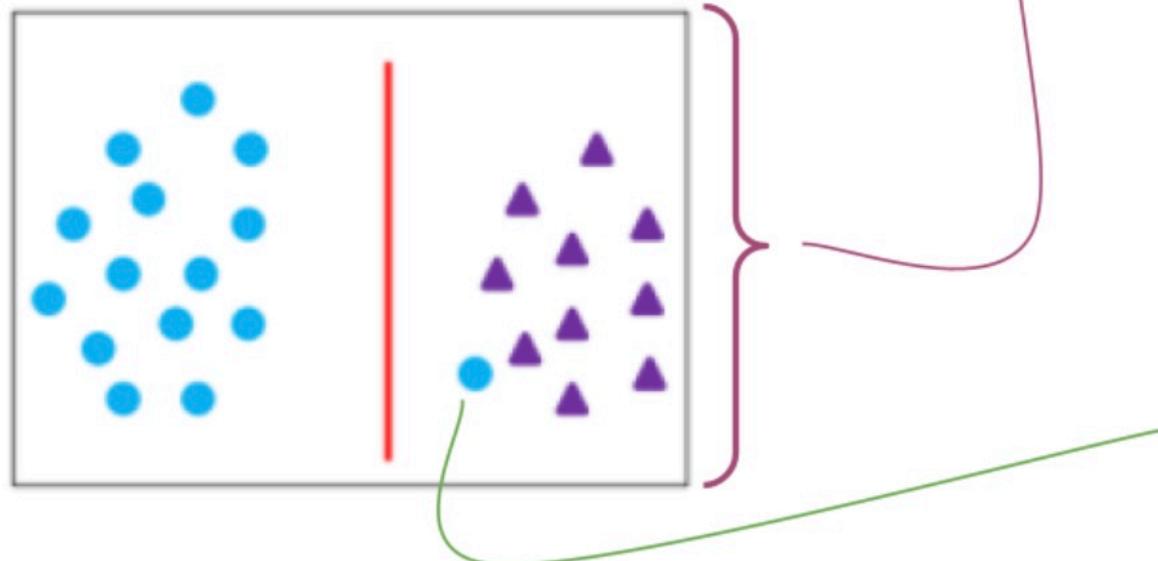
SVM Theory

Soft Margin Classification



Data linearly separable by only a **very narrow margin.** (Hard Margin)

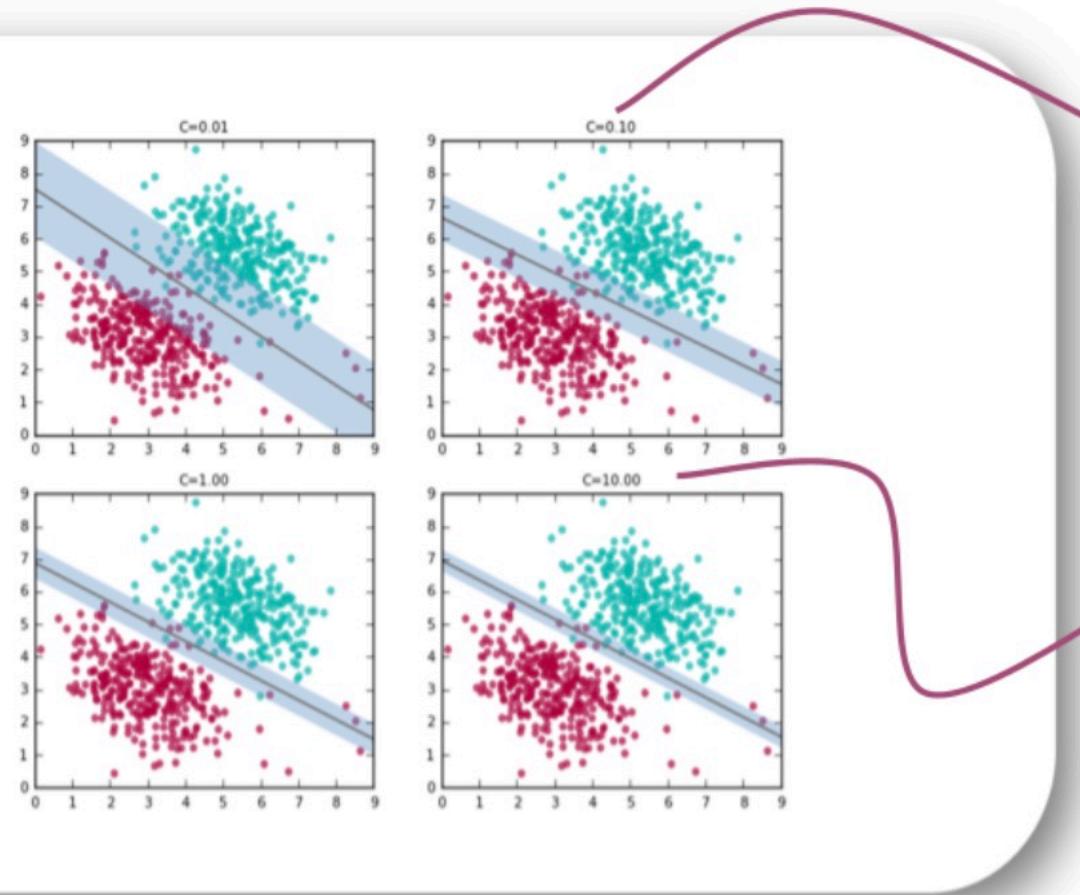
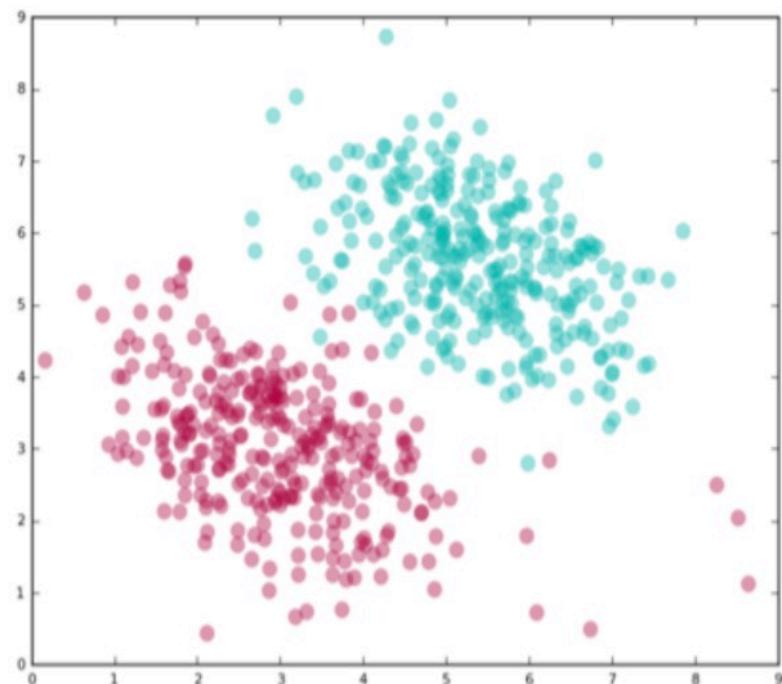
Large margin separation **is better** in case of **minor misclassifications.** (Soft Margin)



* **Hard margin classification** requires that all data points are classified correctly.

* **Soft margin classification** allow misclassification on noisy data points.

SVM Theory



“C” parameter is the **regularization** parameter of the error.

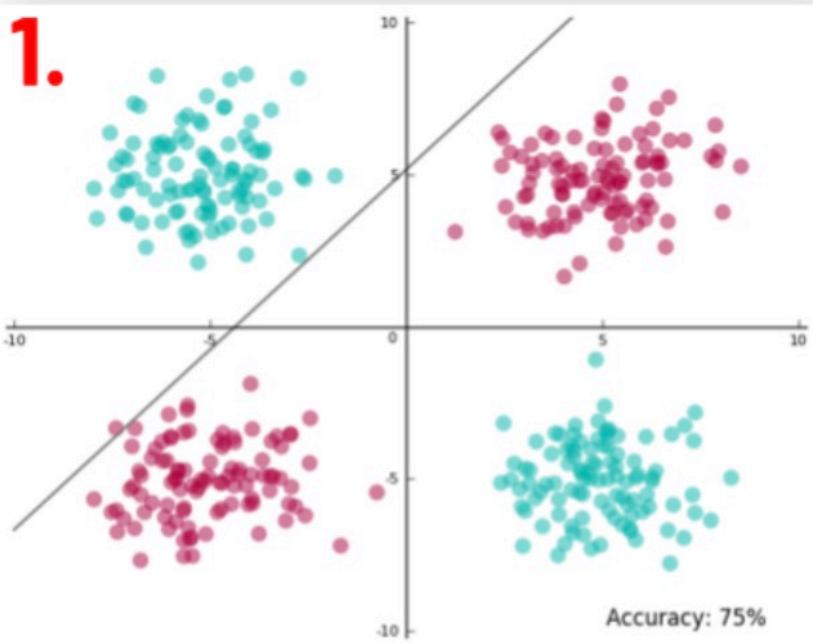
- * Although there are very close values above, we see a data set that can be separated quite successfully linearly.
- * We can estimate the approximate line although there are **some errors**.
- * With the changes in the “C” **parameter** we can change the margin size and **determine how much error we have tolerance**.

SVM Theory



What if the data is non linearly divisible?

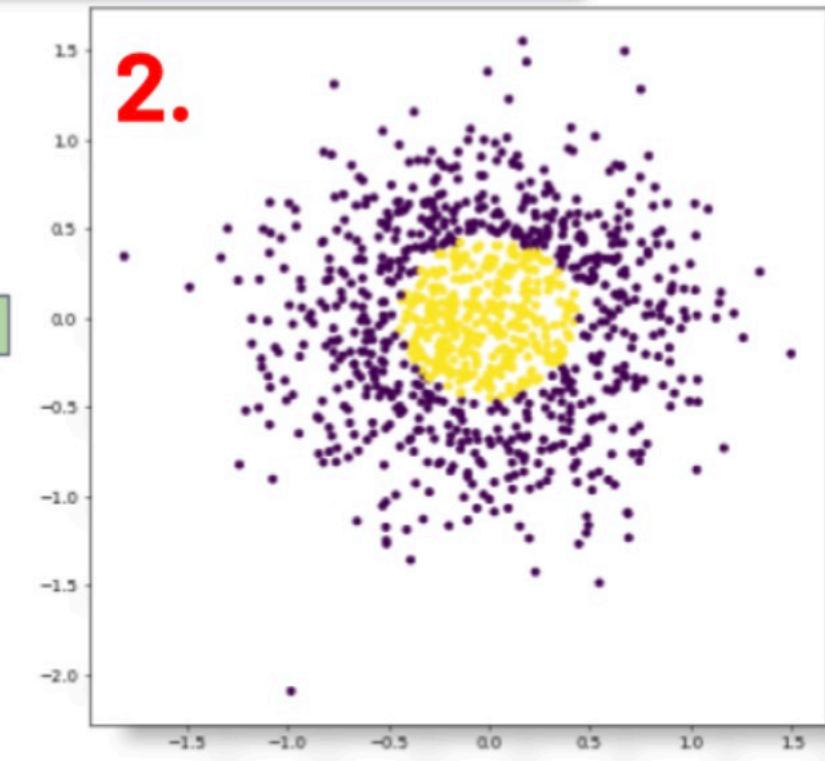
1.



How do we
separate the
classes ?



2.



3.

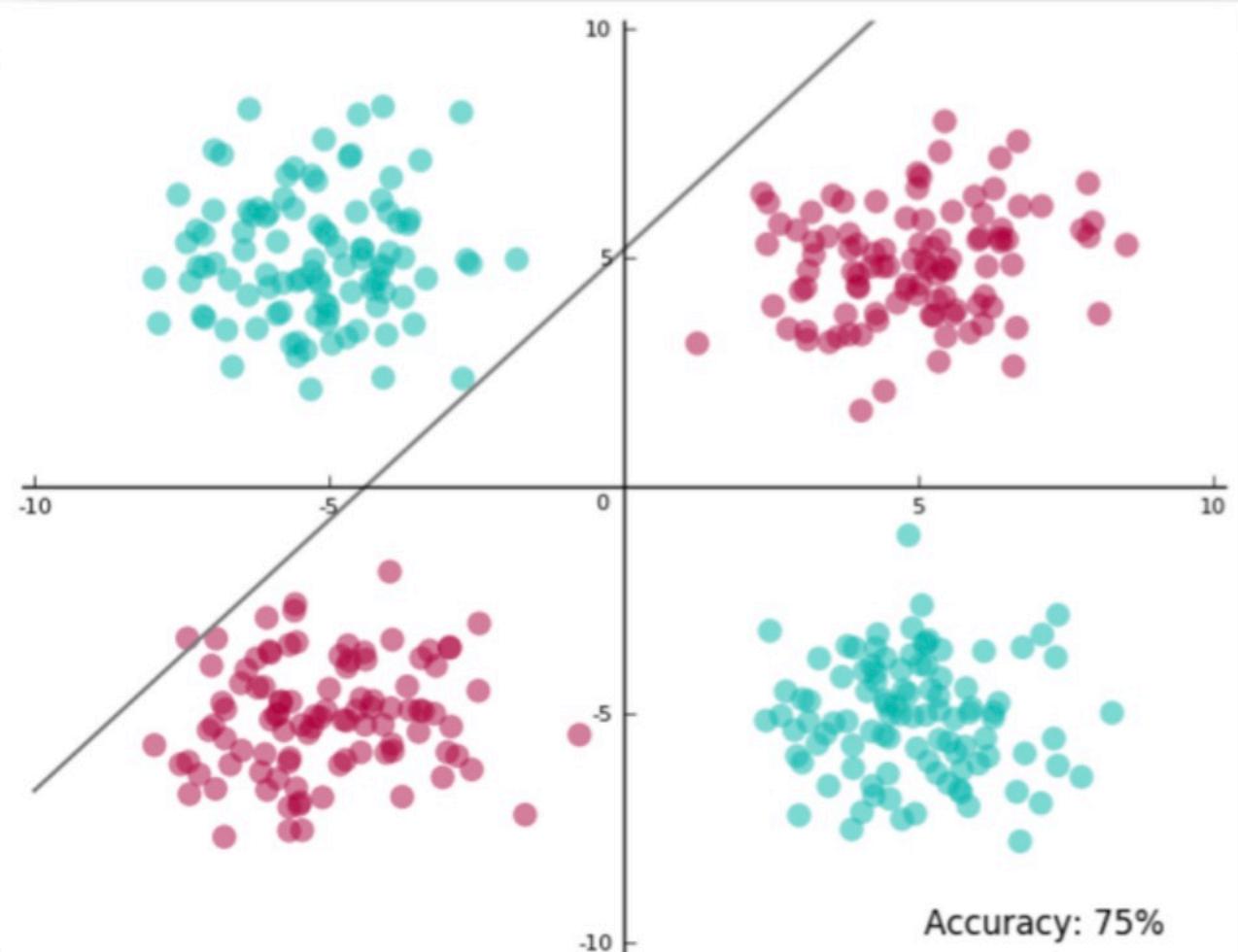
Dosage (mg):



KERNEL TRICK

SVM Theory

Sample-1



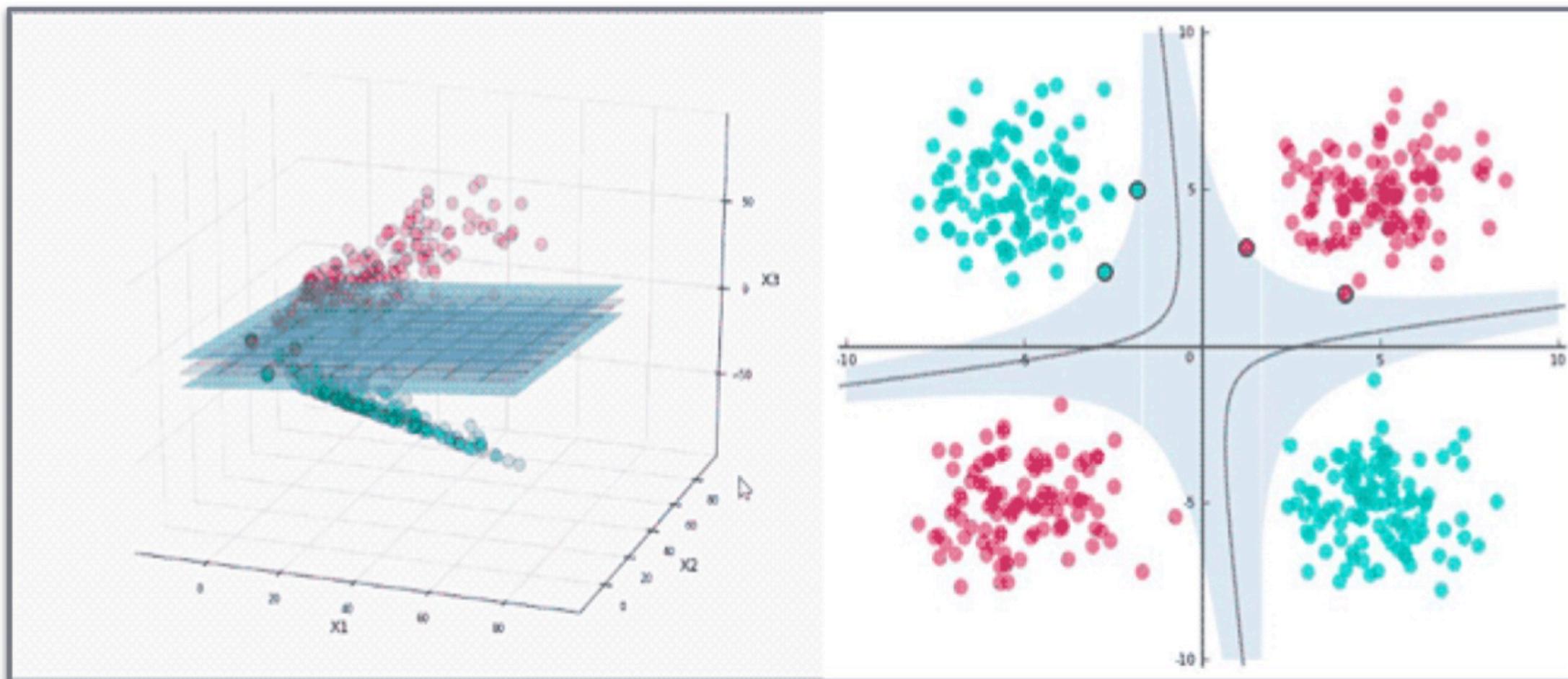
If a hyperplane is selected like the example, the success of the model will not exceed 75%.

If we make our **2-dimensional dataset to 3-dimensional**, we can divide our data with a **more uniform hyperplane**.

SVM Theory

Sample-1

When we **square** our variables (**2 D**) and **produce a new variable (3 D)**, our data will become better separable.



2D to 3D

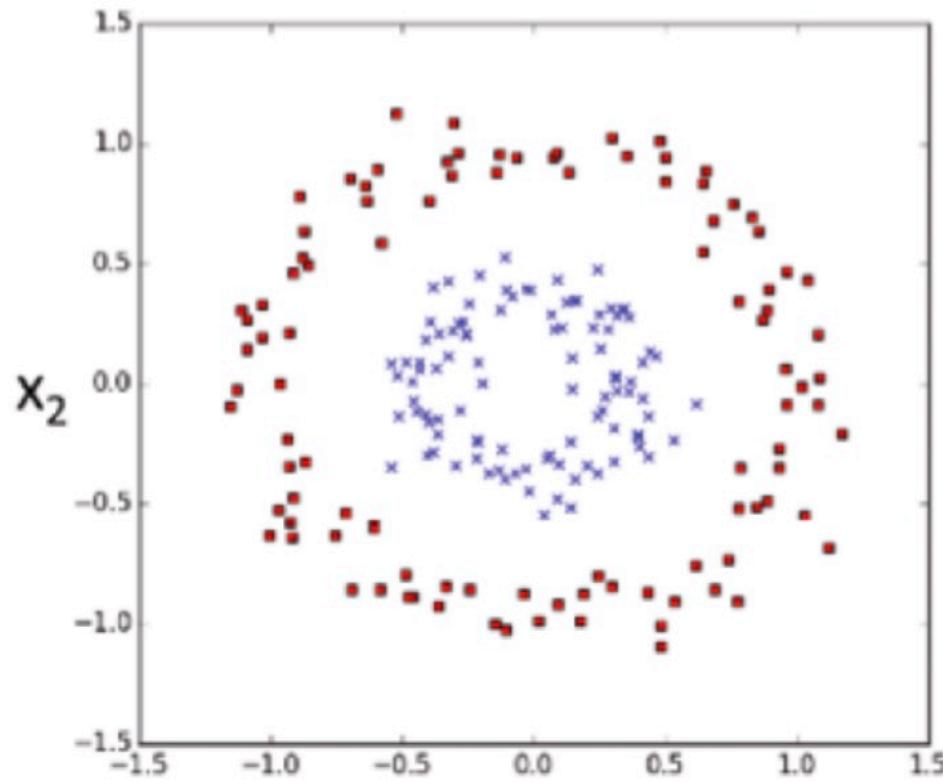
$$X_1 = x_1^2$$

$$X_2 = x_2^2$$

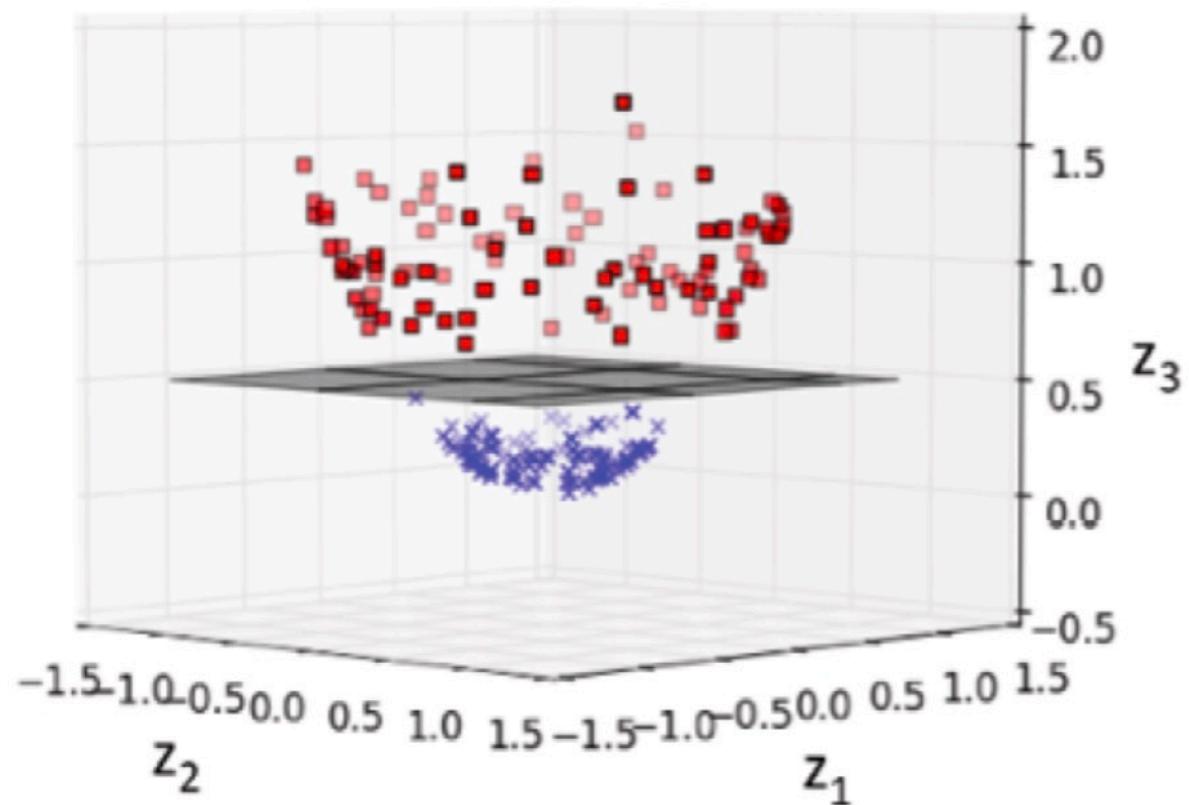
$$X_3 = \sqrt{2x_1x_2}$$

SVM Theory

Sample-2



2D to 3D



SVM Theory

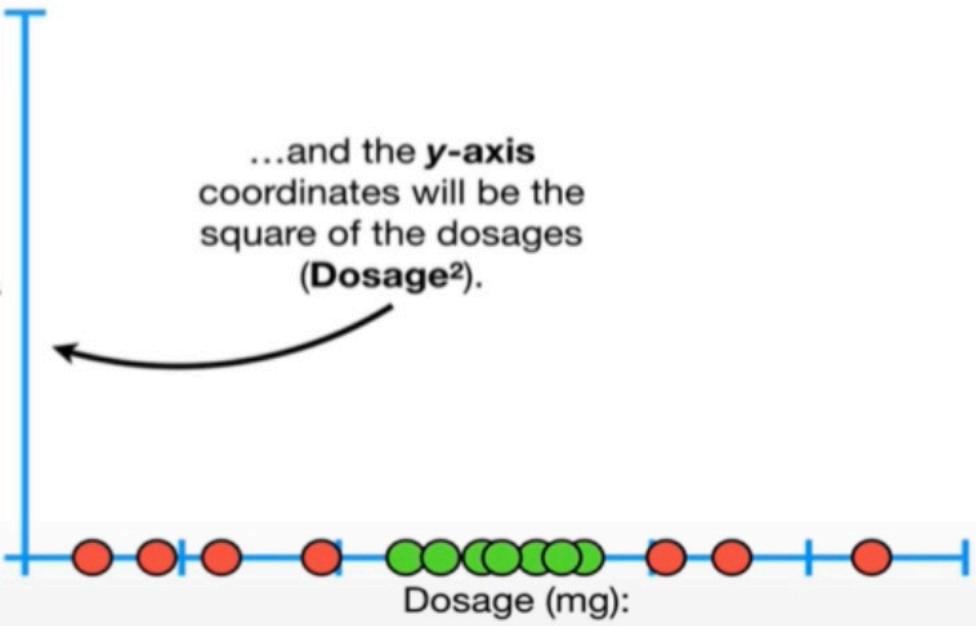
Sample-3

1.

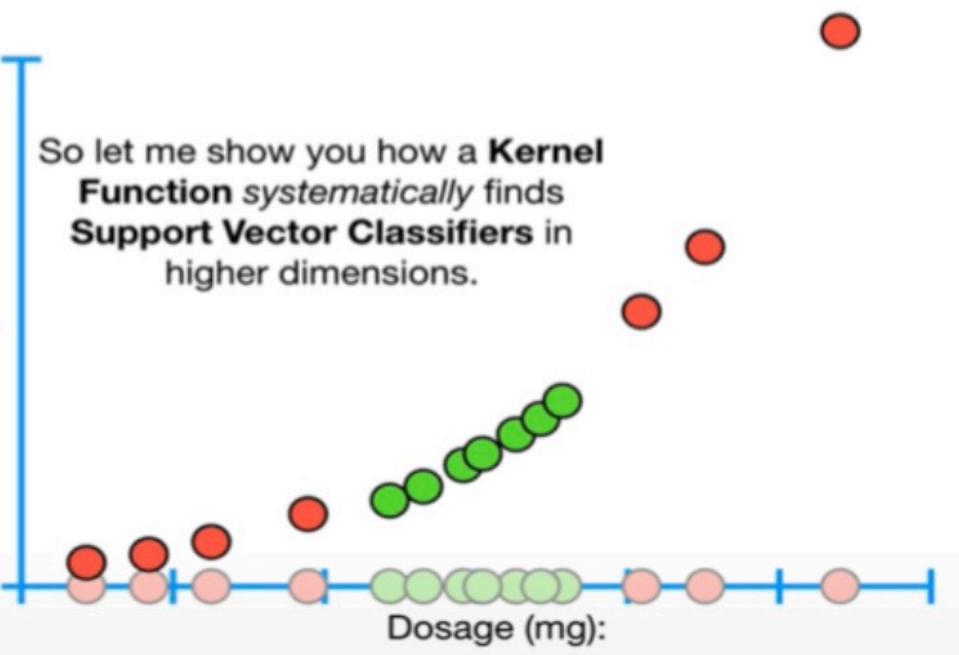
Dosage (mg):



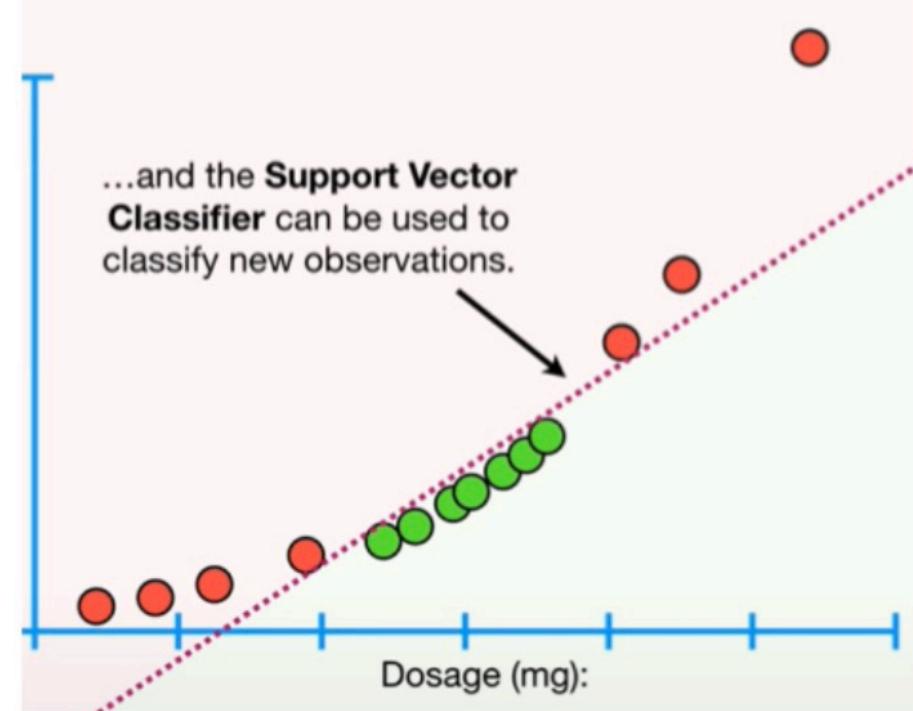
...and the **y**-axis coordinates will be the square of the dosages (**Dosage²**).



So let me show you how a **Kernel Function** systematically finds **Support Vector Classifiers** in higher dimensions.



...and the **Support Vector Classifier** can be used to classify new observations.



2. New axis (y)

3. 1D to 2D

4. Hyperplane

SVM Theory



Different Kernel Functions of SVM

	Formula	Parameters
<i>Linear</i>	$K(x, x_i) = x \cdot x_i$	/
<i>Polynomial</i>	$K(x, x_i) = [\gamma * (x \cdot x_i) + coef]^d$	$\gamma, coef, d$
<i>RBF</i>	$K(x, x_i) = \exp(-\gamma * \ x - x_i\ ^2)$	γ .
<i>Sigmoid</i>	$K(x, x_i) = \tanh(\gamma(x \cdot x_i) + coef)$	$\gamma, coef$

SVM Theory

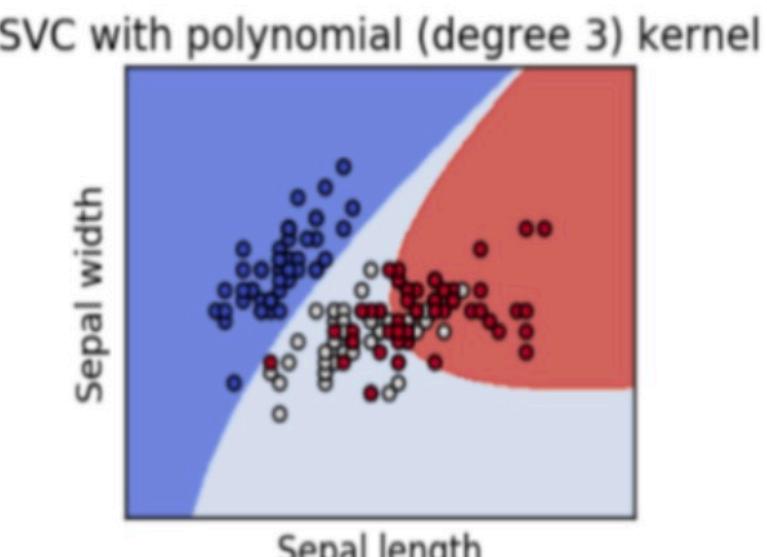
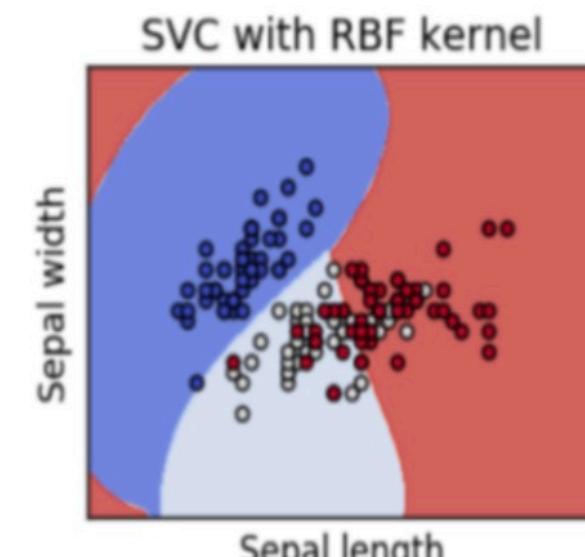
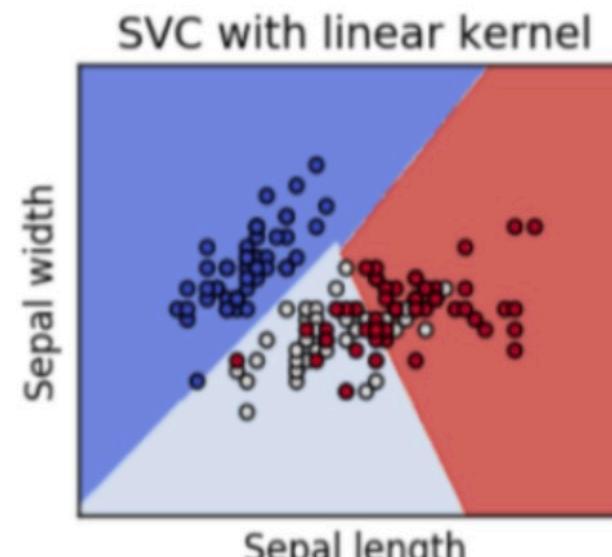


SVM Algorithm:

Hyperparameters

“kernel” parameter: (default=“rbf”)
{'linear', 'poly', 'rbf', 'sigmoid', 'precomputed'}

Specifies the kernel type to be used in the algorithm.



SVM Theory

SVM Algorithm:

Hyperparameters

“kernel” parameter: (default = “rbf”)
{'linear', 'poly', 'rbf', 'sigmoid', 'precomputed'}

What to use when?

- A **linear SVM** can perform well for problems with **many features** but **limited number of instances**,
- A **rbf kernel (default)** is good for **complex, nonlinear problems** where the number of **features is small and number of instances is large**.

SVM Theory



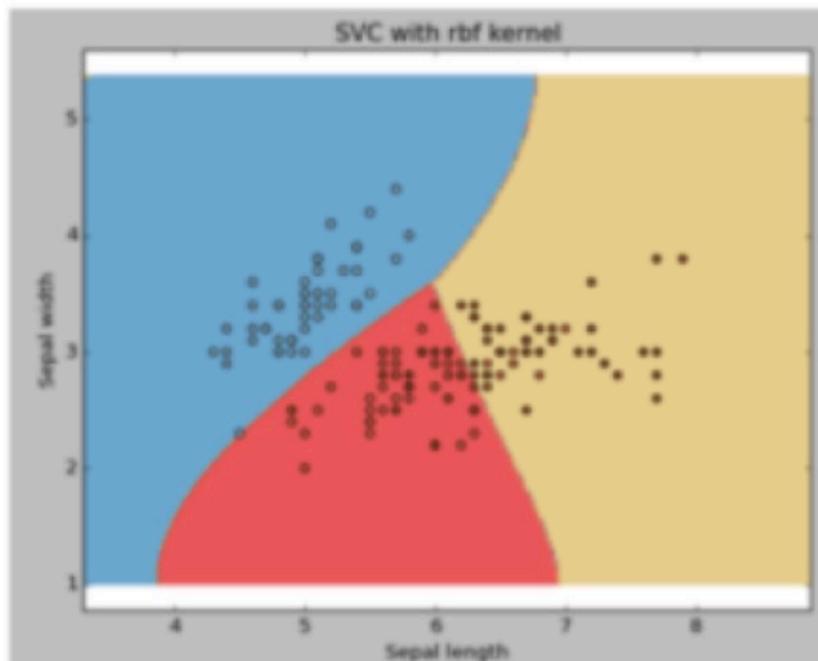
SVM Algorithm:

Hyperparameters

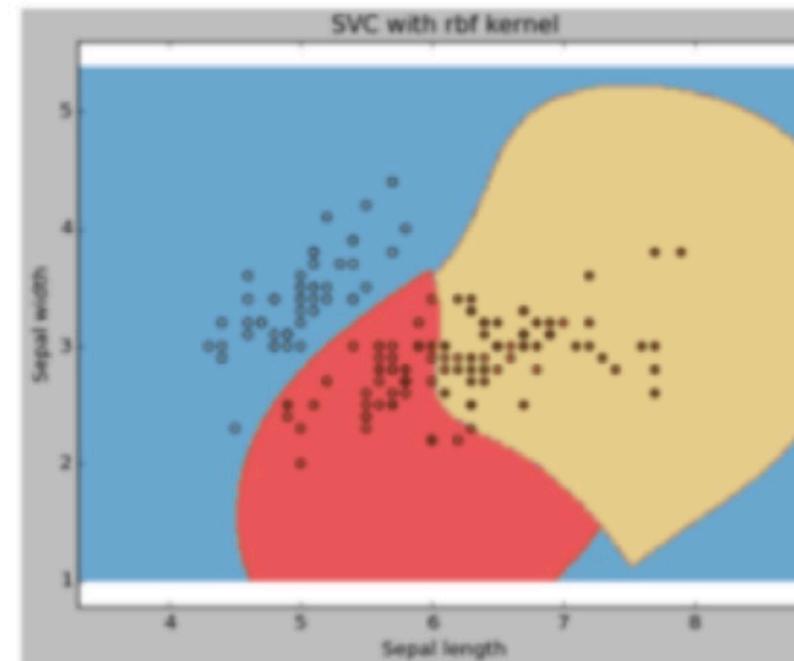
"C" parameter: (default = 1)

Penalty parameter of the error term.

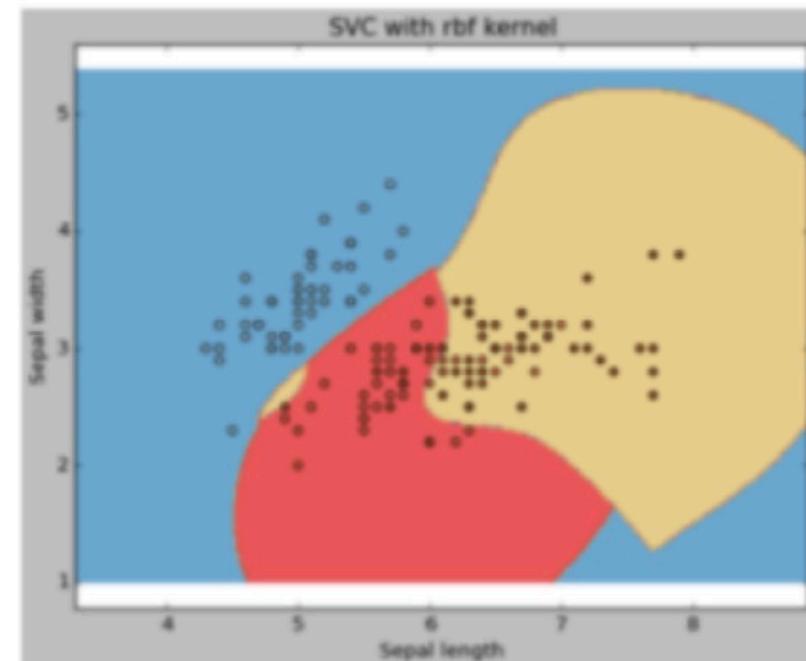
c=1 (soft/large margin hyperplane)



C=100



c=1000 (hard margin)



SVM Theory



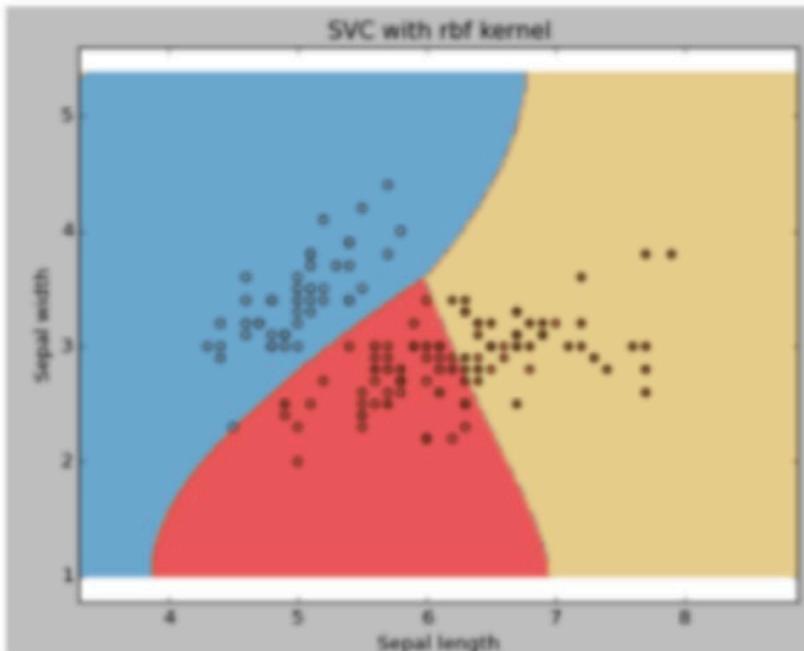
SVM Algorithm:

Hyperparameters

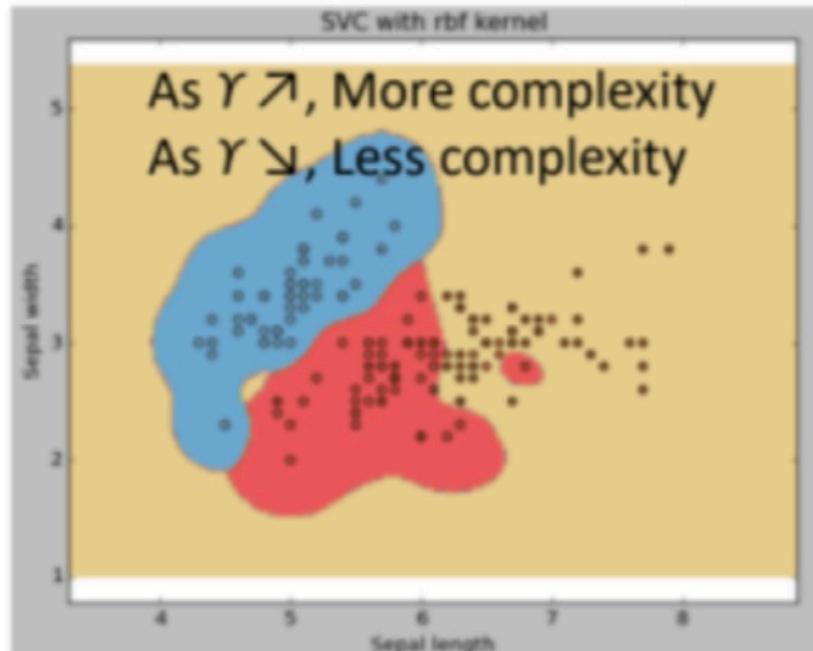
“gamma” parameter: (default = 1)

Kernel coefficient for ‘rbf’, ‘poly’ and ‘sigmoid’.

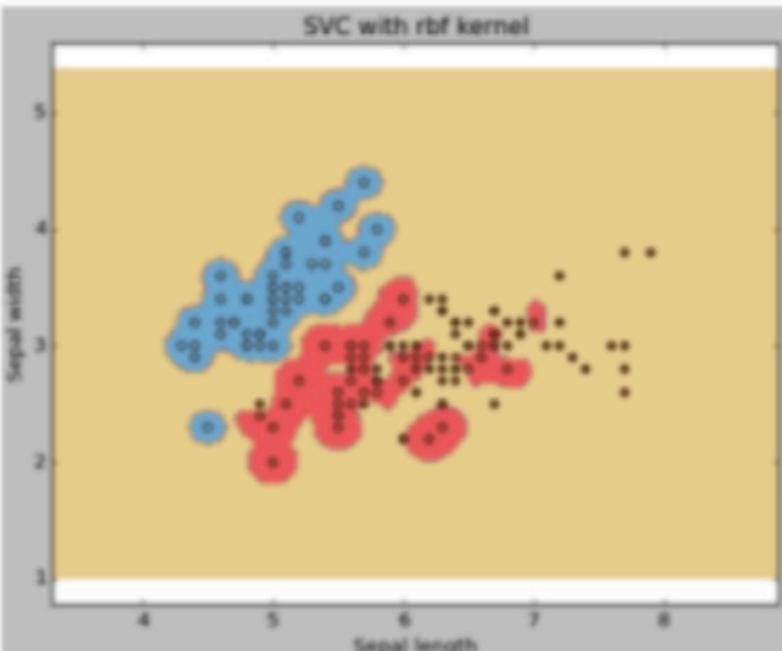
gamma=0



gamma=10



gamma=100



**if gamma up,
overfit
possibility
up**

SVM Theory



Pros & Cons

Pros:

- Works great with Computer Vision problems
- Low generalization error
- Can model complex relationships (powerful & flexible kernels)

Cons:

- Need parameter tuning and sensitive to kernel choice
- Sensitive to noise in the data