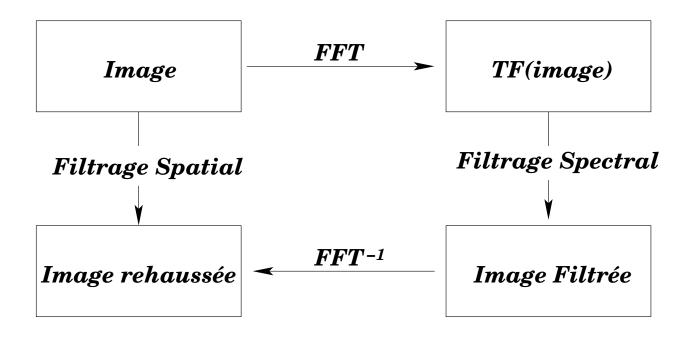
FILTRAGE FRÉQUENTIEL SOMMAIRE

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FILTRAGE FRÉQUENTIEL INTRODUCTION

Rehaussement d'Images par Filtrage Spatial/Fréquentiel



Théorème de Convolution -Rappel-

donc, si f(x,y) est l'image à filtrer et $G(u,\nu)$, le filtre fréquentiel

$$f(x,y) * g(x,y) = \mathcal{F}^{-1} \{ F(u,v) \cdot G(u,\nu) \}$$

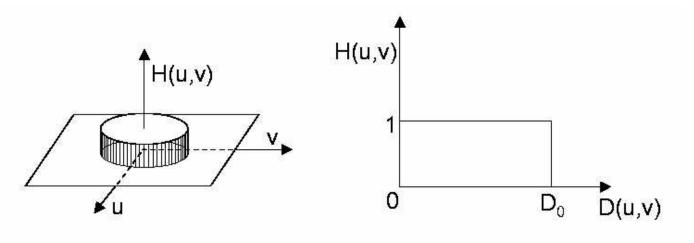
2

FILTRE PASSE-BAS IDÉAL (1)

$$H(u,\nu) = \begin{cases} 1 & D(u,\nu) \le D_0 \\ 0 & D(u,\nu) > D_0 \end{cases}$$

$$D(u,\nu) = \sqrt{u^2 + \nu^2}$$

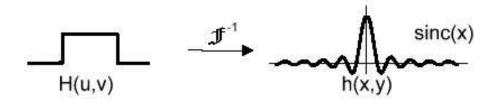
 D_0 : Fréquence de Coupure



Problème

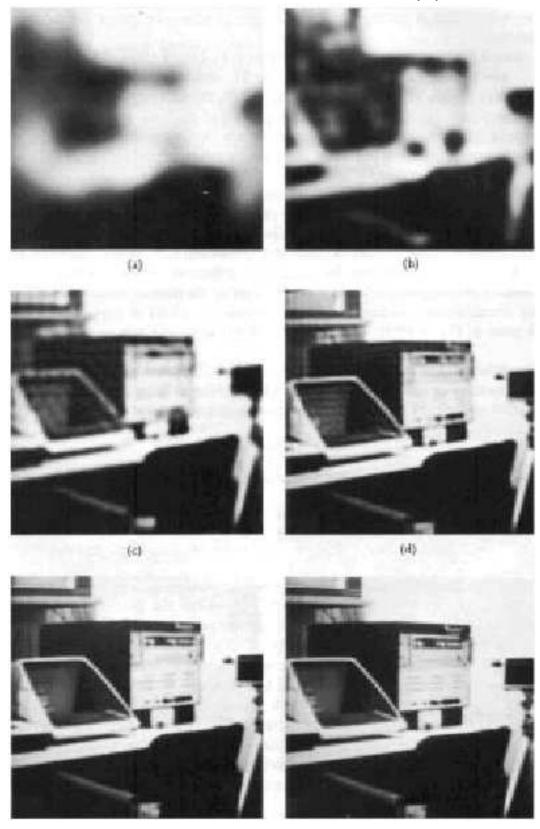
$$G(u,v) = F(u,v) \cdot H(u,v)$$

Convolution Theorm
$$g(x,y) = f(x,y) \cdot h(x,y)$$



 $\uparrow D_0 \longrightarrow \downarrow Rayons des ondulations (-flou)$

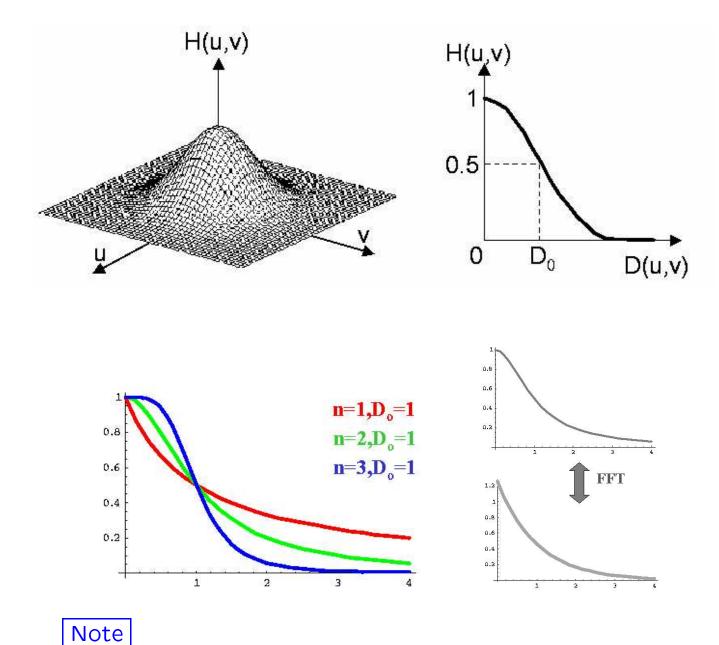
FILTRAGE FRÉQUENTIELS PATIALE FILTRE PASSE-BAS IDÉAL (2)



FILTRAGE FRÉQUENTIEL FILTRE PASSE-BAS DE BUTTERWORTH (1)

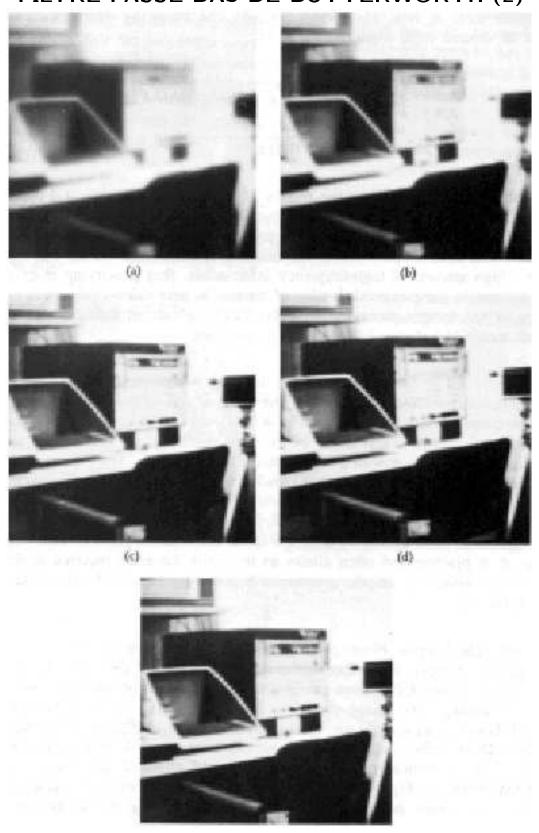
$$H(u,\nu) = \frac{1}{1 + (D(u,v)/D_0)^{2n}}$$
$$D(u,\nu) = \sqrt{u^2 + \nu^2}$$

 D_0 : Fréquence de Coupure



- Flou moins brutal et aucune ondulation -

FILTRAGE SFRÉQUENTIEL FILTRE PASSE-BAS DE BUTTERWORTH (2)

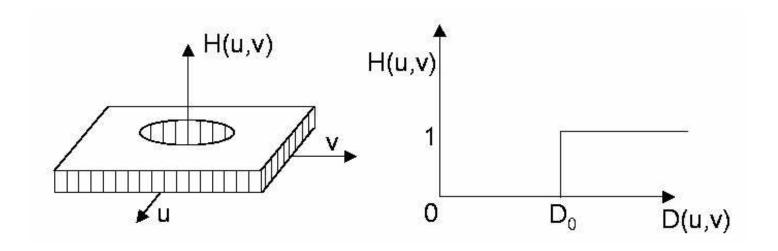


FILTRE PASSE-HAUT IDÉAL

$$H(u,\nu) = \begin{cases} 1 & D(u,\nu) \ge D_0 \\ 0 & D(u,\nu) < D_0 \end{cases}$$

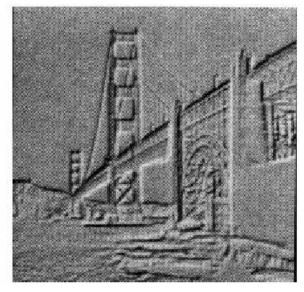
$$D(u,\nu) = \sqrt{u^2 + \nu^2}$$

 D_0 : Fréquence de Coupure



Exemple

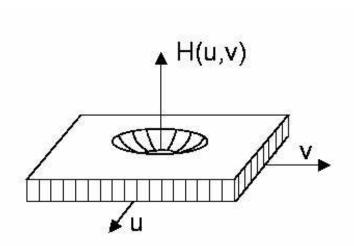


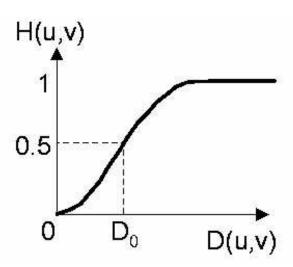


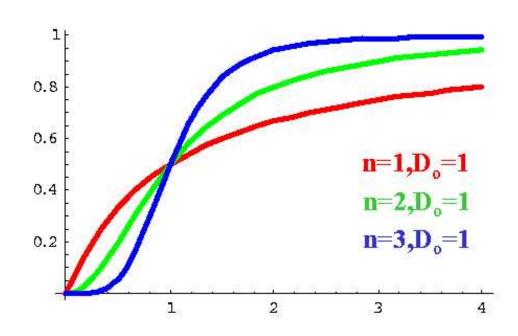
FILTRAGE FRÉQUENTIEL FILTRE PASSE-HAUT DE BUTTERWORTH

$$H(u,\nu) = \frac{1}{1 + (D_0/D(u,v))^{2n}}$$
$$D(u,\nu) = \sqrt{u^2 + \nu^2}$$

 D_0 : Fréquence de Coupure



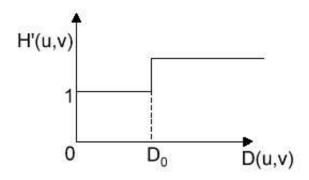




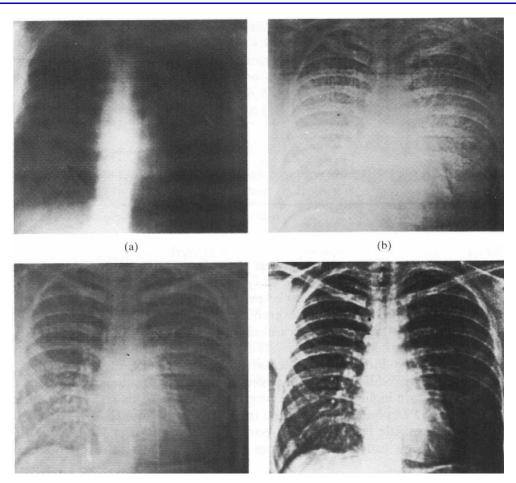
REHAUSSEMENT DES HAUTES FRÉQUENCES

- Maintient la moyenne et les BF
- Amplifie les HF

$$H'(u,v) = K_0 + H(u,v)$$



Exemple : Filtre PH Butterworth+Rehaussement HF+Égalisation



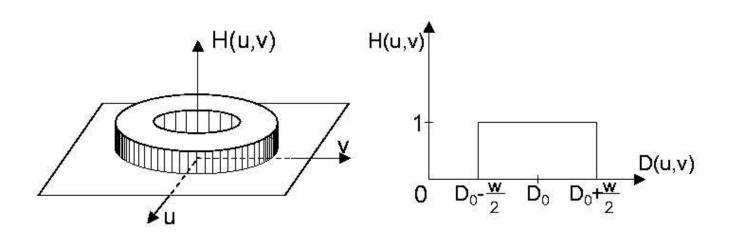
FILTRE PASSE-BANDE

$$H(u,\nu) = \begin{cases} 0 & D(u,\nu) \le D_0 - \frac{w}{2} \\ 1 & D_0 - \frac{w}{2} < D(u,\nu) < D_0 + \frac{w}{2} \\ 0 & D(u,\nu) \ge D_0 + \frac{w}{2} \end{cases}$$

$$D(u,\nu) = \sqrt{u^2 + \nu^2}$$

 D_0 : Fréquence de Coupure

w : Largeur de Bande



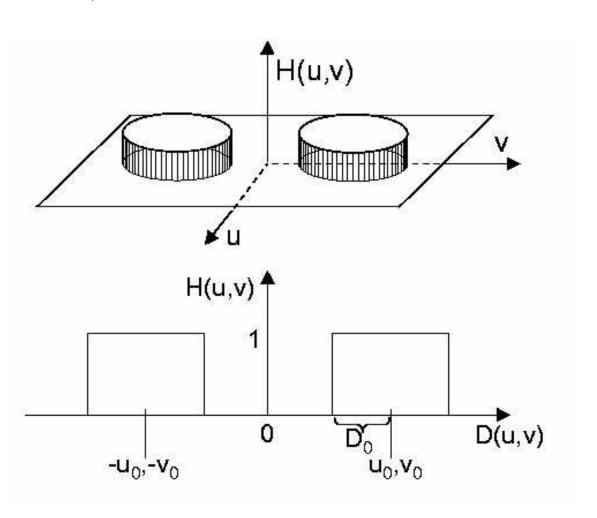
FILTRAGE FRÉQUENTIEL FILTRE SPECTRAL LOCAL

$$H(u,\nu)=egin{cases} 1 & D_1(u,\nu) \leq D_0 & \text{ou } D_2(u,\nu) \leq D_0 \\ 0 & \text{sinon} \end{cases}$$

$$D_1(u,\nu) = \sqrt{(u-u_0)^2 + (\nu-\nu_0)^2}$$

$$D_2(u,\nu) = \sqrt{(u+u_0)^2 + (\nu+\nu_0)^2}$$

 D_0 : Rayon autour de la fréquence locale u_0, ν_0 : Coordonné de la fréquence locale



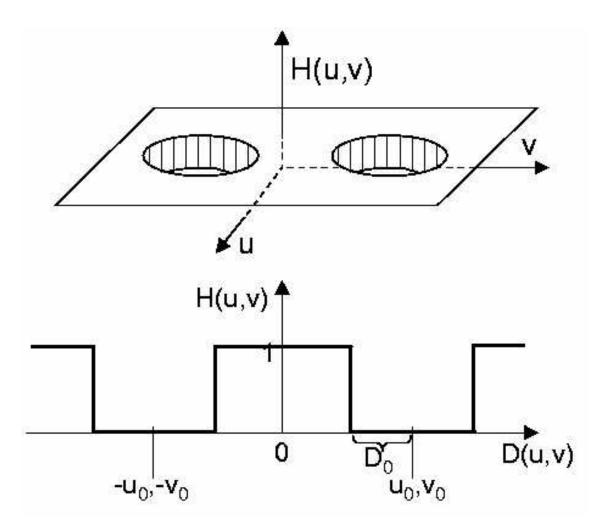
FILTRAGE FRÉQUENTIEL FILTRE A REJECTION DE BANDE (1)

$$H(u,\nu)= egin{cases} 0 & D_1(u,
u) \leq D_0 & \text{ou } D_2(u,
u) \leq D_0 \ 1 & ext{sinon} \end{cases}$$

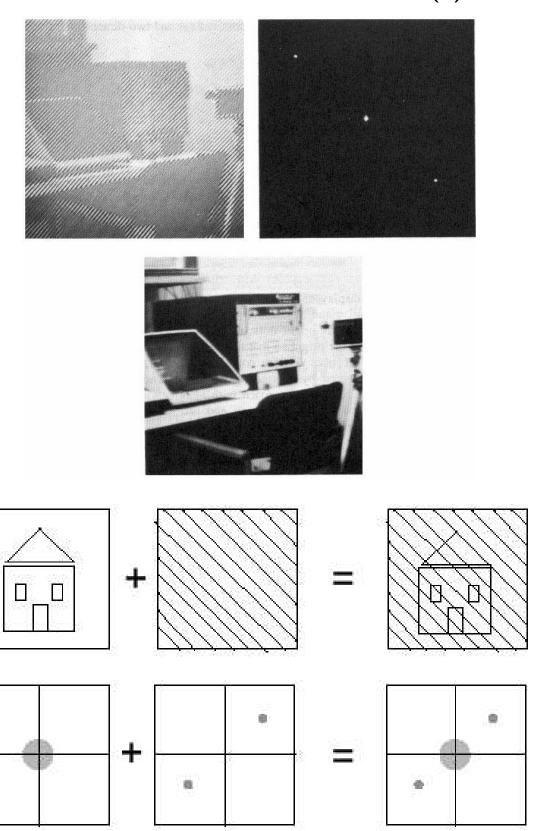
$$D_1(u,\nu) = \sqrt{(u-u_0)^2 + (\nu-\nu_0)^2}$$

$$D_2(u,\nu) = \sqrt{(u+u_0)^2 + (\nu+\nu_0)^2}$$

 D_0 : Rayon autour de la fréquence locale u_0, ν_0 : Coordonné de la fréquence locale



FILTRAGE FRÉQUENTIEL FILTRE A REJECTION DE BANDE (2)



FILTRAGE FRÉQUENTIEL FILTRAGE HOMOMORPHIQUE (1)

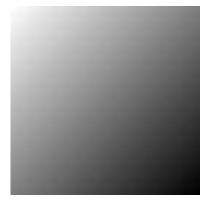


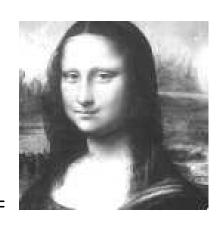
$$f(x,y) = i(x,y) \cdot r(x,y)$$

- i(x,y) : Illumination \blacktriangleright très basses fréquences
- r(x,y) : Réflectance \blacktriangleright plus hautes fréquences

► Opération Ponctuelle







Filtrage Homomorphique

FILTRAGE HOMOMORPHIQUE (2)

$$z(x,y) = \log(f(x,y))$$

= log(i(x,y) • (r(x,y)) = log(i(x,y)) + log(r(x,y))



$$Z(u,v) = I(u,v) + R(u,v)$$

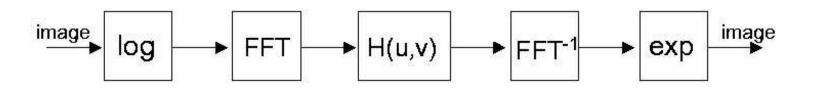
Filtre Passe-haut H(u,v):

$$s(x,y) = i'(x,y) + r'(x,y)$$

$$g(x,y) = \exp(s(x,y)) = \exp(i'(x,y)) \cdot \exp(r'(x,y))$$

$$= i_0(x,y) \cdot r_0(x,y)$$

Diagramme Bloc



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FILTRAGE FRÉQUENTIEL FILTRAGE HOMOMORPHIQUE (3)

