

# 2022 ACM-ICPC Teamnote

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## 1 기본 템플릿

```
1 1 #include <bits/stdc++.h>
2 2 using namespace std;
3 3 typedef long long ll;
4 4
5 5 using vInt = vector<int>;
6 6 using matInt = vector<vInt>;
7 7 using pii = pair<int, int>;
8 8 using vPii = vector<pii>;
9 9 using matPii = vector<vPii>;
10 10 using LL = long long;
11 11 using vLL = vector<LL>;
12 12 using matLL = vector<vLL>;
13 13 using pLL = pair<LL, LL>;
14 14 using vPLL = vector<pLL>;
15 15 using vBool = vector<bool>;
16 16 using matBool = vector<vBool>;
17 17 using vStr = vector<string>;
18 18
19 19 int main(){
20 20     ios::sync_with_stdio(0);
21 21     cin.tie(0);
22 22     freopen("input.txt", "r", stdin);
23 23     freopen("output.txt", "w", stdout);
24 24     // sys.stdin = open("input.txt", "r")
25 25     // sys.stdout = open("output.txt", "w")
26 26
27 27 }
```

## 2 주요 알고리즘

### 2.1 유니온 파인드

```
1 int rank[MAX_SIZE];
2
3 for (int i=0; i<MAX_SIZE; i++)
4     rank[i] = 1;
5
6 int find(int x){
7     if (x==parent[x]){
8         return x;
9     }
10    else{
11        int y = find(parent[x]);
12        parent[x] = y;
13        return y;
14    }
15 }
16
17 void union(int x, int y){
18     x = find(x);
19     y = find(y);
20
21     if (x == y)
22         return;
23
24     if (rank[x] > rank[y]){
25         parent[y] = x;
26         rank[x] += rank[y];
27     }
28     else {
29         parent[x] = y;
30         rank[y] += rank[x];
31     }
32 }
```

### 2.2 다익스트라

```
1 int v,e,st; //정점의 개수, 간선의 개수, 시작 위치
2
3 // {비용, 정점 번호}
```

```
4 vector<pair<int,int>> adj[MAX_SIZE]; //adj[i].push_back({w,x}) 면 i->x
5     ↳ 이고 거리는 w
6 const int INF = 0x3f3f3f3f;
7 int d[MAX_SIZE]; // 최단 거리 테이블
8 fill(d,d+v+1,INF);
9 while(e--){
10     int u,x,w;
11     adj[u].push_back({w,x});
12 }
13 priority_queue<pair<int,int>, vector<pair<int,int>>,
14     ↳ greater<pair<int,int>> > pq;
15 d[st] = 0;
16 // 우선순위 큐에 (0, 시작점) 추가
17 pq.push({d[st],st});
18 while(!pq.empty()){
19     auto cur = pq.top(); pq.pop(); // {비용, 정점 번호}
20     // 거리가 d에 있는 값과 다를 경우 넘어감
21     if(d[cur.second] != cur.first) continue;
22     for(auto nxt : adj[cur.second]){ //이웃하는 모든 노드들 = nxt에 대하여
23         ↳ 반복
24         if(d[nxt.second] <= d[cur.second]+nxt.X) continue;
25         // cur를 거쳐가는 것이 더 작은 값을 가질 경우
26         // d[nxt.Y]을 갱신하고 우선순위 큐에 (거리, nxt.Y)를 추가
27         d[nxt.second] = d[cur.second]+nxt.first;
28         pq.push({d[nxt.second],nxt.second});
29     }
30 }
```

### 2.3 DFS

```
1 bool visited[9];
2 vector<int> graph[9];
3
4 void dfs(int x)
5 {
6     visited[x] = true;
7     cout << x << " ";
8     for (int i = 0; i < graph[x].size(); i++)
9     {
10         int y = graph[x][i];
11         if (!visited[y])
```

```

12         dfs(y);
13     }
14 }

```

## 2.4 BFS

```

1  #define X first
2  #define Y second
3  int board[502][502] =
4  {{1,1,1,0,1,0,0,0,0,0},
5   {1,0,0,0,1,0,0,0,0,0},
6   {1,1,1,0,1,0,0,0,0,0},
7   {1,1,0,0,1,0,0,0,0,0},
8   {0,1,0,0,0,0,0,0,0,0},
9   {0,0,0,0,0,0,0,0,0,0},
10  {0,0,0,0,0,0,0,0,0,0} };
11 bool vis[502][502];
12 int n = 7, m = 10;
13 int dx[4] = {1,0,-1,0};
14 int dy[4] = {0,1,0,-1};
15 int main(void){
16     ios::sync_with_stdio(0);
17     cin.tie(0);
18     queue<pair<int,int> > Q;
19     vis[0][0] = 1;
20     Q.push({0,0});
21     while(!Q.empty()){
22         pair<int,int> cur = Q.front(); Q.pop();
23         cout << '(' << cur.X << ", " << cur.Y << ") -> ";
24         for(int dir = 0; dir < 4; dir++){
25             int nx = cur.X + dx[dir];
26             int ny = cur.Y + dy[dir];
27             if(nx < 0 || nx >= n || ny < 0 || ny >= m) continue;
28             if(vis[nx][ny] || board[nx][ny] != 1) continue;
29             vis[nx][ny] = 1;
30             Q.push({nx,ny});
31         }
32     }
33 }

```

## 2.5 선분 교차 판정

```

1  int ccw(pair<int, int>p1, pair<int, int>p2, pair<int, int>p3) {
2      int s = p1.first * p2.second + p2.first * p3.second + p3.first *
    ↪ p1.second;
3      s -= (p1.second * p2.first + p2.second * p3.first + p3.second *
    ↪ p1.first);
4
5      if (s > 0) return 1;
6      else if (s == 0) return 0;
7      else return -1;
8  }
9
10 #define pii pair<int, int>
11 bool isIntercept(pair<pii, pii> l1, pair<pii, pii> l2) {
12
13     pii p1 = l1.first;
14     pii p2 = l1.second;
15     pii p3 = l2.first;
16     pii p4 = l2.second;
17
18     int p1p2 = ccw(p1, p2, p3) * ccw(p1, p2, p4); // l1 기준
19     int p3p4 = ccw(p3, p4, p1) * ccw(p3, p4, p2); // l2 기준
20
21     // 두 직선이 일직선 상에 존재
22     if (p1p2 == 0 && p3p4 == 0) {
23         // 비교를 일반화하기 위한 점 위치 변경
24         if (p1 > p2) swap(p2, p1);
25         if (p3 > p4) swap(p3, p4);
26
27         return p3 <= p2 && p1 <= p4; // 두 선분이 포개어져 있는지 확인
28     }
29
30     return p1p2 <= 0 && p3p4 <= 0;
31 }
32 }

```

## 2.6 소수 리스트 생성

```

1  import math
2  def prime_list(limit):
3      if limit < 3:

```

```

4         return [2] if limit == 2 else []
5     size = (limit - 3) // 2
6     is_prime = [True] * (size + 1)
7     for i in range(math.isqrt(limit - 3) // 2 + 1):
8         if is_prime[i]:
9             p = i + i + 3
10            s = p * (i + 1) + i
11            is_prime[s:p] = [False] * ((size - s) // p + 1)
12    return [2] + [i + i + 3 for i, v in enumerate(is_prime) if v]

```

## 2.7 소수 판정 알고리즘

```

1  # NO! sqrt(N) 이하의 소인수로 나누어떨어지는지 검사
2  # primes = prime_list(10000000) 으로 소수 리스트 생성 후 실행
3  # 소수 리스트를 백만(10^7)까지 생성한다면 약 (10~14)까지 판별가능
4  def isprime(x):
5      if x == 1:
6          return False
7      for i in primes:
8          if i > x **.5:
9              break
10             if x % i == 0:
11                 return False
12    return True

```

## 2.8 밀러-라빈 소수 판정

```

1  def power(x, y, p):
2      res = 1
3
4      while y > 0:
5          if y % 2 != 0:
6              res = (res * x) % p
7              y //= 2
8              x = (x * x) % p
9      return res
10 def miller_rabin(n, a):
11     r = 0
12     d = n - 1
13     while d % 2 == 0:
14         r += 1
15         d = d // 2

```

```

16
17     x = power(a, d, n)
18     if x == 1 or x == n - 1:
19         return True
20
21     for i in range(r - 1):
22         x = power(x, 2, n)
23         if x == n - 1:
24             return True
25     return False

```

## 2.9 폴라드-로 소인수분해

```

1  import random
2  def is_prime(n):
3      alist = [2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41]
4      if n == 1:
5          return False
6      if n == 2 or n == 3:
7          return True
8      if n % 2 == 0:
9          return False
10     for a in alist:
11         if n == a:
12             return True
13         if not miller_rabin(n, a):
14             return False
15     return True
16
17
18 def pollardRho(n):
19     if is_prime(n):
20         return n
21     if n == 1:
22         return 1
23     if n % 2 == 0:
24         return 2
25     x = random.randrange(2, n)
26     y = x
27     c = random.randrange(1, n)
28     d = 1
29     while d == 1:

```

```

30     x = ((x ** 2 % n) + c + n) % n
31     y = ((y ** 2 % n) + c + n) % n
32     y = ((y ** 2 % n) + c + n) % n
33     d = gcd(abs(x - y), n)
34     if d == n:
35         return pollardRho(n)
36 if is_prime(d):
37     return d
38 else:
39     return pollardRho(d)

```

## 3 수학

### 3.1 NTT

```

1 from decimal import Decimal, setcontext, Context, MAX_EMAX, MAX_PREC
2
3 def multiply(a, b, digit = 0):
4     setcontext(Context(prec=MAX_PREC, Emax=MAX_EMAX))
5     if digit == 0:
6         digit = min(20, len(str(min(len(a), len(b)) * max(a) * max(b))))
7     f = f'0{digit}d'
8     a_dec = Decimal(''.join(format(x, f) for x in a))
9     b_dec = Decimal(''.join(format(x, f) for x in b))
10    c_dec = a_dec * b_dec
11    total_digit = digit * (len(a) + len(b) - 1)
12    c = format(c_dec, f'0{total_digit}f')
13    return [int(c[_i:_i + digit]) for _i in range(0, total_digit, digit)]

```

### 3.2 스프라그-그런디

```

1 def mex(s):
2     if not s:
3         return 0
4     for i in range(100):
5         if i not in s:
6             return i
7
8 b = list(multiinput())
9 dp = [0] * 501
10 for i in range(1, 501):
11     s = set()

```

```

12     for bb in b:
13         if i - bb >= 0:
14             s.add(dp[i - bb])
15     dp[i] = mex(s)
16
17 for _ in range(5):
18     x, y = multiinput()
19     if (dp[x] ^ dp[y]) == 0:
20         print('B')
21     else:
22         print('A')

```

### 3.3 유클리드 호제법

```

1 int GCD(int a, int b)
2 {
3     if(b==0) return a;
4     else return GCD(b,a%b);
5 }

```

### 3.4 확장 유클리드

```

1 # a, b의 gcd가 1일 때만 작동
2 # ax + by = 1의 해를 리턴
3 def eea(a, b):
4     s0, s1, t0, t1 = 1, 0, 0, 1
5     r0, r1 = a, b
6     q1 = r0 // r1
7     while 1:
8         s0, s1, t0, t1 = s1, s0 - s1 * q1, t1, t0 - t1 * q1
9         r0, r1 = r1, r0 - r1 * q1
10        if r1:
11            q1 = r0 // r1
12        else:
13            return s0, t0

```

### 3.5 가우스 소거법

```

1 const double EPS = 1e-9;
2 const int INF = 2; // it doesn't actually have to be infinity or a big
   ↳ number

```

```

3
4 int gauss (vector < vector<double> > a, vector<double> & ans) {
5     int n = (int) a.size();
6     int m = (int) a[0].size() - 1;
7
8     vector<int> where (m, -1);
9     for (int col=0, row=0; col<m && row<n; ++col) {
10         int sel = row;
11         for (int i=row; i<n; ++i)
12             if (abs (a[i][col]) > abs (a[sel][col]))
13                 sel = i;
14         if (abs (a[sel][col]) < EPS)
15             continue;
16         for (int i=col; i<=m; ++i)
17             swap (a[sel][i], a[row][i]);
18         where[col] = row;
19
20         for (int i=0; i<n; ++i)
21             if (i != row) {
22                 double c = a[i][col] / a[row][col];
23                 for (int j=col; j<=m; ++j)
24                     a[i][j] -= a[row][j] * c;
25             }
26         ++row;
27     }
28
29     ans.assign (m, 0);
30     for (int i=0; i<m; ++i)
31         if (where[i] != -1)
32             ans[i] = a[where[i]][m] / a[where[i]][i];
33     for (int i=0; i<n; ++i) {
34         double sum = 0;
35         for (int j=0; j<m; ++j)
36             sum += ans[j] * a[i][j];
37         if (abs (sum - a[i][m]) > EPS)
38             return 0;
39     }
40
41     for (int i=0; i<m; ++i)
42         if (where[i] == -1)
43             return INF;
44     return 1;

```

```

45 }
1 int gauss (vector < bitset<N> > a, int n, int m, bitset<N> & ans) {
2     vector<int> where (m, -1);
3     for (int col=0, row=0; col<m && row<n; ++col) {
4         for (int i=row; i<n; ++i)
5             if (a[i][col]) {
6                 swap (a[i], a[row]);
7                 break;
8             }
9         if (! a[row][col])
10            continue;
11        where[col] = row;
12
13        for (int i=0; i<n; ++i)
14            if (i != row && a[i][col])
15                a[i] ^= a[row];
16        ++row;
17    }
18    // The rest of implementation is the same as above
19 }

```

### 3.6 중국인의 나머지 정리

```

1 int CRT (int a1 , int m1 , int a2 , int m2) {
2     return (a1 ? a2 % m1 + m1) * (11) rev(m2, m1) % m1 * m2 + a2 ;
3 }
4
5 int rev (int x, int m) {
6     if (x == 1) return 1;
7     return (1 - rev(m % x, x) * (11) m) / x + m;
8 }

```

### 3.7 모듈러 곱셈 역원

```

1 def moduluiinv(p, q):
2     mod = 1000000007
3     expo = mod - 2
4     while (expo):
5         if (expo & 1):
6             p = (p * q) % mod
7             q = (q * q) % mod

```

```

8         expo >= 1
9
10    return p

```

### 3.8 좌표 압축

```

1  def comp(arr):
2      dic = {x: i for i, x in enumerate(sorted(set(arr)))}
3      return [dic[x] for x in arr]

```

## 4 그래프

### 4.1 최대 유량

```

1  INF = 10**9
2  # V = 10
3  # capacity = [[1] * V for _ in range(V)]
4  # flow = [[0] * V for _ in range(V)]
5
6
7  V = 4
8  capacity = [[0, 1, 3, 0], [0, 0, 1, 2], [0, 0, 0, 1], [0, 0, 0, 0]]
9  flow = [[0, 0, 0, 0] for _ in range(4)]
10
11
12 def networkFlow(source, sink):
13     totalFlow = 0
14     while 1:
15         parent = [-1] * V
16         q = deque()
17         parent[source] = source
18         q.append(source)
19         while q and parent[sink] == -1:
20             here = q.popleft()
21             for there in range(0, V):
22                 if capacity[here][there] - flow[here][there] > 0 and
23                     ↪ parent[there] == -1:
24                     q.append(there)
25                     parent[there] = here
26             if parent[sink] == -1:
27                 break
28         amount = INF

```

```

28     p = sink
29     while p != source:
30         amount = min(capacity[parent[p]][p] - flow[parent[p]][p],
31                     ↪ amount)
32         p = parent[p]
33     p = sink
34     while p != source:
35         flow[parent[p]][p] += amount
36         flow[p][parent[p]] -= amount
37         p = parent[p]
38     totalFlow += amount
39 return totalFlow

```

### 4.2 이분 매칭

```

1  # N명의 직원이 M개의 일을 나누어서 할 때,
2  # i번째 직원이 할 수 있는 일이 정해져 있음
3  # 할 수 있는 최대 일의 개수 구하기
4  from collections import deque
5  adj = []
6  n, m = map(int, input().split())
7  for i in range(n):
8      s = list(map(int, input().split()))[1:]
9      ss = [0] * m
10     for j in s:
11         ss[j - 1] = 1
12     adj.append(ss)
13
14  aMatch = [-1] * n
15  bMatch = [-1] * m
16
17  def dfs(a, visited):
18      if visited[a]:
19          return 0
20      visited[a] = 1
21      for b in range(0, m):
22          if adj[a][b]:
23              if bMatch[b] == -1 or dfs(bMatch[b], visited):
24                  aMatch[a] = b
25                  bMatch[b] = a
26              return 1

```

```

27     return 0
28 def bipartiteMatch():
29     size = 0
30     for start in range(0, n):
31         visited = [0] * n
32         if dfs(start, visited):
33             size += 1
34     return size

```

## 5 트리

### 5.1 세그먼트 트리

```

1  #include <iostream>
2  #include <cmath>
3  #include <vector>
4  using namespace std;
5  void init(vector<long long> &a, vector<long long> &tree, int node, int
↳ start, int end) {
6      if (start == end) {
7          tree[node] = a[start];
8      } else {
9          init(a, tree, node*2, start, (start+end)/2);
10         init(a, tree, node*2+1, (start+end)/2+1, end);
11         tree[node] = tree[node*2] + tree[node*2+1];
12     }
13 }
14 void update(vector<long long> &a, vector<long long> &tree, int node, int
↳ start, int end, int index, long long val) {
15     if (index < start || index > end) {
16         return;
17     }
18     if (start == end) {
19         a[index] = val;
20         tree[node] = val;
21         return;
22     }
23     update(a, tree, node*2, start, (start+end)/2, index, val);
24     update(a, tree, node*2+1, (start+end)/2+1, end, index, val);
25     tree[node] = tree[node*2] + tree[node*2+1];
26 }

```

```

27 long long query(vector<long long> &tree, int node, int start, int end,
↳ int left, int right) {
28     if (left > end || right < start) {
29         return 0;
30     }
31     if (left <= start && end <= right) {
32         return tree[node];
33     }
34     long long lsum = query(tree, node*2, start, (start+end)/2, left,
↳ right);
35     long long rsum = query(tree, node*2+1, (start+end)/2+1, end, left,
↳ right);
36     return lsum + rsum;
37 }
38 int main() {
39     ios_base::sync_with_stdio(false);
40     cin.tie(nullptr);
41     int n, m, k;
42     cin >> n >> m >> k;
43     vector<long long> a(n);
44     int h = (int)ceil(log2(n));
45     int tree_size = (1 << (h+1));
46     vector<long long> tree(tree_size);
47     m += k;
48     for (int i=0; i<n; i++) {
49         cin >> a[i];
50     }
51     init(a, tree, 1, 0, n-1);
52     while (m-- > 0) {
53         int what;
54         cin >> what;
55         if (what == 1) {
56             int index;
57             long long val;
58             cin >> index >> val;
59             update(a, tree, 1, 0, n-1, index-1, val);
60         } else if (what == 2) {
61             int left, right;
62             cin >> left >> right;
63             cout << query(tree, 1, 0, n-1, left-1, right-1) << '\n';
64         }
65     }

```



```

66     return 0;
67 }

```

## 5.2 레이지 세그먼트 트리

```

1  #include <iostream>
2  #include <cmath>
3  #include <vector>
4  using namespace std;
5  void init(vector<long long> &a, vector<long long> &tree, int node, int
    ↪ start, int end) {
6      if (start == end) {
7          tree[node] = a[start];
8      } else {
9          init(a, tree, node*2, start, (start+end)/2);
10         init(a, tree, node*2+1, (start+end)/2+1, end);
11         tree[node] = tree[node*2] + tree[node*2+1];
12     }
13 }
14 void update_lazy(vector<long long> &tree, vector<long long> &lazy, int
    ↪ node, int start, int end) {
15     if (lazy[node] != 0) {
16         tree[node] += (end-start+1)*lazy[node];
17         if (start != end) {
18             lazy[node*2] += lazy[node];
19             lazy[node*2+1] += lazy[node];
20         }
21         lazy[node] = 0;
22     }
23 }
24 void update_range(vector<long long> &tree, vector<long long> &lazy, int
    ↪ node, int start, int end, int left, int right, long long diff) {
25     update_lazy(tree, lazy, node, start, end);
26     if (left > end || right < start) {
27         return;
28     }
29     if (left <= start && end <= right) {
30         tree[node] += (end-start+1)*diff;
31         if (start != end) {
32             lazy[node*2] += diff;
33             lazy[node*2+1] += diff;
34         }

```

```

35         return;
36     }
37     update_range(tree, lazy, node*2, start, (start+end)/2, left, right,
    ↪ diff);
38     update_range(tree, lazy, node*2+1, (start+end)/2+1, end, left, right,
    ↪ diff);
39     tree[node] = tree[node*2] + tree[node*2+1];
40 }
41 long long query(vector<long long> &tree, vector<long long> &lazy, int
    ↪ node, int start, int end, int left, int right) {
42     update_lazy(tree, lazy, node, start, end);
43     if (left > end || right < start) {
44         return 0;
45     }
46     if (left <= start && end <= right) {
47         return tree[node];
48     }
49     long long lsum = query(tree, lazy, node*2, start, (start+end)/2,
    ↪ left, right);
50     long long rsum = query(tree, lazy, node*2+1, (start+end)/2+1, end,
    ↪ left, right);
51     return lsum + rsum;
52 }
53 int main() {
54     ios_base::sync_with_stdio(false);
55     cin.tie(nullptr);
56     int n, m, k;
57     cin >> n >> m >> k;
58     vector<long long> a(n);
59     int h = (int)ceil(log2(n));
60     int tree_size = (1 << (h+1));
61     vector<long long> tree(tree_size);
62     vector<long long> lazy(tree_size);
63     m += k;
64     for (int i=0; i<n; i++) {
65         cin >> a[i];
66     }
67     init(a, tree, 1, 0, n-1);
68     while (m--) {
69         int what;
70         cin >> what;

```

```

71     if (what == 1) {
72         int left, right;
73         long long diff;
74         cin >> left >> right >> diff;
75         update_range(tree, lazy, 1, 0, n-1, left-1, right-1, diff);
76     } else if (what == 2) {
77         int left, right;
78         cin >> left >> right;
79         cout << query(tree, lazy, 1, 0, n-1, left-1, right-1) <<
↪ '\n';
80     }
81 }
82 return 0;
83 }

```

### 5.3 펜윅 트리

```

1 mod = 998244353
2 class FenwickTree:
3     def __init__(self, size):
4         self.data = [0] * (size + 1)
5         self.size = size
6
7     # i is exclusive
8     def prefix_sum(self, i):
9         s = 0
10        while i > 0:
11            s = (s + self.data[i]) % mod
12            i -= i & -i
13        return s
14
15    def add(self, i, x):
16        i += 1
17        while i <= self.size:
18            self.data[i] = (self.data[i] + x) % mod
19            i += i & -i

```

### 5.4 2차원 펜윅 트리

```

1 class Fenwick2D:
2     def __init__(self, w, h):
3         self.data = [[0] * h for _ in range(w)]

```

```

4         self.w = w
5         self.h = h
6     def prefix_sum(self, r, c):
7         cnt = 0
8         while r > 0:
9             cc = c
10            while cc > 0:
11                cnt += self.data[r][cc]
12                cc -= cc & -cc
13            r -= r & -r
14        return cnt
15    def add(self, r, c, diff):
16        while r <= self.w:
17            cc = c
18            while cc <= self.h:
19                self.data[r][cc] += diff
20                cc += cc & -cc
21            r += r & -r

```

### 5.5 레이지 펜윅 트리

```

1 void update(int bitType, int idx, int diff) {
2     int* bit = bitType==1 ? bit1 : bit2;
3     while (idx <= n) {
4         bit[idx] += diff;
5         idx += idx&-idx;
6     }
7 }
8
9 void rangeUpdate(int a, int b, int diff) {
10    update(1, a, diff);
11    update(1, b+1, -diff);
12    update(2, a, diff * (a-1));
13    update(2, b+1, -diff * b);
14 }
15
16 int getBitValue(int bitType, int idx) {
17     int* bit = bitType==1 ? bit1 : bit2;
18     int answer = 0;
19     while (idx > 0) {
20         answer += bit[idx];
21         idx -= idx&-idx;

```

```

22     }
23     return answer;
24 }
25
26 int prefixSum(int idx) {
27     return getBitValue(1, idx) * idx - getBitValue(2, idx);
28 }
29
30 int query(int a, int b) {
31     return prefixSum(b) - prefixSum(a-1);
32 }

```

```

1  import sys
2
3  # sys.setrecursionlimit(10**6)
4  # import decimal
5
6  # import math
7  # from collections import deque
8  # import itertools
9  # from collections import Counter
10 # from queue import PriorityQueue
11 # import heapq
12 # import decimal
13 # import random
14 # from bisect import bisect_left, bisect_right
15 # import fractions

```

```

16
17 # import re
18 # import datetime
19
20 input = sys.stdin.readline
21
22
23 def multiinput():
24     return map(int, input().split())
25

```

```

26 class LazyFenwick:
27     def __init__(self, size):
28         self.size = size
29         self.bit = [[0] * (size + 1) for _ in range(2)]
30

```

```

31 def update(self, bitType, idx, diff):
32     while idx <= self.size:
33         self.bit[bitType][idx] += diff
34         idx += idx & -idx
35
36 def rangeUpdate(self, a, b, diff):
37     self.update(0, a, diff)
38     self.update(0, b + 1, -diff)
39     self.update(1, a, diff * (a - 1))
40     self.update(1, b + 1, -diff * b)
41
42 def getBitValue(self, bitType, idx):
43     ans = 0
44     while idx > 0:
45         ans += self.bit[bitType][idx]
46         idx -= idx & -idx
47     return ans
48
49 def prefixSum(self, idx):
50     return self.getBitValue(0, idx) * idx - self.getBitValue(1, idx)
51
52 def query(self, a, b):
53     return self.prefixSum(b) - self.prefixSum(a - 1)
54
55
56
57 # decimal.getcontext().prec = 1111
58
59 def main(tc):
60     n, m, k = multiinput()
61     s = LazyFenwick(n)
62     for _ in range(1, n + 1):
63         i = int(input())
64         s.rangeUpdate(_, _, i)
65     for _ in range(m + k):
66         a, *q = multiinput()
67         if a == 1:
68             b, c, d = q
69             s.rangeUpdate(b, c, d)
70         else:
71             b, c = q
72             print(s.query(b, c))

```

```

73
74
75
76
77 # for tc in range(int(input())):
78 for tc in range(1):
79     main(tc)

```

## 6 테크닉

### 6.1 비트마스킹

```

1 a = 1234
2 p = 2
3 # - p번 비트 켜기
4 a |= (1 << p)
5 # - p번 비트 확인하기
6 a & (1 << p)
7 # - p번 비트 끄기
8 a &= ~(1 << p)
9 # - 최하위 비트 구하기
10 a & -a
11 # - 최하위 비트 끄기
12 a &= (a - 1)
13 # - p번 비트 토글
14 a ^= (1 << p)

```

### 6.2 이분탐색

```

1 def bisect_left(a, x, lo=0, hi=None, *, key=None):
2     """Return the index where to insert item x in list a, assuming a is
3     ↪ sorted.
4     The return value i is such that all e in a[:i] have e < x, and all e
5     ↪ in
6     a[i:] have e >= x. So if x already appears in the list, a.insert(i,
7     ↪ x) will
8     insert just before the leftmost x already there.
9     Optional args lo (default 0) and hi (default len(a)) bound the
10    slice of a to be searched.
11    """
12
13    if lo < 0:

```

```

11         raise ValueError('lo must be non-negative')
12    if hi is None:
13        hi = len(a)
14    # Note, the comparison uses "<" to match the
15    # __lt__() logic in list.sort() and in heapq.
16    if key is None:
17        while lo < hi:
18            mid = (lo + hi) // 2
19            if a[mid] < x:
20                lo = mid + 1
21            else:
22                hi = mid
23    else:
24        while lo < hi:
25            mid = (lo + hi) // 2
26            if key(a[mid]) < x:
27                lo = mid + 1
28            else:
29                hi = mid
30    return lo
31 def bisect_right(a, x, lo=0, hi=None, *, key=None):
32     """Return the index where to insert item x in list a, assuming a is
33     ↪ sorted.
34     The return value i is such that all e in a[:i] have e <= x, and all e
35     ↪ in
36     a[i:] have e > x. So if x already appears in the list, a.insert(i,
37     ↪ x) will
38     insert just after the rightmost x already there.
39     Optional args lo (default 0) and hi (default len(a)) bound the
40     slice of a to be searched.
41     """
42
43    if lo < 0:
44        raise ValueError('lo must be non-negative')
45    if hi is None:
46        hi = len(a)
47    # Note, the comparison uses "<" to match the
48    # __lt__() logic in list.sort() and in heapq.
49    if key is None:
50        while lo < hi:
51            mid = (lo + hi) // 2

```

```
49         if x < a[mid]:
50             hi = mid
51         else:
52             lo = mid + 1
53     else:
54         while lo < hi:
```

```
55         mid = (lo + hi) // 2
56         if x < key(a[mid]):
57             hi = mid
58         else:
59             lo = mid + 1
60     return
```