T-501-FMAL Programming languages, Assignment 2 Spring 2021

Due Friday 26 February 2021 at 23:59

The file Assignment2.fs contains partial implementations of two languages. Both languages support variables, arithmetical operations, and comparisons of the form if positive e then et else ef (represented by IIfPositive(e, et, ef) and IfPositive(e, et, ef)). All of these are meant to support both integers and floating point numbers; in particular, variables can hold both integers and floats.

In iexpr, integers are implicitly converted to floats when necessary, for example when adding an integer and a float. In expr, there are no implicit conversions (and so adding an integer to a float will fail), but an explicit cast IntToFloat e yields a float when e is an integer. expr also supports matching on values to determine if they are ints or floats: an expression match e with $l \times i \to ei \mid F \times f \to ef$ (represented by Match(e, xi, ei, xf, ef)) evaluates to the value of ei if e is an integer and to the value of ef if e is a float; the local variable xi resp. xf obtains the value of e.

1. The evaluation function ieval fails for an expression using a variable that does not appear in the environment. Modify it so that variables default to integer 0 (for example, ieval (IVar "x") [] should yield I 0).

Hint: You need to replace the call of lookup with a call to a variation of it.

- 2. The implementation of the evaluation function for the explicit language is incomplete. Modify the evaluation function eval so that Plus works when works when both operands are floats (in addition to when both operands are integers). If one operand is a float and the other is an integer, evaluation should fail. Similarly modify Times and Neg. Also add clauses for IfPositive (which should support both integers and floats) and for Match.
- 3. Code a function to_float : value -> float that converts an element of value to a float (use F#'s builtin function float : int -> float).
- 4. Using Match among other things, implement functions

```
to_float_expr : expr -> expr
plus_expr : expr * expr -> expr
times_expr : expr * expr -> expr

such that

eval (to_float_expr e) env = F (to_float (eval e env))
eval (plus_expr (e1, e2)) env = plus_value (eval e1 env, eval e2 env)
eval (times_expr (e1, e2)) env = times_value (eval e1 env, eval e2 env)
```

You may assume that e, e1, and e2 do not contain variables whose names begin with _ (for example _x). Note that evaluation of IntToFloat e will fail when e is not an integer. For plus_expr (e1, e2) and times_expr (e1, e2), you should allow one operand to be an integer and one to be a float, but if both are integers then the result should be an integer.

Hint: You need to apply Match to the parameters of the functions.

5. Implement a function add_matches: iexpr -> expr to convert from the implicit language to the explicit one. You should use the functions you defined in the previous problem so that evaluation does not fail because of operands having different types. Your function should satisfy

```
eval (add_matches e) env = ieval e env
```

when env contains all of the variables that appear in e.

6. Write a type inference function infer: expr -> typenvir -> typ. The typenvir argument contains the types of the variables. Type inference should fail when the two operands of a Plus or Times have different types and also when the two branches of IfPositive have different types. Type inference should also fail when e is not an integer in IntToFloat e.

Hint: eval is a good starting point for writing infer.

7.	Write a function add_casts : iexpr -> tyenvir -> expr to convert from iexpr to expr, insert-
	ing casts IntToFloat where necessary, but not using Match. If tyenv contains the type of every
	variable that appears in e, then infer (add_casts e tyenv) tyenv should never fail. You should
	only insert the casts that are absolutely necessary to accomplish this; do not unnecessarily convert
	integers to floats.

8.	$\operatorname{Can}\mathtt{eval}$	(add_mat	ches e) []	and ${\tt eval}$	(add_casts	е	[])		have	different	behaviour?
	What abou	ut infer	(add match	es e) [] a	and infer (a	dd	cas	ts	e []) []?	

9. The file Assignment2.fs also contains a copy of the first stack machine from Expressions3.fs. Write a function rlower: rcode -> rcode that compiles away all of the RPop, RDup and RSwap instructions by replacing them with sequences of RLoad, RStore and RErase instructions. The instructions rlower inss should have the same behaviour as inss, but should not contain RPop, RDup or RSwap.