Simulating Pathogenic Behavior and Transmission in Populations

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1 Abstract

In a world recently held captive by the coronavirus (COVID-19) pandemic, an understanding of the population dynamics through which viruses propagate their existence is critical. Fortunately, the field of epidemiology has, for decades, dedicated itself to quantifying the effects of pandemics and epidemics in efforts to better advise public policymakers and average citizens as they live through unprecedented times.

This report looks to employ biological and statistical techniques to characterize pathogenic behavior across a myriad of scenarios. The topics discussed represent risks to the health of humans and include, but are not limited to, viral mutations, co-infection (simultaneous infection of multiple viral strains), and the efficacy and usefulness of vaccinations. Such analysis is achieved through temporal simulations of systems of equations analogous to the SIR family of models [Reference to some website about SIR models], as well as a spatiotemporal, Monte Carlo simulation that invokes principles of stochasticity to mimic population dynamics.

Key Words: epidemiology, SIR Modeling, pathogen, population dynamics, Monte Carlo simulation

2 Other Sections

3 Spatiotemporal Simulations

[Stuff About the Monte Carlo Sims]

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Algorithm 1 Simulation for Basic SIR Model
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Require: S_t + I_t + R_t = N \ \forall t \land N, T \in \mathbb{Z}_+
   x_1, x_2, ..., x_N \sim \mathcal{U}(\text{xmin}, \text{xmax})
   y_1, y_2, ..., y_N \sim \mathcal{U}(ymin, ymax)
   s_{1}, s_{2}, ..., s_{N} := \begin{cases} S & 1 \le i \le S_{t=0} \\ I & S_{t=0} < i \le S_{t=0} + I_{t=0} \\ R & \text{otherwise} \end{cases}
   \mathrm{Res} \leftarrow [0]^{N \times 3}
   t = 1
   while t \leq T do
       m_1, m_2, ..., m_N \sim Bern(p_{\text{move}})
       for i=1, i \leq N do
           if m_i then
               x_i \leftarrow x_i + \mathcal{N}(0, 1)
               y_i \leftarrow y_i + \mathcal{N}(0,1)
            end if
       end for
       \mathbf{D} \leftarrow [0]^{N \times N}
       for i \in [1, N] \cap \mathbb{Z} do
           for j \in [1, N] \cap \mathbb{Z} do
               D_{i,j} = \sqrt{(x_i - x_j)^2 + (y_i - y_j)^2}
           end for
       end for
       for i \in [1, N] \cap \mathbb{Z} do
           for j \in [i+1,N] \cap \mathbb{Z} do
               if (s_i = I \vee s_j = I) \wedge D_{i,j} < d_{\text{thresh}} then
                   \lambda_{inf} = |D_{i,j} - d_{\text{thresh}}|
               end if
               infect \leftarrow Pois(\lambda_{inf})
               if permanent immunity then
                   infect = 0
               else if s_i = R \vee s_j = R then
                   \lambda \leftarrow r_{\text{inf}} * \lambda_{inf}
                   infect \leftarrow Pois(\lambda_{inf})
               end if
               if infect \ge inf_{thresh} then
                   s_i = s_j = I
               end if
           end for
       end for
       for i \in [1, N] \cap \mathbb{Z} do
           if s_i = I \wedge Pois(\lambda_{rec}) \geq rec_{thresh} then
               s_i = R
           end if
      end for n_S = \sum_{i=1}^{N} I[s_i = S]
n_I = \sum_{i=1}^{N} I[s_i = I]
n_R = \sum_{i=1}^{N} I[s_i = R]
       \mathrm{Res}_{t,1} \leftarrow n_S
       \text{Res}_{t,2} \leftarrow n_I
       \text{Res}_{t,3} \leftarrow n_R
                                                                   2
       t \leftarrow t + 1
   end while
   return Res
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