



# Chapter 2: Intro to Relational Model

Database System Concepts, 6<sup>th</sup> Ed.

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# Example of a Relation

The diagram shows a table with four columns: *ID*, *name*, *dept\_name*, and *salary*. Three arrows point from the text "attributes (or columns)" to the header cells of the table. Three arrows point from the text "tuples (or rows)" to the first three data rows of the table.

<i>ID</i>	<i>name</i>	<i>dept_name</i>	<i>salary</i>
10101	Srinivasan	Comp. Sci.	65000
12121	Wu	Finance	90000
15151	Mozart	Music	40000
22222	Einstein	Physics	95000
32343	El Said	History	60000
33456	Gold	Physics	87000
45565	Katz	Comp. Sci.	75000
58583	Califieri	History	62000
76543	Singh	Finance	80000
76766	Crick	Biology	72000
83821	Brandt	Comp. Sci.	92000
98345	Kim	Elec. Eng.	80000



# Attribute Types

- The set of allowed values for each attribute is called the **domain** of the attribute
- Attribute values are (normally) required to be **atomic**; that is, indivisible ) ,
- The special value **null** is a member of every domain
- The null value causes complications in the definition of many operations



# Relation Schema and Instance

- $A_1, A_2, \dots, A_n$  are *attributes*
- $R = (A_1, A_2, \dots, A_n)$  is a *relation schema*

Example:

*instructor* = (*ID*, *name*, *dept\_name*, *salary*)

- Formally, given sets  $D_1, D_2, \dots, D_n$  a **relation *r*** is a subset of  $D_1 \times D_2 \times \dots \times D_n$   
Thus, a relation is a set of  $n$ -tuples  $(a_1, a_2, \dots, a_n)$  where each  $a_i \in D_i$
- The current values (**relation instance**) of a relation are specified by a table
- An element ***t*** of ***r*** is a *tuple*, represented by a *row* in a table



# Relations are Unordered

- Order of tuples is irrelevant (tuples may be stored in an arbitrary order)
- Example: *instructor* relation with unordered tuples

<i>ID</i>	<i>name</i>	<i>dept_name</i>	<i>salary</i>
22222	Einstein	Physics	95000
12121	Wu	Finance	90000
32343	El Said	History	60000
45565	Katz	Comp. Sci.	75000
98345	Kim	Elec. Eng.	80000
76766	Crick	Biology	72000
10101	Srinivasan	Comp. Sci.	65000
58583	Califieri	History	62000
83821	Brandt	Comp. Sci.	92000
15151	Mozart	Music	40000
33456	Gold	Physics	87000
76543	Singh	Finance	80000



# Database

- A database consists of multiple relations
- Information about an enterprise is broken up into parts

*instructor*

*student*

*advisor*

- Bad design:

*univ (instructor -ID, name, dept\_name, salary, student\_Id, ..)*

results in

- repetition of information (e.g., two students have the same instructor)
- the need for null values (e.g., represent an student with no advisor)

- Normalization theory (Chapter 7) deals with how to design “good” relational schemas



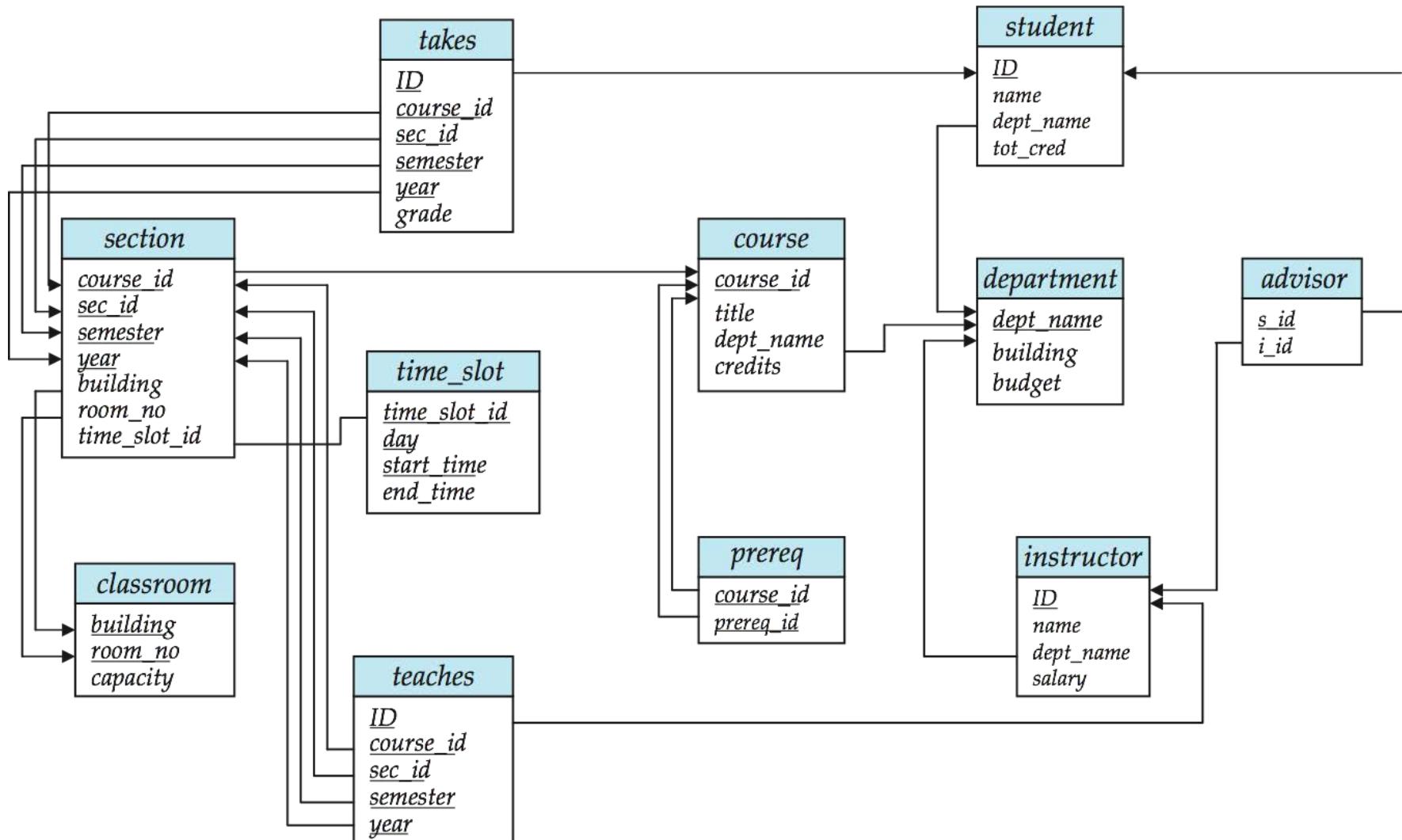
# Keys



- Let  $K \subseteq R$
- $K$  is a **superkey** of  $R$  if values for  $K$  are sufficient to identify a **unique** tuple of each possible relation  $r(R)$ 
  - Example:  $\{ID\}$  and  $\{ID, name\}$  are **both** superkeys of *instructor*.
- Superkey  $K$  is a **candidate key** if  $K$  is minimal  
Example:  $\{ID\}$  is a candidate key for *Instructor*
- One of the candidate keys is selected to be the **primary key**.
  - which one?
- **Foreign key** constraint: Value in one relation must appear in another
  - **Referencing** relation
  - **Referenced** relation



# Schema Diagram for University Database





# Relational Query Languages



- Procedural vs.non-procedural, or declarative
- “Pure” languages:
  - Relational algebra
  - Tuple relational calculus
  - Domain relational calculus
- Relational operators



# Selection of tuples

- Relation r

A	B	C	D
$\alpha$	$\alpha$	1	7
$\alpha$	$\beta$	5	7
$\beta$	$\beta$	12	3
$\beta$	$\beta$	23	10

- Select tuples with A=B  
and D > 5

- $\sigma_{A=B \text{ and } D > 5}(r)$

A	B	C	D
$\alpha$	$\alpha$	1	7
$\beta$	$\beta$	23	10



# Selection of Columns (Attributes)

- Relation  $r$ :

	A	B	C
$\alpha$	10	1	
$\alpha$	20	1	
$\beta$	30	1	
$\beta$	40	2	

- Select A and C
  - Projection
  - $\Pi_{A, C}(r)$

$$\begin{array}{c} \begin{array}{|c|c|} \hline A & C \\ \hline \alpha & 1 \\ \hline \alpha & 1 \\ \hline \beta & 1 \\ \hline \beta & 2 \\ \hline \end{array} & = & \begin{array}{|c|c|} \hline A & C \\ \hline \alpha & 1 \\ \hline \beta & 1 \\ \hline \beta & 2 \\ \hline \end{array} \end{array}$$



# Joining two relations – Cartesian Product

all to all matching

- Relations  $r, s$ :

A	B
$\alpha$	1
$\beta$	2

$r$

C	D	E
$\alpha$	10	a
$\beta$	10	a
$\beta$	20	b
$\gamma$	10	b

$s$

- $r \times s$ :

A	B	C	D	E
$\alpha$	1	$\alpha$	10	a
$\alpha$	1	$\beta$	10	a
$\alpha$	1	$\beta$	20	b
$\alpha$	1	$\gamma$	10	b
$\beta$	2	$\alpha$	10	a
$\beta$	2	$\beta$	10	a
$\beta$	2	$\beta$	20	b
$\beta$	2	$\gamma$	10	b



# Union of two relations

schema    가     가     !     x

- Relations  $r, s$ :

A	B
$\alpha$	1
$\alpha$	2
$\beta$	1

$r$

A	B
$\alpha$	2
$\beta$	3

$s$

- $r \cup s$ :

A	B
$\alpha$	1
$\alpha$	2
$\beta$	1
$\beta$	3



# Set difference of two relations

schema

- Relations  $r$ ,  $s$ :

$A$	$B$
$\alpha$	1
$\alpha$	2
$\beta$	1

$r$

$A$	$B$
$\alpha$	2
$\beta$	3

$s$

- $r - s$ :

$A$	$B$
$\alpha$	1
$\beta$	1



# Set Intersection of two relations

- Relation  $r, s$ :

$A$	$B$
$\alpha$	1
$\alpha$	2
$\beta$	1

$r$

$A$	$B$
$\alpha$	2
$\beta$	3

$s$

- $r \cap s$

$A$	$B$
$\alpha$	2



# Joining two relations – Natural Join

- Let  $r$  and  $s$  be relations on schemas  $R$  and  $S$  respectively. Then, the “natural join” of relations  $R$  and  $S$  is a relation on schema  $R \cup S$  obtained as follows:
  - Consider each pair of tuples  $t_r$  from  $r$  and  $t_s$  from  $s$ .
  - If  $t_r$  and  $t_s$  have the same value on each of the attributes in  $R \cap S$ , add a tuple  $t$  to the result, where
    - ▶  $t$  has the same value as  $t_r$  on  $r$
    - ▶  $t$  has the same value as  $t_s$  on  $s$



# Natural Join Example

- Relations r, s:

A	B	C	D
$\alpha$	1	$\alpha$	a
$\beta$	2	$\gamma$	a
$\gamma$	4	$\beta$	b
$\alpha$	1	$\gamma$	a
$\delta$	2	$\beta$	b

r

B	D	E
1	a	$\alpha$
3	a	$\beta$
1	a	$\gamma$
2	b	$\delta$
3	b	$\varepsilon$

s

- Natural Join
  - $r \bowtie s$

A	B	C	D	E
$\alpha$	1	$\alpha$	a	$\alpha$
$\alpha$	1	$\alpha$	a	$\gamma$
$\alpha$	1	$\gamma$	a	$\alpha$
$\alpha$	1	$\gamma$	a	$\gamma$
$\delta$	2	$\beta$	b	$\delta$



# Figure in-2.1

Symbol (Name)	Example of Use
$\sigma$ (Selection)	$\sigma_{\text{salary} >= 85000}(\text{instructor})$ Return rows of the input relation that satisfy the predicate.
$\Pi$ (Projection)	$\Pi_{ID, \text{salary}}(\text{instructor})$ Output specified attributes from all rows of the input relation. Remove duplicate tuples from the output.
$\bowtie$ (Natural Join)	$\text{instructor} \bowtie \text{department}$ Output pairs of rows from the two input relations that have the same value on all attributes that have the same name.
$\times$ (Cartesian Product)	$\text{instructor} \times \text{department}$ Output all pairs of rows from the two input relations (regardless of whether or not they have the same values on common attributes)
$\cup$ (Union)	$\Pi_{name}(\text{instructor}) \cup \Pi_{name}(\text{student})$ Output the union of tuples from the two input relations.