



# Fractal Analysis as Method for studying Social Hierarchy in Prehistoric Settlement Plans

with case studies from the Linear Pottery and Trypillia cultures (5.500 - 3.500  
cal. BCE)

Hallvard Bruvoll      Department of Archaeology, Conservation and History  
University of Oslo

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# Preface

Thanks to everyone.

Remember to add abstracts

Furholt, Grier, et al. (2020), Furholt, Müller, et al. (2020), Furholt, Müller-Schaeßel, et al. (2020) are three different publications. Furholt, Grier, et al. (2020), Furholt, Müller, et al. (2020), Furholt, Müller-Schaeßel, et al. (2020) are the same three publications in the same order. gfdsdgfs  
, Get on with it!





# **Part I**

## **Frameworks**



# Chapter 1

## Introduction

### 1.1 Background of the study

- Studying social hierarchy in Prehistory through fractal analysis of settlement plans
- In Europe, the Neolithic is the long and messy transition period between mobile hunter-gatherer groups in the Palaeo- and Mesolithic, and the first city states in the Bronze (Aegean) and Iron Ages (Mediterranean and Central Europe)
- Early farming economy, influence from the Near East.
- Large variety in scale and content of archaeologically defined culture groups. Single farmsteads and small hamlets in many phases – some with hardly any settlement evidence at all **examples mid-neo, use** Shennan (2018). Other phases include exceptionally large settlements, probably hosting populations of several thousand inhabitants, like at Maidanetske in central Ukraine around 3.800 BCE (see 3.3). While in some settings, like in Linear Pottery society in much of continental Europe north of the Alps towards 5.100 BCE (see 3.2), the dead were buried in simple pit graves, with very little distinction in treatment between individuals, in other phases some individuals were buried with tremendous amounts of precious goods like in Varna, Romania, or under colossal burial mounds like in Carnac, France, both in the mid-5th millennium (Shennan 2018)**check ref.**

- Seen at a very large scale – across the continent and through the Holocene – the development of society from small scale and relatively egalitarian towards large scale and more hierarchical seems evident (though not to everyone, see Graeber and Wengrow (2021) and Section 4.2). When we look more closely however, this evolution is anything but linear, as both population sizes and levels of hierarchical organisation seem to fluctuate considerably, sometimes over short time spans as from the Trypillia **C2 to D1??, check this**, when the so-called mega-sites are abandoned and their former inhabitants regroup into much smaller settlements during a transition of maybe only **check and ref** years.
- In many cases, the level of social hierarchisation and complexity in a given Prehistoric society is very hard for researchers to evaluate, since many indicators of such structures are either lost from the archaeological record, or were never included in the first place [Perreault (2019); Section 3.1]. Archaeological traces that are often interpreted as signs of social complexity and hierarchy may furthermore be deceiving. Seemingly monumental structures were in many cases built through small additions over centuries, rather than in one colossal construction campaign [**example, Carnac alignments? Danish megaliths?**]. In many megalithic burial contexts, it may be impossible to know how large a segment of the society that had access to such inhumations (**rephrase**).
- New methods for investigating hierarchy: fractal analysis. Borrowed from other disciplines, not much tested in Archaeology. Example from human geography, use:(Batty 2005; Batty and Longley 1994; D’Acci 2019; Jahanmiri and Parker 2022; Lagarias and Prastacos 2021; Tannier and Pumain 2005) (say what fractal analysis does, don’t explain what it is here)(explain just the word fractal and cite section).

## 1.2 Research question and objectives

The overall goal of the present study is to test and assess the utility of fractal analysis techniques as tools for studying hierarchical social organisation in prehistoric societies. Two methodological approaches are under special scrutiny: the distribution fitting approach and the image analysis approach (Brown and Liebovitch 2010; Brown, Witschey, and Liebovitch 2005). These are ap-

plied to architectural data series from well-preserved and documented archaeological samples within neolithic Linear Pottery and Trypillia contexts, as well as to synthetic data series. This thesis is thus not to be considered a culture-historic study of Linear Pottery or Trypillia society, but mainly a methodological study. However, results from the proposed analyses of these case studies may also contribute, as side-effects, to their respective fields of research.

For the distribution fitting approach, house-size distributions within settlements are modelled following a given procedure, and the retained model (the best fit) is interpreted in terms of social generating mechanisms. In particular, it is argued here that so-called power-law distributions reflect hierarchical structure, so that the identification of these within the studied samples may indicate the presence of some social hierarchisation process which warrants further interpretation.

With the image analysis approach, archaeological and synthetic settlement plans are analysed through the calculation of fractal dimension and lacunarity – summary statistics which serve as quantifications of irregular spatial patterns or image textures. I argue here that geometrically irregular settlement plans are indicative of relative independence between households, while settlements that develop within geometrically regular grids indicate stronger overarching social structures, with a continuous range of possibilities in-between. The goal here is to test to which extent quantitative measures like fractal dimension and lacunarity may help differentiating between varying degrees of planning in prehistoric settlements.

While both these methodological approaches are well developed and integrated to other disciplines, their usage in Archaeology have so far remained anecdotal (Diachenko 2018). A further overall goal of this thesis is to identify and explore possible limitations in the nature of archaeological data that may limit the applicability of fractal analysis methods within this discipline. For example, does fractal analysis of settlement plans require a data quality that would be practically unattainable in archaeological settings? But also inversely, as it is impossible to explore all potential applications within the framework of one doctoral thesis, suggestions for future research are provided in the last chapter.

## 1.3 Some definitions

Just the minimum required to present the thesis in general terms.

- Hierarchy Pumain (2006), Xia et al. (2021),

Wolves:

Cafazzo, Lazzaroni, and Marshall-Pescini (2016), Packard (2003): linear hierarchy and leadership among wolves.

Rodríguez et al. (2017): wolf “hierarchy”, even when illustrated as pyramidal, is really linear (me).

In Muro et al. (2011): simulating wolf-pack hunting strategies without hierarchy

Mech (1999): “linear dominance hierarchy” model doesn’t fit well with most wolf packs in the wild, consisting of a single breeding couple and their offspring.

- Inequality Kohler and Smith (2018), Midlarsky (1999), Price and Feinman (2010), Price and Feinman (1995) NA
- Social complexity Daems (2021) NA

## 1.4 Main findings here?

Maybe leave to the end, and fill in, like abstract.

## 1.5 Research ethics

- Social complexity and evolution. Are less complex societies simple? Is that a bad thing?
- Open science and open-source scripts

- Terminology and spelling (British English for text. For geographical place names, Slovak special characters are kept as far as possible, even though it can be a pain in the xxx to render in Rmarkdown on Windows OS, and the 2010 Ukranian National transliteration system with only ASCII characters and no soft sign)
- Abstracts in Slovak and Ukranian (and not only in Norwegian)

## 1.6 Structure of the thesis

This thesis is structured as a monograph in four parts. In the first part the overall framework of the study is exposed, with the general introduction above, the overarching theoretical framework in Chapter 2, and the background of the study material in Chapter 3. Parts II and III are devoted to each their methodological approach to the material: Part II to the study of hierarchy in size distributions, and Part III to the quantification of image textures. Each of these parts consists of three chapters, the first of which – Chapters 4 and 7 – exposes the theoretical and interpretative background of the applied methods and their relevance to Archaeology. The following chapters – Chapters 5 and 8 – detail the technical specifics of the two approaches and their implementation in this study, and the last chapters within these parts – Chapters 6 and 9 – provide the actual analyses and summaries of results. In Part IV, the findings are summarised and further discussed. Chapter 10 gives an attempt of interpreting the results in the context of the culture-historical setting of the European Neolithic, while Chapter 11 reviews the possibilities and limitations of the fractal analysis framework in Archaeology. Concluding remarks and suggestions for further study are given in Chapter 12.

Some readers might react to an apparent deviation from the academic tradition of devoting a separate chapter to research history. This is a deliberate choice, not to suggest that historiography is unimportant, but rather as a result of the fundamentally interdisciplinary scope of the study. In fact, there is very little extant history of applying fractal analysis in Archaeology – the few studies that, to my knowledge, have been done in this direction are discussed primarily in Sections 4.5 and 7.3. Fractal analysis itself holds a research history of its own (see Section 2.2), and so does the study of Linear Pottery (Section 3.2) and Trypillia societies (Section 3.3), not to mention the

general study of social complexity in Prehistory (mainly Section 3.1). In short, instead of trying to shoehorn these parallel histories into a clearly delimited but rather hybrid chapter, I have opted for what I believe to be a more useful approach, namely to fit them in more seamlessly where they belong, in the various associated theory and methods chapters.

An additional note should be made here regarding the writing style of the different parts and chapters. It is my belief that a major obstacle for fractal analysis methods to become more integrated into the standard tool kits of archaeological research, is the excessively technical nature of much of the associated literature. Archaeology as a discipline remains profoundly rooted in the Humanities, as seen in the inbuilt structure of teaching, research and funding institutions in most (at least European) countries. Fractal analysis is derived from pure mathematics, and most applications so far have been developed within the natural sciences (**ref necessary?**). Archaeologists who are trained within a humanistic scholarly tradition cannot be expected to hold a skill level of mathematics more advanced than what is achieved in high school, and code programming is hardly taught at all within the walls of Humanities faculties. Technical details regarding the methods and analyses applied in this thesis are therefore – as much as possible – limited to the devoted Chapters 5 and 8, and readers who are interested in these may also refer to the online code repository for more details and reproducibility **cite repository**. In the rest of the thesis I have opted for a more narrative approach, in an attempt to invite a somewhat larger audience of archaeologists into the fascinating complexities of fractals.

END Chapter

Here I skipped a line.

Here I added a backslash.

Figures and tables with captions will be placed in figure and table environments, respectively.

```
par(mar = c(4, 4, .1, .1))  
plot(pressure, type = 'b', pch = 19)
```

Reference a figure by its code chunk label with the `fig:` prefix, e.g., see Figure 1.1. Similarly, you can reference tables generated from `knitr::kable()`, e.g., see Table 1.1.



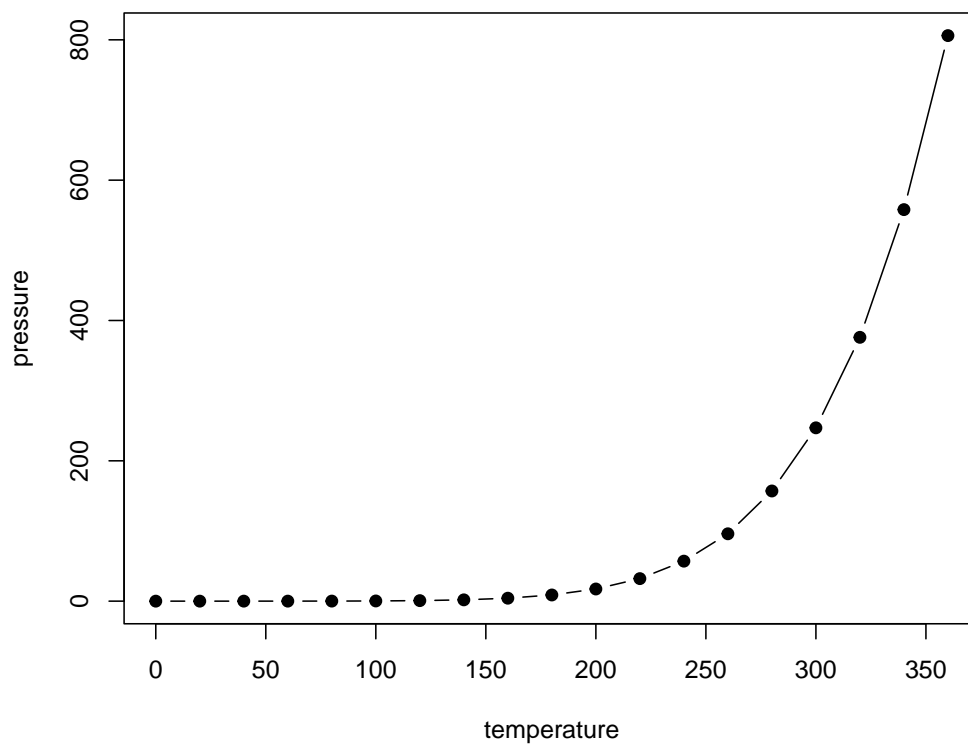


Figure 1.1: Here is a nice figure!

```
knitr::kable(  
  head(iris, 20), caption = 'Here is a nice table!',  
  booktabs = TRUE  
)
```

You can write citations, too. For example, we are using the **bookdown** package (**R-bookdown?**) in this sample book, which was built on top of R Markdown and **knitr** (Xie 2015).

Test: Morgan (1965).

Test: Mandelbrot (2021). jløkj fdsasdfadfasdfadf new text

Table 1.1: Here is a nice table!

Sepal.Length	Sepal.Width	Petal.Length	Petal.Width	Species
5.1	3.5	1.4	0.2	setosa
4.9	3.0	1.4	0.2	setosa
4.7	3.2	1.3	0.2	setosa
4.6	3.1	1.5	0.2	setosa
5.0	3.6	1.4	0.2	setosa
5.4	3.9	1.7	0.4	setosa
4.6	3.4	1.4	0.3	setosa
5.0	3.4	1.5	0.2	setosa
4.4	2.9	1.4	0.2	setosa
4.9	3.1	1.5	0.1	setosa
5.4	3.7	1.5	0.2	setosa
4.8	3.4	1.6	0.2	setosa
4.8	3.0	1.4	0.1	setosa
4.3	3.0	1.1	0.1	setosa
5.8	4.0	1.2	0.2	setosa
5.7	4.4	1.5	0.4	setosa
5.4	3.9	1.3	0.4	setosa
5.1	3.5	1.4	0.3	setosa
5.7	3.8	1.7	0.3	setosa
5.1	3.8	1.5	0.3	setosa

## **Chapter 2**

# **Theoretical framework: Complexity and Fractals**

## **2.1 Very short introduction to Complexity Theory / Dynamical Systems Theory**

Lit. use Daems (2021) and Bentley and Maschner (2007).

For Dynamical Systems, use Awrejcewicz and Grzelczyk (2020) and Devaney (2020), but don't go into detail.

Describe complexity, dynamical systems, chaos, feedback loops, criticality, emergence. Scale West (2017) NA

Mention the most common applications in Archaeology: ABMs, **and what?** check in literature.

## **2.2 Very short introduction to Fractals and Fractal Analysis**

Lit. use Mandelbrot (2021), Falconer and Falconer (2013) (general), also Brown and Liebovitch (2010), Brown et al. (2005) and Diachenko (2018) (for Archaeology)

Two sentences on history of fractals? Mandelbrot. Maybe cut?

Fractals as irregular patterns/structures

Fractals as hierarchy

Self-similarity and scale invariance

Processes/mechanisms that produce fractals:

- Cascading bifurcations and confluences (splitting or merging - tree structure/arborescence/branching, and relation to size. Terminology borrowed from biology and fluid dynamics (including turbulence/turbulent flow))

The role of randomness - tidy and messy fractals (romanesco broccolis are not more fractal than regular broccolis, only more regular.

The relationship with criticality and chaos: deterministic *and* unpredictable

Fractals embedded in

- Space (hence “fractal geometry”): geomorphology, plants, ocean and wind currents, galaxies, also human constructed features (see Chapter xx for details)
- Time series: earthquakes, finance (not applied in this study, though should be done later)
- Networks/abstract: hierarchical organisations, income distributions, word counts, 1/f or pink noise, www. etc. (see Chapter xxx for details)
- Pure mathematics: Julia and Mandelbrot sets, strange attractors (don’t go into details!)

No, not everything is fractal: e.g. Central Limit Theorem

Fractal analysis for studying irregular phenomena (methods described in more detail Chapters xxx), and thus as a tool for quantitative empirical research.

## 2.3 Very short introduction to micro-macro approaches in social theory

- Lévi-Strauss and Structuralism
- Giddens and Structuration Theory
- Delanda and Assemblage Theory
- Latour and Actor-Network Theory

What these approaches all have in common, is that they are entirely qualitative (**check**).

- That's not a problem in itself.
- Quant approach is both possible for the stated purpose, and desirable for reasons of comparative analysis.
- Data deluge (refer to chap. on geomagn data). The goal here is to establish a quantitative framework for studying social complexity and hierarchy in archaeological/prehistoric settings. Further articulating fractal analysis with existing social theoretical approaches is not the primary goal here, as it could constitute a separate research project. In the present thesis, bla bla.

END chapter.

Math can be added in body using usual syntax like this

$p$  is unknown but expected to be around  $1/3$ . Standard error will be approximated

$$SE = \sqrt{\left(\frac{p(1-p)}{n}\right)} \approx \sqrt{\frac{1/3(1-1/3)}{300}} = 0.027$$

You can also use math in footnotes like this<sup>1</sup>.

We will approximate standard error to  $0.027$ <sup>2</sup>

---

<sup>1</sup>where we mention  $p = \frac{a}{b}$

<sup>2</sup> $p$  is unknown but expected to be around  $1/3$ . Standard error will be approximated

---

$$SE = \sqrt{\frac{p(1-p)}{n}} \approx \sqrt{\frac{1/3(1-1/3)}{300}} = 0.027$$

# Chapter 3

## Material and data: social complexity in the European Neolithic

### 3.1 Studying social complexity in Archaeology and Prehistory.

- Grave goods
- Burial monuments
- The denominator problem
- The use of ethnography
- Other approaches (osteological, isotopes **refs**)
- This project: house-size distributions and settlement layouts (details in subsequent chapters), just very short argumentation.
- Comparative approach: Neolithic technology (not bronze axes), wood and wattle-and-daub architecture, (near) complete settlement plans/extensive documentation

## **3.2 The Linear Pottery culture complex**

- General intro to the culture
- Linear Pottery architecture and house construction
- Organisation of Linear Pottery society: egalitarian or hierarchic?
- The Žitava valley and research project

## **3.3 The Cucutení-Trypillia culture complex**

- General intro to the culture
- Trypillia architecture and house construction
- Trypillia social organisation: current debate
- The B2/C1 and the mega-sites of the Southern Bug – Dnipro interfluvium

## **3.4 Reading site plans from geomagnetic imagery**

- Caveats: fill in here.

## **3.5 Synthetic data**

- And why I'm not (this time) relying on ethnographic data.
- Don't go into technicalities here, just the reasoning.



## **Part II**

### **Size distributions**



# Chapter 4

## House sizes and social meaning

### 4.1 What is social hierarchy?

- Political assumptions – all hierarchical social structures are not despotic top-down rule. Democracies can also be very hierarchical. Matter of scale rather than political system Graeber and Wengrow (2021). But, tendencies? Use Pumain (2006), also furholt2020b.
- Nested and non-nested social hierarchies, hierarchical hunter-gatherers? Hamilton et al. (2007), Whitridge (2016) (or use in Chapter 11?)
- Biologically defined thresholds to group size? Dunbar's number and controversies, Dunbar (2022), West et al. (2023) (add published papers). Scalar stress Johnson (1982), Alberti (2014), Zhou et al. (2005)

### 4.2 Social typologies and their critique

- Tools for classifying societies, or evolutionary model? Discussion of Johnson and Earle (1987), Testart (2005), Service (1971), Earle (1997).
- Anti-evolution critique in Yoffee (1993), Yoffee (2005), Kienlin and Zimmermann (2012), Lund, Furholt, and Austvoll (2022), Furholt, Grier, et al. (2020). Anarchistic critique:

Crumley (1995), Haude and Wagner (2019), Graeber and Wengrow (2021)

### 4.3 Possible reasons for house-size difference

Often underlying assumptions: household wealth or size? Or both?

- Kinship and households: who lives in a house? Sahlins (2013), Ensor (2013), Ensor, Irish, and Keegan (2017)
- Do clan leaders have bigger houses? check Haude and Wagner (2019)

Discuss some archaeo references

Functional difference:

- Ethnography of initiation houses, communal/assembly houses, ritual houses, including Barley (2011), Godelier (1986), Wilk (1983), Fraser (1968), Haude and Wagner (2019)
- Caveats: building materials and constraints

### 4.4 Interpreting distribution types and their underlying mechanisms

- Power-law distributions, hierarchy and scale invariance.
- Normal distributions and the Central Limit Theorem.
- Exponential distributions and growth rates.
- Combinations: Log-normal, stretched exponential, parabolic fractal
- Notes on terminology: Power law, Pareto and Zipf, Newman (2005)
- A law (distribution) is not a law (of nature), see Grove (2011) for review of the long-lasting confusion in Archaeology (e.g. Hodder (1979)), also “rank-size rule”

## 4.5 Fitting heavy-tailed distributions in Archaeology

- Lit. use Strawinska-Zanko et al. (2018), Crabtree et al. (2017), Maschner and Bentley (2003), Grove (2011) ++
- Zipf law and Settlement Scaling theory, Bettencourt (2021), Gomez-Lievano, Youn, and Bettencourt (2012), Lobo et al. (2020). Connection with Central Place Theory, e.g. Müller-Schneeßel (2007), Chen (2011). Why I'm not doing settlement scaling in this study.

END chapter



# Chapter 5

## Methods: Distribution fitting

### 5.1 Heavy-tailed distributions, testing for power laws

- Technical characteristics of power laws, Newman (2005), do I need more?
- Old style distribution fitting (which is used in Brown and Liebovitch (2010) and Brown et al. (2005) and check. Mitzenmacher (2004), Harrison (1981)
- New style presented in Clauset, Shalizi, and Newman (2009), Stumpf and Porter (2012), implemented in R with the powerLaw package Gillespie (2015), and used in Strawinska-Zanko et al. (2018) and Crabtree et al. (2017). More recent?

### 5.2 Methodological procedure

- Reminder of main goal for this part of the study: identify power-law structures in the house-size distributions of the Linear Pottery and Trypillia samples.
- Synthetic data generation:
  - Why?
    1. Process: how long/much does it take for a normal distribution to become power-law? And reverse sense?

2. Temporal resolution issue: does the temporal palimpsest of several phases with e.g. log-normal distributions produce false power-law signals?
  - How?
    - \* Random number generation and iterated multiplicative (1.) or additive (2.) sequences, with K-S testing (Gillespie 2015) at each stage. Report when the distributions become power laws.
- Present data set with categories (settlements, quarters/neighbourhoods, time samples for Vráble)
- Parameter settings: dist. types, xmin, testing the pl hypothesis etc. Minimal house-count cutoff (min. sample size). Isolating top house.

## 5.3

END chapter



# Chapter 6

## Results: Distribution fitting

### 6.1 Synthetic distributions

Fill in analysis for

1. Multiplicative process
2. Additive process

### 6.2 Settlements

House-size distributions of whole settlements (both Linear Pottery and Trypillia)

### 6.3 Quarters/neighbourhoods

House-size distributions of separate quarters (Nebelivka) and neighbourhoods (Vráble). Can I include separate Nebelivka neighbourhoods as well? (prob. too small, but check)

## 6.4 Temporal samples (Vráble)

If time, I can add more Žitava sitesre, but not necessary. I can also analyse temporal samples of Vráble neighbourhoods separately.

## 6.5 Summary of findings

END Chapter

## **Part III**

### **Settlement Plans**



# Chapter 7

## Village planning in Prehistory

### 7.1 Settlement layout and social structure

Or the social organisation of village layout. Research background:

Lit. use Furholt (2016), Fraser (1968), Ensor et al. (2017) (not the correct reference, I should ask him!)

Use the Trypillia volumes. Also Müller-Scheeßel (2019), Trebsche, Müller-Scheeßel, and Reinhold (2010)

Factors affecting village layout:

- Political structure (but, as with hierarchy, an organised layout does not necessarily equate top-down despotic decision making).
- Kinship, matrimonial and locality structures
- Cosmology (e.g. Linear Pottery house orientations)
- Economic and ritual functions of village elements (constructed and non-constructed)
- Local landscape setting (to be factored out)

## 7.2 The geometries of conscious planning vs. emergent behaviour

- I need to find some references here!
- Euclid: grids, lines, circles – how humans think in shapes. Social settings: architect/planner, strong common institutions/ideals (examples?)
- Mandelbrot: irregular, self-similar, scale independent (i.e. fractal) shapes – emergent, not consciously preconceived. Self-organisation. Does the “no pattern” case exist? Emergence from repetitive sequences of simple choices/mechanisms. Examples.
- Binary or continuum? Needs to be studied empirically.

## 7.3 Fractal image analysis in archaeology

END Chapter

# Chapter 8

## Methods: Fractal image analysis

fdasdf

### 8.1 Fractal dimension and lacunarity

- Box-counting, lit. Mancuso (2021), Li, Du, and Sun (2009), Klinkenberg (1994)
- Gliding-box algorithms, Allain and Cloitre (1991), Hingee et al. (2019), Cheng (1997), Plotnick et al. (1996)
- Caveats:
  - Fractional box-counting dimension does not equal self-similarity in a simple way
  - My summary  $L$  is not equal to the one used in *FracLac* and thus by Farías-Pelayo (2017)

### 8.2 Image preparation

- Procedure for archaeological samples, same as in article
- Procedure for synthetic sample

END Chapter



# **Chapter 9**

## **Results: Image analysis**

### **9.1 Synthetic settlement plans**

### **9.2 Settlements**

### **9.3 Quarters/neighbourhoods**

### **9.4 Temporal samples (Vráble)**

### **9.5 Summary of findings**

END Chapter



## **Part IV**

# **Synthesis**



## **Chapter 10**

### **Discussion: Social complexity in Linear Pottery and Trypillia settlements**

fdsasdf

END Chapter



# **Chapter 11**

## **Discussion: Fractal Analysis and Archaeological data**

fdsasdf

END Chapter





# Chapter 12

## Conclusion and Outlook

### 12.1 Things I would like to have done, but that didn't fit into this study

- Ethnoarchaeology: Measure house sizes and settlement layouts in contemporary settings, and relate to social organisation (largely overlooked by ethnographers)
- Test distributions and settlement layout analysis on other settings: Lake dwellings, later/historic periods, other materials (e.g. megaliths)... Add more complex distribution models, add observation windows on images. Try on remote sensing imagery.
- Settlement Scaling on Neolithic settings
- Time series: Hurst exponent and scale invariance in temporal development of e.g. regional settlement or population
- Integrate – bridge the gap – between opposite theoretical (nat. and soc./hum.) approaches to the same phenomena
- Chaos and strange attractors in Archaeology
- More?

## 12.2 Concluding remarks

END Thesis

# References

- Alberti, Gianmarco. 2014. “Modeling Group Size and Scalar Stress by Logistic Regression from an Archaeological Perspective.” *PLOS ONE* 9(3):e91510. doi: 10.1371/journal.pone.0091510.
- Allain, C., and M. Cloitre. 1991. “Characterizing the Lacunarity of Random and Deterministic Fractal Sets.” *Physical Review A* 44(6):3552–58. doi: 10.1103/PhysRevA.44.3552.
- Awrejcewicz, Jan, and Dariusz Grzelczyk. 2020. *Dynamical Systems Theory*.
- Barley, Nigel. 2011. *The Innocent Anthropologist: Notes from a Mud Hut*. Eland.
- Batty, Michael. 2005. *Cities and complexity: understanding cities with cellular automata, agent-based models, and fractals*. Cambridge, Mass.: MIT Press.
- Batty, Michael, and Paul Longley. 1994. *Fractal Cities - a Geometry of Form and Function*. London: Academic Press.
- Bentley, R. Alexander, and Herbert D. G. Maschner. 2007. “Complexity Theory.” *Handbook of Archaeological Theories* 245–70.
- Bettencourt, Luís M. A. 2021. *Introduction to Urban Science: Evidence and Theory of Cities as Complex Systems*. Cambridge, MA, USA: MIT Press.
- Brown, Clifford T., Walter RT Witschey, and Larry S. Liebovitch. 2005. “The Broken past: Fractals in Archaeology.” *Journal of archaeological method and theory* 12(1):3778. doi: 10.1007/s10816-005-2396-6.
- Brown, Clifford, and Larry Liebovitch. 2010. *Fractal Analysis*. 2455 Teller Road, Thousand Oaks California 91320 United States of America: SAGE Publications, Inc.
- Cafazzo, Simona, Martina Lazzaroni, and Sarah Marshall-Pescini. 2016. “Dominance Relationships in a Family Pack of Captive Arctic Wolves (*Canis Lupus Arctos*): The Influence of Competition for Food, Age and Sex.” *PeerJ* 4:e2707. doi: 10.7717/peerj.2707.

- Chen, Yanguang. 2011. “Fractal Systems of Central Places Based on Intermittency of Space-Filling.” *Chaos, Solitons & Fractals* 44:619–32.
- Cheng, Qiuming. 1997. “Multifractal Modeling and Lacunarity Analysis.” *Mathematical geology* 29(7):919–32. doi: 10.1023/A:1022355723781.
- Clauset, Aaron, Cosma Rohilla Shalizi, and M. E. J. Newman. 2009. “Power-Law Distributions in Empirical Data.” *Society for Industrial and Applied Mathematics Review* 51(4):661–703.
- Crabtree, Stefani A., R. Kyle Bocinsky, Paul L. Hooper, Susan C. Ryan, and Timothy A. Kohler. 2017. “How to Make a Polity (in the Central Mesa Verde Region).” *American Antiquity* 82(1):71–95. doi: 10.1017/aaq.2016.18.
- Crumley, Carole L. 1995. “Heterarchy and the Analysis of Complex Societies.” *Archaeological Papers of the American Anthropological Association* 6(1):1–5. doi: <https://doi.org/10.1525/ap3a.1995.6.1.1>.
- D’Acci, Luca, ed. 2019. *The Mathematics of Urban Morphology*. Cham: Springer International Publishing.
- Daems, Dries. 2021. *Social complexity and complex systems in archaeology*. London, New York: Routledge.
- Devaney, Robert L. 2020. *A First Course In Chaotic Dynamical Systems: Theory And Experiment*. Milton: CRC Press.
- Diachenko, Alexandr. 2018. “Fractal Models” edited by S. López Varela.
- Dunbar, Robin. 2022. *Annales Academiæ Scientiarum Fennicæ [Forthcoming] Reconstructing Dunbar’s Number: A Guide for the Perplexed to Some Pitfalls, Indiscretions and Fallacies*.
- Earle, Timothy K. 1997. *How chiefs come to power: the political economy in prehistory*. Stanford, Calif: Stanford University Press.
- Ensor, Bradley E. 2013. *The Archaeology of Kinship: Advancing Interpretation and Contributions to Theory*. University of Arizona Press.
- Ensor, Bradley E., Joel D. Irish, and William F. Keegan. 2017. “The Bioarchaeology of Kinship: Proposed Revisions to Assumptions Guiding Interpretation.” *Current Anthropology* 58(6):739–61. doi: 10.1086/694584.
- Falconer, Kenneth, and Kenneth Falconer. 2013. *Fractals: A Very Short Introduction*. Oxford,

- New York: Oxford University Press.
- Fariás-Pelayo, Sabrina. 2017. “Characterization of Cultural Traits by Means of Fractal Analysis.” edited by F. Brambila. IntechOpen.
- Fraser, Douglas. 1968. *Village Planning in the Primitive World*. New York: George Braziller.
- Furholt, Martin. 2016. “Settlement Layout and Social Organisation in the Earliest European Neolithic.” *Antiquity* 90(353):1196–1212.
- Furholt, Martin, Colin Grier, Matthew Spriggs, and Timothy Earle. 2020. “Political Economy in the Archaeology of Emergent Complexity: A Synthesis of Bottom-Up and Top-Down Approaches.” *Journal of Archaeological Method and Theory* 27(2):157–91. doi: 10.1007/s10816-019-09422-0.
- Furholt, Martin, Johannes Müller, Alena Bistáková, Maria Wunderlich, Ivan Cheben, and Nils Müller-Scheeßel. 2020. *Archaeology in the Zitava Valley 1 - the LBK and Zeliezovce Settlement Site of Vráble*. Leiden: Sidestone Press.
- Furholt, Martin, Nils Müller-Scheeßel, Maria Wunderlich, Ivan Cheben, and Johannes Müller. 2020. “Communality and Discord in an Early Neolithic Settlement Agglomeration: The LBK Site of Vráble, Southwest Slovakia.” *Cambridge Archaeological Journal* 30(3):469–89.
- Gillespie, Colin S. 2015. “Fitting Heavy Tailed Distributions: The powerLaw Package.” *Journal of Statistical Software* 64(2).
- Godelier, Maurice. 1986. *The making of great men: male domination and power among the New Guinea Baruya*. Vol. 56. Cambridge: University Press.
- Gomez-Lievano, Andres, Hyejin Youn, and Luís Bettencourt. 2012. “The Statistics of Urban Scaling and Their Connection to Zipf’s Law.” *PloS One* 7:e40393. doi: 10.1371/journal.pone.0040393.
- Graeber, David, and David Wengrow. 2021. *The dawn of everything: a new history of humanity*. New York: Farrar, Straus; Giroux.
- Grove, Matt. 2011. “An Archaeological Signature of Multi-Level Social Systems: The Case of the Irish Bronze Age.” *Journal of Anthropological Archaeology* 30(1):44–61. doi: 10.1016/j.jaa.2010.12.002.
- Hamilton, Marcus, Bruce Milne, Robert Walker, Oskar Burger, and James Brown. 2007. “The Complex Structure of Hunter-Gatherer Social Networks.” *Proceedings of the Royal Society*

*B* 274:2195–2202.

- Harrison, Alan. 1981. “A Tale of Two Distributions.” *The Review of Economic Studies* 48(4):621–31.
- Haude, Rüdiger, and Thomas Wagner. 2019. *Herrschaftsfreie Institutionen : Texte zur Stabilisierung staatsloser, egalitärer Gesellschaften*. Heidelberg: Verlag Graswurzelrevolution.
- Hingee, Kassel, Adrian Baddeley, Peter Caccetta, and Gopalan Nair. 2019. “Computation of Lacunarity from Covariance of Spatial Binary Maps.” *Journal of Agricultural, Biological and Environmental Statistics* 24(2):264–88. doi: 10.1007/s13253-019-00351-9.
- Hodder, Ian. 1979. “Simulating the Growth of Hierarchies.” Pp. 117–44 in, edited by C. Renfrew and K. L. Cooke. New York: Academic Press.
- Jahanmiri, Fatemeh, and Dawn Cassandra Parker. 2022. “An Overview of Fractal Geometry Applied to Urban Planning.” *Land* 11(4):475. doi: 10.3390/land11040475.
- Johnson, Allen, and Timothy Earle. 1987. *The Evolution of Human Societies : From Foraging Group to Agrarian State*. Stanford: Stanford University Press.
- Johnson, Gregory A. 1982. “Organizational Structure and Scalar Stress.” Pp. 389–421 in, edited by C. Renfrew, M. J. Rowlands, and B. A. Segraves. New York: Academic Press.
- Kienlin, Tobias L., and Andreas Zimmermann. 2012. *Beyond Elites - Alternatives to Hierarchical Systems in Modelling Social Formations: International Conference at the Ruhr-Universität Bochum, Germany, ... Zur Prähistorischen Archäologie*. Bonn: Habelt, R.
- Klinkenberg, Brian. 1994. “A Review of Methods Used to Determine the Fractal Dimension of Linear Features.” *Mathematical Geology* 26(1):23–46. doi: 10.1007/BF02065874.
- Kohler, Timothy A., and Michael E. Smith. 2018. *Ten Thousand Years of Inequality: The Archaeology of Wealth Differences*. Tucson: University of Arizona Press.
- Lagarias, Apostolos, and Poulicos Prastacos. 2021. “Fractal Dimension of European Cities: A Comparison of the Patterns of Built-up Areas in the Urban Core and the Peri-Urban Ring.” *Cybergeog: European Journal of Geography*. doi: 10.4000/cybergeog.37243.
- Li, Jian, Qian Du, and Caixin Sun. 2009. “An Improved Box-Counting Method for Image Fractal Dimension Estimation.” *Pattern Recognition* 42(11):2460–69. doi: 10.1016/j.patcog.2009.03.001.
- Lobo, Jose, Luis MA Bettencourt, Michael E. Smith, and Scott Ortman. 2020. “Settlement

- Scaling Theory: Bridging the Study of Ancient and Contemporary Urban Systems.” *Urban Studies* 57(4):731–47. doi: 10.1177/0042098019873796.
- Lund, Julie, Martin Furholt, and Knut Ivar Austvoll. 2022. “Reassessing Power in the Archaeological Discourse. How Collective, Cooperative and Affective Perspectives May Impact Our Understanding of Social Relations and Organization in Prehistory.” *Archaeological Dialogues* 1–18. doi: 10.1017/S1380203822000162.
- Mancuso, Francesco Paolo. 2021. “fractD: Estimation of Fractal Dimension of a Black Area in 2D and 3D (Slices) Images.”
- Mandelbrot, Benoit B. 2021. *The Fractal Geometry of Nature*. Brattleboro: Echo Point Books & Media, LLC.
- Maschner, Herbert, and Alexander Bentley. 2003. “The Power Law of Rank and Household on the North Pacific.” Pp. 47–143 in, edited by A. Bentley and H. Maschner. Salt Lake City: The University of Utah Press.
- Mech, L. David. 1999. “Alpha Status, Dominance, and Division of Labor in Wolf Packs.” *Canadian Journal of Zoology* 77(8):1196–1203. doi: 10.1139/z99-099.
- Midlarsky, Manus I. 1999. *The Evolution of Inequality: War, State Survival, and Democracy in Comparative Perspective*. Stanford: Stanford University Press.
- Mitzenmacher, Michael. 2004. “A Brief History of Generative Models for Power Law and Log-normal Distributions.” *Internet Mathematics* 1(2):226–51. doi: 10.1080/15427951.2004.10129088.
- Morgan, Lewis H. 1965. *Houses and House-Life of the American Aborigines*. Chicago: The University of Chicago Press.
- Müller-Scheeßel, Niels. 2007. “Further Thoughts on the Hidden Settlement Structures of the Hallstatt Period in Southern Germany: Testing for Auto-Correlation.” *Archäologisches Korrespondenzblatt* 37(1):57–66.
- Müller-Scheeßel, Nils. 2019. “A New Approach to the Temporal Significance of House Orientations in European Early Neolithic Settlements.” doi: 10.17026/DANS-XU6-C6YR.
- Muro, C., R. Escobedo, L. Spector, and R. P. Coppinger. 2011. “Wolf-Pack (*Canis Lupus*) Hunting Strategies Emerge from Simple Rules in Computational Simulations.” *Behavioural Processes* 88(3):192–97. doi: 10.1016/j.beproc.2011.09.006.
- Newman, M. E. J. 2005. “Power Laws, Pareto Distributions and Zipf’s Law.” *Contemporary*

- Physics* 46(5):325–51. doi: 10.1080/00107510500052444.
- Packard, Jane. 2003. “Wolf Behavior: Reproductive, Social and Intelligent.” Pp. 35–65 in *Wolves: Behavior, ecology, and conservation*, edited by L. D. Mech and L. Boitani. Chicago and London: The University of Chicago Press.
- Perreault, Charles. 2019. *The quality of the archaeological record*. Chicago: The University of Chicago Press.
- Plotnick, Roy E., Robert H. Gardner, William W. Hargrove, Karen Prestegard, and Martin Perlmutter. 1996. “Lacunarity Analysis: A General Technique for the Analysis of Spatial Patterns.” *Physical Review E* 53(5):5461–68. doi: 10.1103/PhysRevE.53.5461.
- Price, T. Douglas, and Gary M. Feinman. 1995. *Foundations of social inequality*. New York: Plenum Press.
- Price, T. Douglas, and Gary M. Feinman. 2010. *Pathways to Power: New Perspectives on the Emergence of Social Inequality*. New York, NY: Springer.
- Pumain, Denise. 2006. *Hierarchy in Natural and Social Sciences*. Vol. 3. 1st ed. 2006. Dordrecht: Springer Netherlands : Imprint: Springer.
- Rodríguez, Luis, Oscar Castillo, José Soria, Patricia Melin, Fevrier Valdez, Claudia I. Gonzalez, Gabriela E. Martinez, and Jesus Soto. 2017. “A Fuzzy Hierarchical Operator in the Grey Wolf Optimizer Algorithm.” *Applied Soft Computing* 57:315–28. doi: 10.1016/j.asoc.2017.03.048.
- Sahlins, Marshall. 2013. *What kinship is - and is not*. Chicago: University of Chicago Press.
- Service, Elman. 1971. *Primitive Social Organization : An Evolutionary Perspective*. 2nd ed. New York: Random House.
- Shennan, Stephen. 2018. *The first farmers of Europe: an evolutionary perspective*. Cambridge: University Press.
- Strawinska-Zanko, Urszula, Larry Liebovitch, April Watson, and Clifford Brown. 2018. “Capital in the First Century: The Evolution of Inequality in Ancient Maya Society.” Pp. 161–92 in, *Computational Social Sciences*, edited by U. Strawinska-Zanko and L. Liebovitch. Cham: Springer International Publishing.
- Stumpf, Michael P. H., and Mason A. Porter. 2012. “Critical Truths about Power Laws.” *Science* 335(6069):665–66. doi: 10.1126/science.1216142.



- Tannier, Cécile, and Denise Pumain. 2005. “Fractals in Urban Geography: A Theoretical Outline and an Empirical Example.” *Cybergeo : European Journal of Geography*. doi: <https://doi.org/10.4000/cybergeo.3275>.
- Testart, Alain. 2005. *Eléments de Classification Des Sociétés*. Paris, France: Éditions Errance : ill. en noir, tabl., cartes, schémas, couv. ill. en coul.
- Trebsche, Peter, Nils Müller-Scheeßel, and Sabine Reinhold. 2010. *Der gebaute Raum: Bausteine einer Architektursoziologie vormoderner Gesellschaften*. Münster: Waxmann.
- West, Bruce, Robin Dunbar, Culbreth Garland, and Paolo Grigolini. 2023. *Fractal Structure of Human and Primate Social Networks Optimizes Information Flow*.
- West, Geoffrey B. 2017. *Scale: the universal laws of growth, innovation, sustainability, and the pace of life in organisms, cities, economies, and companies*. New York: Penguin Press.
- Whitridge, Peter. 2016. “Fractal Worlds: An Archaeology of Nested Spatial Scales.” *ARCTIC* 69(5):1–10. doi: 10.14430/arctic4659.
- Wilk, Richard R. 1983. “Little house in the jungle: The causes of variation in house size among modern Kekchi Maya.” *Journal of anthropological archaeology* 2(2):99–116. doi: 10.1016/0278-4165(83)90009-0.
- Xia, Dong-Po, Xi Wang, Paul A. Garber, Bing-Hua Sun, Lori K. Sheeran, Lixing Sun, and Jin-Hua Li. 2021. “Effects of Hierarchical Steepness on Grooming Patterns in Female Tibetan Macaques (*Macaca Thibetana*).” *Frontiers in Ecology and Evolution* 9. doi: 10.3389/fevo.2021.631417.
- Xie, Yihui. 2015. *Dynamic Documents with R and Knitr*. 2nd ed. Boca Raton, Florida: Chapman; Hall/CRC.
- Yoffee, Norman. 1993. “Too Many Chiefs? (Or, Safe Texts for the '90s).” Pp. 60–78 in, edited by N. Yoffee and A. Sherratt. Cambridge University Press.
- Yoffee, Norman. 2005. *Myths of the Archaic State : Evolution of the Earliest Cities, States, and Civilizations*. Cambridge: Cambridge University Press.
- Zhou, W.-X., D. Sornette, R. A. Hill, and R. I. M. Dunbar. 2005. “Discrete Hierarchical Organization of Social Group Sizes.” *Proceedings of the Royal Society B: Biological Sciences* 272(1561):439–44. doi: 10.1098/rspb.2004.2970.



# **Appendix A**

**This is my first appendix**

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## **Appendix B**

**This is my second one**

Bla bla bla