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Dynamic Scheduling

Instruction-Level Parallelism (2)

Lecture 5
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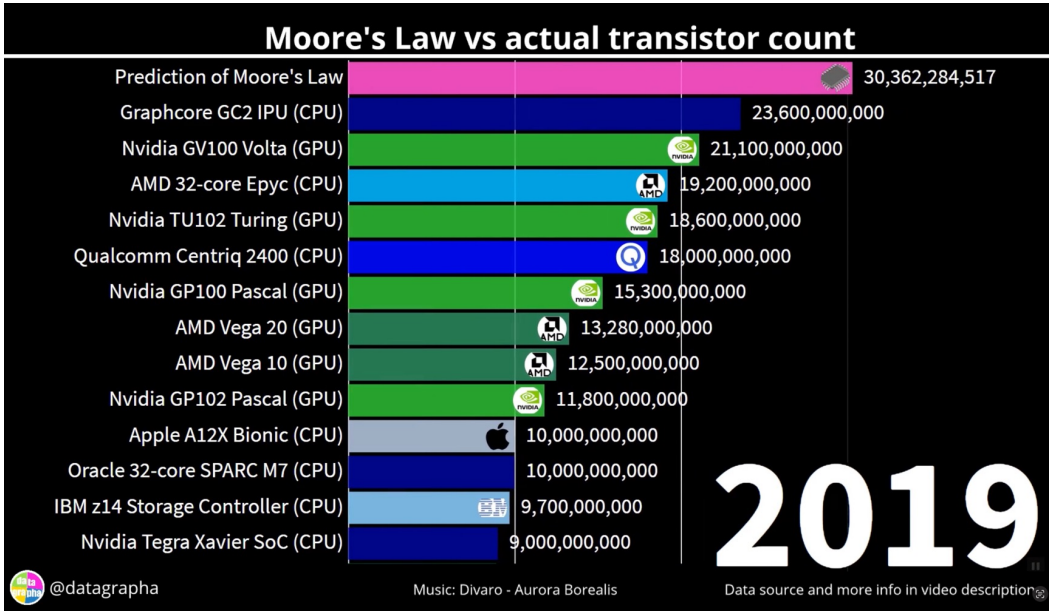


[Animation: Visualizing Moore's Law in Action (1971-2019)]
https://www.visualcapitalist.com/visualizing-moores-law-in-action-1971-2019/

This video clip compares the predictions of Moore's Law with data from actual computer chip innovations occurring between 1971 (Intel 4004) to 2019. The most recent NVIDIA H100 (Hopper) GPU reportedly has 80 billion transistors in TSMC 4N process (2022).

Dynamic Scheduling

- **Rearrange order of instructions to reduce stalls while maintaining data flow**

- **Advantages:**
  - Compiler doesn't need to have knowledge of microarchitecture
  - Handles cases where dependencies are unknown at compile time

- **Disadvantages:**
  - Substantial increase in hardware complexity
  - Complicates exceptions

Dynamic Scheduling

- **Dynamic scheduling implies:**
  - Out-of-order execution
  - Out-of-order completion
- **Creates the possibility for WAR and WAW hazards**
  - WAR Example:

```
fdiv.d   F0,F2,F4   // assume takes long time
fadd.d   F10,F0,F8  // RAW hazard on F0
fsub.d   F8,F8,F14  // WAR hazard on F8
```

- **Two dynamic scheduling algorithms we cover: Scoreboard and Tomasulo Algorithm**
  - Both track when operands are available
  - Tomasulo further introduces register renaming in hardware
    - Minimizes WAW and WAR hazards

Outline

Textbook: Appendix C.7 (Scoreboard),
Chapter 3.4-3.5 (Tomasulo Algorithm)

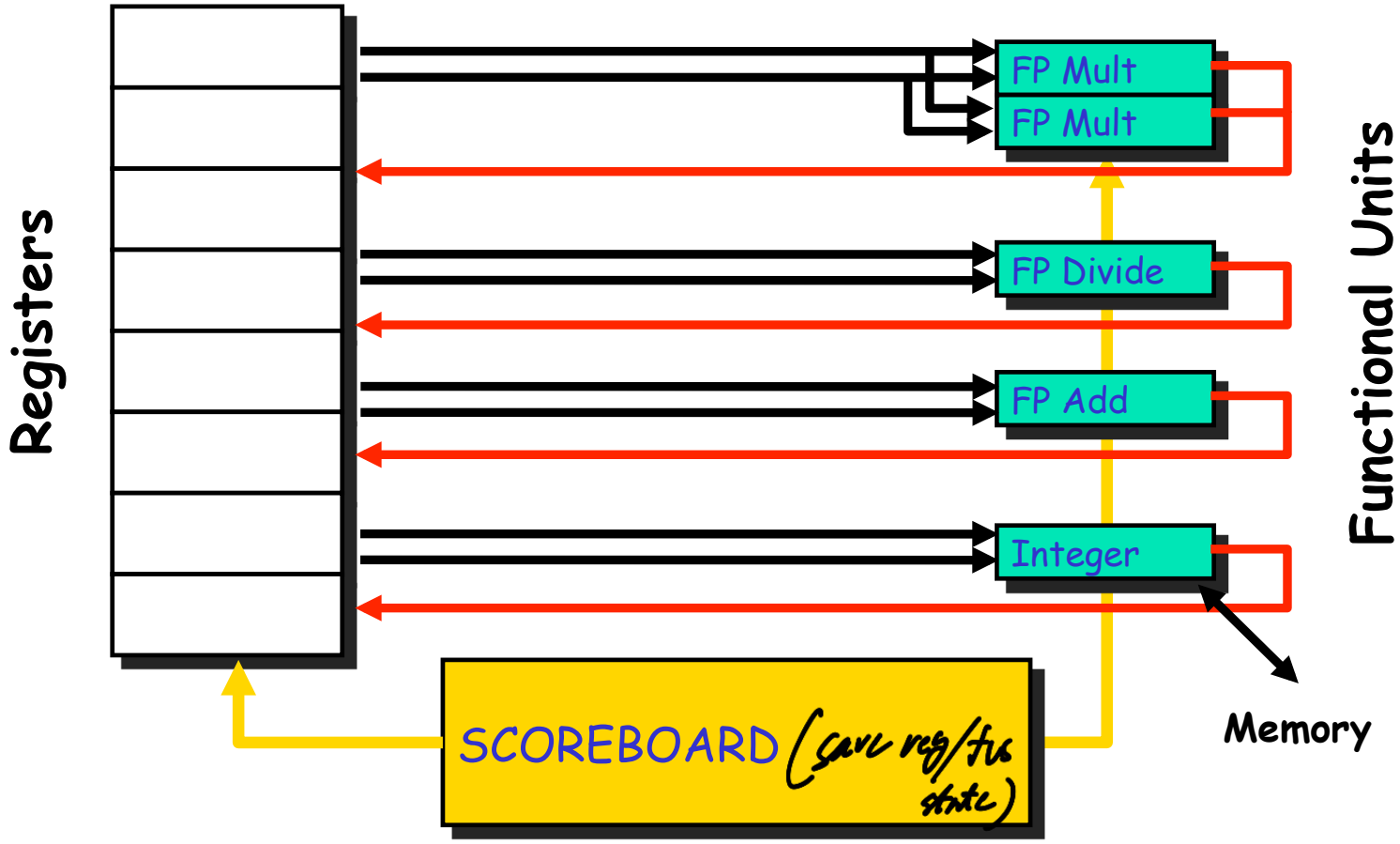
- **Scoreboard for Dynamic Scheduling**
- **Scoreboard Example**
- **Tomasulo Algorithm: Another Dynamic Algorithm**
- **Tomasulo Example One: A Straight-Line Code**
- **Tomasulo Example Two: A Loop**

Scoreboard for Dynamic Scheduling

- **Scoreboard: a bookkeeping technique**
  - Out-of-order execution divides ID stage:
    1. Issue—decode instructions, check for structural hazards
    2. Read operands—wait until no data hazards, then read operands
  - Scoreboards date to CDC6600 in 1963
  - Instructions execute whenever not dependent on previous instructions and no hazards.
  - CDC 6600: In-order issue, out-of-order execution, out-of-order commit (or completion)
    - No forwarding!
    - Imprecise interrupt/exception model for now

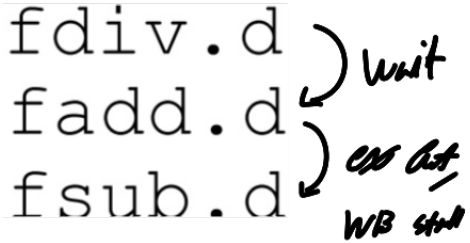
Scoreboard for Dynamic Scheduling

- Scoreboard architecture (CDC 6600)



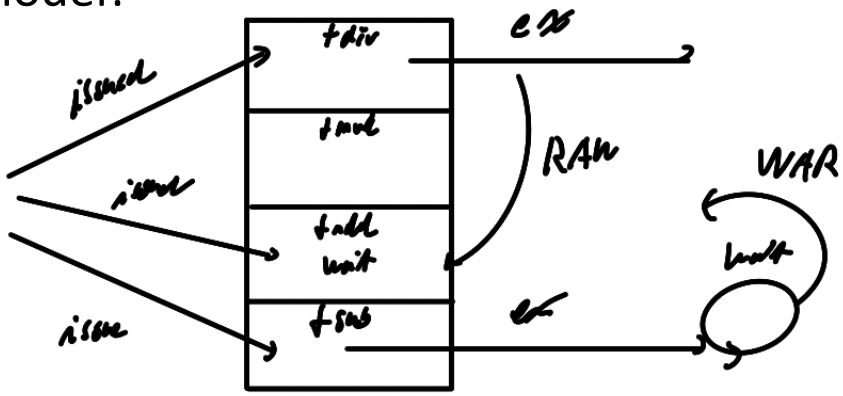
Scoreboard for Dynamic Scheduling

- **Scoreboard implications**
  - Out-of-order completion => WAR, WAW hazards?
  - Solutions for WAR:
    - Stall writeback until registers have been read
    - Read registers only during Read Operands stage
  - Solution for WAW:
    - Detect hazard and stall issue of new instr until other preceding instr completes
  - Need to have multiple instructions in execution phase => multiple execution units or pipelined execution units
  - Scoreboard keeps track of dependencies between instructions that have already issued
  - Scoreboard replaces ID, EX, WB (in 5-stage MIPS) with 4 stages



Scoreboard for Dynamic Scheduling

- **Four stages of scoreboard control (1)**
  - Issue—decode instructions & check for structural hazards (ID1)
    - Instructions issued in program order (for hazard checking)
    - Don't issue if structural hazard
    - Don't issue if instruction is output dependent on any previously issued but uncompleted instruction (no WAW hazards)
  - Read operands—wait until no data hazards, then read operands (ID2)
    - All real dependencies (RAW hazards) resolved in this stage, since we wait for instructions to write back data.
    - No forwarding of data in this model!



Scoreboard for Dynamic Scheduling

- **Four stages of scoreboard control (2)**
  - Execution—operate on operands (EX)
    - The functional unit begins execution upon receiving operands. When the result is ready, it notifies the scoreboard that it has completed execution.
  - Write result—finish execution (WB)
    - Stall until no WAR hazards with previous instructions:

Example:

```
fdiv.d   F0,F2,F4
fadd.d   F10,F0,F8
fsub.d   F8,F8,F14
```

RAW (stall in ID2)

WAR (stall WB)

CDC 6600 scoreboard would stall SUBD until ADDD reads operands

Scoreboard for Dynamic Scheduling

- **Three components of the scoreboard**
  - Instruction status: Which of 4 steps the instruction is in
  - Functional unit status:—Indicates the state of the functional unit (FU). 9 fields for each functional unit
    - Busy: Indicates whether the unit is busy or not (run or not)
    - Op: Operation to perform in the unit (e.g., + or –)
    - Fi: Destination register
    - Fj,Fk: Source-register numbers
    - Qj,Qk: Functional units producing source registers Fj, Fk (RAW)
    - Rj,Rk: Flags indicating when Fj, Fk are ready AND not read
  - Register result status—Indicates which functional unit will write (WAW, WAR) each register, if one exists. Blank when no pending instructions will write that register

Scoreboard Example (MIPS)

MIPS to RISC-V conversion

LD → fld
MULTD → fmul.d
SUBD → fsub.d
DIVD → fdiv.d
ADDD → fadd.d

R2, R3 → x2, x3

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2				
LD	F2	45+	R3				
MULTD	F0	F2	F4				
SUBD	F8	F6	F2				
DIVD	F10	F0	F6				
ADDD	F6	F8	F2				

RAW dep

Functional unit status:

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	No								
	Mult1	No								
	Mult2	No								
	Add	No								
	Divide	No								

Register result status:

Clock	F0	F2	F4	F6	F8	F10	F12	...	F30
FU									

Scoreboard Example

- **Detailed scoreboard pipeline control**

Instruction status	Wait until	Bookkeeping
Issue	Not busy (FU) and not result(D)	Busy(FU) ← yes; Op(FU) ← op; Fi(FU) ← `D'; Fj(FU) ← `S1'; Fk(FU)←`S2'; Qj←Result('S1'); Qk←Result(`S2'); Rj←not Qj; Rk←not Qk; Result('D')←FU;
Read operands	Rj and Rk	Rj ← No; Rk ← No
Execution complete	Functional unit done	
Write result	∀f((Fj(f)≠Fi(FU) or Rj(f)=No) & (Fk(f)≠Fi(FU) or Rk(f)=No))	∀f(if Qj(f)=FU then Rj(f) ← Yes); ∀f(if Qk(f)=FU then Rj(f) ← Yes); Result(Fi(FU)) ← 0; Busy(FU) ← No

Scoreboard Example: Cycle 1

Instruction status:

Cycle #

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1			
LD	F2	45+	R3				
MULTD	F0	F2	F4				
SUBD	F8	F6	F2				
DIVD	F10	F0	F6				
ADDD	F6	F8	F2				

Functional unit status:

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	Yes	Load	F6		R2				Yes
	Mult1	No								
	Mult2	No								
	Add	No								
	Divide	No								

available

indicate dest

Register result status:

Clock 1

	F0	F2	F4	F6	F8	F10	F12	...	F30
FU				Integer					

ALU

Scoreboard Example: Cycle 2

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1	2		
LD	F2	45+	R3				
MULTD	F0	F2	F4				
SUBD	F8	F6	F2				
DIVD	F10	F0	F6				
ADDD	F6	F8	F2				

Stall because Integer is filled now (Structural hazard)
But, if more ALU exist, then we can issue(not -clap)

- **Issue 2nd LD?**

Functional unit status:

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	Yes	Load	F6		R2				Yes
	Mult1	No								
	Mult2	No								
	Add	No								
	Divide	No								

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
2	FU				Integer					

Scoreboard Example: Cycle 3

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1	2	3	
LD	F2	45+	R3				
MULTD	F0	F2	F4				
SUBD	F8	F6	F2				
DIVD	F10	F0	F0				
ADDD	F6	F8	F2				

- **Issue MULTD?**
  no, In-order issue

pass read, then get no to check WAR

Functional unit status:

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	Yes	Load	F6		R2				No
	Mult1	No								
	Mult2	No								
	Add	No								
	Divide	No								

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
3	FU	Integer								

Scoreboard Example: Cycle 4

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1	2	3	4
LD	F2	45+	R3				
MULTD	F0	F2	F4				
SUBD	F8	F6	F2				
DIVD	F10	F0	F6				
ADDD	F6	F8	F2				

Functional unit status:

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	No								
	Mult1	No								
	Mult2	No								
	Add	No								
	Divide	No								

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
4	FU				Integer					

Scoreboard Example: Cycle 5

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1	2	3	4
LD	F2	45+	R3	5			
MULTD	F0	F2	F4				
SUBD	F8	F6	F2				
DIVD	F10	F0	F6				
ADDD	F6	F8	F2				

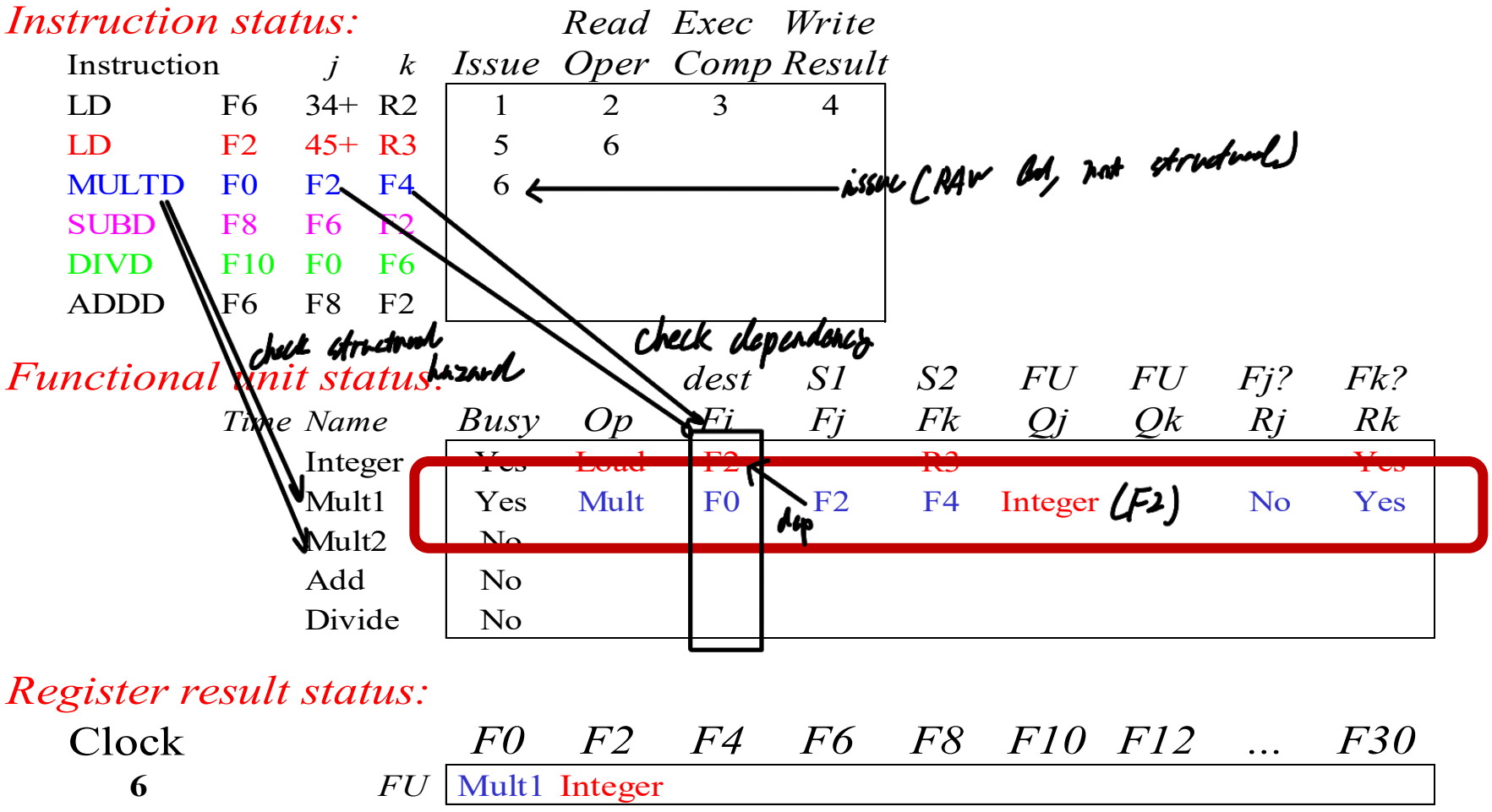
Functional unit status:

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	Yes	Load	F2		R3				Yes
	Mult1	No								
	Mult2	No								
	Add	No								
	Divide	No								

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
5	FU		Integer							

Scoreboard Example: Cycle 6



Scoreboard Example: Cycle 7

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1	2	3	4
LD	F2	45+	R3	5	6	7	
MULTD	F0	F2	F4	6	(Stall)		
SUBD	F8	F6	F2	7	issue		
DIVD	F10	F0	F6				
ADDD	F6	F8	F2				

- **Read multiply operands?**

Functional unit status:

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	Yes	Load	F2		R3				No
	Mult1	Yes	Mult	F0	F2	F4	Integer		No	Yes
	Mult2	No								
	Add	Yes	Sub	F8	F6	F2		Integer	Yes	No
	Divide	No								

dep

(Fj)

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
7	FU	Mult1	Integer			Add				

Scoreboard Example: Cycle 8a (1st Half Cycle)

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1	2	3	4
LD	F2	45+	R3	5	6	7	
MULTD	F0	F2	F4	6			
SUBD	F8	F6	F2	7			
DIVD	F10	F0	F6	8			
ADDD	F6	F8	F2				

Functional unit status:

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	Yes	Load	F2		R3				No
	Mult1	Yes	Mult	F0	F2	F4	Integer		No	Yes
	Mult2	No								
	Add	Yes	Sub	F8	F6	F2		Integer	Yes	No
	Divide	Yes	Div	F10	F0	F6	Mult1		No	Yes

dep

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
8	FU	Mult1	Integer			Add	Divide			

Scoreboard Example: Cycle 8b (2nd Half Cycle)

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1	2	3	4
LD	F2	45+	R3	5	6	7	8
MULTD	F0	F2	F4	6			
SUBD	F8	F6	F2	7			
DIVD	F10	F0	F6	8			
ADDD	F6	F8	F2				

Functional unit status:

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	No								
	Mult1	Yes	Mult	F0	F2	F4			Yes	Yes
	Mult2	No								
	Add	Yes	Sub	F8	F6	F2			Yes	Yes
	Divide	Yes	Div	F10	F0	F6	Mult1		No	Yes

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
8	FU	Mult1				Add	Divide			

Scoreboard Example: Cycle 9

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1	2	3	4
LD	F2	45+	R3	5	6	7	8
MULTD	F0	F2	F4	6	9		
SUBD	F8	F6	F2	7	9		
DIVD	F10	F0	F6	8			
ADDD	F6	F8	F2				

structural hazard

- **Read operands for MULT & SUB?**
- **Issue ADDD?**

Functional unit status:

Note: Remaining

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	No							executable!	
10	Mult1	Yes	Mult	F0	F2	F4			Yes	Yes
	Mult2	No								
2	Add	Yes	Sub	F8	F6	F2			Yes	Yes
	Divide	Yes	Div	F10	F0	F6	Mult1		No	Yes

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
9	FU	Mult1				Add	Divide			

Scoreboard Example: Cycle 10

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1	2	3	4
LD	F2	45+	R3	5	6	7	8
MULTD	F0	F2	F4	6	9		
SUBD	F8	F6	F2	7	9		
DIVD	F10	F0	F6	8			
ADDD	F6	F8	F2				

Functional unit status:

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	No								
9	Mult1	Yes	Mult	F0	F2	F4			No	No
	Mult2	No								
1	Add	Yes	Sub	F8	F6	F2			No	No
	Divide	Yes	Div	F10	F0	F6	Mult1		No	Yes

finish read.

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
10	FU	Mult1				Add	Divide			

Scoreboard Example: Cycle 11

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1	2	3	4
LD	F2	45+	R3	5	6	7	8
MULTD	F0	F2	F4	6	9		
SUBD	F8	F6	F2	7	9	11	
DIVD	F10	F0	F6	8			
ADDD	F6	F8	F2				

Functional unit status:

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	No								
8	Mult1	Yes	Mult	F0	F2	F4			No	No
	Mult2	No								
done 0	Add	Yes	Sub	F8	F6	F2			No	No
	Divide	Yes	Div	F10	F0	F6	Mult1		No	Yes

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
11	FU	Mult1				Add	Divide			

Scoreboard Example: Cycle 12

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1	2	3	4
LD	F2	45+	R3	5	6	7	8
MULTD	F0	F2	F4	6	9		
SUBD	F8	F6	F2	7	9	11	12
DIVD	F10	F0	F6	8			
ADDD	F6	F8	F2				

- **Read operands for DIVD?**

Functional unit status:

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	No								
7	Mult1	Yes	Mult	F0	F2	F4			No	No
	Mult2	No								
	Add	No								
	Divide	Yes	Div	F10	F0	F6	Mult1		No	Yes

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
12	FU	Mult1					Divide			

Scoreboard Example: Cycle 13

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1	2	3	4
LD	F2	45+	R3	5	6	7	8
MULTD	F0	F2	F4	6	9		
SUBD	F8	F6	F2	7	9	11	12
DIVD	F10	F0	F6	8			
ADDD	F6	F8	F2	13			

Functional unit status:

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	No								
6	Mult1	Yes	Mult	F0	F2	F4			No	No
	Mult2	No								
	Add	Yes	Add	F6	F8	F2			Yes	Yes
	Divide	Yes	Div	F10	F0	F6	Mult1		No	Yes

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
13	FU	Mult1			Add		Divide			

Scoreboard Example: Cycle 14

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1	2	3	4
LD	F2	45+	R3	5	6	7	8
MULTD	F0	F2	F4	6	9		
SUBD	F8	F6	F2	7	9	11	12
DIVD	F10	F0	F6	8			
ADDD	F6	F8	F2	13	14		

Functional unit status:

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	No								
5	Mult1	Yes	Mult	F0	F2	F4			No	No
	Mult2	No								
2	Add	Yes	Add	F6	F8	F2			Yes	Yes
	Divide	Yes	Div	F10	F0	F6	Mult1		No	Yes

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
14	*FU*	Mult1			Add		Divide			

Scoreboard Example: Cycle 15

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1	2	3	4
LD	F2	45+	R3	5	6	7	8
MULTD	F0	F2	F4	6	9		
SUBD	F8	F6	F2	7	9	11	12
DIVD	F10	F0	F6	8			
ADDD	F6	F8	F2	13	14		

Functional unit status:

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	No								
4	Mult1	Yes	Mult	F0	F2	F4			No	No
	Mult2	No								
1	Add	Yes	Add	F6	F8	F2			No	No
	Divide	Yes	Div	F10	F0	F6	Mult1		No	Yes

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
15	FU	Mult1			Add		Divide			

Scoreboard Example: Cycle 16

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1	2	3	4
LD	F2	45+	R3	5	6	7	8
MULTD	F0	F2	F4	6	9		
SUBD	F8	F6	F2	7	9	11	12
DIVD	F10	F0	F6	8			
ADDD	F6	F8	F2	13	14	16	

Functional unit status:

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	No								
3	Mult1	Yes	Mult	F0	F2	F4			No	No
	Mult2	No								
0	Add	Yes	Add	F6	F8	F2			No	No
	Divide	Yes	Div	F10	F0	F6	Mult1		No	Yes

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
16	FU	Mult1			Add		Divide			

Scoreboard Example: Cycle 17

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1	2	3	4
LD	F2	45+	R3	5	6	7	8
MULTD	F0	F2	F4	6	9		
SUBD	F8	F6	F2	7	9	11	12
DIVD	F10	F0	F6	8			
ADDD	F6	F8	F2	13	14	16	

- **Why not write result of ADD???**

WAR Hazard!

Functional unit status:

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	No								
	Mult1	Yes	Mult	F0	F2	F4			No	No
	Mult2	No								
	Add	Yes	Add	F6	F8	F2			No	No
	Divide	Yes	Div	F10	F0	F6	Mult1		No	Yes

check!

$(F_i == F_k)$ && R_k = WAR hazard

Register result status:

Clock	F0	F2	F4	F6	F8	F10	F12	...	F30
17	Mult1			Add		Divide			

Scoreboard Example: Cycle 18

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1	2	3	4
LD	F2	45+	R3	5	6	7	8
MULTD	F0	F2	F4	6	9		
SUBD	F8	F6	F2	7	9	11	12
DIVD	F10	F0	F6	8			
ADDD	F6	F8	F2	13	14	16	

Functional unit status:

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	No								
1	Mult1	Yes	Mult	F0	F2	F4			No	No
	Mult2	No								
	Add	Yes	Add	F6	F8	F2			No	No
	Divide	Yes	Div	F10	F0	F6	Mult1		No	Yes

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
18	FU	Mult1			Add		Divide			

Scoreboard Example: Cycle 19

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1	2	3	4
LD	F2	45+	R3	5	6	7	8
MULTD	F0	F2	F4	6	9	19	
SUBD	F8	F6	F2	7	9	11	12
DIVD	F10	F0	F6	8			
ADDD	F6	F8	F2	13	14	16	

Functional unit status:

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	No								
0	Mult1	Yes	Mult	F0	F2	F4			No	No
	Mult2	No								
	Add	Yes	Add	F6	F8	F2			No	No
	Divide	Yes	Div	F10	F0	F6	Mult1		No	Yes

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
19	FU	Mult1			Add		Divide			

Scoreboard Example: Cycle 20

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1	2	3	4
LD	F2	45+	R3	5	6	7	8
MULTD	F0	F2	F4	6	9	19	20
SUBD	F8	F6	F2	7	9	11	12
DIVD	F10	F0	F6	8			
ADDD	F6	F8	F2	13	14	16	

Functional unit status:

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	No								
	Mult1	No								
	Mult2	No								
	Add	Yes	Add	F6	F8	F2			No	No
	Divide	Yes	Div	F10	F0	F6			Yes	Yes

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
20	*FU*				Add		Divide			

Scoreboard Example: Cycle 21

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1	2	3	4
LD	F2	45+	R3	5	6	7	8
MULTD	F0	F2	F4	6	9	19	20
SUBD	F8	F6	F2	7	9	11	12
DIVD	F10	F0	F6	8	21		
ADDD	F6	F8	F2	13	14	16	

- **WAR Hazard is now gone...**

Functional unit status:

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	No								
	Mult1	No								
	Mult2	No								
	Add	Yes	Add	F6	F8	F2			No	No
	Divide	Yes	Div	F10	F0	F6			Yes	Yes

WB ckb!

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
21	FU				Add		Divide			

Scoreboard Example: Cycle 22

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1	2	3	4
LD	F2	45+	R3	5	6	7	8
MULTD	F0	F2	F4	6	9	19	20
SUBD	F8	F6	F2	7	9	11	12
DIVD	F10	F0	F6	8	21		
ADDD	F6	F8	F2	13	14	16	22

Functional unit status:

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	No								
	Mult1	No								
	Mult2	No								
	Add	No								
39	Divide	Yes	Div	F10	F0	F6			No	No

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
22	*FU*						Divide			

Scoreboard Example (Cont)

Faster than light computation (skip a couple of cycles)…

Scoreboard Example: Cycle 61

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1	2	3	4
LD	F2	45+	R3	5	6	7	8
MULTD	F0	F2	F4	6	9	19	20
SUBD	F8	F6	F2	7	9	11	12
DIVD	F10	F0	F6	8	21	61	
ADDD	F6	F8	F2	13	14	16	22

Functional unit status:

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	No								
	Mult1	No								
	Mult2	No								
	Add	No								
0	Divide	Yes	Div	F10	F0	F6			No	No

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
61	*FU*						Divide			

Scoreboard Example: Cycle 62

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1	2	3	4
LD	F2	45+	R3	5	6	7	8
MULTD	F0	F2	F4	6	9	19	20
SUBD	F8	F6	F2	7	9	11	12
DIVD	F10	F0	F6	8	21	61	62
ADDD	F6	F8	F2	13	14	16	22

Functional unit status:

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	No								
	Mult1	No								
	Mult2	No								
	Add	No								
	Divide	No								

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
62	*FU*									

Review: Scoreboard Example: Cycle 62

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1	2	3	4
LD	F2	45+	R3	5	6	7	8
MULTD	F0	F2	F4	6	9	19	20
SUBD	F8	F6	F2	7	9	11	12
DIVD	F10	F0	F6	8	21	61	62
ADDD	F6	F8	F2	13	14	16	22

- **In-order issue; Out-of-order execute & commit**

Functional unit status:

Time	Name	Busy	Op	dest Fi	S1 Fj	S2 Fk	FU Qj	FU Qk	Fj? Rj	Fk? Rk
	Integer	No								
	Mult1	No								
	Mult2	No								
	Add	No								
	Divide	No								

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
62	FU									

Scoreboard Example

- **CDC 6600 Scoreboard**
  - Speedup 1.7 from compiler; 2.5 by hand
    - BUT slow memory (no cache) limits benefit
  - Limitations of 6600 scoreboard:
    - No forwarding hardware
    - Limited to instructions in basic block (small *window*)
    - Small number of functional units (structural hazards), especially integer/load store units
    - Do not issue on structural hazards
    - Wait for WAR hazards
    - Prevent WAW hazards

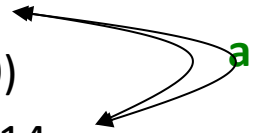
Tomasulo Algorithm: Another Dynamic Algorithm

- **For IBM 360/91 about 3 years after CDC 6600 (1966)**
- **Goal: High Performance without special compilers**
- **Differences between IBM 360 & CDC 6600 ISA**
  - IBM has only 2 register specifiers/instr vs. 3 in CDC 6600
  - IBM has 4 FP registers vs. 8 in CDC 6600
  - IBM has memory-register ops
- **Why Study? lead to Alpha 21264, HP 8000, MIPS 10000, Pentium II, PowerPC 604, …**

Tomasulo Algorithm

- **Register renaming to overcome WAR/WAW hazards (1)**
  - Example:

```
fdiv.d  F0,F2,F4
fadd.d F6,F0,F8
fsd      F6,0(x10)
fsub.d F8,F10,F14
fmul.d F6,F10,F8
```



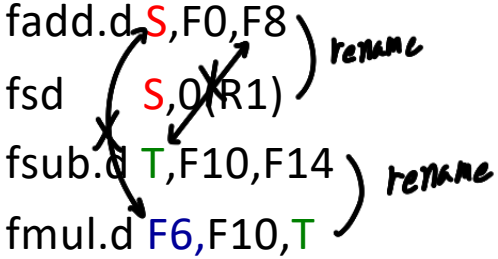
anti-dependence (WAR)

anti- (output) dependence (WAW)

+ name dependences with F6 and F8

Tomasulo Algorithm

- **Register renaming to overcome WAR/WAW hazards (2)**
  - Example:



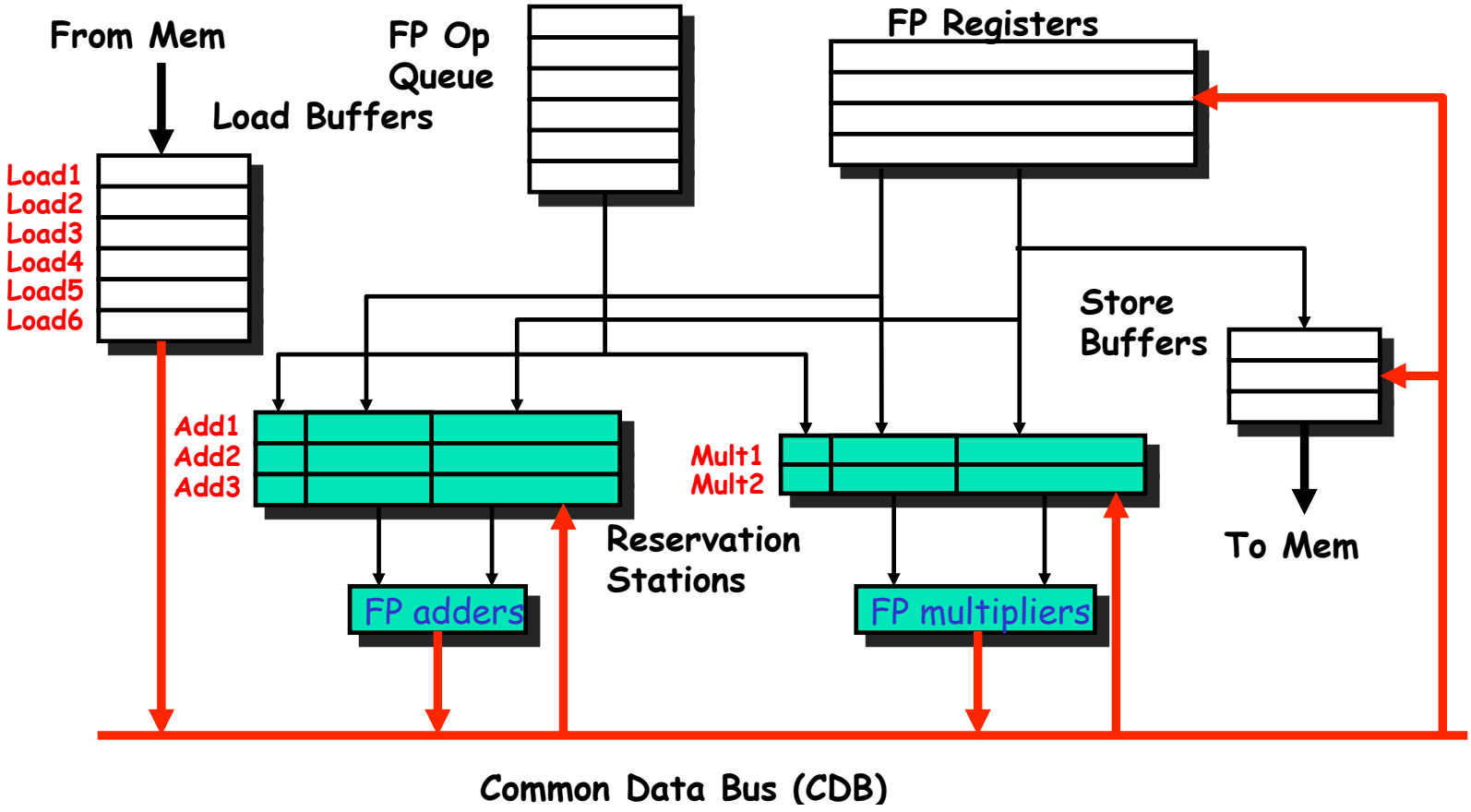
  - Now only RAW hazards remain, which can be strictly ordered

Tomasulo Algorithm

- **Register renaming is provided by reservation stations (RS) in Tomasulo Algorithm**
  - Contains:
    - The instruction
    - Buffered operand values (when available)
    - Reservation station number of instruction providing the operand values
  - RS fetches and buffers an operand as soon as it becomes available (not necessarily involving register file)
  - Pending instructions designate the RS to which they will send their output
    - Result values broadcast on a result bus, called the common data bus (CDB)
  - Only the last output updates the register file
  - As instructions are issued, the register specifiers are renamed with the reservation station
  - May be more reservation stations than registers

Tomasulo Algorithm

- Tomasulo organization



Tomasulo Algorithm

- **Tomasulo Algorithm vs. Scoreboard**
  - Control & buffers distributed with Function Units (FU) vs. centralized in scoreboard;
    - FU buffers called "reservation stations"; have pending operands
  - Registers in instructions replaced by values or pointers to reservation stations (RS); called register renaming ;
    - avoids WAR, WAW hazards
    - More reservation stations than registers, so can do optimizations compilers can't
  - Results to FU from RS, not through registers, over Common Data Bus (CDB) that broadcasts results to all FUs
  - Load and Stores treated as FUs with RSs as well
  - Integer instructions can go past branches, allowing FP ops beyond basic block in FP queue

Tomasulo Algorithm

- **Reservation station (RS) components**

  Op: Operation to perform in the unit (e.g., + or –)

  Vj, Vk: Value of Source operands

  - Store buffers has V field, result to be stored

  Qj, Qk: Reservation stations producing source registers (value to be written)

  - Note: No ready flags as in Scoreboard; Qj,Qk=0 => ready
  - Store buffers only have Qi for RS producing result

  Busy: Indicates reservation station or FU is busy

  Register result status—Indicates which functional unit will write each register, if one exists. Blank when no pending instructions that will write that register.

Tomasulo Algorithm

- **Three stages of Tomasulo Algorithm**
  1. Issue—get instruction from FP Op Queue

     If reservation station free (no structural hazard),
     control issues instr & sends operands (renames registers).
  2. Execution—operate on operands (EX)

     When both operands ready then execute;
     if not ready, watch Common Data Bus for result
  3. Write result—finish execution (WB)

     Write on Common Data Bus to all awaiting units;
     mark reservation station available
  - Normal data bus: data + destination ("go to" bus)
  - Common data bus: data + source ("come from" bus)
    - 64 bits of data + 4 bits of Functional Unit source address
    - Write if matches expected Functional Unit (produces result)
    - Does the broadcast

Tomasulo Example One: A Straight-Line Code

Instruction status:

Instruction		*j*	*k*	*Issue*	*Exec Comp*	*Write Result*
LD	F6	34+	R2			
LD	F2	45+	R3			
MULTD	F0	F2	F4			
SUBD	F8	F6	F2			
DIVD	F10	F0	F6			
ADDD	F6	F8	F2			

	Busy	Address
Load1	No	
Load2	No	
Load3	No	

Reservation Stations:

Time	*Name*	*Busy*	*Op*	*S1 Vj*	*S2 Vk*	*RS Qj*	*RS Qk*
	Add1	No					
	Add2	No					
	Add3	No					
	Mult1	No					
	Mult2	No					

Register result status:

Clock		*F0*	*F2*	*F4*	*F6*	*F8*	*F10*	*F12*	...	*F30*
0	*FU*									

Tomasulo Example One: Cycle 1

Instruction status:

Instruction		j	k	Issue	Exec Comp	Write Result
LD	F6	34+	R2	1		
LD	F2	45+	R3			
MULTD	F0	F2	F4			
SUBD	F8	F6	F2			
DIVD	F10	F0	F6			
ADDD	F6	F8	F2			

	Busy	Address
Load1	Yes	34+R2
Load2	No	
Load3	No	

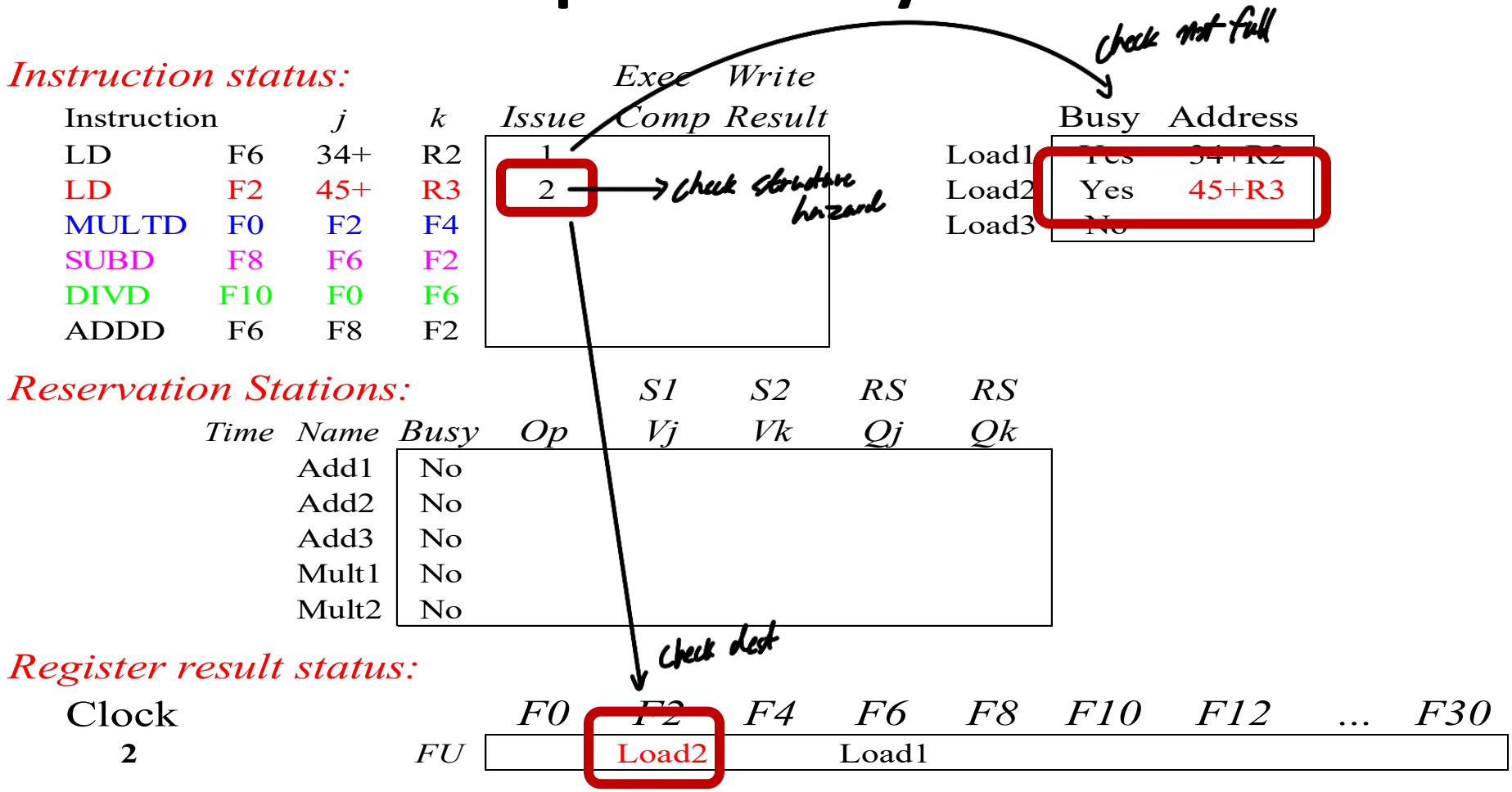
Reservation Stations:

Time	Name	Busy	Op	S1 Vj	S2 Vk	RS Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
	Mult1	No					
	Mult2	No					

Register result status:

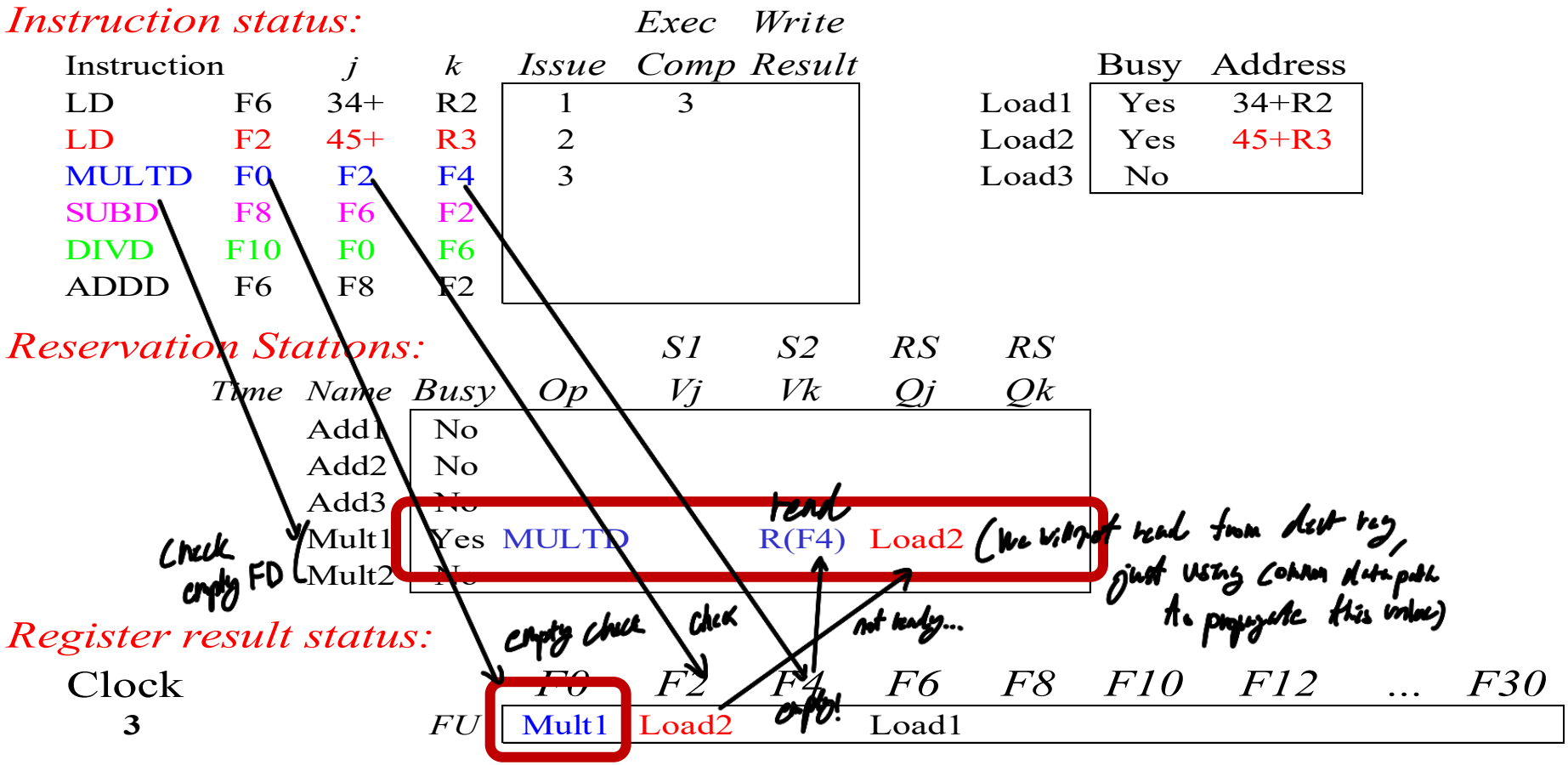
Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
1	FU				Load1					

Tomasulo Example One: Cycle 2



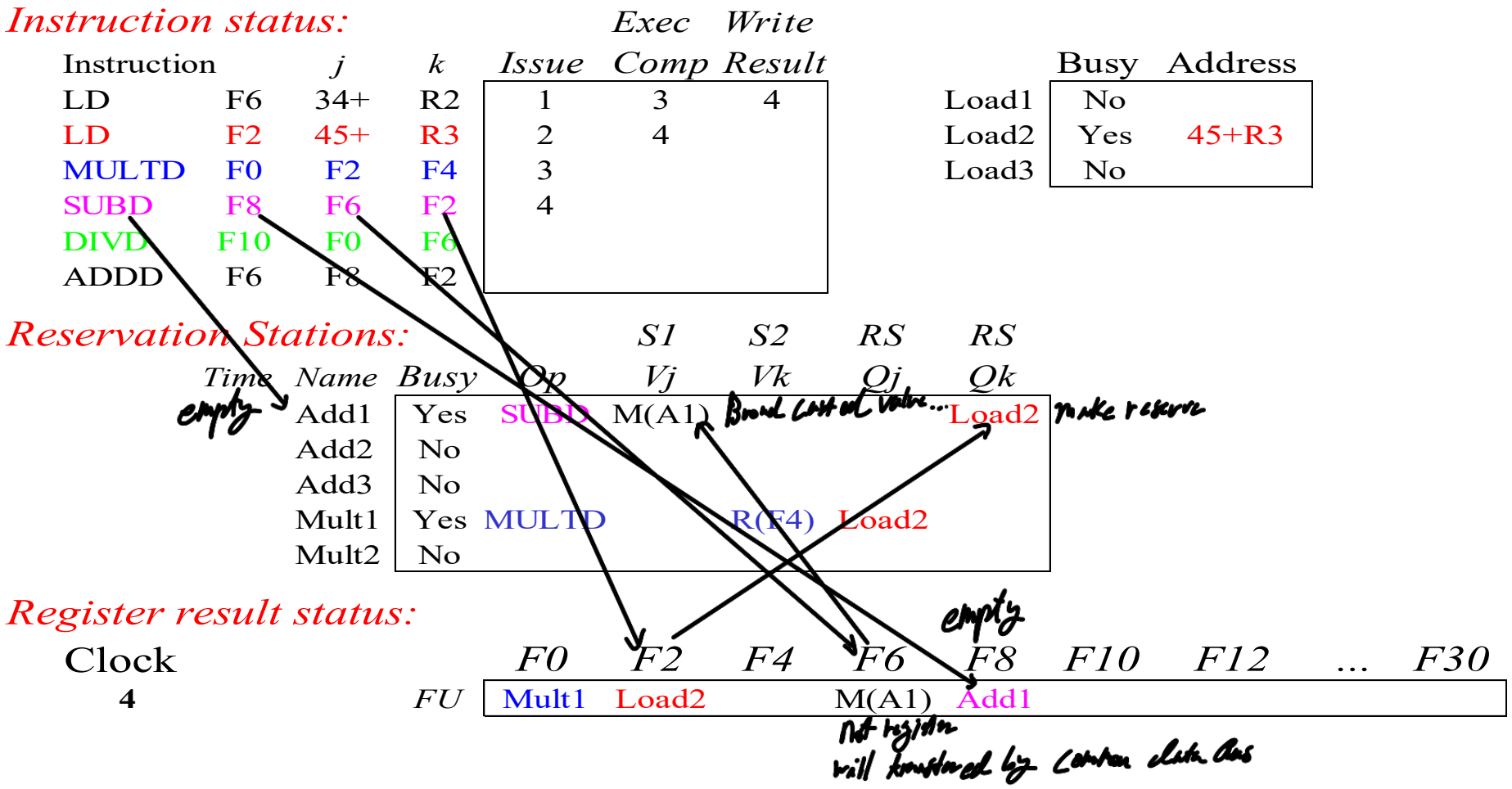
Note: Unlike 6600, can have multiple loads outstanding

Tomasulo Example One: Cycle 3



- **Note: registers names are removed ("renamed") in Reservation Stations; MULT issued vs. scoreboard**
- **Load1 completing; what is waiting for Load1?**

Tomasulo Example One: Cycle 4



- **Load2 completing; what is waiting for Load2?**

Tomasulo Example One: Cycle 5

Instruction status:

Instruction		j	k	Issue	Exec Comp	Write Result
LD	F6	34+	R2	1	3	4
LD	F2	45+	R3	2	4	5
MULTD	F0	F2	F4	3		
SUBD	F8	F6	F2	4		
DIVD	F10	F0	F6	5		
ADDD	F6	F8	F2			

	Busy	Address
Load1	No	
Load2	No	
Load3	No	

Reservation Stations:

Time	Name	Busy	Op	S1 Vj	S2 Vk	RS Qj	RS Qk
2	Add1	Yes	SUBD	M(A1)	M(A2)		
	Add2	No					
	Add3	No					
10	Mult1	Yes	MULTD	M(A2)	R(F4)		
	Mult2	Yes	DIVD		M(A1)	Mult1	

propagated

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
5	FU	Mult1	M(A2)		M(A1)	Add1	Mult2			

Tomasulo Example One: Cycle 6

Instruction status:

Instruction		j	k	Issue	Exec Comp	Write Result
LD	F6	34+	R2	1	3	4
LD	F2	45+	R3	2	4	5
MULTD	F0	F2	F4	3		
SUBD	F8	F6	F2	4		
DIVD	F10	F0	F6	5		
ADDD	F6	F8	F2	6		

	Busy	Address
Load1	No	
Load2	No	
Load3	No	

Reservation Stations:

Time	Name	Busy	Op	S1 Vj	S2 Vk	RS Qj	RS Qk
1	Add1	Yes	SUBD	M(A1)	M(A2)		
	Add2	Yes	ADDD		M(A2)	Add1	
	Add3	No					
9	Mult1	Yes	MULTD	M(A2)	R(F4)		
	Mult2	Yes	DIVD		M(A1)	Mult1	

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
6	FU	Mult1	M(A2)		Add2	Add1	Mult2			

changed!

- **Issue ADDD here vs. scoreboard?**

Tomasulo Example One: Cycle 7

Instruction status:

Instruction		j	k	Issue	Exec Comp	Write Result
LD	F6	34+	R2	1	3	4
LD	F2	45+	R3	2	4	5
MULTD	F0	F2	F4	3		
SUBD	F8	F6	F2	4	7	
DIVD	F10	F0	F6	5		
ADDD	F6	F8	F2	6		

	Busy	Address
Load1	No	
Load2	No	
Load3	No	

Reservation Stations:

Time	Name	Busy	Op	S1 Vj	S2 Vk	RS Qj	RS Qk
0	Add1	Yes	SUBD	M(A1)	M(A2)		
	Add2	Yes	ADDD		M(A2)	Add1	
	Add3	No					
8	Mult1	Yes	MULTD	M(A2)	R(F4)		
	Mult2	Yes	DIVD		M(A1)	Mult1	

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
7	FU	Mult1	M(A2)		Add2	Add1	Mult2			

- **Add1 completing; what is waiting for it?**

Tomasulo Example One: Cycle 8

Instruction status:

Instruction		j	k	Issue	Exec Comp	Write Result
LD	F6	34+	R2	1	3	4
LD	F2	45+	R3	2	4	5
MULTD	F0	F2	F4	3		
SUBD	F8	F6	F2	4	7	8
DIVD	F10	F0	F6	5		
ADDD	F6	F8	F2	6		

	Busy	Address
Load1	No	
Load2	No	
Load3	No	

Reservation Stations:

Time	Name	Busy	Op	S1 Vj	S2 Vk	RS Qj	RS Qk
	Add1	No					
2	Add2	Yes	ADDD	(M-M)	M(A2)		
	Add3	No					
7	Mult1	Yes	MULTD	M(A2)	R(F4)		
	Mult2	Yes	DIVD		M(A1)	Mult1	

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
8	FU	Mult1	M(A2)		Add2	(M-M)	Mult2			

Tomasulo Example One: Cycle 9

Instruction status:

Instruction		j	k	Issue	Exec Comp	Write Result
LD	F6	34+	R2	1	3	4
LD	F2	45+	R3	2	4	5
MULTD	F0	F2	F4	3		
SUBD	F8	F6	F2	4	7	8
DIVD	F10	F0	F6	5		
ADDD	F6	F8	F2	6		

	Busy	Address
Load1	No	
Load2	No	
Load3	No	

Reservation Stations:

Time	Name	Busy	Op	S1 Vj	S2 Vk	RS Qj	RS Qk
	Add1	No					
1	Add2	Yes	ADDD	(M-M)	M(A2)		
	Add3	No					
6	Mult1	Yes	MULTD	M(A2)	R(F4)		
	Mult2	Yes	DIVD		M(A1)	Mult1	

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
9	FU	Mult1	M(A2)		Add2	(M-M)	Mult2			

Tomasulo Example One: Cycle 10

Instruction status:

Instruction		j	k	Issue	Exec Comp	Write Result
LD	F6	34+	R2	1	3	4
LD	F2	45+	R3	2	4	5
MULTD	F0	F2	F4	3		
SUBD	F8	F6	F2	4	7	8
DIVD	F10	F0	F6	5		
ADDD	F6	F8	F2	6	10	

	Busy	Address
Load1	No	
Load2	No	
Load3	No	

Reservation Stations:

Time	Name	Busy	Op	S1 Vj	S2 Vk	RS Qj	RS Qk
	Add1	No					
0	Add2	Yes	ADDD	(M-M)	M(A2)		
	Add3	No					
5	Mult1	Yes	MULTD	M(A2)	R(F4)		
	Mult2	Yes	DIVD		M(A1)	Mult1	

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
10	FU	Mult1	M(A2)		Add2	(M-M)	Mult2			

- **Add2 completing; what is waiting for it?**

Tomasulo Example One: Cycle 11

Instruction status:

Instruction		j	k	Issue	Exec Comp	Write Result
LD	F6	34+	R2	1	3	4
LD	F2	45+	R3	2	4	5
MULTD	F0	F2	F4	3		
SUBD	F8	F6	F2	4	7	8
DIVD	F10	F0	F6	5		
ADDD	F6	F8	F2	6	10	11

	Busy	Address
Load1	No	
Load2	No	
Load3	No	

Reservation Stations:

Time	Name	Busy	Op	S1 Vj	S2 Vk	RS Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
4	Mult1	Yes	MULTD	M(A2)	R(F4)		
	Mult2	Yes	DIVD		M(A1)	Mult1	

already read!

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
11	FU	Mult1	M(A2)		(M-M+M	(M-M)	Mult2			

- **Write result of ADDD here vs. scoreboard?**
- **All quick instructions complete in this cycle!**

Tomasulo Example One: Cycle 12

Instruction status:

Instruction		j	k	Issue	Exec Comp	Write Result
LD	F6	34+	R2	1	3	4
LD	F2	45+	R3	2	4	5
MULTD	F0	F2	F4	3		
SUBD	F8	F6	F2	4	7	8
DIVD	F10	F0	F6	5		
ADDD	F6	F8	F2	6	10	11

	Busy	Address
Load1	No	
Load2	No	
Load3	No	

Reservation Stations:

Time	Name	Busy	Op	S1 Vj	S2 Vk	RS Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
3	Mult1	Yes	MULTD	M(A2)	R(F4)		
	Mult2	Yes	DIVD		M(A1)	Mult1	

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
12	FU	Mult1	M(A2)		(M-M+M	(M-M)	Mult2			

Tomasulo Example One: Cycle 13

Instruction status:

Instruction		j	k	Issue	Exec Comp	Write Result
LD	F6	34+	R2	1	3	4
LD	F2	45+	R3	2	4	5
MULTD	F0	F2	F4	3		
SUBD	F8	F6	F2	4	7	8
DIVD	F10	F0	F6	5		
ADDD	F6	F8	F2	6	10	11

	Busy	Address
Load1	No	
Load2	No	
Load3	No	

Reservation Stations:

Time	Name	Busy	Op	S1 Vj	S2 Vk	RS Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
2	Mult1	Yes	MULTD	M(A2)	R(F4)		
	Mult2	Yes	DIVD		M(A1)	Mult1	

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
13	FU	Mult1	M(A2)		(M-M+M	(M-M)	Mult2			

Tomasulo Example One: Cycle 14

Instruction status:

Instruction		j	k	Issue	Exec Comp	Write Result
LD	F6	34+	R2	1	3	4
LD	F2	45+	R3	2	4	5
MULTD	F0	F2	F4	3		
SUBD	F8	F6	F2	4	7	8
DIVD	F10	F0	F6	5		
ADDD	F6	F8	F2	6	10	11

	Busy	Address
Load1	No	
Load2	No	
Load3	No	

Reservation Stations:

Time	Name	Busy	Op	S1 Vj	S2 Vk	RS Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
1	Mult1	Yes	MULTD	M(A2)	R(F4)		
	Mult2	Yes	DIVD		M(A1)	Mult1	

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
14	FU	Mult1	M(A2)		(M-M+M	(M-M)	Mult2			

Tomasulo Example One: Cycle 15

Instruction status:

Instruction		j	k	Issue	Exec Comp	Write Result
LD	F6	34+	R2	1	3	4
LD	F2	45+	R3	2	4	5
MULTD	F0	F2	F4	3	15	
SUBD	F8	F6	F2	4	7	8
DIVD	F10	F0	F6	5		
ADDD	F6	F8	F2	6	10	11

	Busy	Address
Load1	No	
Load2	No	
Load3	No	

Reservation Stations:

Time	Name	Busy	Op	S1 Vj	S2 Vk	RS Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
0	Mult1	Yes	MULTD	M(A2)	R(F4)		
	Mult2	Yes	DIVD		M(A1)	Mult1	

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
15	FU	Mult1	M(A2)		(M-M+M	(M-M)	Mult2			

Tomasulo Example One: Cycle 16

Instruction status:

Instruction		j	k	Issue	Exec Comp	Write Result
LD	F6	34+	R2	1	3	4
LD	F2	45+	R3	2	4	5
MULTD	F0	F2	F4	3	15	16
SUBD	F8	F6	F2	4	7	8
DIVD	F10	F0	F6	5		
ADDD	F6	F8	F2	6	10	11

	Busy	Address
Load1	No	
Load2	No	
Load3	No	

Reservation Stations:

Time	Name	Busy	Op	S1 Vj	S2 Vk	RS Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
	Mult1	No					
40	Mult2	Yes	DIVD	M*F4	M(A1)		

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
16	FU	M*F4	M(A2)		(M-M+M	(M-M)	Mult2			

Tomasulo Example One (Cont)

Faster than light computation (skip a couple of cycles)…

Tomasulo Example One: Cycle 55

Instruction status:

Instruction		j	k	Issue	Exec Comp	Write Result
LD	F6	34+	R2	1	3	4
LD	F2	45+	R3	2	4	5
MULTD	F0	F2	F4	3	15	16
SUBD	F8	F6	F2	4	7	8
DIVD	F10	F0	F6	5		
ADDD	F6	F8	F2	6	10	11

	Busy	Address
Load1	No	
Load2	No	
Load3	No	

Reservation Stations:

Time	Name	Busy	Op	S1 Vj	S2 Vk	RS Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
	Mult1	No					
1	Mult2	Yes	DIVD	M*F4	M(A1)		

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
55	FU	M*F4	M(A2)		(M-M+M	(M-M)	Mult2			

Tomasulo Example One: Cycle 56

Instruction status:

Instruction		j	k	Issue	Exec Comp	Write Result
LD	F6	34+	R2	1	3	4
LD	F2	45+	R3	2	4	5
MULTD	F0	F2	F4	3	15	16
SUBD	F8	F6	F2	4	7	8
DIVD	F10	F0	F6	5	56	
ADDD	F6	F8	F2	6	10	11

	Busy	Address
Load1	No	
Load2	No	
Load3	No	

Reservation Stations:

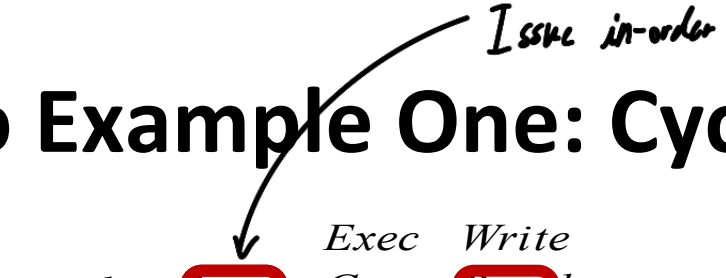
Time	Name	Busy	Op	S1 Vj	S2 Vk	RS Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
	Mult1	No					
0	Mult2	Yes	DIVD	M*F4	M(A1)		

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
56	FU	M*F4	M(A2)		(M-M+M	(M-M)	Mult2			

- **Mult2 is completing; what is waiting for it?**

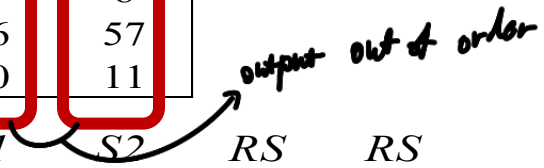
Tomasulo Example One: Cycle 57



Instruction status:

Instruction		j	k	Issue	Exec Comp	Write Result
LD	F6	34+	R2	1	3	4
LD	F2	45+	R3	2	4	5
MULTD	F0	F2	F4	3	15	16
SUBD	F8	F6	F2	4	7	8
DIVD	F10	F0	F6	5	56	57
ADDD	F6	F8	F2	6	10	11

	Busy	Address
Load1	No	
Load2	No	
Load3	No	



Reservation Stations:

Time	Name	Busy	Op	S1 Vj	S2 Vk	RS Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
	Mult1	No					
	Mult2	Yes	DIVD	M*F4	M(A1)		

Register result status:

Clock		F0	F2	F4	F6	F8	F10	F12	...	F30
56	FU	M*F4	M(A2)		(M-M+M	(M-M)	Result			

- **Once again: In-order issue, out-of-order execution and completion.**

Tomasulo Example One

- **Compare to Scoreboard Cycle 62**

Instruction status:

Instruction		j	k	Issue	Read Oper	Exec Comp	Write Result
LD	F6	34+	R2	1	2	3	4
LD	F2	45+	R3	5	6	7	8
MULTD	F0	F2	F4	6	9	19	20
SUBD	F8	F6	F2	7	9	11	12
DIVD	F10	F0	F6	8	21	61	62
ADDD	F6	F8	F2	13	14	16	22

Issue	Exec Comp	Write Result
1	3	4
2	4	5
3	15	16
4	7	8
5	56	57
6	10	11

- **Why take longer on Scoreboard/6600?**
  - Structural Hazards
  - Lack of forwarding (LDB)

Tomasulo Algorithm

- **Tomasulo vs. Scoreboard (IBM 360/91 v. CDC 6600)**

Pipelined Functional Units	Multiple Functional Units
(6 load, 3 store, 3 +, 2 x/÷)	(1 load/store, 1 + , 2 x, 1 ÷)
window size: ≤ 14 instructions	≤ 5 instructions
No issue on structural hazard	same
WAR: renaming avoids	stall completion
WAW: renaming avoids	stall issue
Broadcast results from FU	Write/read registers
Control: reservation stations	central scoreboard

Tomasulo Example Two: A Loop

- **Recall: Unrolled Loop That Minimizes Stalls**
  What assumptions made when moved code?
  - OK to move store past addi even though changes register
  - OK to move loads before stores: get right data?
  - When is it safe for compiler to do such changes?

Compiler Techniques for Exposing ILP

- **Technique 2: Loop unrolling**
  - What if we combine loop unrolling with pipeline scheduling?

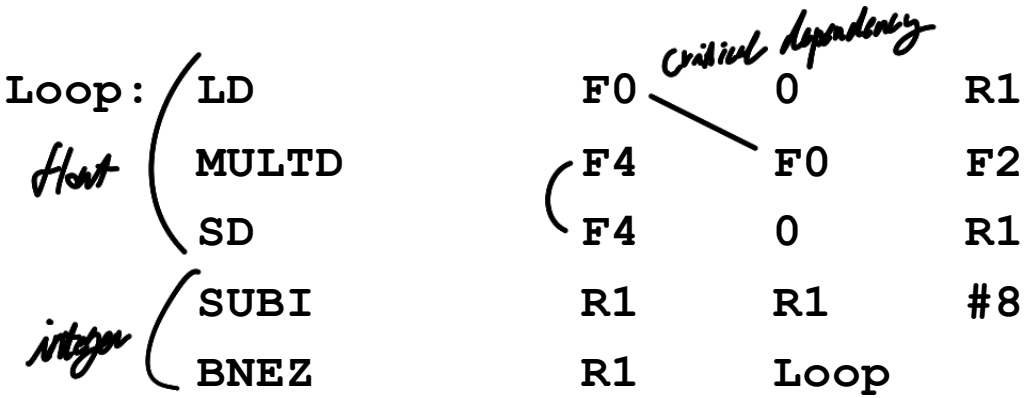
```
Loop:   fld      f0,0(x1)
        fld      f6,-8(x1)
        fld      f8,-16(x1)
        fld      f14,-24(x1)
        fadd.d   f4,f0,f2
        fadd.d   f8,f6,f2
        fadd.d   f12,f0,f2
        fadd.d   f16,f14,f2
        fsd      f4,0(x1)
        fsd      f8,-8(x1)
        fsd      f12,-16(x1)
        fsd      f16,-24(x1)
        addi     x1,x1,-32
        bne      x1,x2,Loop
```

How may cycles it would take??

14 clock cycles, or 3.5 per iteration!

Tomasulo Example Two: A Loop

- **Loop example code (MIPS)**



MIPS to RISC-V conversion

LD	→ fld
MULTD	→ fmul.d
SD	→ fsd
SUBI	→ addi (negative)
BNEZ	→ BNE (w/ rs2=x0)
R1	→ x1

- Assume Multiply takes 4 clocks
- Assume first load takes 8 clocks (cache miss), second load takes 1 clock (hit)
- To be clear, will show clocks for SUBI, BNEZ
- Reality: integer instructions ahead

Tomasulo Example Two: A Loop

Instruction status:

	ITER	Instruction		j	k	Issue	Exec Comp	Write Result
	1	LD	F0	0	R1			
	1	MULTD	F4	F0	F2			
Branch	1	SD	F4	0	R1			
	2	LD	F0	0	R1			
	2	MULTD	F4	F0	F2			
	2	SD	F4	0	R1			

	Busy	Addr	Fu
Load1	No		
Load2	No		
Load3	No		
Store1	No		
Store2	No		
Store3	No		

Reservation Stations:

Time	Name	Busy	Op	Vj	S1 Vk	S2 Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
	Mult1	No					
	Mult2	No					

Code:

```
LD     F0   0    R1
MULTD  F4   F0   F2
SD     F4   0    R1
SUBI   R1   R1   #8
BNEZ   R1   Loop
```

Register result status

Clock	R1		F0	F2	F4	F6	F8	F10	F12	...	F30
0	80	Fu									

Tomasulo Example Two: Cycle 1

Instruction status:

ITER	Instruction		j	k	Issue	Exec Comp	Write Result
1	LD	F0	0	R1	1		
1	MULTD	F4	F0	F2			
1	SD	F4	0	R1			
2	LD	F0	0	R1			
2	MULTD	F4	F0	F2			
2	SD	F4	0	R1			

	Busy	Addr	Fu
Load1	Yes	80	
Load2	No		
Load3	No		
Store1	No		
Store2	No		
Store3	No		

Reservation Stations:

Time	Name	Busy	Op	S1 Vj	S1 Vk	S2 Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
	Mult1	No					
	Mult2	No					

Code:

```
LD    F0  0  R1
MULTD F4  F0 F2
SD    F4  0  R1
SUBI  R1  R1 #8
BNEZ  R1  Loop
```

Register result status

Clock	R1		F0	F2	F4	F6	F8	F10	F12	...	F30
1	80	Fu	Load1								

Tomasulo Example Two: Cycle 2

Instruction status:

ITER	Instruction		j	k	Issue	Exec Comp	Write Result
1	LD	F0	0	R1	1		
1	MULTD	F4	F0	F2	2		
1	SD	F4	0	R1			
2	LD	F0	0	R1			
2	MULTD	F4	F0	F2			
2	SD	F4	0	R1			

	Busy	Addr	Fu
Load1	Yes	80	
Load2	No		
Load3	No		
Store1	No		
Store2	No		
Store3	No		

Reservation Stations:

Time	Name	Busy	Op	Vj	S1 Vk	S2 Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
	Mult1	Yes	Multd		R(F4)	Load1	
	Mult2	No					

Code:

```
LD    F0  0  R1
MULTD F4  F0 F2
SD    F4  0  R1
SUBI  R1  R1 #8
BNEZ  R1  Loop
```

Register result status

Clock	R1		F0	F2	F4	F6	F8	F10	F12	...	F30
2	80	Fu	Load1		Mult1						

Tomasulo Example Two: Cycle 3

- **Implicit renaming sets up "DataFlow" graph**

Instruction status:

ITER	Instruction		j	k	Issue	Exec Comp	Write Result
1	LD	F0	0	R1	1		
1	MULTD	F4	F0	F2	2		
1	SD	F4	0	R1	3		
2	LD	F0	0	R1			
2	MULTD	F4	F0	F2			
2	SD	F4	0	R1			

	Busy	Addr	Fu
Load1	Yes	80	
Load2	No		
Load3	No		
Store1	Yes	80	Mult1
Store2	No		
Store3	No		

dep

Reservation Stations:

Time	Name	Busy	Op	S1 Vj	S2 Vk	RS Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
	Mult1	Yes	Multd		R(F4)	Load1	
	Mult2	No					

Code:

```
LD    F0  0   R1
MULTD F4  F0  F2
SD    F4  0   R1
SUBI  R1  R1  #8
BNEZ  R1  Loop
```

Register result status

Clock	R1		F0	F2	F4	F6	F8	F10	F12	...	F30
3	80	Fu	Load1		Mult1						

Tomasulo Example Two: Cycle 4

- **Dispatching SUBI Instruction**

Instruction status:

ITER	Instruction		j	k	Issue	Exec Comp	Write Result
1	LD	F0	0	R1	1		
1	MULTD	F4	F0	F2	2		
1	SD	F4	0	R1	3		
2	LD	F0	0	R1			
2	MULTD	F4	F0	F2			
2	SD	F4	0	R1			

	Busy	Addr	Fu
Load1	Yes	80	
Load2	No		
Load3	No		
Store1	Yes	80	Mult1
Store2	No		
Store3	No		

Reservation Stations:

Time	Name	Busy	Op	Vj	S1 Vk	S2 Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
	Mult1	Yes	Multd		R(F4)	Load1	
	Mult2	No					

Code:

```
LD    F0  0   R1
MULTD F4  F0  F2
SD    F4  0   R1
SUBI  R1  R1  #8
BNEZ  R1  Loop
```

Register result status

Clock	R1		F0	F2	F4	F6	F8	F10	F12	...	F30
4	80	Fu	Load1		Mult1						

Tomasulo Example Two: Cycle 5

- **And, BNEZ instruction**

Instruction status:

ITER	Instruction		j	k	Issue	Exec Comp	Write Result
1	LD	F0	0	R1	1		
1	MULTD	F4	F0	F2	2		
1	SD	F4	0	R1	3		
2	LD	F0	0	R1			
2	MULTD	F4	F0	F2			
2	SD	F4	0	R1			

	Busy	Addr	Fu
Load1	Yes	80	
Load2	No		
Load3	No		
Store1	Yes	80	Mult1
Store2	No		
Store3	No		

Reservation Stations:

Time	Name	Busy	Op	Vj	S1 Vk	S2 Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
	Mult1	Yes	Multd		R(F4)	Load1	
	Mult2	No					

Code:

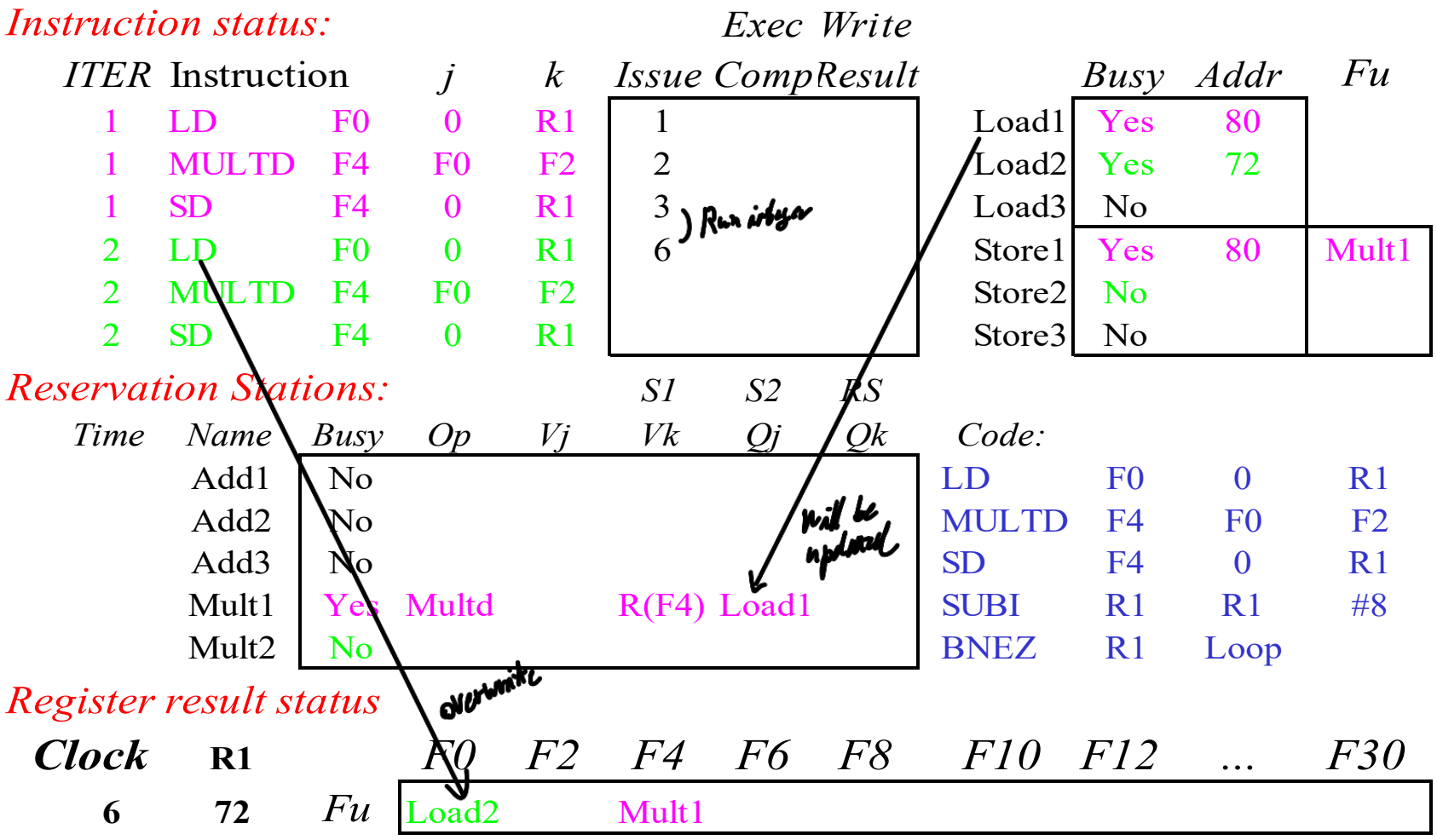
```
LD    F0  0   R1
MULTD F4  F0  F2
SD    F4  0   R1
SUBI  R1  R1  #8
BNEZ  R1  Loop
```

Register result status

Clock	R1		F0	F2	F4	F6	F8	F10	F12	...	F30
5	72	Fu	Load1		Mult1						

Tomasulo Example Two: Cycle 6

- **Notice that F0 never sees Load from location 80**



Tomasulo Example Two: Cycle 7

- Register file completely detached from computation
- First and second iteration completely overlapped

Instruction status:

ITER	Instruction		j	k	Issue	Exec Comp	Write Result
1	LD	F0	0	R1	1		
1	MULTD	F4	F0	F2	2		
1	SD	F4	0	R1	3		
2	LD	F0	0	R1	6		
2	MULTD	F4	F0	F2	7		
2	SD	F4	0	R1			

	Busy	Addr	Fu
Load1	Yes	80	
Load2	Yes	72	
Load3	No		
Store1	Yes	80	Mult1
Store2	No		
Store3	No		

Reservation Stations:

Time	Name	Busy	Op	Vj	S1 Vk	S2 Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
	Mult1	Yes	Multd		R(F2)	Load1	
	Mult2	Yes	Multd		R(F2)	Load2	

Code:

LD	F0	0	R1
MULTD	F4	F0	F2
SD	F4	0	R1
SUBI	R1	R1	#8
BNEZ	R1	Loop	

Register result status

Clock	R1		F0	F2	F4	F6	F8	F10	F12	...	F30
7	72	Fu	Load2		Mult2						

Tomasulo Example Two: Cycle 8

Instruction status:

ITER	Instruction		j	k	Issue	Exec Comp	Write Result
1	LD	F0	0	R1	1		
1	MULTD	F4	F0	F2	2		
1	SD	F4	0	R1	3		
2	LD	F0	0	R1	6		
2	MULTD	F4	F0	F2	7		
2	SD	F4	0	R1	8		

	Busy	Addr	Fu
Load1	Yes	80	
Load2	Yes	72	
Load3	No		
Store1	Yes	80	Mult1
Store2	Yes	72	Mult2
Store3	No		

Reservation Stations:

Time	Name	Busy	Op	Vj	S1 Vk	S2 Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
	Mult1	Yes	Multd		R(F2)	Load1	
	Mult2	Yes	Multd		R(F2)	Load2	

Code:

```
LD    F0  0   R1
MULTD F4  F0  F2
SD    F4  0   R1
SUBI  R1  R1  #8
BNEZ  R1  Loop
```

Register result status

Clock	R1		F0	F2	F4	F6	F8	F10	F12	...	F30
8	72	Fu	Load2		Mult2						

Tomasulo Example Two: Cycle 9

- **Load1 completing: who is waiting?**
- **Note: Dispatching SUBI**

Instruction status:

ITER	Instruction		j	k	Issue	Exec Comp	Write Result
1	LD	F0	0	R1	1	9	
1	MULTD	F4	F0	F2	2		
1	SD	F4	0	R1	3		
2	LD	F0	0	R1	6		
2	MULTD	F4	F0	F2	7		
2	SD	F4	0	R1	8		

	Busy	Addr	Fu
Load1	Yes	80	
Load2	Yes	72	
Load3	No		
Store1	Yes	80	Mult1
Store2	Yes	72	Mult2
Store3	No		

Reservation Stations:

Time	Name	Busy	Op	Vj	S1 Vk	S2 Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
	Mult1	Yes	Multd		R(F2)	Load1	
	Mult2	Yes	Multd		R(F2)	Load2	

Code:

```
LD    F0  0  R1
MULTD F4  F0 F2
SD    F4  0  R1
SUBI  R1  R1 #8
BNEZ  R1  Loop
```

Register result status

Clock	R1		F0	F2	F4	F6	F8	F10	F12	...	F30
9	72	Fu	Load2		Mult2						

Tomasulo Example Two: Cycle 10

- **Load2 completing: who is waiting?**
- **Note: Dispatching BNEZ**

Instruction status:

ITER	Instruction		j	k	Issue	Exec Comp	Write Result
1	LD	F0	0	R1	1	9	10
1	MULTD	F4	F0	F2	2		
1	SD	F4	0	R1	3		
2	LD	F0	0	R1	6	10	
2	MULTD	F4	F0	F2	7		
2	SD	F4	0	R1	8		

	Busy	Addr	Fu
Load1	No		
Load2	Yes	72	
Load3	No		
Store1	Yes	80	Mult1
Store2	Yes	72	Mult2
Store3	No		

Reservation Stations:

Time	Name	Busy	Op	S1 Vj	S1 Vk	S2 Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
4	Mult1	Yes	Multd	M[80]	R(F2)		
	Mult2	Yes	Multd		R(F2)	Load2	

Code:

LD	F0	0	R1
MULTD	F4	F0	F2
SD	F4	0	R1
SUBI	R1	R1	#8
BNEZ	R1	Loop	

Register result status

Clock	R1		F0	F2	F4	F6	F8	F10	F12	...	F30
10	64	Fu	Load2		Mult2						

Tomasulo Example Two: Cycle 11

- **Next load in sequence**

Instruction status:

ITER	Instruction		j	k	Issue	Exec Comp	Write Result
1	LD	F0	0	R1	1	9	10
1	MULTD	F4	F0	F2	2		
1	SD	F4	0	R1	3		
2	LD	F0	0	R1	6	10	11
2	MULTD	F4	F0	F2	7		
2	SD	F4	0	R1	8		

	Busy	Addr	Fu
Load1	No		
Load2	No		
Load3	Yes	64	
Store1	Yes	80	Mult1
Store2	Yes	72	Mult2
Store3	No		

Reservation Stations:

Time	Name	Busy	Op	S1 Vj	S2 Vk	RS Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
3	Mult1	Yes	Multd	M[80]	R(F2)		
4	Mult2	Yes	Multd	M[72]	R(F2)		

Code:

```
LD    F0  0  R1
MULTD F4  F0 F2
SD    F4  0  R1
SUBI  R1  R1 #8
BNEZ  R1  Loop
```

Register result status

Clock	R1		F0	F2	F4	F6	F8	F10	F12	...	F30
11	64	Fu	Load3		Mult2						

Tomasulo Example Two: Cycle 12

- **Why not issue third multiply?**

Instruction status:

ITER	Instruction		j	k	Issue	Exec Comp	Write Result
1	LD	F0	0	R1	1	9	10
1	MULTD	F4	F0	F2	2		
1	SD	F4	0	R1	3		
2	LD	F0	0	R1	6	10	11
2	MULTD	F4	F0	F2	7		
2	SD	F4	0	R1	8		

	Busy	Addr	Fu
Load1	No		
Load2	No		
Load3	Yes	64	
Store1	Yes	80	Mult1
Store2	Yes	72	Mult2
Store3	No		

Reservation Stations:

Time	Name	Busy	Op	S1 Vj	S2 Vk	RS Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
2	Mult1	Yes	Multd	M[80]	R(F2)		
3	Mult2	Yes	Multd	M[72]	R(F2)		

Code:

```
LD    F0  0  R1
MULTD F4  F0 F2
SD    F4  0  R1
SUBI  R1  R1 #8
BNEZ  R1  Loop
```

Register result status

Clock	R1		F0	F2	F4	F6	F8	F10	F12	...	F30
12	64	Fu	Load3		Mult2						

Tomasulo Example Two: Cycle 13

Instruction status:

ITER	Instruction		j	k	Issue	Exec Comp	Write Result
1	LD	F0	0	R1	1	9	10
1	MULTD	F4	F0	F2	2		
1	SD	F4	0	R1	3		
2	LD	F0	0	R1	6	10	11
2	MULTD	F4	F0	F2	7		
2	SD	F4	0	R1	8		

	Busy	Addr	Fu
Load1	No		
Load2	No		
Load3	Yes	64	
Store1	Yes	80	Mult1
Store2	Yes	72	Mult2
Store3	No		

Reservation Stations:

Time	Name	Busy	Op	S1 Vj	S2 Vk	RS Qj	Qk
	Add1	No					
	Add2	No					
	Add3	No					
1	Mult1	Yes	Multd	M[80]	R(F2)		
2	Mult2	Yes	Multd	M[72]	R(F2)		

Code:

```
LD    F0  0   R1
MULTD F4  F0  F2
SD    F4  0   R1
SUBI  R1  R1  #8
BNEZ  R1  Loop
```

Register result status

Clock	R1		F0	F2	F4	F6	F8	F10	F12	...	F30
13	64	Fu	Load3		Mult2						

Tomasulo Example Two: Cycle 14

- **Mult1 completing. Who is waiting?**

Instruction status:

ITER	Instruction		j	k	Issue	Exec Comp	Write Result
1	LD	F0	0	R1	1	9	10
1	MULTD	F4	F0	F2	2	14	
1	SD	F4	0	R1	3		
2	LD	F0	0	R1	6	10	11
2	MULTD	F4	F0	F2	7		
2	SD	F4	0	R1	8		

	Busy	Addr	Fu
Load1	No		
Load2	No		
Load3	Yes	64	
Store1	Yes	80	Mult1
Store2	Yes	72	Mult2
Store3	No		

Reservation Stations:

Time	Name	Busy	Op	S1 Vj	S2 Vk	RS Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
0	Mult1	Yes	Multd	M[80]	R(F2)		
1	Mult2	Yes	Multd	M[72]	R(F2)		

Code:

```
LD    F0  0   R1
MULTD F4  F0  F2
SD    F4  0   R1
SUBI  R1  R1  #8
BNEZ  R1  Loop
```

Register result status

Clock	R1		F0	F2	F4	F6	F8	F10	F12	...	F30
14	64	Fu	Load3		Mult2						

Tomasulo Example Two: Cycle 15

- **Mult2 completing. Who is waiting?**

Instruction status:

ITER	Instruction		j	k	Issue	Exec Comp	Write Result
1	LD	F0	0	R1	1	9	10
1	MULTD	F4	F0	F2	2	14	15
1	SD	F4	0	R1	3		
2	LD	F0	0	R1	6	10	11
2	MULTD	F4	F0	F2	7	15	
2	SD	F4	0	R1	8		

	Busy	Addr	Fu
Load1	No		
Load2	No		
Load3	Yes	64	
Store1	Yes	80	[80]*R2
Store2	Yes	72	Mult2
Store3	No		

Reservation Stations:

Time	Name	Busy	Op	S1 Vj	S2 Vk	RS Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
	Mult1	No					
0	Mult2	Yes	Multd	M[72]	R(F2)		

Code:

```
LD    F0  0  R1
MULTD F4  F0 F2
SD    F4  0  R1
SUBI  R1  R1 #8
BNEZ  R1  Loop
```

Register result status

Clock	R1		F0	F2	F4	F6	F8	F10	F12	...	F30
15	64	Fu	Load3		Mult2						

Tomasulo Example Two: Cycle 16

Instruction status:

ITER	Instruction		j	k	Issue	Exec Comp	Write Result
1	LD	F0	0	R1	1	9	10
1	MULTD	F4	F0	F2	2	14	15
1	SD	F4	0	R1	3		
2	LD	F0	0	R1	6	10	11
2	MULTD	F4	F0	F2	7	15	16
2	SD	F4	0	R1	8		

	Busy	Addr	Fu
Load1	No		
Load2	No		
Load3	Yes	64	
Store1	Yes	80	[80]*R2
Store2	Yes	72	[72]*R2
Store3	No		

Reservation Stations:

Time	Name	Busy	Op	Vj	S1 Vk	S2 Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
	Mult1	Yes	Multd		R(F2)	Load3	
	Mult2	No					

Code:

```
LD    F0  0   R1
MULTD F4  F0  F2
SD    F4  0   R1
SUBI  R1  R1  #8
BNEZ  R1  Loop
```

Register result status

Clock	R1		F0	F2	F4	F6	F8	F10	F12	...	F30
16	64	Fu	Load3		Mult1						

Tomasulo Example Two: Cycle 17

Instruction status:

ITER	Instruction		j	k	Issue	Exec Comp	Write Result
1	LD	F0	0	R1	1	9	10
1	MULTD	F4	F0	F2	2	14	15
1	SD	F4	0	R1	3		
2	LD	F0	0	R1	6	10	11
2	MULTD	F4	F0	F2	7	15	16
2	SD	F4	0	R1	8		

	Busy	Addr	Fu
Load1	No		
Load2	No		
Load3	Yes	64	
Store1	Yes	80	[80]*R2
Store2	Yes	72	[72]*R2
Store3	Yes	64	Mult1

Reservation Stations:

Time	Name	Busy	Op	Vj	S1 Vk	S2 Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
	Mult1	Yes	Multd		R(F2)	Load3	
	Mult2	No					

Code:

```
LD    F0  0   R1
MULTD F4  F0  F2
SD    F4  0   R1
SUBI  R1  R1  #8
BNEZ  R1  Loop
```

Register result status

Clock	R1		F0	F2	F4	F6	F8	F10	F12	...	F30
17	64	Fu	Load3		Mult1						

Tomasulo Example Two: Cycle 18

Instruction status:

ITER	Instruction		j	k	Issue	Exec Comp	Write Result
1	LD	F0	0	R1	1	9	10
1	MULTD	F4	F0	F2	2	14	15
1	SD	F4	0	R1	3	18	
2	LD	F0	0	R1	6	10	11
2	MULTD	F4	F0	F2	7	15	16
2	SD	F4	0	R1	8		

	Busy	Addr	Fu
Load1	No		
Load2	No		
Load3	Yes	64	
Store1	Yes	80	[80]*R2
Store2	Yes	72	[72]*R2
Store3	Yes	64	Mult1

Reservation Stations:

Time	Name	Busy	Op	Vj	S1 Vk	S2 Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
	Mult1	Yes	Multd		R(F2)	Load3	
	Mult2	No					

Code:

```
LD    F0  0   R1
MULTD F4  F0  F2
SD    F4  0   R1
SUBI  R1  R1  #8
BNEZ  R1  Loop
```

Register result status

Clock	R1		F0	F2	F4	F6	F8	F10	F12	...	F30
18	64	Fu	Load3		Mult1						

Tomasulo Example Two: Cycle 19

Instruction status:

ITER	Instruction		j	k	Issue	Exec Comp	Write Result
1	LD	F0	0	R1	1	9	10
1	MULTD	F4	F0	F2	2	14	15
1	SD	F4	0	R1	3	18	19
2	LD	F0	0	R1	6	10	11
2	MULTD	F4	F0	F2	7	15	16
2	SD	F4	0	R1	8	19	

	Busy	Addr	Fu
Load1	No		
Load2	No		
Load3	Yes	64	
Store1	No		
Store2	Yes	72	[72]*R2
Store3	Yes	64	Mult1

Reservation Stations:

Time	Name	Busy	Op	Vj	S1 Vk	S2 Qj	RS Qk
	Add1	No					
	Add2	No					
	Add3	No					
	Mult1	Yes	Multd		R(F2)	Load3	
	Mult2	No					

Code:

```
LD    F0  0   R1
MULTD F4  F0  F2
SD    F4  0   R1
SUBI  R1  R1  #8
BNEZ  R1  Loop
```

Register result status

Clock	R1		F0	F2	F4	F6	F8	F10	F12	...	F30
19	64	Fu	Load3		Mult1						

Tomasulo Example Two: Cycle 20

Instruction status:

ITER	Instruction		j	k	Issue	Exec Comp	Write Result
1	LD	F0	0	R1	1	9	10
1	MULTD	F4	F0	F2	2	14	15
1	SD	F4	0	R1	3	18	19
2	LD	F0	0	R1	6	10	11
2	MULTD	F4	F0	F2	7	15	16
2	SD	F4	0	R1	8	19	20

	Busy	Addr	Fu
Load1	No		
Load2	No		
Load3	Yes	64	
Store1	No		
Store2	No		
Store3	Yes	64	Mult1

Reservation Stations:

Time	Name	Busy	Op	S1 Vj	S1 Vk	S2 Qj	S2 Qk	RS
	Add1	No						
	Add2	No						
	Add3	No						
	Mult1	Yes	Multd		R(F2)	Load3		
	Mult2	No						

Code:

```
LD    F0  0   R1
MULTD F4  F0  F2
SD    F4  0   R1
SUBI  R1  R1  #8
BNEZ  R1  Loop
```

Register result status

Clock	R1		F0	F2	F4	F6	F8	F10	F12	...	F30
20	64	Fu	Load3		Mult1						

Tomasulo Example Two

- **Why can Tomasulo overlap iterations of loops?**
  - Register renaming
    - Multiple iterations use different physical destinations for registers (dynamic loop unrolling).
  - Reservation stations
    - Permit instruction issue to advance past integer control flow operations
  - Other idea: Tomasulo building dynamic “DataFlow” graph from instructions

Summary

- **Scoreboard: Track dependencies through reservations**
  - Simple scheme for out-of-order execution
  - WAW and WAR hazards force stalls – cannot handle multiple instructions with same destination register
- **Reservations stations: *renaming* to larger set of registers + buffering source operands**
  - Prevents registers as bottleneck
  - Avoids WAR, WAW hazards of Scoreboard
  - Allows loop unrolling in HW
- **Dynamic hardware schemes can unroll loops dynamically in hardware**
  - Form of limited dataflow
  - Register renaming is essential
- **Lasting Contributions of Tomasulo Algorithm**
  - Dynamic scheduling
  - Register renaming
  - Load/store disambiguation
- **IBM 360/91 descendants: Pentium II, PPC 604, MIPS R10000, Alpha 21264, etc.**