



Computer Sciences Dept.

Midterm Exam (Fall 2023/2024)

MATH204 – Probability and Statistics I

Code: EXM-FR 01/1
ED:2.1

Stu. Name: ID Number:	Inst. Name: Dr. Ayman El Zein Section: B	Booklet Needed: No Exam Date: 23/11/2023
Exam Time: 1h 15 min		Grade:/100

Exercise 1: (22 pts)

We roll a die three times. At each time, we note the obtained number. At the end of the experiment, we obtain a number of 3 digits.

For instance, if we obtain first a 3, then a 2 and finally a 6, then the obtained number is 326.

- a. How many numbers can be obtained at the end of the experiment?
- b. How many of these numbers is even?
- c. How many of these numbers is greater than 400?
- d. How many of these numbers is less than 200?
- e. How many of these numbers is at least equal to 352?
- f. How many of these numbers contains a 1 followed by a 6?

Exercise 2: (22 pts)

An urn contains:

Four red balls numbered 0, 0, 1, 2

Three blue balls numbered 0, 1, 1

And, two white balls numbered 1, 2

We draw randomly and simultaneously two balls from the urn. Consider the following events:

A: “The two balls have the same color”

B: “The two balls have the same number”

C: “The sum of the two numbers of the balls is 2”

D: “The product of the two numbers of the balls is 0”

Calculate $P(A)$, $P(B)$, $P(C)$, $P(D)$ and $P(A \cup B)$.

Exercise 3: (12 pts)

A set of 3 red balls, 3 green balls, and 3 yellow balls has to be distributed into three boxes labeled A , B and C .

- a. What is the total number of ways to distribute these balls.
- b. Calculate the probability that the box A contains the 3 red balls.
- c. Calculate the probability that the box A contains the 3 red balls, the box B contains the 3 green balls, and the box C contains the 3 yellow balls.
- d. Calculate the probability that each box contains 3 balls of same color.

Exercise 4: (14 pts)

Three events A , B and C are such that $P(A) = 0.4$, $P(B) = 0.7$, $P(C) = 0.2$, $P(\overline{A} \cap \overline{B}) = 0.18$ and $P(A \cup C) = 0.5$.

- a. Show that A and B are independent events.
- b. Calculate $P(A \cap \overline{B})$ and $P(A|C)$.

Exercise 5: (30 pts)

- A. The faces of a coin are numbered 1 and 2. We flip the coin two successive times.

Consider the following events:

S_2 : "The sum of the two appeared numbers is 2"

S_3 : "The sum of the two appeared numbers is 3"

S_4 : "The sum of the two appeared numbers is 4"

Calculate $P(S_2)$, $P(S_3)$ and $P(S_4)$.

- B. A box contains 3 red cards and 5 black cards. A game consists of flipping the coin whose faces are numbered 1 and 2 two successive times, then to draw, simultaneously, a number of cards from the box equal to the sum of the two numbers. We consider the following event:

R : "Exactly one red card is drawn from the box"

a. Calculate $P(R|S_2)$ and deduce $P(R \cap S_2)$.

b. Calculate $P(R)$.

c. Knowing that exactly one red ball is drawn, what is the probability that the two faces of the flipped coin were numbered 2?

Bonus exercise:

A game consists of flipping a coin, successively, many times. The game stops when obtaining a tail for the first time. What is the minimum number of flips for which the probability to attain is less than 1%?