

// 2st solution: add 2 insulation layers of glass wool of L_2 meters thickness, the following calculations are done to find L_2 required to comply with the rules

//Knowns given:

A = 0.422 [m^2] // The total surface area on which we aim to insulate

L_1 = 0.635/1000 // thickness of the main aluminum firewall base

k_6061 = 166 [W/K-m]

k_GW = 0.04 [W/K-m]

T_inf = 298.15 [K]

Ts_1 = 402.59[K]

Ts_2 = 333.15 [K]

T_delta = Ts_1 - T_inf

h_conv_air = 5 [W/m^2*K]

//Thermal Resistances connected in series:

R_cond_6061 = L_1/(K_6061*A)

R_conv_air = 1/(h_conv_air * A)

R_cond_GW = L_2/(A*k_GW)

// the sumation of the thermal resitsnaces in the wall

R_total_GW = R_cond_6061 + R_conv_air + (2*R_cond_GW)

// Thermal power:

Q_GW = T_delta/ R_total_GW

// Surfcae temperature 2:

Ts_2 = (- (2* R_cond_GW + R_cond_6061)*Q_GW) + Ts_1

$$A = 0.422 \text{ [m}^2\text{]}$$

$$L_1 = \frac{0.635}{1000}$$

$$k_{6061} = 166 \text{ [W/K-m]}$$

$$k_{GW} = 0.04 \text{ [W/K-m]}$$

$$T_{inf} = 298.15 \text{ [K]}$$

$$Ts_1 = 402.59 \text{ [K]}$$

$$Ts_2 = 333.15 \text{ [K]}$$

$$T_{\delta} = Ts_1 - T_{inf}$$

$$h_{conv,air} = 5 \text{ [W/m}^2\text{*K]}$$

$$R_{cond,6061} = \frac{L_1}{k_{6061} \cdot A}$$

$$R_{conv,air} = \frac{1}{h_{conv,air} \cdot A}$$

$$R_{cond,GW} = \frac{L_2}{A \cdot k_{GW}}$$

$$R_{total,GW} = R_{cond,6061} + R_{conv,air} + 2 \cdot R_{cond,GW}$$

$$Q_{GW} = \frac{T_{\delta}}{R_{total,GW}}$$

$$Ts_2 = - (2 \cdot R_{\text{cond,GW}} + R_{\text{cond,6061}}) \cdot Q_{\text{GW}} + Ts_1$$

SOLUTION

Unit Settings: SI K Pa J mass rad

$$A = 0.422 \text{ [m}^2\text{]}$$

$$k_{6061} = 166 \text{ [W/K-m]}$$

$$L_1 = 0.000635 \text{ [m]}$$

$$Q_{\text{GW}} = 73.85 \text{ [W]}$$

$$R_{\text{cond,GW}} = 0.4701 \text{ [K/W]}$$

$$R_{\text{total,GW}} = 1.414 \text{ [K/W]}$$

$$Ts_2 = 333.2 \text{ [K]}$$

$$T_{\text{inf}} = 298.2 \text{ [K]}$$

$$h_{\text{conv,air}} = 5 \text{ [W/m}^2\text{*K]}$$

$$k_{\text{GW}} = 0.04 \text{ [W/K-m]}$$

$$L_2 = 0.007936 \text{ [m]}$$

$$R_{\text{cond,6061}} = 0.000009065 \text{ [K/W]}$$

$$R_{\text{conv,air}} = 0.4739 \text{ [K/W]}$$

$$Ts_1 = 402.6 \text{ [K]}$$

$$T_{\delta} = 104.4 \text{ [K]}$$

No unit problems were detected.