Team Notebook

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November 16, 2024

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1 DP

1.1 Divide and Conquer

```
int m, n;
vector<long long> dp_before(n), dp_cur(n);
long long C(int i, int j);
// compute dp_cur[1], ... dp_cur[r] (inclusive)
void compute(int 1, int r, int optl, int optr) {
    if (1 > r)
       return;
    int mid = (1 + r) >> 1:
    pair<long long, int> best = {LLONG_MAX, -1};
    for (int k = optl; k <= min(mid, optr); k++) {</pre>
       best = min(best, \{(k ? dp_before[k - 1] : 0) + C(k,
            mid), k});
    dp cur[mid] = best.first:
    int opt = best.second;
    compute(1, mid - 1, optl, opt);
    compute(mid + 1, r, opt, optr);
}
int solve() {
    for (int i = 0; i < n; i++)</pre>
       dp_before[i] = C(0, i);
    for (int i = 1: i < m: i++) {</pre>
       compute(0, n - 1, 0, n - 1);
       dp before = dp cur:
    return dp_before[n - 1];
```

1.2 SOS

```
// sum over subsets O(N * 2^N)
for (int i = 0; i < (1LL << n); i++) {
    sos[i] = cnt[i];
}
for (int i = 0; i < n; i++) {</pre>
```

2 Data Structures

2.1 CentroidDecomp

```
vector<vector<int>> adj;
vector<bool> is_removed;
vector<int> subtree size:
/** DFS to calculate the size of the subtree rooted at 'node
int get_subtree_size(int node, int parent = -1) {
subtree size[node] = 1:
for (int child : adj[node]) {
 if (child == parent || is_removed[child]) { continue; }
 subtree_size[node] += get_subtree_size(child, node);
return subtree size[node]:
* Returns a centroid (a tree may have two centroids) of the
* containing node 'node' after node removals
* Oparam node current node
* @param tree size size of current subtree after node
* Oparam parent parent of u
* @return first centroid found
int get_centroid(int node, int tree_size, int parent = -1) {
for (int child : adi[node]) {
 if (child == parent || is_removed[child]) { continue; }
 if (subtree_size[child] * 2 > tree_size) {
 return get_centroid(child, tree_size, node);
```

```
return node;
}

/** Build up the centroid decomposition recursively */
void build_centroid_decomp(int node = 0) {
  int centroid = get_centroid(node, get_subtree_size(node));

// do something

is_removed[centroid] = true;

for (int child : adj[centroid]) {
  if (is_removed[child]) { continue; }
  build_centroid_decomp(child);
}

}
```

2.2 CoordinateCompression

2.3 DSU

```
struct DSU {
    int n;
    vector<int> par, sz;

DSU(int n): n(n) {
        par = sz = vector<int> (n + 1);
        fill(all(sz), 1LL);
        iota(all(par), OLL);
    }
    int find(int v) {
        while (v != par[v]) v = par[v] = par[par[v]];
    }
}
```

```
return v;
}

bool join(int u, int v) {
    u = find(u);
    v = find(v);
    if (u == v) return false;
    if (sz[u] < sz[v]) swap(u, v);
    sz[u] += sz[v];
    par[v] = u;
    return true;
}

int same(int u, int v) {
    return find(u) == find(v);
}
};</pre>
```

2.4 FakeFenwick

```
struct FakeFenwick {
       vector<vector<int>> fw, val;
      int n:
      FakeFenwick() {}
      FakeFenwick(int n): n(n), val(n + 1, vector<int>()),
            fw(n + 1) {}
      bool iscc = 0;
       void fakeU(int x, int y) {
              iscc = 0:
              for (; x <= n; x += x & -x) val[x].push_back(y</pre>
                   ):
      }
       void cc() {
              if (iscc) return:
              for (int x = 1; x <= n; x++) {</pre>
                      sort(all(val[x]));
                     val[x].erase(unique(all(val[x])), val[x
                          ].end());
                     fw[x].resize(val[x].size() + 1):
              }
              iscc = 1;
       void update(int x, int y, int v) {
              assert(iscc);
              for (: x <= n: x += x & -x) {
                     int yy = upper_bound(all(val[x]), y) -
                          val[x].begin();
                     for (; yy <= val[x].size(); yy += yy &</pre>
                           -vv) {
```

2.5 Fenwick

```
template<typename T>
struct fenwick {
vector<T> f:
int n;
fenwick(int n): n(n) {
 f.resize(n + 1);
void add(int i, T v) {
 dbg(i);
 for (: i <= n: i += i & -i) {
 f[i] += v:
  dbg(i, v);
T get(int i) {
 T ans = 0;
 for (; i >= 1; i -= i & -i) ans += f[i];
 return ans:
T find(T k) {
 T sum = 0:
 int pos = 0;
 for (int i = _-lg(n); i >= 0; i--)
  if (pos + (1 << i) < n && sum + f[pos + (1 << i)] < k)</pre>
   sum += f[pos + (1 << i)];
   pos += (1 << i);
```

```
}
return pos + 1;
};
```

2.6 HLD

```
struct HLD {
       int n:
       int root;
       vector<int> sz, par, dep, top, in, out, seq;
       vector<vector<int>> adj;
       int curdfs = 0;
       HLD(int n): n(n) {
              par = sz = dep = top = in = out = seq = vector
                   \langle int \rangle (n + 1);
              adi.resize(n + 1):
       }
       void addEdge(int u, int v) {
              adj[u].push_back(v);
              adj[v].push_back(u);
       void start(int root = 1) {
              this->root = root;
              par[root] = root;
              top[root] = root;
              dfssz(root):
              dfshld(root);
      }
       void dfssz(int u) {
              if (u != root) adj[u].erase(find(all(adj[u]),
                   par[u]));
              sz[u] = 1:
              for (int &v : adj[u]) {
                     dep[v] = dep[u] + 1;
                     par[v] = u:
                     dfssz(v);
                      sz[u] += sz[v];
                     if (sz[v] > sz[adj[u][0]]) swap(adj[u
                          ][0]. v):
              }
       }
       void dfshld(int u) {
              in[u] = ++curdfs:
              seq[in[u]] = u;
              for (int v : adj[u]) {
                      top[v] = (v == adj[u][0] ? top[u] : v);
                     dfshld(v);
```

2.7 LinkCutTree

```
typedef long long 11;
typedef struct snode *sn:
struct snode {
                    ////// VARIABLES
                 // parent, children
sn p, c[2];
bool flip = 0; // subtree flipped or not
                 // # nodes in current splay tree
11 sub. vsub = 0: // vsub stores sum of virtual children
                 // value in node
snode(int _val) : val(_val) {
 p = c[0] = c[1] = NULL;
 calc();
friend int getSz(sn x) { return x ? x->sz : 0: }
friend 11 getSub(sn x) { return x ? x->sub : 0; }
void prop() { // lazy prop
 if (!flip) return;
 swap(c[0], c[1]);
 flip = 0:
 for (int i = 0; i < 2; i++)
 if (c[i]) c[i]->flip ^= 1:
void calc() { // recalc vals
 for (int i = 0; i < 2; i++)
 if (c[i]) c[i]->prop();
 sz = 1 + getSz(c[0]) + getSz(c[1]);
 sub = val + getSub(c[0]) + getSub(c[1]) + vsub:
////// SPLAY TREE OPERATIONS
int dir() {
 if (!p) return -2;
```

```
for (int i = 0: i < 2: i++)
 if (p->c[i] == this) return i;
return -1; // p is path-parent pointer
} // -> not in current splay tree
// test if root of current splay tree
bool isRoot() { return dir() < 0: }</pre>
friend void setLink(sn x, sn y, int d) {
if (y) y \rightarrow p = x;
if (d >= 0) x -> c[d] = y;
void rot() { // assume p and p->p propagated
assert(!isRoot()):
int x = dir():
sn pa = p;
 setLink(pa->p, this, pa->dir());
 setLink(pa, c[x ^1], x);
setLink(this, pa, x ^ 1);
pa->calc();
void splay() {
while (!isRoot() && !p->isRoot()) {
 p->p->prop(), p->prop(), prop();
 dir() == p->dir() ? p->rot() : rot();
 rot():
if (!isRoot()) p->prop(), prop(), rot();
prop():
calc():
sn fbo(int b) { // find by order
prop();
int z = getSz(c[0]); // of splay tree
if (b == z) {
 splay();
 return this:
return b < z? c[0] \rightarrow fbo(b) : c[1] \rightarrow fbo(b - z - 1):
////// BASE OPERATIONS
void access() { // bring this to top of tree, propagate
for (sn v = this, pre = NULL; v; v = v->p) {
 v->splay(); // now switch virtual children
 if (pre) v->vsub -= pre->sub:
 if (v->c[1]) v->vsub += v->c[1]->sub;
 v - c[1] = pre;
 v->calc():
 pre = v;
assert(!c[1]); // right subtree is empty
```

```
void makeRoot() {
access():
flip ^= 1:
access();
assert(!c[0] && !c[1]):
////// QUERIES
friend sn lca(sn x, sn y) {
if (x == y) return x;
x->access(), y->access();
if (!x->p) return NULL:
x->splay();
return x->p ?: x; // y was below x in latter case
} // access at v did not affect x -> not connected
friend bool connected(sn x, sn y) { return lca(x, y); }
// # nodes above
int distRoot() {
access():
return getSz(c[0]);
sn getRoot() { // get root of LCT component
access():
sn a = this:
while (a->c[0]) a = a->c[0], a->prop();
a->access():
return a:
sn getPar(int b) { // get b-th parent on path to root
access():
b = getSz(c[0]) - b;
assert(b >= 0);
return fbo(b):
} // can also get min, max on path to root, etc
////// MODIFICATIONS
void set(int v) {
access():
val = v:
 calc();
friend void link(sn x. sn v. bool force = 0) {
assert(!connected(x, y));
if (force) v->makeRoot(): // make x par of v
 else {
 y->access();
 assert(!v->c[0]):
 x->access():
 setLink(v. x. 0):
 v->calc():
```

```
friend void cut(sn y) { // cut y from its parent
    y->access();
    assert(y->c[0]);
    y->c[0]->p = NULL;
    y->cl0] = NULL;
    y->calc();
}
friend void cut(sn x, sn y) { // if x, y adj in tree
    x->makeRoot();
    y->access();
    assert(y->c[0] == x && !x->c[0] && !x->c[1]);
    cut(y);
}
};
```

2.8 OrderedSet

2.9 PURQ

```
struct Info {
  int val;
  bool empty;
  Info(): val(0), empty(1) { }
  Info(int val): val(val), empty(0) { }
  friend Info operator + (Info lef, Info rig) {
    if (lef.empty || rig.empty) {
      return lef.empty ? rig : lef;
    }
  Info res;
  res.empty = 0;
```

```
res.val = lef.val + rig.val:
 return res:
}:
struct Segtree {
vector<Info> st;
int n:
#define lc id << 1
#define rc id << 1 | 1
#define mi ((1 + r) >> 1)
Segtree() {}
Segtree(int n): n(n), st(n << 2, Info(0)) {
 void update(int i, int x, int id, int l, int r) {
 if (1 == r) {
  st[id].val += x:
  return;
 if (i <= mi) update(i, x, lc, l, mi);</pre>
 else update(i, x, rc, mi+1, r);
 st[id] = st[lc] + st[rc]:
 Info get(int u, int v, int id, int l, int r) {
 if (u > r | | 1 > v) {
  return Info():
 if (u <= 1 && r <= v) {
  return st[id];
 return get(u, v, lc, l, mi) + get(u, v, rc, mi+1, r);
#undef lc
#undef rc
#undef mi
```

${\bf 2.10} \quad {\bf Persistent Segment Tree}$

```
struct PSTNode {
    int val;
    PSTNode *lef, *rig;
    PSTNode (int val) {
        this->val = val;
        lef = rig = nullptr;
    }
    PSTNode (PSTNode *lef, PSTNode *rig) {
        this->lef = lef;
        this->rig = rig;
    }
}
```

```
val = 0:
              if (lef) val += lef->val;
              if (rig) val += rig->val;
       PSTNode (PSTNode *p) {
              this->lef = p->lef:
              this->rig = p->rig;
              this->val = p->val;
       }
};
struct PST {
       int n, nv;
       vector<PSTNode*> rt;
       PST() {}
       PST(int n, int nv, vector<int> vec) {
              this \rightarrow n = n:
              this->nv = nv;
              rt.resize(nv + 1):
              rt[0] = build(1, n, vec);
       }
       PSTNode *build(int 1, int r, vector<int> &vec) {
              if (1 == r) {
                      return new PSTNode(vec[1]);
              int mi = (1 + r) >> 1:
              return new PSTNode(build(1, mi, vec), build(mi
                   +1, r, vec));
       }
       int get(int i, PSTNode *p, int 1, int r) {
              if (1 == r) {
                     return p->val;
              int mi = (1 + r) >> 1:
              if (i <= mi) return get(i, p->lef, l, mi);
              else return get(i, p->rig, mi+1, r);
       int get(int i, int v) {
              return get(i, rt[v], 1, n):
       PSTNode *update(int i, int val, PSTNode *p, int 1,
            int r) {
              if (1 == r) {
                      return new PSTNode(val):
              int mi = (1 + r) >> 1:
              if (i <= mi) return new PSTNode(update(i, val,</pre>
                    p->lef, 1, mi), p->rig);
```

5

2.11 RMQ

```
struct RMQ {
       int n, lg;
       vector<int> v:
       vector<vector<int>> st;
       RMO(vector<int> & v): v(v), n(v.size() - 1) {
              lg = lg(n) + 1:
              st.resize(n + 1, vector<int> (lg + 1));
              for (int i = 1; i <= n; i++) {</pre>
                      st[i][0] = v[i];
              for (int i = 1; i <= lg; i++) {</pre>
                      for (int j = 1; j + (1LL << i) - 1 <= n | #define rc id << 1 | 1
                          ; j++) {
                             st[i][i] = min(st[i][i - 1], st
                                  [j + (1LL << (i - 1))][i -
                                  17):
                      }
       }
       int get(int 1, int r) {
              assert(1 <= r):
              int len = _{-}lg(r - 1 + 1);
              return min(st[1][len], st[r - (1 << len) + 1][
                   len]):
       }
};
```

2.12 RURQ

```
struct Tag {
  int add;
  Tag(): add(0) {}
```

```
Tag(int add): add(add) {}
struct Info {
int val:
 bool emptv = 1:
Info(): val(0) {
 empty = 1;
 Info(int val): val(val) {
 emptv = 0:
 friend Info operator + (Info lef, Info rig) {
 if (lef.empty || rig.empty) {
 return lef.empty ? rig : lef;
 Info res:
 res.empty = 0;
 res.val = lef.val + rig.val:
 return res:
}:
struct Segtree {
vector<Info> st;
vector<Tag> lz;
int n:
#define lc id << 1
#define mi ((1 + r) >> 1)
Segtree() {}
Segtree(int n): n(n), st(n \ll 2, Info(0)), lz(n \ll 2, Tag()
     ) {
 void push(int id, int 1, int r) {
 if (lz[id].add == 0) return:
 int x = 1z[id].add:
 lz[id].add = 0;
 update(1, mi, x, lc, 1, mi);
 update(mi+1, r, x, rc, mi+1, r);
 void update(int u, int v, int x, int id, int l, int r) {
 if (u > r | | 1 > v) {
  return:
 if (u <= 1 && r <= v) {
  st[id].val += x * (r - 1 + 1);
  lz[id].add += x:
  return:
```

```
push(id, 1, r);
  update(u, v, x, lc, 1, mi);
  update(u, v, x, rc, mi+1, r);
  st[id] = st[lc] + st[rc];
}
Info get(int u, int v, int id, int 1, int r) {
  if (u > r || 1 > v) {
    return Info();
  }
  if (u <= 1 && r <= v) {
    return st[id];
  }
  push(id, 1, r);
  return get(u, v, lc, 1, mi) + get(u, v, rc, mi+1, r);
  }
#undef lc
#undef rc
#undef mi
};</pre>
```

2.13 Treap

```
struct Treap {
Treap *lef, *rig;
Treap *par;
int num:
int prio;
int sz:
Treap(int num):
num(num),
prio(rnd()),
sz(1).
par(nullptr),
lef(nullptr).
rig(nullptr) {}
int getsz(Treap *p) {
return (p ? p->sz : 0);
int getnum(Treap *p) {
return (p ? p->num : 0);
void pull(Treap *p) {
if (!p) return;
p->sz = getsz(p->lef) + 1 + getsz(p->rig);
p->par = nullptr;
```

```
if (p\rightarrow lef) p\rightarrow lef\rightarrow par = p:
if (p->rig) p->rig->par = p;
}
void merge(Treap *&p, Treap *lef, Treap *rig) {
 if (!lef || !rig) {
 p = (lef ? lef : rig);
 return;
 if (lef->prio > rig->prio) {
 merge(lef->rig, lef->rig, rig);
 }
 else {
 merge(rig->lef, lef, rig->lef);
 p = rig;
pull(p);
void splitbynum(Treap *p, Treap *&lef, Treap *&rig, int k) {
        if (p == nullptr) {
               lef = rig = nullptr;
               return:
       }
       if (getnum(p) <= k) {</pre>
               splitbynum(p->rig, p->rig, rig, k);
               lef = p:
       }
       else {
               splitbynum(p->lef, lef, p->lef, k);
               rig = p;
       pull(p);
}
void splitbysz(Treap *p, Treap *&lef, Treap *&rig, int k) {
 if (p == nullptr) {
 lef = rig = nullptr;
 return:
 if (getsz(p->lef) < k) {</pre>
 splitbysz(p->rig, p->rig, rig, k - getsz(p->lef) - 1);
 lef = p;
 }
 splitbysz(p->lef, lef, p->lef, k);
 rig = p;
 pull(p);
```

```
int index(Treap *p, Treap *pre = nullptr) {
  if (!p) return OLL;
  if (pre && p->lef == pre) {
    return index(p->par, p);
  }
  else {
    return index(p->par, p) + getsz(p->lef) + 1;
  }
}
```

2.14 Trie

```
struct trie {
trie* ch[2]:
int sum, cnt, end;
 trie() {
 ch[0] = ch[1] = nullptr;
 sum = cnt = end = 0;
};
int MXVAL = 0: // 2^{(MX + 1)} - 1
trie *rt = new trie():
void add(int num) {
auto p = rt:
for (int i = 30; i >= 0; i--) {
 int b = (num >> i) & 1LL;
 if (p->ch[b] == nullptr) p->ch[b] = new trie();
 p = p - ch[b]:
 p->cnt++;
 p->sum += num:
p->end++:
int find(int num) {
auto p = rt;
for (int i = 30; i >= 0; i--) {
 int b = (num >> i) & 1LL:
 if (p->ch[b] == nullptr) return false;
 p = p->ch[b];
return p->end:
bool del(trie *p, int num, int i, int d) {
if (i >= 0) {
 int b = (num >> i) & 1LL;
```

```
if (del(p->ch[b], num, i-1, d)) p->ch[b] = nullptr:
else {
 p->end -= d:
if (p != rt) {
 p->cnt -= d;
 p->sum -= num * d;
 if (p->cnt == 0) {
 delete(p);
  return true:
return false:
void del(int num, int t) {
int d = find(num);
if (d == 0) return;
if (t == 0) del(rt. num. 30, 1):
else del(rt, num, 30, d);
int kth(int k) {
auto p = rt;
int res = 0:
for (int i = 30; i >= 0; i--) {
 for (int b = 0; b < 2; b++) {
 if (p->ch[b]) {
 if (p\rightarrow ch[b]\rightarrow cnt >= k) {
   p = p - ch[b];
   res += (b << i);
    break:
   else {
   k -= p->ch[b]->cnt;
 }
 }
return res;
int sum(int u, int v, trie *p, int l, int r) {
if (u > r || 1 > v || p == nullptr) {
return 0:
if (u <= 1 && r <= v) {
 return p->cnt;
int mi = (1 + r)/2:
return sum(u, v, p->ch[0], 1, mi) + sum(u, v, p->ch[1], mi
```

```
}
int sum(int 1, int r) {
  return sum(1, r, rt, 0, MXVAL);
}
int xr(int num) {
  auto p = rt;
  int res = 0;
  for (int i = 30; i >= 0; i--) {
    int b = (num >> i) & 1LL;
    if (p->ch[1 ^ b] != nullptr) {
      p = p->ch[1 ^ b];
      res |= (1 << i);
    }
  else {
      p = p->ch[b];
    }
  return res;
}
```

2.15 Wavelet

```
struct wavelet {
wavelet *lc. *rc:
vector<int> pf;
int lo. hi:
wavelet(vector<int> a): wavelet(1 + all(a), *min_element(1
     + all(a)), *max_element(1 + all(a))){}
wavelet(vector<int>::iterator 1, vector<int>::iterator r,
     int lo, int hi): lo(lo), hi(hi) {
 if (lo == hi || l >= r) return:
 int mi = lo + (hi - lo)/2;
 pf.reserve(r - 1 + 1):
 pf.push_back(OLL);
 for (auto it = 1; it != r; it++) {
 pf.push_back(pf.back() + (*it <= mi));</pre>
 auto m = stable_partition(1, r, [&](int num) { return num
 lc = new wavelet(1, m, lo, mi);
 rc = new wavelet(m, r, mi+1, hi);
// tim so nho thu k trong doan (1, r);
int kth(int 1, int r, int k) {
 if (1 > r) return 0;
 if (lo == hi) {
 return lo:
```

3 Geometry

3.1 Basic

```
struct Point {
    double x, y;
    Point() { x = y = 0.0; }
    Point(double x, double y) : x(x), y(y) {}
    Point operator + (const Point &a) const { return Point(x
        + a.x, y + a.y); }
    Point operator - (const Point &a) const { return Point(x
        - a.x, y - a.y); }
    Point operator * (double k) const { return Point(x * k, y
    Point operator / (double k) const { return Point(x / k, y
         / k): }
}:
struct Line { // Ax + By = C
    double a. b. c:
    Line(double a = 0, double b = 0, double c = 0): a(a), b(
        b), c(c) {}
    Line(Point A. Point B) {
       a = B.v - A.v;
       b = A.x - B.x;
       c = a * A.x + b * A.y;
}:
Line Perpendicular_Bisector(Point A, Point B) {
```

3.2 ConvexHull

```
// Kiu im
struct Point {
  int x, y;
// Tch c hng ca AB v AC
long long cross(const Point &A, const Point &B, const Point
  return 1LL * (B.x - A.x) * (C.y - A.y) - 1LL * (C.x - A.x)
       ) * (B.v - A.v);
// A -> B -> C i theo th t theo chiu kim
    (-1), thng hng (0), ngc chiu kim
int ccw(const Point &A, const Point &B, const Point &C) {
  long long S = cross(A, B, C);
   if (S < 0) return -1:
  if (S == 0) return 0;
  return 1;
// Tr v bao li vi th t cc
    lit k ngc chiu kim ng
vector<Point> convexHull(vector<Point> p, int n) {
  // a im c tung
                             nh nht (v tri nht)
  for (int i = 1; i < n; ++i) {
      if (p[0].y > p[i].y \mid | (p[0].y == p[i].y && p[0].x >
          p[i].x)) {
         swap(p[0], p[i]);
  }
  // Sp xp cc im I theo gc to bi trc
       honh theo chiu dng v OI
  sort(p.begin() + 1, p.end(), [&p](const Point &A, const
       Point &B) {
      int c = ccw(p[0], A, B);
```

3.3 LineContainer

```
/**
 * Author: Simon Lindholm
 * Date: 2017-04-20
 * License: CCO
 * Source: own work
 * Description: Container where you can add lines of the
      form kx+m, and query maximum values at points x.
 * Useful for dynamic programming (''convex hull trick'').
 * Time: O(\log N)
 * Status: stress-tested
 */
#pragma once
struct Line {
mutable ll k, m, p;
bool operator<(const Line& o) const { return k < o.k; }</pre>
bool operator<(ll x) const { return p < x; }</pre>
}:
struct LineContainer : multiset<Line, less<>>> {
// (for doubles, use inf = 1/.0, div(a,b) = a/b)
 static const 11 inf = LLONG_MAX;
 11 div(11 a, 11 b) { // floored division
 return a / b - ((a ^ b) < 0 && a % b); }
 bool isect(iterator x, iterator y) {
 if (y == end()) return x \rightarrow p = inf, 0;
 if (x->k == y->k) x->p = x->m > y->m ? inf : -inf;
```

```
else x->p = div(y->m - x->m, x->k - y->k);
    return x->p >= y->p;
}
// y = kx + m
void add(ll k, ll m) {
    auto z = insert({k, m, 0}), y = z++, x = y;
    while (isect(y, z)) z = erase(z);
    if (x != begin() && isect(--x, y)) isect(x, y = erase(y));
    while ((y = x) != begin() && (--x)->p >= y->p)
        isect(x, erase(y));
}
ll query(ll x) {
    assert(!empty());
    auto l = *lower_bound(x);
    return l.k * x + l.m;
}
};
```

4 Graphs

4.1 Articular

```
(u == rt && ch[u].size() > 1) || (low[v] >= num[u] for some v in ch[u])
```

4.2 Bellman-Ford

```
x = e.b:
   }
if (x == -1) {
    cout << "No negative cycle found.";</pre>
} else {
    for (int i = 0; i < n; ++i)</pre>
       x = p[x];
    vector<int> cvcle:
    for (int v = x;; v = p[v]) {
        cycle.push_back(v);
        if (v == x && cycle.size() > 1)
           break;
    reverse(cycle.begin(), cycle.end());
    cout << "Negative cycle: ";</pre>
    for (int v : cycle)
        cout << v << ' ';
    cout << endl;</pre>
```

4.3 Bridge

```
low[u] = num[u]
```

4.4 Matching

```
class matching {
      public:
       vector<vector<int>> g;
       vector<int> pa;
       vector<int> pb;
       vector<int> was:
       int n, m;
       int res:
       int iter:
       matching(int _n, int _m) : n(_n), m(_m) {
              assert(0 <= n && 0 <= m);
              pa = vector<int>(n, -1);
              pb = vector < int > (m, -1);
              was = vector<int>(n, 0);
              g.resize(n):
              res = 0;
```

```
iter = 0:
void add(int from, int to) {
       assert(0 \le from \&\& from < n \&\& 0 \le to \&\& to
            < m):
       g[from].push back(to):
bool dfs(int v) {
       was[v] = iter:
       for (int u : g[v]) {
              if (pb[u] == -1) {
                      pa[v] = u:
                      pb[u] = v;
                      return true:
              }
       }
       for (int u : g[v]) {
              if (was[pb[u]] != iter && dfs(pb[u])) {
                      pa[v] = u:
                      pb[u] = v;
                      return true;
              }
       }
       return false;
}
int solve() {
       while (true) {
              iter++:
              int add = 0;
              for (int i = 0: i < n: i++) {</pre>
                      if (pa[i] == -1 && dfs(i)) {
                             add++;
               if (add == 0) {
                      break:
              res += add:
       return res:
int run_one(int v) {
       if (pa[v] != -1) {
              return 0:
       iter++:
       return (int)dfs(v);
```

};

4.5 Maximum Flow

```
// https://pastebin.com/exQM152L
template <typename T>
class flow_graph {
public:
 static constexpr T eps = (T) 1e-9;
 struct edge {
   int to:
   T c:
   Tf;
   int rev:
 };
 vector<vector<edge>> g;
 vector<int> ptr;
 vector<int> d:
 vector<int> q;
 vector<int> cnt_on_layer;
 vector<int> prev_edge;
 bool can_reach_sink;
 int n:
 int st, fin;
 T flow:
 flow_graph(int _n, int _st, int _fin) : n(_n), st(_st),
   assert(0 <= st && st < n && 0 <= fin && fin < n && st !=
        fin):
   g.resize(n):
   ptr.resize(n);
   d.resize(n):
   q.resize(n);
   cnt_on_layer.resize(n + 1);
   prev edge.resize(n):
   flow = 0;
 void clear flow() {
   for (int i = 0; i < n; i++) {</pre>
     for (edge &e : g[i]) {
      e.f = 0;
   }
   flow = 0;
```

```
void add(int from, int to, T forward cap, T backward cap)
 assert(0 <= from && from < n && 0 <= to && to < n);
 int from size = g[from].size();
 int to_size = g[to].size();
 g[from].push_back({to, forward_cap, 0, to_size});
 g[to].push_back({from, backward_cap, 0, from_size});
bool expath() {
 fill(d.begin(), d.end(), n);
 a[0] = fin:
 d[fin] = 0;
 fill(cnt_on_layer.begin(), cnt_on_layer.end(), 0);
 cnt_on_laver[n] = n - 1;
 cnt_on_layer[0] = 1;
 int beg = 0, end = 1;
 while (beg < end) {</pre>
   int i = a[beg++]:
   for (const edge &e : g[i]) {
     const edge &back = g[e.to][e.rev];
     if (back.c - back.f > eps && d[e.to] == n) {
       cnt_on_layer[d[e.to]]--;
       d[e.to] = d[i] + 1;
       cnt_on_layer[d[e.to]]++;
       q[end++] = e.to;
 return (d[st] != n):
T augment(int &v) {
 T cur = numeric_limits<T>::max();
 int i = fin:
 while (i != st) {
   const edge &e = g[i][prev_edge[i]];
   const edge &back = g[e.to][e.rev];
   cur = min(cur, back.c - back.f);
   i = e.to:
 i = fin;
 while (i != st) {
   edge &e = g[i][prev_edge[i]];
   edge &back = g[e.to][e.rev];
   back.f += cur:
   e.f -= cur;
   i = e.to:
   if (back.c - back.f <= eps) {</pre>
     v = i:
```

```
}
 return cur;
int retreat(int v) {
 int new_dist = n - 1;
 for (const edge &e : g[v]) {
   if (e.c - e.f > eps && d[e.to] < new_dist) {</pre>
     new_dist = d[e.to];
 cnt_on_layer[d[v]]--;
 if (cnt_on_layer[d[v]] == 0) {
   if (new dist + 1 > d[v]) {
     can_reach_sink = false;
 d[v] = new dist + 1:
 cnt on laver[d[v]]++:
 if (v != st) {
   v = g[v][prev_edge[v]].to;
 return v;
T max flow() {
 can reach sink = true:
 for (int i = 0; i < n; i++) {</pre>
   ptr[i] = (int) g[i].size() - 1:
  if (expath()) {
   int v = st:
   while (d[st] < n) {
     while (ptr[v] >= 0) {
       const edge &e = g[v][ptr[v]];
       if (e.c - e.f > eps && d[e.to] == d[v] - 1) {
        prev_edge[e.to] = e.rev;
        v = e.to;
         if (v == fin) {
          flow += augment(v):
         break:
       ptr[v]--;
     if (ptr[v] < 0) {</pre>
       ptr[v] = (int) g[v].size() - 1;
       v = retreat(v):
       if (!can reach sink) {
```

4.6 Minimum Cost Maximum Flow

```
#include <bits/extc++.h>
template <typename T, typename C>
class MCMF {
public:
 static constexpr T eps = (T) 1e-9;
 struct edge {
   int from;
   int to:
   T c:
   T f:
   C cost:
 };
 vector<vector<int>> g;
 vector<edge> edges;
 vector<C> d:
 vector<C> pot:
 __gnu_pbds::priority_queue<pair<C, int>> q;
 vector<typename decltype(q)::point_iterator> its;
 vector<int> pe;
 const C INF C = numeric limits<C>::max() / 2:
 explicit MCMF(int n_{-}) : n(n_{-}), g(n), d(n), pot(n, 0), its(
      n), pe(n) {}
```

```
int add(int from, int to, T forward cap, T backward cap, C
     edge cost) {
 assert(0 <= from && from < n && 0 <= to && to < n);
 assert(forward cap >= 0 && backward cap >= 0):
 int id = static_cast<int>(edges.size());
 g[from].push back(id):
 edges.push_back({from, to, forward_cap, 0, edge_cost});
 g[to].push_back(id + 1);
 edges.push_back({to, from, backward_cap, 0, -edge_cost});
void expath(int st) {
 fill(d.begin(), d.end(), INF_C);
 g.clear():
 fill(its.begin(), its.end(), q.end());
 its[st] = q.push({pot[st], st});
 d[st] = 0;
 while (!a.emptv()) {
   int i = q.top().second;
   q.pop();
   its[i] = q.end();
   for (int id : g[i]) {
     const edge &e = edges[id];
     int j = e.to;
     if (e.c - e.f > eps && d[i] + e.cost < d[j]) {</pre>
      d[j] = d[i] + e.cost;
      pe[i] = id:
      if (its[j] == q.end()) {
        its[j] = q.push({pot[j] - d[j], j});
      } else {
        q.modify(its[j], {pot[j] - d[j], j});
   }
 swap(d, pot);
pair<T. C> max flow min cost(int st, int fin) {
 T flow = 0:
 C cost = 0:
 bool ok = true:
 for (auto& e : edges) {
   if (e.c - e.f > eps && e.cost + pot[e.from] - pot[e.to]
         < 0) {
     ok = false;
     break:
 }
```

```
if (ok) {
  expath(st);
} else {
 vector<int> deg(n, 0);
 for (int i = 0; i < n; i++) {</pre>
   for (int eid : g[i]) {
     auto& e = edges[eid];
     if (e.c - e.f > eps) {
       deg[e.to] += 1;
   }
  }
  vector<int> que;
  for (int i = 0; i < n; i++) {</pre>
   if (deg[i] == 0) {
     que.push_back(i);
 }
 for (int b = 0; b < (int) que.size(); b++) {</pre>
   for (int eid : g[que[b]]) {
     auto& e = edges[eid];
     if (e.c - e.f > eps) {
       deg[e.to] -= 1;
       if (deg[e.to] == 0) {
         que.push_back(e.to);
   }
 fill(pot.begin(), pot.end(), INF_C);
 pot[st] = 0;
  if (static_cast<int>(que.size()) == n) {
   for (int v : que) {
     if (pot[v] < INF_C) {</pre>
       for (int eid : g[v]) {
         auto& e = edges[eid]:
         if (e.c - e.f > eps) {
           if (pot[v] + e.cost < pot[e.to]) {</pre>
             pot[e.to] = pot[v] + e.cost;
            pe[e.to] = eid;
        }
     }
  } else {
   que.assign(1, st);
   vector<bool> in_queue(n, false);
   in_queue[st] = true;
   for (int b = 0; b < (int) que.size(); b++) {</pre>
```

```
int i = que[b]:
         in_queue[i] = false;
         for (int id : g[i]) {
           const edge &e = edges[id];
           if (e.c - e.f > eps && pot[i] + e.cost < pot[e.to</pre>
            pot[e.to] = pot[i] + e.cost;
            pe[e.to] = id;
            if (!in_queue[e.to]) {
              que.push_back(e.to);
              in_queue[e.to] = true;
   while (pot[fin] < INF_C) {</pre>
     T push = numeric limits<T>::max():
     int v = fin:
     while (v != st) {
       const edge &e = edges[pe[v]];
       push = min(push, e.c - e.f);
       v = e.from:
     v = fin;
     while (v != st) {
       edge &e = edges[pe[v]];
       e.f += push;
       edge &back = edges[pe[v] ^ 1];
       back.f -= push;
       v = e.from;
     flow += push;
     cost += push * pot[fin];
     expath(st):
   return {flow, cost};
};
```

4.7 SCC

```
void tarjan(int u, int p) {
  in[u] = low[u] = ++curdfs;
  st.push(u);
  for (int v : adj[u]) {
   if (!in[v]) {
    tarjan(v, u);
  }
}
```

```
low[u] = min(low[u], low[v]);
} else if (!del[v]) {
low[u] = min(low[u], in[v]);
}
if (low[u] == in[u]) {
int v;
do {
  v = st.top();
  st.pop();
  scc[u].push_back(v);
  top[v] = u;
  del[v] = true;
} while (v != u);
};
```

4.8 Topological Sort

```
void kahn(int u) {
  din[u] = -1;
  topo.push_back(u);
  for (int v : aa[u]) {
    din[v]--;
    if (din[v] == 0) kahn(v);
  }
}
```

4.9 TwoSatSolver

```
struct TSS {
       int nvar. nvrt:
       vector<vector<int>> adj;
       vector<bool> res;
       TSS(int nvar): nvar(nvar), nvrt(nvar * 2), adj(nvrt +
            1), res(nvar + 1) {}
       int coni(int u) {
              if (u > nvar) return u - nvar;
              return u + nvar:
       int operator[](int i) { return res[i]; }
       void add(int u, bool nu, int v, bool nv) {
              if (nu) u = coni(u):
              if (nv) v = conj(v);
              adj[u].push_back(v);
       }
       bool solve() {
```

```
vector<int> in(nvrt + 1). low(nvrt + 1). id(
           nvrt + 1):
       stack<int> st:
       int curdfs = 0, curidx = 2 * nvrt + 1;
       auto tarjan = [&](auto&& f, int u) -> void {
              in[u] = low[u] = ++curdfs;
              st.push(u);
              for (int v : adj[u]) {
                     if (!in[v]) {
                             f(f, v);
                             low[u] = min(low[u], low
                                  [v]):
                     } else if (!id[v]) {
                             low[u] = min(low[u], in[
                     }
              }
              if (low[u] == in[u]) {
                     int v:
                     do {
                             v = st.top();
                             st.pop();
                             id[v] = curidx;
                     } while (v != u):
                     --curidx:
              }
       }:
       for (int i = 1: i <= nvrt: i++)</pre>
              if (!in[i]) tarjan(tarjan, i);
       for (int i = 1: i <= nvar: i++) {
              if (id[i] == id[conj(i)]) return false;
              res[i] = id[i] > id[conj(i)];
       return true;
}
```

5 Maths

5.1 Matrix

```
// S lng hng ca ma trn
int col() const { return data[0].size(); }
auto & operator [] (int i) { return data[i]; }
const auto & operator[] (int i) const { return data[i]: }
Matrix() = default;
Matrix(int r, int c): data(r, vector <type> (c)) { }
Matrix(const vector <vector <tvpe> > &d): data(d) {
   // Kim tra cc hng c cng size khng v size c
          ln hn O hav khng
   // Tuy nhin khng the s en thit, ta e
         th b cc dng /**/ i
   /**/ assert(d.size());
   /**/ int size = d[0].size():
   /**/ assert(size):
   /**/ for (auto x : d) assert(x.size() == size);
// In ra ma trn.
friend ostream & operator << (ostream &out, const Matrix</pre>
   for (auto x : d.data) {
      for (auto v : x) out << v << ' ':
      out << '\n';
   return out;
// Ma trn n v
static Matrix identity(long long n) {
   Matrix a = Matrix(n, n):
   while (n--) a[n][n] = 1;
   return a:
}
// Nhn ma trn
Matrix operator * (const Matrix &b) {
   Matrix a = *this:
   // Kim tra iu kin nhn ma trn
   assert(a.col() == b.row());
   Matrix c(a.row(), b.col()):
   for (int i = 0; i < a.row(); ++i)</pre>
      for (int j = 0; j < b.col(); ++j)</pre>
```

5.2 Mod Int

```
struct M {
   int MOD:
   explicit operator int() const { return v; }
   M() {}
   M(int MOD) : v(0), MOD(MOD) {}
   M(int_v, int_MOD) : MOD(MOD), v(v MOD) { v += (v < 0)}
        * MOD: }
   M& operator+=(M o) {
      if ((v += o.v) >= MOD) v -= MOD:
      return *this;
   M& operator-=(M o) {
       if ((v -= o.v) < 0) v += MOD;
       return *this:
   }
   M& operator*=(M o) {
      v = (int)((long long)v * o.v % MOD); // Use long long
            to prevent overflow
      return *this:
   }
   friend M binpow(M a, int p) {
       assert(p >= 0);
      return p == 0 ? M(1, a.MOD) : binpow(a * a, p / 2) *
           (p & 1 ? a : M(1, a.MOD));
```

```
friend M inv(M a) {
       assert(a.v != 0);
       return binpow(a, a.MOD - 2);
    friend M operator+(M a, M b) { return a += b; }
    friend M operator-(M a, M b) { return a -= b; }
    friend M operator*(M a, M b) { return a *= b; }
    friend M operator/(M a, M b) { return a *= inv(b); }
    friend ostream& operator << (ostream& out. M a) { return (
        out << a.v): }
};
template<int... MODS>
struct bigM {
    static const int size = sizeof...(MODS):
    static constexpr array<int, size> mods = {MODS...}:
       for (int i = 0; i < size; ++i) {</pre>
           v[i] = M(mods[i]):
    bigM(int v) {
       for (int i = 0; i < size; ++i) {</pre>
           v[i] = M(v, mods[i]):
       }
    }
    bigM& operator+=(bigM o) {
       for (int i = 0; i < size; i++) {</pre>
           v[i] += o.v[i]:
       }
       return *this:
    bigM& operator-=(bigM o) {
       for (int i = 0: i < size: i++) {</pre>
           v[i] -= o.v[i];
       return *this:
    bigM& operator*=(bigM o) {
       for (int i = 0; i < size; i++) {</pre>
           v[i] *= o.v[i];
       return *this;
    bigM& operator/=(bigM o) {
```

for (int i = 0: i < size: i++) {

```
v[i] /= o.v[i]:
      return *this:
   friend bigM binpow(bigM a, int p) {
      assert(p >= 0):
       return p == 0? bigM(1): binpow(a * a, p / 2) * (p &
            1 ? a : bigM(1)):
   friend bigM inv(bigM a) {
       bigM res:
       for (int i = 0: i < size: i++) {</pre>
          res.v[i] = inv(a.mods[i]):
       return res:
   friend bool operator==(bigM a, bigM b) {
      for (int i = 0; i < size; i++) {</pre>
          if (a.v[i].v != b.v[i].v) return false:
       return true;
   friend bool operator!=(bigM a, bigM b) {
       return !(a == b):
   friend bigM operator+(bigM a, bigM b) { return a += b; }
   friend bigM operator-(bigM a, bigM b) { return a -= b; }
   friend bigM operator*(bigM a, bigM b) { return a *= b; }
   friend bigM operator/(bigM a, bigM b) { return a /= b; }
using MM = bigM<1035972859, 1704760909, 1234567891>;
```

5.3 Precal Modulo Inverse

```
int n = 10, p = 1000000007;
int inv[n + 1];
inv[1] = 1;
for (int i = 2; i <= n; i ++) inv[i] = 1LL * (p - p / i) *
    inv[p % i] % p;
```

5.4 Rabin-Miller

```
using u64 = uint64_t;
using u128 = __uint128_t;
u64 binpower(u64 base, u64 e, u64 mod) {
```

```
u64 result = 1:
   base %= mod:
   while (e) {
       if (e & 1)
          result = (u128)result * base % mod;
       base = (u128)base * base % mod:
   return result:
bool check composite(u64 n. u64 a. u64 d. int s) {
   u64 x = binpower(a, d, n);
   if (x == 1 | | x == n - 1)
       return false:
   for (int r = 1; r < s; r++) {</pre>
       x = (u128)x * x % n:
       if (x == n - 1)
          return false:
   return true:
};
bool MillerRabin(u64 n) { // returns true if n is prime,
    else returns false.
   if (n < 2)
       return false:
   int r = 0:
   u64 d = n - 1:
   while ((d & 1) == 0) {
       d >>= 1:
       r++:
   for (int a: {2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31,
        37}) {
       if (n == a)
          return true;
       if (check_composite(n, a, d, r))
          return false;
   return true:
```

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6 Miscellaneous

6.1 Clion

```
set(GCC_COVERAGE_COMPILE_FLAGS "-02 -Dbinhball")
set(CMAKE_CXX_FLAGS "${CMAKE_CXX_FLAGS} ${
    GCC_COVERAGE_COMPILE_FLAGS}")
```

6.2 Debug

```
#ifdef hvmegy
#define dbg(...) logger(#__VA_ARGS__, __VA_ARGS__)
template<typename ...Args>
void logger(string vars, Args&&... values) {
  cerr << "[" << vars << " : ";
  string delim = "";
  (..., (cerr << delim << values, delim = ", "));
  cerr << "]" << '\n';
}
#else
#define dbg(...)
#endif</pre>
```

6.3 mt19937

6.4 time

```
cerr << '\n' << clock() * 1000.0 / CLOCKS_PER_SEC << "ms" << '\n';
```

7 Strings

7.1 Aho Corasick

```
struct aho_corasick{
    struct node{
        int suffix_link = -1, exit_link = -1, nxt[128];
        vector<int> leaf;
        node() {fill(nxt, nxt+128, -1);}
```

```
vector<node> g = {node()};
void insert_string(const string &s, int sidx){
   int p = 0:
   for (char c: s){
       if (g[p].nxt[c] == -1){
           g[p].nxt[c] = g.size();
           g.emplace_back();
       p = g[p].nxt[c];
   g[p].leaf.push_back(sidx);
}
void build_automaton(){
   for (deque<int> q = {0}; q.size(); q.pop_front()){
       int v = q.front(), suffix_link = g[v].suffix_link
       if (v) g[v].exit_link = g[suffix_link].leaf.size
            () ? suffix link : g[suffix link].exit link:
       for (int i=0: i<128: i++){</pre>
          int &nxt = g[v].nxt[i], nxt_sf = v ? g[
               suffix_link].nxt[i] : 0;
          if (nxt == -1) nxt = nxt_sf;
              g[nxt].suffix_link = nxt_sf;
              q.push_back(nxt);
       }
   }
vector<int> get_sindex(int p){
   vector<int> a;
   for (int v = g[p].leaf.size() ? p : g[p].exit_link; v
         !=-1; v = g[v].exit_link)
       for (int j: g[v].leaf)
          a.push_back(j);
   return a;
```

7.2 Hash

```
const int mod1 = 1035972859;
const int mod2 = 1704760909;
const int base = ;
struct hashing{
   int mod, n;
   vector<int> h, power;
   int binpow(int a, int n){
```

```
if (n == 0)
                     return 1LL:
              int res = binpow(a, n/2);
              if (n % 2)
                     return res * res % mod * a % mod;
              return res * res % mod:
       }
       hashing() {}
       hashing(string s, int mod): mod(mod){
              this->n = s.length();
              power = h = vector<int> (n):
              power[0] = 1:
              h[0] = s[0];
              for (int i = 1; i < n; i++){</pre>
                     power[i] = power[i - 1] * base % mod;
                     h[i] = (h[i - 1] * base + s[i]) % mod;
              }
       }
       int getH(int 1, int r){
              return (!1 ? h[r] : (h[r] - h[1 - 1] * power[r
                    -1 + 1] + mod * mod) % mod):
       }
};
struct bighash{
       bighash() {}
       hashing a. b:
       bighash(string s){
              a = hashing(s, mod1);
              b = hashing(s, mod2);
       int get(int 1, int r){
              return a.getH(1, r) * b.getH(1, r);
};
```

7.3 KMP

```
int next_x[N];
   int j = next_x[0] = 0;
   n = s.length();
   m = t.length();
   for (int i = 1; i < n; i++){
      while (j > 0 && s[j] != s[i]){
            j = next_x[j - 1];
      }
      if (s[i] == s[j])
            j++;
```

```
next_x[i] = j;
}
j = 0;
for (int i = 0; i < m; i++){
   while (j > 0 && s[j] != t[i])
        j = next_x[j - 1];
   if (s[j] == t[i])
        j++;
   if (j == n){
        cout << i - n + 2 << " ";
}
}</pre>
```

7.4 Z Function

```
z[0] = n;

int 1 = 0, r = 0;

for (int i = 1; i < n; i++){

if (i > r){

    1 = r = i;

    while (r < n && s[r] == s[r-1]) ++r;

    z[i] = r - 1;

    r-=1;

}

else{
```