Team Notebook

HopeNBH

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Contents

1 DP

1.1 Divide and Conquer

```cpp
int m, n;
vector<long long> dp_before(n), dp_cur(n);

long long C(int i, int j);

// compute dp_cur[l], ... dp_cur[r] (inclusive)
void compute(int l, int r, int optl, int optr) {
    if (l > r)
        return;

    int mid = (l + r) >> 1;
    pair<long long, int> best = {LLONG_MAX, -1};

    for (int k = optl; k <= min(mid, optr); k++) {
        best = min(best, {(k ? dp_before[k - 1] : 0) + C(k,
             mid), k});
    }

    dp_cur[mid] = best.first;
    int opt = best.second;

    compute(l, mid - 1, optl, opt);
    compute(mid + 1, r, opt, optr);
}

int solve() {
    for (int i = 0; i < n; i++)
        dp_before[i] = C(0, i);

    for (int i = 1; i < m; i++) {
        compute(0, n - 1, 0, n - 1);
        dp_before = dp_cur;
    }

    return dp_before[n - 1];
}
```

2 Data Structures

2.1 Centroid Decomposition

```cpp
vector<vector<int>> adj;
vector<bool> is_removed;
vector<int> subtree_size;

/** DFS to calculate the size of the subtree rooted at `node
    ` */
int get_subtree_size(int node, int parent = -1) {
 subtree_size[node] = 1;
 for (int child : adj[node]) {
  if (child == parent || is_removed[child]) { continue; }
  subtree_size[node] += get_subtree_size(child, node);
 }
 return subtree_size[node];
}

/**
 * Returns a centroid (a tree may have two centroids) of the
      subtree
 * containing node `node` after node removals
 * @param node current node
 * @param tree_size size of current subtree after node
     removals
 * @param parent parent of u
 * @return first centroid found
 */
int get_centroid(int node, int tree_size, int parent = -1) {
 for (int child : adj[node]) {
  if (child == parent || is_removed[child]) { continue; }
  if (subtree_size[child] * 2 > tree_size) {
   return get_centroid(child, tree_size, node);
  }
 }
 return node;
}

/** Build up the centroid decomposition recursively */
void build_centroid_decomp(int node = 0) {
 int centroid = get_centroid(node, get_subtree_size(node));

 // do something

 is_removed[centroid] = true;


 for (int child : adj[centroid]) {
  if (is_removed[child]) { continue; }
  build_centroid_decomp(child);

 }

}
```

2.2 DSU Tree

```cpp
struct DSUTree {
 vector<int> par, in, out, val, d;
 vector<vector<int>> adj;
 vector<vector<int>> up, mx;
 int num, n;
 int cur = 0;
 int find(int v) {
  while (v != par[v]) v = par[v] = par[par[v]];
  return v;
 }
 int newnode() {
  num++;
  par.push_back({});
  adj.push_back({});
  in.push_back({});
  out.push_back({});
  val.push_back({});
  d.push_back({});
  par[num] = num;
  return num;
 }
 bool join(int u, int v, int i) {
  u = find(u);
  v = find(v);
  if (u == v) return false;
  int p = newnode();
  val[p] = i;
  par[u] = par[v] = p;
  adj[p].push_back(u);
  adj[p].push_back(v);
  return true;
 }
 void init(int n) {
  num = this->n = n;
  adj.resize(n + 1);
  par.resize(n + 1);
  in.resize(n + 1);
  out.resize(n + 1);
  val.resize(n + 1);
  d.resize(n + 1);
  iota(all(par), 0);
 }
 void dfs(int u) {
  in[u] = ++cur;
  for (int v : adj[u]) {
   d[v] = d[u] + 1;
   up[v][0] = u;
   mx[v][0] = max(val[v], val[u]);
```

```
  dfs(v);
 }
 out[u] = cur;
}
void work() {
 up = mx = vector<vector<int>>(num + 1, vector<int> (18));
 for (int i = 1; i <= num; i++) {
  if (i == find(i)) {
   up[i][0] = i;
   mx[i][0] = val[i];
   dfs(i);
  }
 }
 for (int i = 1; i <= 18; i ++) {
  for (int u = 1; u <= num; u++) {
   up[u][i] = up[up[u][i-1]][i-1];
   mx[u][i] = max(mx[u][i-1], mx[up[u][i-1]][i-1]);
  }
 }
}
pair<int, int> LCA(int u, int v) {
 int ans = max(val[u], val[v]);
 if (d[u] < d[v]) swap(u, v);
 int det = d[u] - d[v];
 for (int i = 18; i >= 0; i--) {
  if ((det >> i) & 1) {
   ans = max(ans, mx[u][i]);
   u = up[u][i];
  }
 }
 if (u == v) {
  return {u, ans};
 }
 for (int i = 18; i >= 0; i--) {
  if (up[u][i] != up[v][i]) {
   ans = max({ans, mx[u][i], mx[v][i]});
   u = up[u][i];
   v = up[v][i];
  }
 }
 return {up[v][0], max({ans, up[u][0], up[v][0]})};
}
};
```

2.3 DSU

```
struct DSU {
	int n;
	vector<int> par, sz;
	DSU(int n): n(n) {
		par = sz = vector<int> (n + 1);
		fill(all(sz), 1LL);
		iota(all(par), 0LL);
	}
	int find(int v) {
		while (v != par[v]) v = par[v] = par[par[v]];
		return v;
	}

	bool join(int u, int v) {
		u = find(u);
		v = find(v);
		if (u == v) return false;
		if (sz[u] < sz[v]) swap(u, v);
		sz[u] += sz[v];
		par[v] = u;
		return true;
	}

	int same(int u, int v) {
		return find(u) == find(v);
	}
};
```

2.4 Fenwick

```
struct fenwick {
	vector<int> f;
	int n;
	fenwick(int n): n(n) {
		f.resize(n + 1);
	}
	void add(int i, int v) {
		for (; i <= n; i += i & -i) f[i] += v;
	}
	int get(int i) {
		int ans = 0;
		for (; i >= 1; i -= i & -i) ans += f[i];
		return ans;
	}
	int range(int u, int v) {
		return get(v) - get(u-1);
	}
};
```

2.5 HLD

```
struct HLD {
	int n;
	int root;
	vector<int> sz, par, dep, top, in, out, seq;
	vector<vector<int>> adj;
	int curdfs = 0;
	HLD(int n): n(n) {
		par = sz = dep = top = in = out = seq = vector
		    <int> (n + 1);
		adj.resize(n + 1);
	}

	void edge(int u, int v) {
		adj[u].push_back(v);
		adj[v].push_back(u);
	}

	void start(int root = 1) {
		this->root = root;
		par[root] = root;
		top[root] = root;
		dfssz(root);
		dfshld(root);
	}

	void dfssz(int u) {
		if (u != root) {
			adj[u].erase(find(all(adj[u]), par[u]))
			    ;
		}
		sz[u] = 1;
		for (int &v : adj[u]) {
			dep[v] = dep[u] + 1;
			par[v] = u;
			dfssz(v);
			sz[u] += sz[v];
			if (sz[v] > sz[adj[u][0]]) {
				swap(adj[u][0], v);
			}
		}
	}

	void dfshld(int u) {
		in[u] = ++curdfs;
		seq[in[u]] = u;
		for (int v : adj[u]) {
			top[v] = (v == adj[u][0] ? top[u] : v);
			dfshld(v);
```

```
            }
            out[u] = curdfs;
        }

        int lca(int u, int v) {
            while (top[u] != top[v]) {
                if (dep[top[u]] > dep[top[v]]) {
                    u = par[top[u]];
                }
                else {
                    v = par[top[v]];
                }
            }
            return (dep[u] < dep[v] ? u : v);
        }

        bool isancestor(int u, int v) {
            return in[u] <= in[v] && out[v] <= out[u];
        }
};
```

2.6 Link-Cut Tree

```
#include <bits/stdc++.h>
using namespace std;

// BeginCodeSnip{Link Cut Tree}
struct Node {
 int x;
 Node *l = 0;
 Node *r = 0;
 Node *p = 0;
 bool rev = false;

 Node() = default;

 Node(int v) { x = v; }

 void push() {
  if (rev) {
   rev = false;
   swap(l, r);
   if (l) l->rev ^= true;
   if (r) r->rev ^= true;
  }
 }

 bool is_root() { return p == 0 || (p->l != this && this !=
     p->r); }
};

struct LCT {
 vector<Node> a;

 LCT(int n) {
  a.resize(n + 1);
  for (int i = 1; i <= n; ++i) a[i].x = i;
 }

 void rot(Node *c) {
  auto p = c->p;
  auto g = p->p;

  if (!p->is_root()) (g->r == p ? g->r : g->l) = c;

  p->push();
  c->push();

  if (p->l == c) { // rtr
   p->l = c->r;
   c->r = p;
   if (p->l) p->l->p = p;
  } else { // rtl
   p->r = c->l;
   c->l = p;
   if (p->r) p->r->p = p;
  }

  p->p = c;
  c->p = g;
 }

 void splay(Node *c) {
  while (!c->is_root()) {
   auto p = c->p;
   auto g = p->p;
   if (!p->is_root()) rot((g->r == p) == (p->r == c) ? p : c
       );
   rot(c);
  }
  c->push();
 }

 Node *access(int v) {
  Node *last = 0;
  Node *c = &a[v];
  for (Node *p = c; p; p = p->p) {
   splay(p);
   p->r = last;
   last = p;
  }
  splay(c);
  return last;
 }

 void make_root(int v) {
  access(v);
  auto *c = &a[v];
  if (c->l) c->l->rev ^= true, c->l = 0;
 }

 void link(int u, int v) {
  make_root(v);
  Node *c = &a[v];
  c->p = &a[u];
 }

 void cut(int u, int v) {
  make_root(u);
  access(v);
  if (a[v].l) {
   a[v].l->p = 0;
   a[v].l = 0;
  }
 }

 bool connected(int u, int v) {
  access(u);
  access(v);
  return a[u].p;
 }
};
// EndCodeSnip

int N, M;

int main() {
 cin.tie(0)->sync_with_stdio(0);

 cin >> N >> M;

 LCT lc(N);

 while (M--) {
  string a;
  cin >> a;
  int b, c;
  cin >> b >> c;
  if (a == "add") { lc.link(b, c); }
```

```
  if (a == "rem") { lc.cut(b, c); }

  if (a == "conn") {
   cout << (lc.connected(b, c) ? "YES" : "NO") << "\n";
  }
 }
}
```

2.7 Ordered Set

```
#include <bits/stdc++.h>
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>

using namespace std;
using namespace __gnu_pbds;
template <class type1>
using ordered_set = tree<type1, null_type, less_equal<type1
    >, rb_tree_tag, tree_order_statistics_node_update>;
```

2.8 Persistent Segment Tree

```
struct Node {
	int val;
	Node *lef, *rig;
	Node (int val) {
		this->val = val;
		lef = rig = nullptr;
	}
	Node (Node *lef, Node *rig) {
		this->lef = lef;
		this->rig = rig;
	}
	Node (Node *p) {
		this->lef = p->lef;
		this->rig = p->rig;
		this->val = p->val;
	}
};

struct PSegtree {
	int n, nv;
	vector<Node*> rt;
	PSegtree() {}
	PSegtree(int n, int nv, vector<int> vec) {
		this->n = n;
		this->nv = nv;
		rt.resize(nv + 1);
		rt[0] = build(1, n, vec);
	}

	Node *build(int l, int r, vector<int> &vec) {
		if (l == r) {
			return new Node(vec[l]);
		}
		int mi = (l + r) >> 1;
		return new Node(build(l, mi, vec), build(mi+1,
		    r, vec));
	}

	int get(int i, Node *p, int l, int r) {
		if (l == r) {
			return p->val;
		}
		int mi = (l + r) >> 1;
		if (i <= mi) return get(i, p->lef, l, mi);
		else return get(i, p->rig, mi+1, r);
	}
	int get(int i, int v) {
		return get(i, rt[v], 1, n);
	}
	Node *update(int i, int val, Node *p, int l, int r) {
		if (l == r) {
			return new Node(val);
		}
		int mi = (l + r) >> 1;
		if (i <= mi) return new Node(update(i, val, p
		    ->lef, l, mi), p->rig);
		else return new Node(p->lef, update(i, val, p
		    ->rig, mi+1, r));
	}

	void update(int i, int val, int v) {
		rt[v] = update(i, val, rt[v], 1, n);
	}

	void copy(int t1, int t2) {
		rt[t2] = rt[t1];
	}
};
```

2.9 RMQ

```
struct RMQ {
	int n, lg;
	vector<int> v;
	vector<vector<int>> st;
	RMQ(vector<int> & v): v(v), n(v.size() - 1) {
		lg = __lg(n) + 1;
		st.resize(n + 1, vector<int> (lg + 1));
		for (int i = 1; i <= n; i++) {
			st[i][0] = v[i];
		}
		for (int i = 1; i <= lg; i++) {
			for (int j = 1; j + (1LL << i) - 1 <= n
			    ; j++) {
				st[j][i] = min(st[j][i - 1], st
				    [j + (1LL << (i - 1))][i -
				    1]);
			}
		}
	}
	int get(int l, int r) {
		int len = __lg(r - l + 1);
		return min(st[l][len], st[r - (1 << len) + 1][
		    len]);
	}
};
```

2.10 Treap

```
struct Treap {
 Treap *lef, *rig;
 int num;
 int prio;
 int sz;
 Treap(int num):
 num(num),
 prio(rnd()),
 sz(1),
 lef(nullptr),
 rig(nullptr) {}
};

int sz(Treap *p) {
 return (p ? p->sz : 0);
}

void pull(Treap *p) {
 if (!p) return;
 p->sz = sz(p->lef) + 1 + sz(p->rig);
}
```

```
void merge(Treap *&p, Treap *lef, Treap *rig) {
 if (!lef || !rig) {
  p = (lef ? lef : rig);
  return;
 }
 if (lef->prio > rig->prio) {
  merge(lef->rig, lef->rig, rig);
  p = lef;
 }
 else {
  merge(rig->lef, lef, rig->lef);
  p = rig;
 }
 pull(p);
}

void split(Treap *p, Treap *&lef, Treap *&rig, int k) {
 if (!p) {
  lef = rig = nullptr;
  return;
 }
 if (sz(p->lef) < k) {
  split(p->rig, p->rig, rig, k - 1 - sz(p->lef));
  lef = p;
 }
 else {
  split(p->lef, lef, p->lef, k);
  rig = p;
 }
 pull(p);
}
```

2.11 Trie

```
struct trie {
 trie* ch[2];
 int sum, cnt, end;
 trie() {
  ch[0] = ch[1] = nullptr;
  sum = cnt = end = 0;
 }
};

int MXVAL = 0; // 2^(MX + 1) - 1

trie *rt = new trie();
void add(int num) {
 auto p = rt;
 for (int i = 30; i >= 0; i--) {
  int b = (num >> i) & 1LL;
  if (p->ch[b] == nullptr) p->ch[b] = new trie();
  p = p->ch[b];
  p->cnt++;
  p->sum += num;
 }
 p->end++;
}
int find(int num) {
 auto p = rt;
 for (int i = 30; i >= 0; i--) {
  int b = (num >> i) & 1LL;
  if (p->ch[b] == nullptr) return false;
  p = p->ch[b];
 }
 return p->end;
}
bool del(trie *p, int num, int i, int d) {
 if (i >= 0) {
  int b = (num >> i) & 1LL;
  if (del(p->ch[b], num, i-1, d)) p->ch[b] = nullptr;
 }
 else {
  p->end -= d;
 }
 if (p != rt) {
  p->cnt -= d;
  p->sum -= num * d;
  if (p->cnt == 0) {
   delete(p);
   return true;
  }
 }
 return false;
}
void del(int num, int t) {
 int d = find(num);
 if (d == 0) return;
 if (t == 0) del(rt, num, 30, 1);
 else del(rt, num, 30, d);
}
int kth(int k) {
 auto p = rt;
 int res = 0;
 for (int i = 30; i >= 0; i--) {
  for (int b = 0; b < 2; b++) {
   if (p->ch[b]) {
    if (p->ch[b]->cnt >= k) {
     p = p->ch[b];
     res += (b << i);
     break;
    }
    else {
     k -= p->ch[b]->cnt;
    }
   }
  }
 }
 return res;
}
int sum(int u, int v, trie *p, int l, int r) {
 if (u > r || l > v || p == nullptr) {
  return 0;
 }
 if (u <= l && r <= v) {
  return p->cnt;
 }
 int mi = (l + r)/2;
 return sum(u, v, p->ch[0], l, mi) + sum(u, v, p->ch[1], mi
     +1, r);
}
int sum(int l, int r) {
 return sum(l, r, rt, 0, MXVAL);
}
int xr(int num) {
 auto p = rt;
 int res = 0;
 for (int i = 30; i >= 0; i--) {
  int b = (num >> i) & 1LL;
  if (p->ch[1 ^ b] != nullptr) {
   p = p->ch[1 ^ b];
   res |= (1 << i);
  }
  else {
   p = p->ch[b];
  }
 }
 return res;
}
```

2.12 Wavelet

```
struct wavelet {
 wavelet *lc, *rc;
 vector<int> pf;
 int lo, hi;

 wavelet(vector<int> a): wavelet(1 + all(a), *min_element(1
     + all(a)), *max_element(1 + all(a))){}
```

```
 wavelet(vector<int>::iterator l, vector<int>::iterator r,
     int lo, int hi): lo(lo), hi(hi) {
  if (lo == hi || l >= r) return;
  int mi = lo + (hi - lo)/2;
  pf.reserve(r - l + 1);
  pf.push_back(0LL);
  for (auto it = l; it != r; it++) {
   pf.push_back(pf.back() + (*it <= mi));
  }
  auto m = stable_partition(l, r, [&](int num) { return num
      <= mi; });
  lc = new wavelet(l, m, lo, mi);
  rc = new wavelet(m, r, mi+1, hi);
 }
 // tim so nho thu k trong doan (l, r);
 int kth(int l, int r, int k) {
  if (l > r) return 0;
  if (lo == hi) {
   return lo;
  }
  int lef = pf[r] - pf[l-1];
  if (lef >= k) return lc->kth(pf[l-1] + 1, pf[r], k);
  else return rc->kth(l - pf[l-1], r - pf[r], k - lef);
 }
 // dem so > k trong doan (l r)
 int count(int l, int r, int num) {
  if (l > r || hi <= num) return 0LL;
  if (lo > num) {
   return (r - l + 1);
  }
  return lc->count(pf[l-1] + 1, pf[r], num) + rc->count(l -
      pf[l-1], r - pf[r], num);
 }
};
```

3 Geometry

3.1 Basic

```
struct Point {
    double x, y;
    Point() { x = y = 0.0; }
    Point(double x, double y) : x(x), y(y) {}

    Point operator + (const Point &a) const { return Point(x
        + a.x, y + a.y); }
    Point operator - (const Point &a) const { return Point(x
        - a.x, y - a.y); }
    Point operator * (double k) const { return Point(x * k, y
        * k); }
    Point operator / (double k) const { return Point(x / k, y
        / k); }
};

struct Line { // Ax + By = C
    double a, b, c;
    Line(double a = 0, double b = 0, double c = 0) : a(a), b(
        b), c(c) {}
    Line(Point A, Point B) {
        a = B.y - A.y;
        b = A.x - B.x;
        c = a * A.x + b * A.y;
    }
};



Line Perpendicular_Bisector(Point A, Point B) {
    Point M = (A + B) / 2;
    Line d = Line(A, B);
    // the equation of a perpendicular line has the form: -Bx
        + Ay = D
    double D = -d.b * M.x + d.a * M.y;
    return Line(-d.b, d.a, D);
}
```

3.2 ConvexHull

```
// Kiu   im
struct Point {
    int x, y;
};

// Tch  c   hng   ca  AB  v  AC
long long cross(const Point &A, const Point &B, const Point
    &C) {
    return 1LL * (B.x - A.x) * (C.y - A.y) - 1LL * (C.x - A.x
        ) * (B.y - A.y);
}

// A -> B -> C i theo  th   t  theo  chiu  kim   ng    h
    (-1),  thng  hng  (0),   ngc   chiu  kim   ng    h
    (1)
int ccw(const Point &A, const Point &B, const Point &C) {
    long long S = cross(A, B, C);
    if (S < 0) return -1;
    if (S == 0) return 0;
    return 1;
}

// Tr   v  bao  li   vi   th   t   cc   im     c
    lit   k   ngc    chiu  kim   ng   h
vector<Point> convexHull(vector<Point> p, int n) {
    //  a    im   c  tung      nh   nht  ( v  tri  nht )
        ln   u   tp
    for (int i = 1; i < n; ++i) {
        if (p[0].y > p[i].y || (p[0].y == p[i].y && p[0].x >
            p[i].x)) {
            swap(p[0], p[i]);
        }
    }

    //  Sp   xp   cc   im   I theo gc  to   bi   trc
        honh  theo  chiu   dng   v  OI
    sort(p.begin() + 1, p.end(), [&p](const Point &A, const
        Point &B) {
        int c = ccw(p[0], A, B);
        if (c > 0) return true;
        if (c < 0) return false;
        return A.x < B.x || (A.x == B.x && A.y < B.y);
    });

    //  Tp  bao  li
    vector<Point> hull;
    hull.push_back(p[0]);

    //  Dng  bao  li
    for (int i = 1; i < n; ++i) {
        while (hull.size() >= 2 && ccw(hull[hull.size() - 2],
            hull.back(), p[i]) < 0) {
            hull.pop_back();
        }
        hull.push_back(p[i]);
    }
    return hull;
}
```

3.3 LineContainer

```
/**
 * Author: Simon Lindholm
 * Date: 2017-04-20
 * License: CC0
 * Source: own work
 * Description: Container where you can add lines of the
     form kx+m, and query maximum values at points x.
```

```
 * Useful for dynamic programming (``convex hull trick'').
 * Time: O(\log N)
 * Status: stress-tested
 */
#pragma once

struct Line {
 mutable ll k, m, p;
 bool operator<(const Line& o) const { return k < o.k; }
 bool operator<(ll x) const { return p < x; }
};

struct LineContainer : multiset<Line, less<>> {
 // (for doubles, use inf = 1/.0, div(a,b) = a/b)
 static const ll inf = LLONG_MAX;
 ll div(ll a, ll b) { // floored division
  return a / b - ((a ^ b) < 0 && a % b); }
 bool isect(iterator x, iterator y) {
  if (y == end()) return x->p = inf, 0;
  if (x->k == y->k) x->p = x->m > y->m ? inf : -inf;
  else x->p = div(y->m - x->m, x->k - y->k);
  return x->p >= y->p;
 }
 void add(ll k, ll m) {
  auto z = insert({k, m, 0}), y = z++, x = y;
  while (isect(y, z)) z = erase(z);
  if (x != begin() && isect(--x, y)) isect(x, y = erase(y));
  while ((y = x) != begin() && (--x)->p >= y->p)
   isect(x, erase(y));
 }
 ll query(ll x) {
  assert(!empty());
  auto l = *lower_bound(x);
  return l.k * x + l.m;
 }
};
```

4 Graphs

4.1 Bellman-Ford

```
struct Edge {
    int a, b, cost;
};

int n, m;
vector<Edge> edges;
const int INF = 1000000000;

void solve()
{
    vector<int> d(n);
    vector<int> p(n, -1);
    int x;
    for (int i = 0; i < n; ++i) {
        x = -1;
        for (Edge e : edges) {
            if (d[e.a] + e.cost < d[e.b]) {
                d[e.b] = d[e.a] + e.cost;
                p[e.b] = e.a;
                x = e.b;
            }
        }
    }

    if (x == -1) {
        cout << "No negative cycle found.";
    } else {
        for (int i = 0; i < n; ++i)
            x = p[x];

        vector<int> cycle;
        for (int v = x;; v = p[v]) {
            cycle.push_back(v);
            if (v == x && cycle.size() > 1)
                break;
        }
        reverse(cycle.begin(), cycle.end());

        cout << "Negative cycle: ";
        for (int v : cycle)
            cout << v << ' ';
        cout << endl;
    }
```

4.2 Kosaraju

```
vector<vector<int>> adj, adj_rev;
vector<bool> used;
vector<int> order, component;

void dfs1(int v) {
    used[v] = true;

    for (auto u : adj[v])
        if (!used[u])
            dfs1(u);
    order.push_back(v);
}

void dfs2(int v) {
    used[v] = true;
    component.push_back(v);

    for (auto u : adj_rev[v])
        if (!used[u])
            dfs2(u);
}

int main() {
    int n;
    // ... read n ...

    for (;;) {
        int a, b;
        // ... read next directed edge (a,b) ...
        adj[a].push_back(b);
        adj_rev[b].push_back(a);
    }

    used.assign(n, false);

    for (int i = 0; i < n; i++)
        if (!used[i])
            dfs1(i);

    used.assign(n, false);
    reverse(order.begin(), order.end());

    for (auto v : order)
        if (!used[v]) {
            dfs2 (v);

            // ... processing next component ...

            component.clear();
        }
}
```

4.3 Max Flow

```
int n;
vector<vector<int>> capacity;
vector<vector<int>> adj;
```

```
int bfs(int s, int t, vector<int>& parent) {
    fill(parent.begin(), parent.end(), -1);
    parent[s] = -2;
    queue<pair<int, int>> q;
    q.push({s, INF});

    while (!q.empty()) {
        int cur = q.front().first;
        int flow = q.front().second;
        q.pop();

        for (int next : adj[cur]) {
            if (parent[next] == -1 && capacity[cur][next]) {
                parent[next] = cur;
                int new_flow = min(flow, capacity[cur][next]);
                if (next == t)
                    return new_flow;
                q.push({next, new_flow});
            }
        }
    }

    return 0;
}

int maxflow(int s, int t) {
    int flow = 0;
    vector<int> parent(n);
    int new_flow;

    while (new_flow = bfs(s, t, parent)) {
        flow += new_flow;
        int cur = t;
        while (cur != s) {
            int prev = parent[cur];
            capacity[prev][cur] -= new_flow;
            capacity[cur][prev] += new_flow;
            cur = prev;
        }
    }

    return flow;
}
```

4.4 Tim cau

```
void dfs(int v, int p = -1) {
    visited[v] = true;
    tin[v] = low[v] = timer++;
    for (int to : adj[v]) {
        if (to == p) continue;
        if (visited[to]) {
            low[v] = min(low[v], tin[to]);
        } else {
            dfs(to, v);
            low[v] = min(low[v], low[to]);
            if (low[to] > tin[v])
                IS_BRIDGE(v, to);
        }
    }
}
```

4.5 Tim khop

```
void dfs(int v, int p = -1) {
    visited[v] = true;
    tin[v] = low[v] = timer++;
    int children=0;
    for (int to : adj[v]) {
        if (to == p) continue;
        if (visited[to]) {
            low[v] = min(low[v], tin[to]);
        } else {
            dfs(to, v);
            low[v] = min(low[v], low[to]);
            if (low[to] >= tin[v] && p!=-1)
                IS_CUTPOINT(v);
            ++children;
        }
    }
    if(p == -1 && children > 1)
        IS_CUTPOINT(v);
}
```

5 Maths

5.1 Matrix

```
struct Matrix {
    vector <vector <type> > data;

    // S    lng    hng    ca   ma   trn
    int row() const { return data.size(); }
    // S    lng    hng    ca   ma   trn
    int col() const { return data[0].size(); }

    auto & operator [] (int i) { return data[i]; }

    const auto & operator[] (int i) const { return data[i]; }

    Matrix() = default;

    Matrix(int r, int c): data(r, vector <type> (c)) { }

    Matrix(const vector <vector <type> > &d): data(d) {

        // Kim tra cc hng c cng size khng v size c
            ln hn 0 hay khng
        // Tuy nhin khng thc s cn thit , ta c
            th b cc dng /**/ i
        /**/ assert(d.size());
        /**/ int size = d[0].size();
        /**/ assert(size);
        /**/ for (auto x : d) assert(x.size() == size);
    }

    // In ra ma trn .
    friend ostream & operator << (ostream &out, const Matrix
        &d) {
        for (auto x : d.data) {
            for (auto y : x) out << y << ' ';
            out << '\n';
        }
        return out;
    }

    // Ma trn n v
    static Matrix identity(long long n) {
        Matrix a = Matrix(n, n);
        while (n--) a[n][n] = 1;
        return a;
    }

    // Nhn ma trn
    Matrix operator * (const Matrix &b) {
        Matrix a = *this;

        // Kim tra iu kin nhn ma trn
        assert(a.col() == b.row());

        Matrix c(a.row(), b.col());
        for (int i = 0; i < a.row(); ++i)
            for (int j = 0; j < b.col(); ++j)
```

```
            for (int k = 0; k < a.col(); ++k)
                c[i][j] += a[i][k] * b[k][j];
        return c;
    }

    // Ly  tha  ma  trn
    Matrix pow(long long exp) {

        // Kim  tra  iu  kin  ly  tha  ma  trn  ( l  ma
            trn  vung )
        assert(row() == col());

        Matrix base = *this, ans = identity(row());
        for (; exp > 0; exp >>= 1, base = base * base)
            if (exp & 1) ans = ans * base;
        return ans;
    }
};
```

5.2 Mod Int

```
/**
 * Description: Modular arithmetic. Assumes $MOD$ is prime.
 * Source: KACTL
 * Verification: https://open.kattis.com/problems/
     modulararithmetic
 * Usage: mi a = MOD+5; inv(a); // 400000003
 */

template<int MOD, int RT> struct mint {
 static const int mod = MOD;
 static constexpr mint rt() { return RT; } // primitive root
  int v;
  explicit operator int() const { return v; }
 mint():v(0) {}
 mint(ll _v):v(int(_v%MOD)) { v += (v<0)*MOD; }
 mint& operator+=(mint o) {
  if ((v += o.v) >= MOD) v -= MOD;
  return *this; }
 mint& operator-=(mint o) {
  if ((v -= o.v) < 0) v += MOD;
  return *this; }
 mint& operator*=(mint o) {
  v = int((ll)v*o.v%MOD); return *this; }
 friend mint pow(mint a, ll p) { assert(p >= 0);
  return p==0?1:pow(a*a,p/2)*(p&1?a:1); }
 friend mint inv(mint a) { assert(a.v != 0); return pow(a,
     MOD-2); }
 friend mint operator+(mint a, mint b) { return a += b; }
 friend mint operator-(mint a, mint b) { return a -= b; }
 friend mint operator*(mint a, mint b) { return a *= b; }
};
using mi = mint<(int)1e9+7, 5>;
using vmi = V<mi>;
```

5.3 Precal Modulo Inverse

```
int n = 10, p = 1000000007;
int inv[n + 1];
inv[1] = 1;
for (int i = 2; i <= n; i ++) inv[i] = 1LL * (p - p / i) *
     inv[p % i] % p;
```

5.4 Rabin-Miller

```
using u64 = uint64_t;
using u128 = __uint128_t;

u64 binpower(u64 base, u64 e, u64 mod) {
    u64 result = 1;
    base %= mod;
    while (e) {
        if (e & 1)
            result = (u128)result * base % mod;
        base = (u128)base * base % mod;
        e >>= 1;
    }
    return result;
}

bool check_composite(u64 n, u64 a, u64 d, int s) {
    u64 x = binpower(a, d, n);
    if (x == 1 || x == n - 1)
        return false;
    for (int r = 1; r < s; r++) {
        x = (u128)x * x % n;
        if (x == n - 1)
            return false;
    }
    return true;
};

bool MillerRabin(u64 n, int iter=5) { // returns true if n
     is probably prime, else returns false.
    if (n < 4)
        return n == 2 || n == 3;

    int s = 0;
    u64 d = n - 1;
    while ((d & 1) == 0) {
        d >>= 1;
        s++;
    }

    for (int i = 0; i < iter; i++) {
        int a = 2 + rand() % (n - 3);
        if (check_composite(n, a, d, s))
            return false;
    }
    return true;
}
```

6 Miscellaneous

6.1 Clion

```
set(GCC_COVERAGE_COMPILE_FLAGS "-O2 -Dbinhball")
set(CMAKE_CXX_FLAGS "${CMAKE_CXX_FLAGS} ${
     GCC_COVERAGE_COMPILE_FLAGS}" )
```

6.2 Debug

```
#ifdef hvmegy
#define dbg(...) logger(#__VA_ARGS__, __VA_ARGS__)
template<typename ...Args>
void logger(string vars, Args&&... values) {
 cerr << "[" << vars << " : ";
 string delim = "";
 (..., (cerr << delim << values, delim = ", "));
 cerr << "]" << '\n';
}
#else
#define dbg(...)
#endif
```

6.3 mt19937

```
mt19937_64 rnd(chrono::steady_clock::now().time_since_epoch
     ().count());
```

6.4 time

```
cerr << '\n' << clock() * 1000.0 / CLOCKS_PER_SEC << "ms" <<
     '\n';
```

7 Strings

7.1 Hash

```
int base = 311;
int const MOD = 1000000007;
int hashS[MAX];
int POW[MAX];
int gethash(int i, int j, int hashS[MAX]){
    return (hashS[j] - hashS[i - 1] * POW[j - i + 1] + MODMOD
        ) % MOD;
}
void setHash(){
    string s;
    n = s.length();
    POW[0] = 1;
    s = " " + s;
    t = " " + t;
    for (int i = 1; i <= n; i++)
        POW[i] = (base POW[i - 1])%MOD;
    for (int i = 1; i <= n; i++){
        hashS[i] = (hashS[i - 1] * base + s[i]) % MOD;
    }
    for (int i = 1; i <= m; i++)
        hashT[i] = (hashT[i - 1] * base + t[i]) % MOD;
}
```

7.2 KMP

```
int next_x[N];
    int j = next_x[0] = 0;
    n = s.length();
    m = t.length();
    for (int i = 1; i < n; i++){
        while (j > 0 && s[j] != s[i]){
            j = next_x[j - 1];
        }
        if (s[i] == s[j])
            j++;
        next_x[i] = j;
    }
    j = 0;
    for (int i = 0; i < m; i++){
        while (j > 0 && s[j] != t[i])
            j = next_x[j - 1];
        if (s[j] == t[i])
            j++;
        if (j == n){
            cout << i - n + 2 << " ";
        }
    }
```

7.3 Z Function

```
z[0] = n;
    int l = 0, r = 0;
    for (int i = 1; i < n; i++){
        if (i > r){
            l = r = i;
            while (r < n && s[r] == s[r-l]) ++r;
            z[i] = r - l;
            r-=1;
        }
        else{
            int k= i - l;
            if (z[k] < r - i + 1) z[i] = [k];
            else{
                l = i;
                while (r < n && s[r] == s[r - l]) r++;
                z[i]= r - l;
                r--;
            }
        }
    }
```