

①

0.4 = 4 AEM 2011 EXAM 2 } = 30.5

1. $h(x, y) = (0.2y + 0.5) \text{ m}$ m s = 30
 $0 \leq x \leq 4 \text{ m}$ and $0 \leq y \leq 5 \text{ m}$

$$\rho = 300 \text{ kg/m}^3$$

$$\begin{aligned} \text{Volume} = V &= \iint_A h(x, y) \, dx \, dy \\ &= \int_0^4 \int_0^5 (0.2y + 0.5) \, dy \, dx \\ &= \int_0^4 5 \, dx = 20 \end{aligned}$$

$$m = \rho V = 300 \times 20 = 6000 \text{ kg}$$

$$W = mg = 58.86 \text{ kN}$$

(a) $\vec{W} = -58.86 \text{ kN } \hat{j}$

(b) $\int_V x \, dV = \iint_A x h(x, y) \, dx \, dy$

$$\begin{aligned} &= \int_0^4 \int_0^5 (0.5x + 0.2xy) \, dy \, dx \\ &= \int_0^4 \left[(0.5x)y \Big|_0^5 + 0.2x \frac{y^2}{2} \Big|_0^5 \right] dx \\ &= \int_0^4 \left[(0.5x)5 + (0.1x)25 \right] dx \end{aligned}$$

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$$20 \bar{x} = \int_0^4 5x \, dx = 5 \frac{x^2}{2} \Big|_0^4 = 40$$

$$\bar{x} = 2 \text{ m}$$

$$h(x,y) = (0.5y + 0.5x) \text{ m} \quad 0 \leq x \leq 4 \text{ m} \quad 0 \leq y \leq 2 \text{ m}$$

$$\rho = 300 \text{ kg/m}^3$$

$$V = \iint_A h(x,y) \, dx \, dy = \text{Volume}$$

$$= \int_0^2 \int_0^4 (0.5y + 0.5x) \, dx \, dy$$

$$= \int_0^2 2 \, dy = 4$$

$$M = \rho V = 300 \times 4 = 1200 \text{ kg}$$

$$M = 1200 \text{ kg}$$

$$\bar{M} = -28.86 \text{ kN} \quad (a)$$

$$V = \iint_A h(x,y) \, dx \, dy = 4 \quad (b)$$

$$= \int_0^2 \int_0^4 (0.5x + 0.5y) \, dx \, dy$$

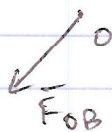
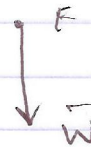
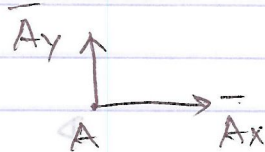
$$= \int_0^2 \left[0.25x^2 + 0.5xy \right]_0^4 \, dy$$

$$= \int_0^2 (2 + 2y) \, dy$$

2. $W = 30 \text{ kN}$

Assume OB is in tension

$$\hat{OB} = \frac{\vec{OB}}{|\vec{OB}|} = \frac{(5, 20)}{5\sqrt{17}} = \left(\frac{1}{\sqrt{17}}, \frac{4}{\sqrt{17}}\right)$$



$$\vec{F}_A = (A_x, A_y)$$

$$\vec{F}_{OB} = -F_{OB} \hat{OB} = -F_{OB} \left(\frac{1}{\sqrt{17}}, \frac{4}{\sqrt{17}}\right)$$

$$\sum F_x: A_x - \frac{F_{OB}}{\sqrt{17}} = 0$$

$$\sum F_y: A_y - F_{OB} \cdot \frac{4}{\sqrt{17}} - 30 \times 3 = 0$$

$$\sum M_A: -\frac{F_{OB}}{\sqrt{17}} (10) - 30 \times 3 (25) = 0$$

$$F_{OB} \frac{10}{\sqrt{17}} = -0.75 \times 10^6$$

$$F_{OB} = -309.23 \text{ kN}$$

$$A_x = -75 \text{ kN}$$

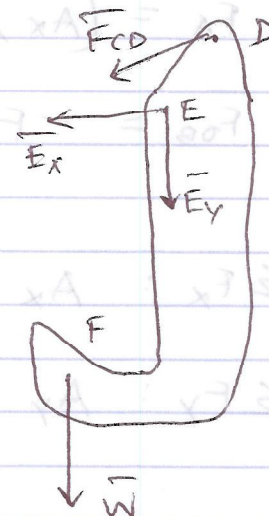
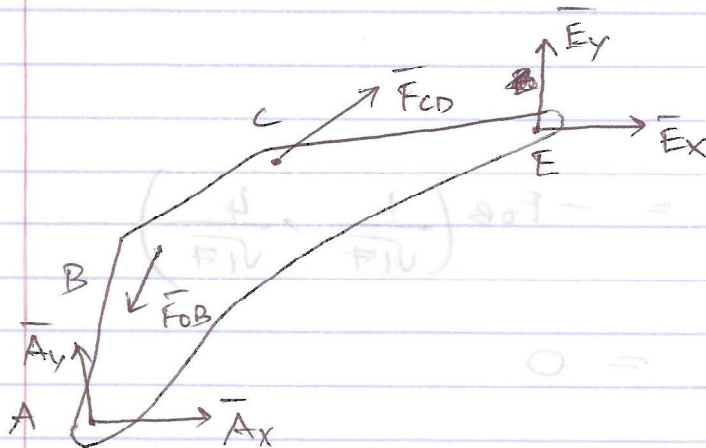
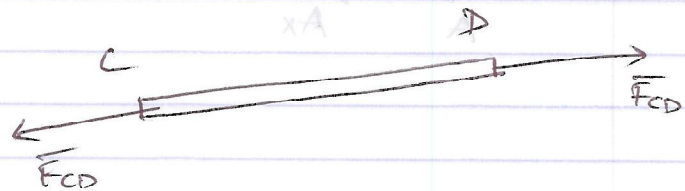
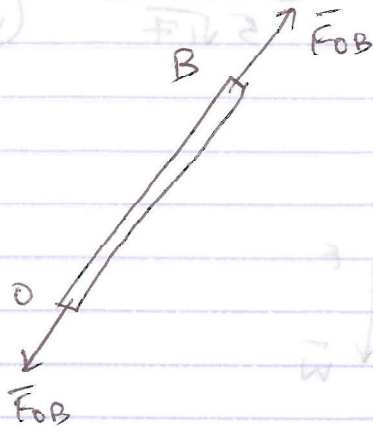
$$A_y = -270 \text{ kN}$$

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(a)

$$\begin{aligned} \bar{A}_x &= 75 \text{ kN} \leftarrow \\ \bar{A}_y &= 270 \text{ kN} \downarrow \\ F_{OB} &= 309.23 \text{ kN (compression)} \end{aligned}$$

(b)



(c)

Consider member ABCE. We already solved for A_x , A_y , and F_{OB} . There are three unknowns: F_{CD} , E_x , and E_y . Note that since CD is a two-force member, the direction of F_{CD} is already known — only its magnitude is unknown. Alternatively, member DEF may be considered. The 3 unknowns can be solved for from 3 equations.

Problem - 3

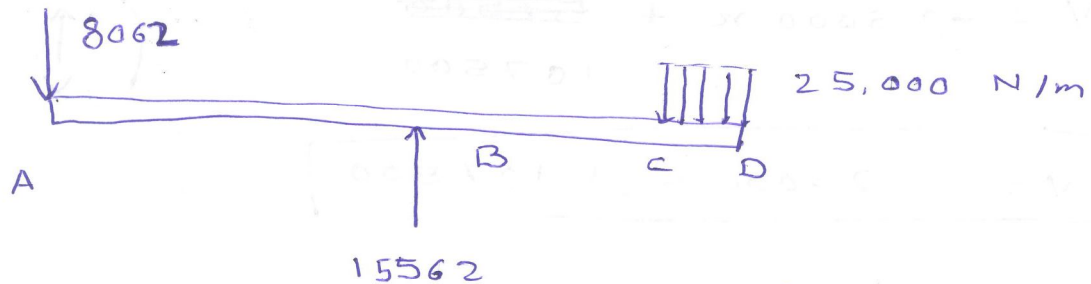
a) $W = 7500 \text{ N}$

$$\text{Height density} = \frac{W}{0.3 \text{ m}}$$

$$\Rightarrow w(x) = \frac{7500}{0.3} = 25000 \text{ N/m}$$

$$= 25 \text{ kN/m}$$

b) FBD



→ For AB

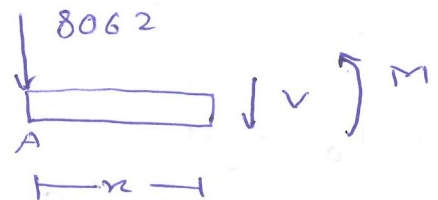
$$\sum F_y = 0$$

$$\Rightarrow V = -8062 \text{ N}$$

$$\sum M_A = 0$$

$$\Rightarrow -Vx + M = 0$$

$$\Rightarrow M = -8062x \text{ Nm}$$

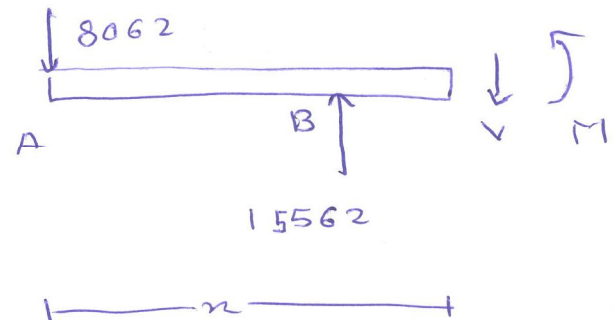


→ For BC

$$\sum F_y = 0$$

$$\Rightarrow V = 15562 - 8062$$

$$\Rightarrow V = 7500 \text{ N}$$



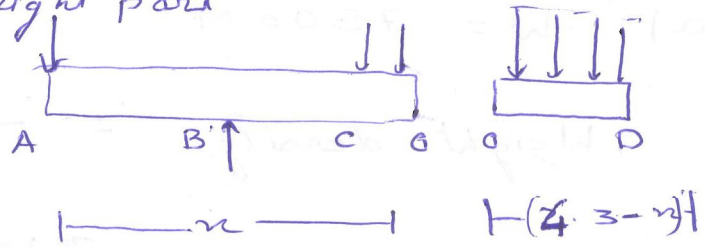
$$\sum M_A = 0$$

$$15562 \times x + M = 0 \Rightarrow$$

$$M = 7500x - 31124$$

→ For CD

We will consider the right part

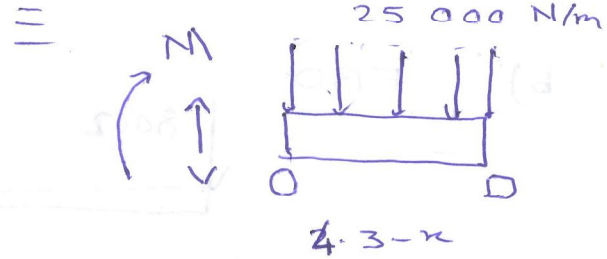


$$\sum F_y = 0$$

$$\Rightarrow V - 25000 \times (4.3 - x) = 0$$

$$\Rightarrow V = -25000x + \frac{107500}{1}$$

$$\Rightarrow \boxed{V = -25000x + 107500}$$



$$\sum M_o = 0$$

$$\Rightarrow -M - \left[25000 \times (4.3 - x) \right] \times \frac{(4.3 - x)}{2} = 0$$

$$\Rightarrow \boxed{M = -12500x^2 + 107500x - 231125 \text{ Nm}}$$

Plotting these, we get

