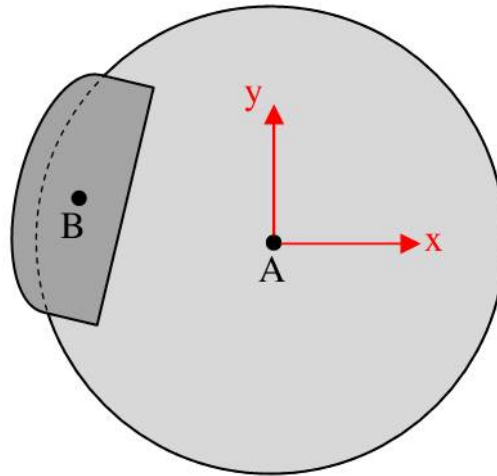


Unless otherwise mentioned, these problems should be solvable using a basic calculator. Practice clear communication by showing all work (free body diagrams, algebra, etc). This will be required to receive full credit on any graded problems.

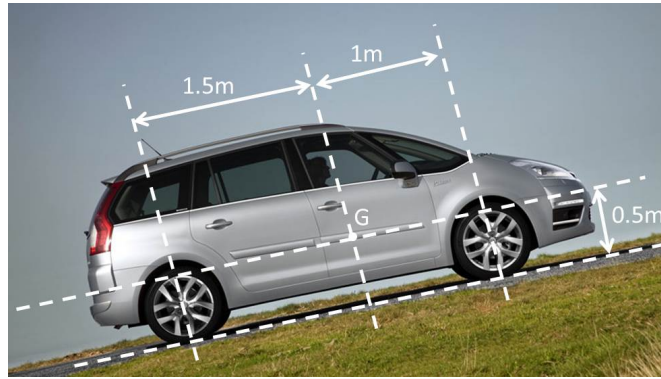
1. Disc brakes are the most common type of brakes used in modern automobiles. They work by having a disc fixed to each wheel of the vehicle, and a hydraulic caliper which applies a force to the disc. The friction between the brake pads and the disc will slow down and ultimately stop the rotation of the wheel.

The diagram below shows a disc brake and caliper assembly. The disc rotates about point A , and when the brakes are actuated, a force of $-N\mathbf{k}$ (into the page) is applied to the front of the disc, and a force of $+N\mathbf{k}$ (out of the page) is applied to the back of the disc. Both forces act at point B , which is given by $-10\mathbf{i} + 3\mathbf{j}$ centimeters. The coefficients of friction between the brake pads and disc are $\mu_s = 0.5$ and $\mu_k = 0.4$.

- (a) When the brakes are fully actuated, the force N reaches its maximum value of $20kN$. If the car is at rest and the brakes are fully actuated, what is the maximum moment that can be supplied by the axle before the brakes fail and the car begins to move?
- (b) When the car is coasting down a steep hill, a moment of $200\text{ N} \cdot \text{m}$ is generated about the axle. If light brake pressure is applied, the car will move down the hill at a constant speed instead of accelerating. What is the force N that the brakes must apply for the car to move at a constant speed?



2. Imagine that you are a material scientist working for a popular car tire manufacturer. Your job involves applying concepts from tribology (the study of friction) to decide on the material that will be used to manufacture the car tires. In this problem, you will design material-level properties, in particular the coefficients of static and kinetic friction between the rubber and the road, given higher-level requirements on the car. The car, shown in the figure below, has a mass of 1,000kg. The center of gravity of the car is located 0.5m from the road, 1m from the forward axle, and 1.5m from the rear axle. In answering the following questions, you may assume that the car is two-dimensional, i.e. you do not have to split the forces on the front/rear tires since there are two sets of front/rear tires.
- (a) The car company is especially concerned about the maximum steepness of the slopes on which its cars can be parked. Choose the coefficient of static friction such that the cars can be parked on ramps ranging in inclination from 0° to 40° .
 - (b) Given that the car is parked on a ramp of inclination 35° , find the normal reactions and friction forces on both the front and rear tires.
 - (c) The car company wants to ensure that if the car started sliding down the ramp, due to an external disturbance, it would not continue to slide down. For a 35° ramp, choose the lowest possible value for the coefficient of kinetic friction such that a car disturbed from its parked position returns to a complete stop.



3. Race tracks and speedways are designed with turns that are banked at an angle. Banked turns help cars execute the turn at higher speeds as compared to flat turns. In the figure below, a car is shown executing a 25° banked turn. Since this is actually a problem in dynamics, we will simply assume that a centripetal force F_C acts in the horizontal direction on the car. This centripetal force has the following expression:

$$F_C = m \frac{V^2}{R}$$

where, m is the mass of the car, V is the speed of the car, and R is the radius of curvature of the turn. The coefficient of static friction between the tires and the road is $\mu_s = 0.8$.

Under the constraint that a car should not slide along the banked turn, find the percentage increase in the maximum possible speed at which a car can execute a banked turn as compared to a flat turn.

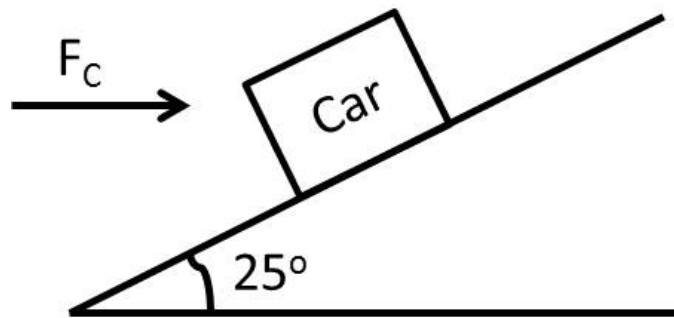


Diagram of car executing banked turn (car is driving into the page).

4. Book problems:

(a) 8.48

(b) 8.56

Additional Practice Problems: 8.15, 8.17, 8.23, 8.52

The quiz problem will not be selected from these additional practice problems. However, these exercises contain important elements of the course and similar problems may appear on the exam.