

LINEAR DATA STRUCTURES: VECTORS AND LINKED LIST

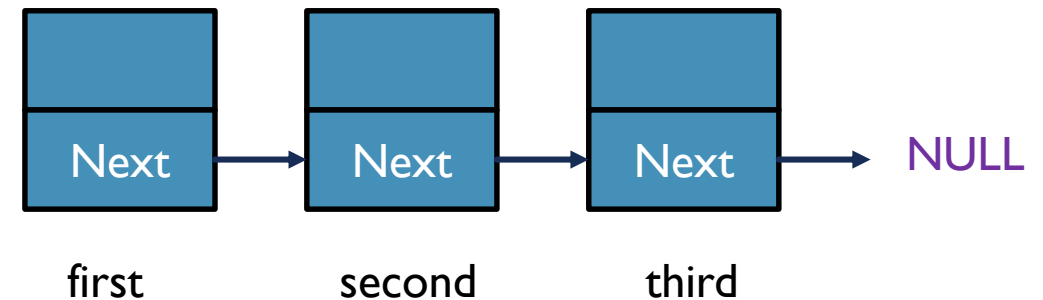
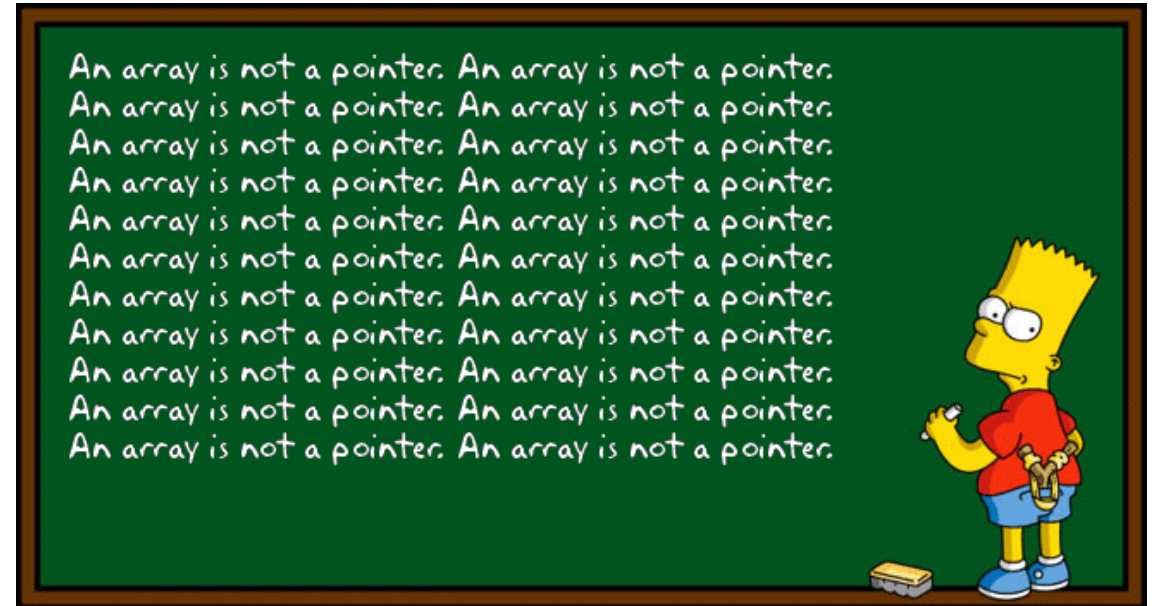
ALGORITHMS AND DATA STRUCTURES



LINEAR DATA STRUCTURES: VECTORS AND LINKED LISTS

Content

- Vectors (Dynamic Arrays)
 - Structure
 - Resizing and pushing
- Lists
 - Creation of structure
 - Append (attaching to the end of the list)
 - Push (attaching to the first element)
 - Insert
 - Insert after
 - Insert before
 - Deleting the node
- Lists Algorithms
 - Loop Detection
 - Merge point detection



VECTORS

LINEAR STRUCTURES: VECTORS AND LINKED LIST



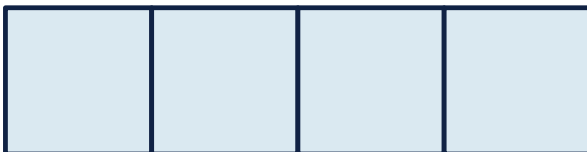
VECTORS

Structure

- Vectors represent a dynamic arrays
- Can be resized and reallocated

```
vector<double> age(4);
```

```
age[0] = 32.0;  
age[1] = 43.2;  
age[2] = 54.5;  
age[3] = 64.1;
```



```
class vector{  
  
    int sz;  
    double* elem;  
  
public:  
  
    vector(int s):sz(s), // init sz  
                elem(new double[s]) // init elem  
    {  
        for (int i = 0; i < s; i++)  
            elem[i] = 0;  
    }  
    int size()const{return sz;} // current size  
  
};
```

VECTOR IMPLEMENTATION

```
template<class T>
class Vector
{
public:
    typedef T * iterator;
    Vector();
    Vector(unsigned int size);
    Vector(unsigned int size, const T & initial);
    Vector(const Vector<T> & v);           // copy constructor
    ~Vector();
    unsigned int capacity() const;        // return capacity of vector (in elements)
    unsigned int size() const;           // return the number of elements in the vector
    bool empty() const;
    iterator begin();                    // return an iterator pointing to the first element
    iterator end();                      // return an iterator pointing to one past the last element
    T & front();                         // return a reference to the first element
    T & back();                          // return a reference to the last element
    void push_back(const T & value);     // add a new element
    void pop_back();                     // remove the last element
    void reserve(unsigned int capacity); // adjust capacity
    void resize(unsigned int size);      // adjust size
    T & operator[](unsigned int index);   // return reference to numbered element
    Vector<T> & operator=(const Vector<T> &);
private:
    unsigned int my_size;
    unsigned int my_capacity;
    T * buffer;
};
```

VECTOR IMPLEMENTATION

```
template<class T>//
Vector<T>::Vector()
{
    my_capacity = 0;
    my_size = 0;
    buffer = 0;
}
template<class T>
Vector<T>::Vector(const Vector<T> & v)
{
    my_size = v.my_size;
    my_capacity = v.my_capacity;
    buffer = new T[my_size];
    for (int i = 0; i < my_size; i++)
        buffer[i] = v.buffer[i];
}
template<class T>//
Vector<T>::Vector(unsigned int size)
{
    my_capacity = size;
    my_size = size;
    buffer = new T[size];
}
```

```
template<class T>//
Vector<T>::Vector(unsigned int size, const T & initial)
{
    my_size;
    my_capacity = size;
    buffer = new T [size];
    for (int i = 0; i < size; i++)
        buffer[i] = initial;
}
template<class T>//
Vector<T> & Vector<T>::operator = (const Vector<T> & v)
{
    delete[ ] buffer;
    my_size = v.my_size;
    my_capacity = v.my_capacity;
    buffer = new T [my_size];
    for (int i = 0; i < my_size; i++)
        buffer[i] = v.buffer[i];
    return *this;
}
template<class T>//
typename Vector<T>::iterator Vector<T>::begin()
{
    return buffer;
}
template<class T>//
typename Vector<T>::iterator Vector<T>::end()
{
    return buffer + size();
}
```

VECTOR IMPLEMENTATION

```

template<class T>//
T& Vector<T>::Vector<T>::front()
{
    return buffer[0];
}
template<class T>//
T& Vector<T>::Vector<T>::back()
{
    return buffer[size - 1];
}
template<class T>
void Vector<T>::push_back(const T & v)
{
    if (my_size >= my_capacity)
        reserve(my_capacity +5);
    buffer [my_size++] = v;
}
template<class T>//
void Vector<T>::pop_back()
{
    my_size--;
}

```

```

template<class T>//
void Vector<T>::reserve(unsigned int capacity)
{
    if(buffer == 0)
    {
        my_size = 0;
        my_capacity = 0;
    }
    if (capacity <= my_capacity)
return;
    T * new_buffer = new T [capacity];
    assert(new_buffer);
    copy (buffer, buffer + my_size, new_buffer);
    my_capacity = capacity;
    delete[] buffer;
    buffer = new_buffer;
}
template<class T>//
unsigned int Vector<T>::size()const
{
    return my_size;
}
template<class T>//
void Vector<T>::resize(unsigned int size)
{
    reserve(size);
    my_size = size;
}

```

VECTOR IMPLEMENTATION

```
template<class T>//  
T& Vector<T>::operator[](unsigned int index)  
{  
    return buffer[index];  
}
```

```
template<class T>//  
unsigned int Vector<T>::capacity()const  
{  
    return my_capacity;  
}
```

```
template<class T>//  
Vector<T>::~~Vector()  
{  
    delete[]buffer;  
}
```


LINKED LIST

LINEAR STRUCTURES: VECTORS AND LINKED LIST



LINKED LIST

```
struct Node
{
    int data;
    Node *next;
};
```

Integer data holder

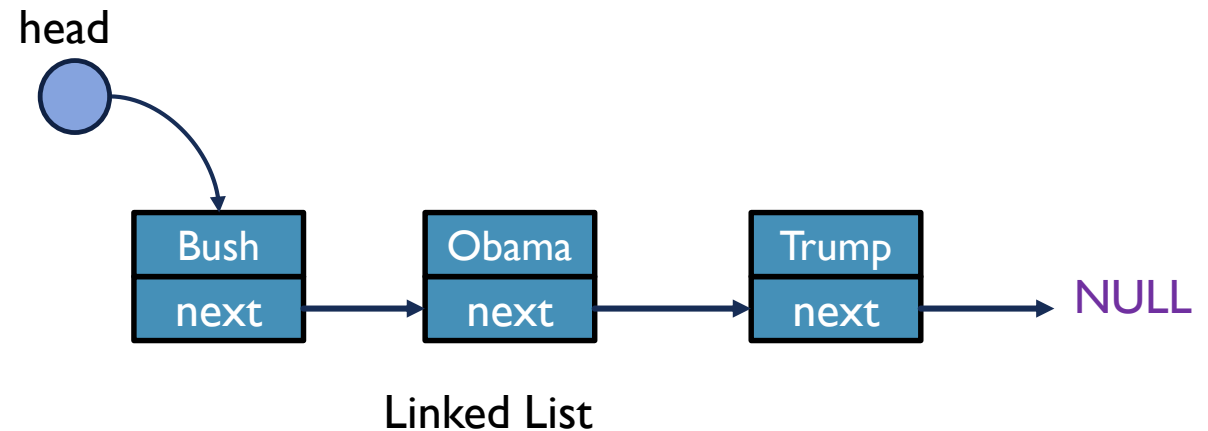
```
template<typename T>
struct Node
{
    T data;
    Node *next;
};
```

General case



Building Block
Additional pointer

- If a node contains a data member that is a pointer to another node, then many nodes can be strung together using only one variable to access the entire sequence of nodes. Such a sequence of nodes is the most frequently used implementation of a linked list
- If a node has a link only to its successor in this sequence, the list is called a singly linked list
- Data could be any type



NODE AS BUILDING BLOCKS

```
struct Node
{
    int data;
    Node *next;
};

void printList(Node *n)
{
    while (n != NULL)
    {
        cout<<n->data<<" ";
        n = n->next;
    }
}

int main(){

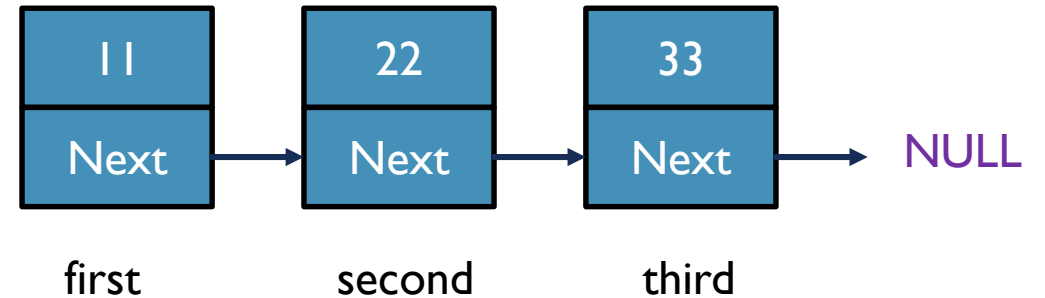
    Node* first = new Node();
    Node* second = new Node();
    Node* third = new Node();

    first->data = 11;
    first->next = second;

    second->data = 22;
    second->next = third;

    third->data = 33;
    third->next = NULL;

    Node* head = first;
    printList(head);
    system("pause");
}
```



LINKED LIST APPENDING

```
void append(Node** head, int added_data)
{
    Node* new_node = new Node();
    new_node->data = added_data;
    new_node->next = NULL;

    if (*head == NULL){
        *head = new_node;
        return;
    }

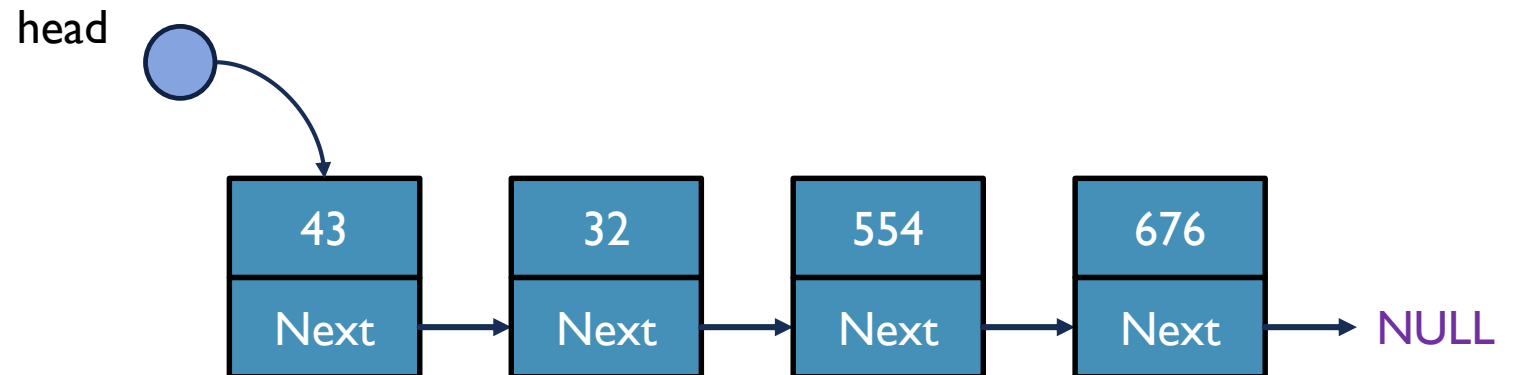
    Node *tail = *head; // initial

    while (tail->next != NULL)
        tail = tail->next;

    tail->next = new_node;
    return;
}
```

```
int main(){
    Node* h = NULL;
    append(&h, 43);
    append(&h, 32);
    append(&h, 554);
    append(&h, 676);

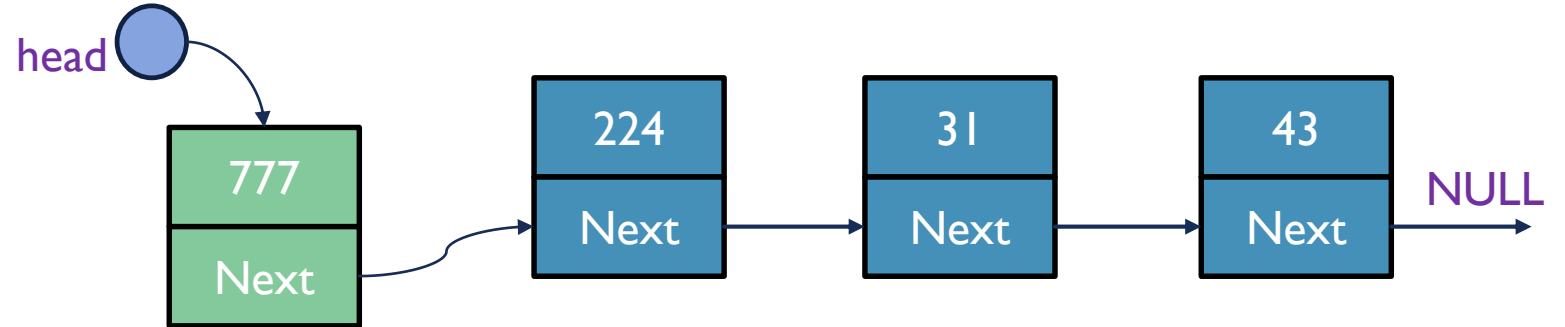
    printList(h);
    system("pause");
}
```



INSERTING A NODE

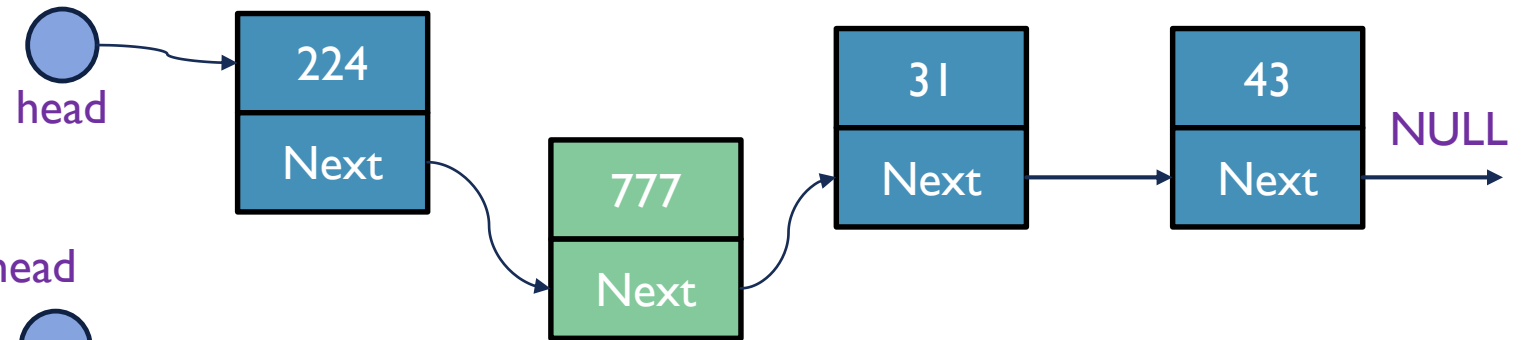
- inserting to the front

- `push()`



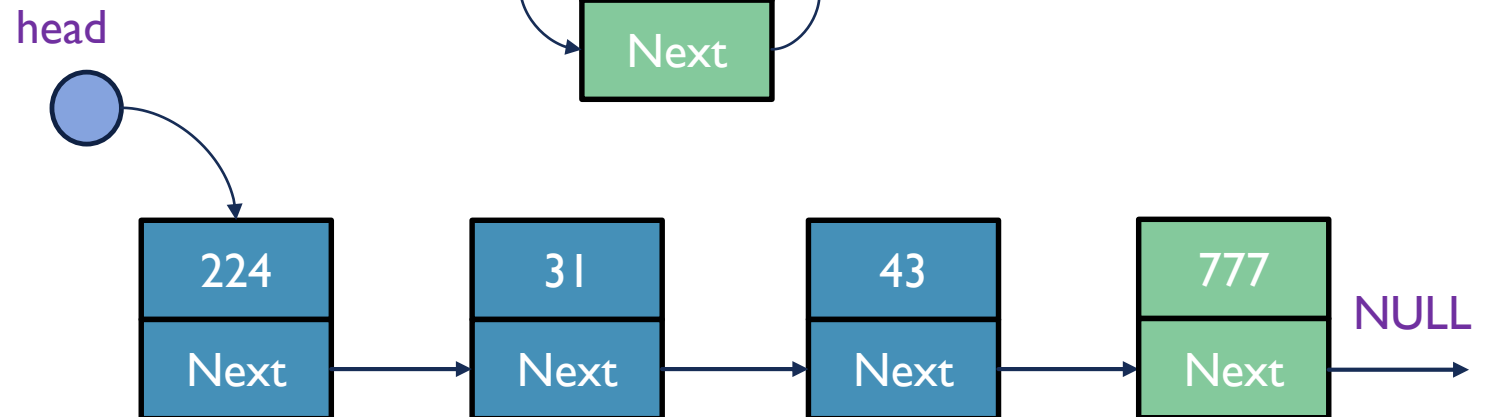
- inserting after given node

- `insert_after()`

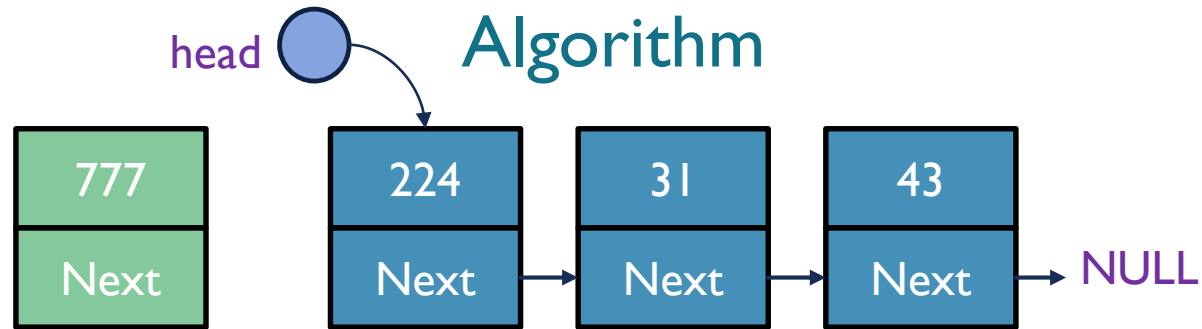


- Inserting at the end of the list

- `append()`



INSERTING TO THE FRONT PUSH METHOD



```
void push(Node** head, int new_data)
{
```

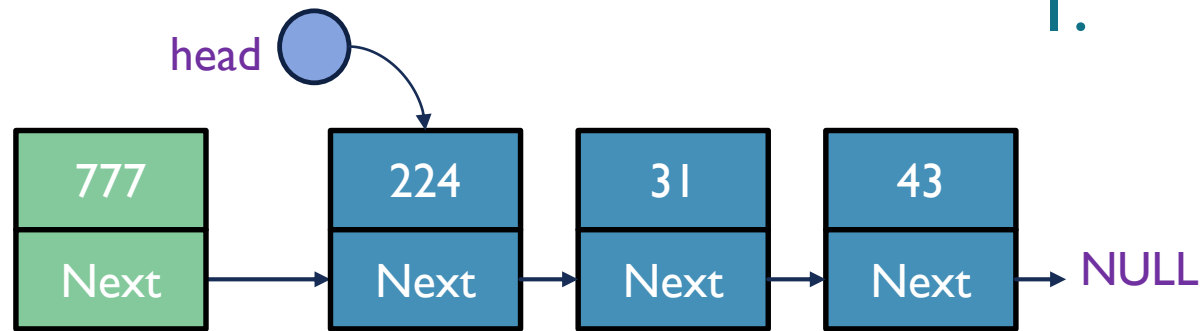
1.

```
Node* new_node = new Node;
```

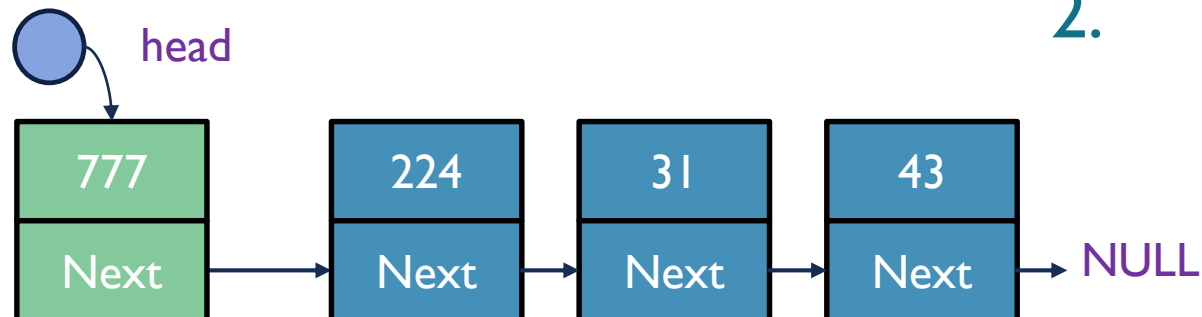
```
new_node->data = new_data;
new_node->next = *head;
```

```
*head = new_node;
```

```
}
```



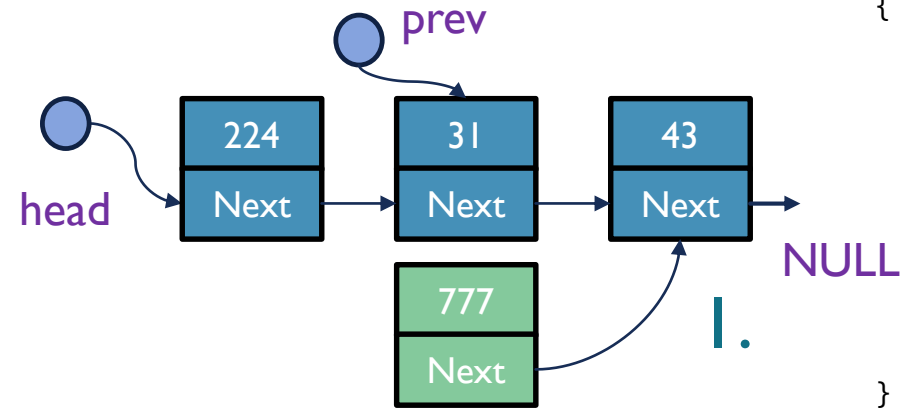
2.



3.

INSERT AFTER METHODS

Algorithm



```
void insertAfter(Node* prev_node, int new_data) {
    if (prev_node == NULL)
    {
        return;
    }

    Node* new_node = new Node();
    new_node->data = new_data;

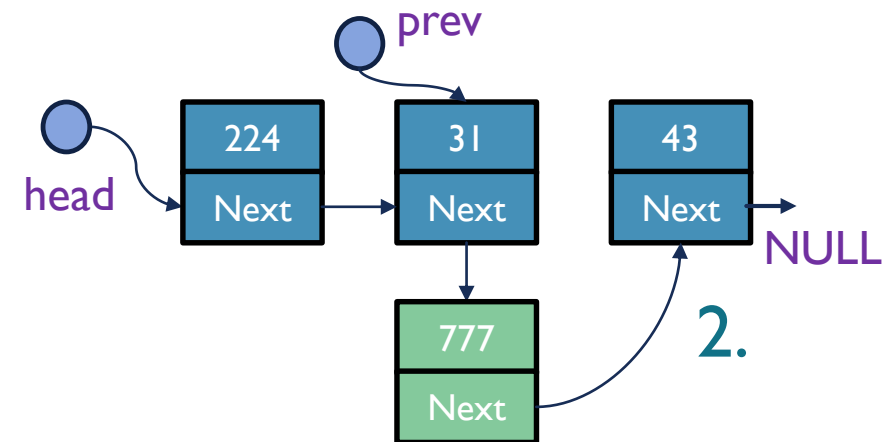
    new_node->next = prev_node->next;
    prev_node->next = new_node;
}

void insert_after_pos(Node* head, int pos, int new_data)
{
    if (head == NULL)
    {
        return;
    }

    Node* new_node = new Node();
    new_node->data = new_data;

    Node* pos_before = head;
    while (pos > 1)
    {
        pos_before = pos_before->next;
        pos--;
    }

    new_node->next = pos_before->next;
    pos_before->next = new_node;
}
```

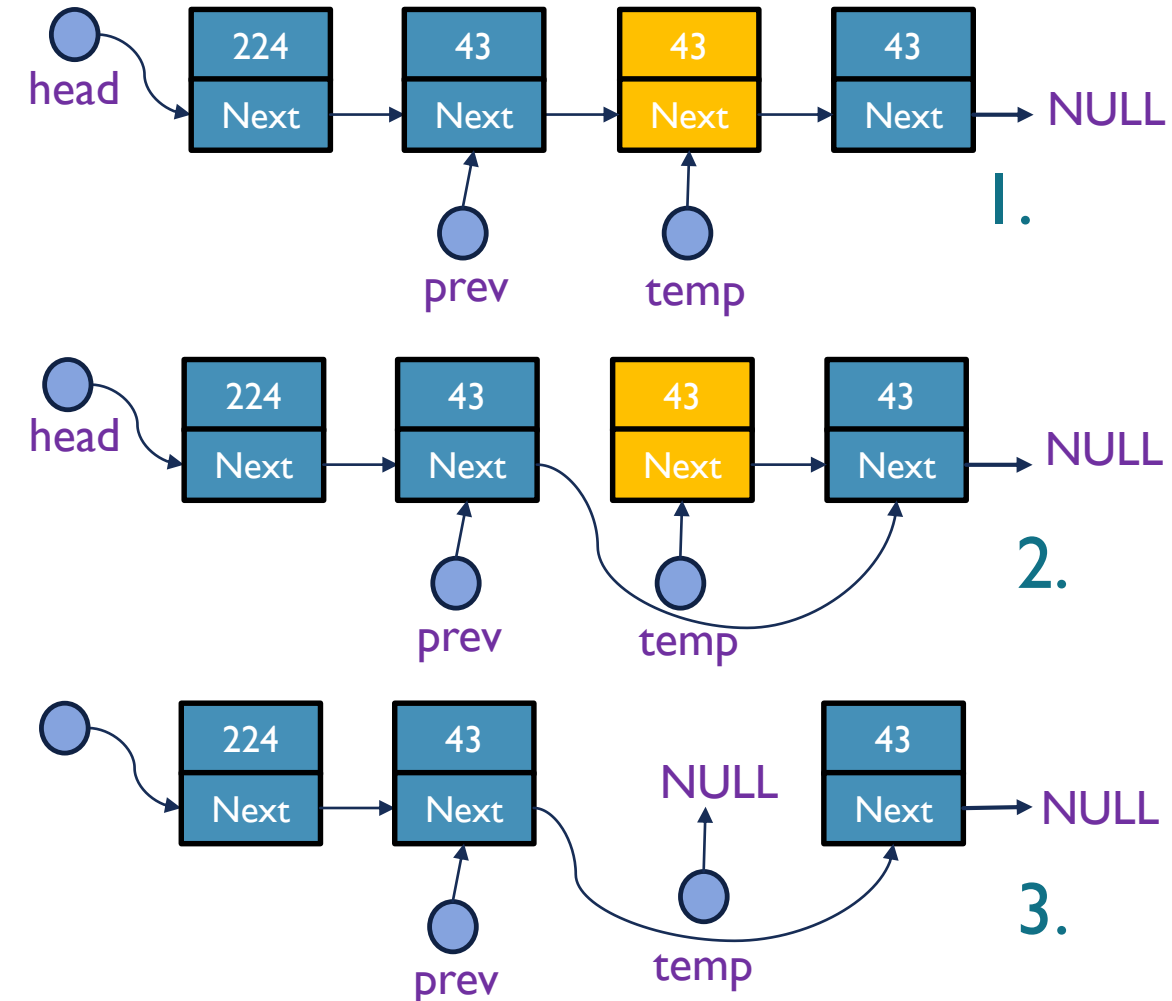


After prev pointer

After counter

DELETING THE NODE

Algorithm

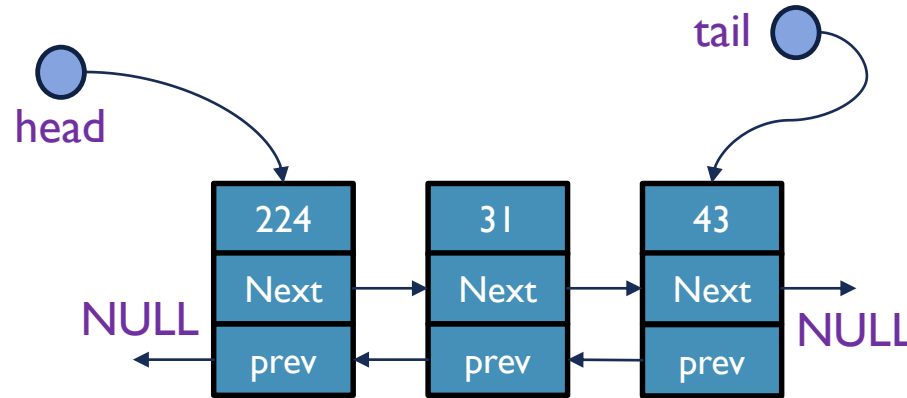


```
void deleteNode(Node **head_ref, int key)
{
    Node *temp = *head_ref, *prev;
    if (temp != NULL && temp->data == key)
    {
        *head_ref = temp->next;
        delete temp;
        return;
    }
    while (temp != NULL && temp->data != key)
    {
        prev = temp;
        temp = temp->next;
    }
    if (temp == NULL)
        return;
    prev->next = temp->next;
    delete temp;
}
```

ALTERNATIVE LINKED LISTS

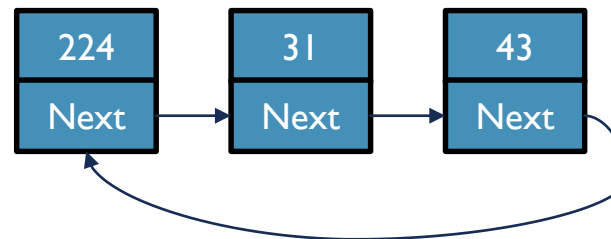
Doubly Linked List

- Cyclic linked lists
- Bidirectional Linked list (Doubly linked list)
- Linked list with additional pointers



```
template<typename T>
struct Node
{
    T data;
    Node *next;
    Node * prev;
};
```

Additional pointer



Must keep track on
number

```
template<typename T>
struct Node
{
    T data;
    Node *next;
    unsigned int elements;
};
```

Must keep track on
elements

LISTS ALGORITHMS

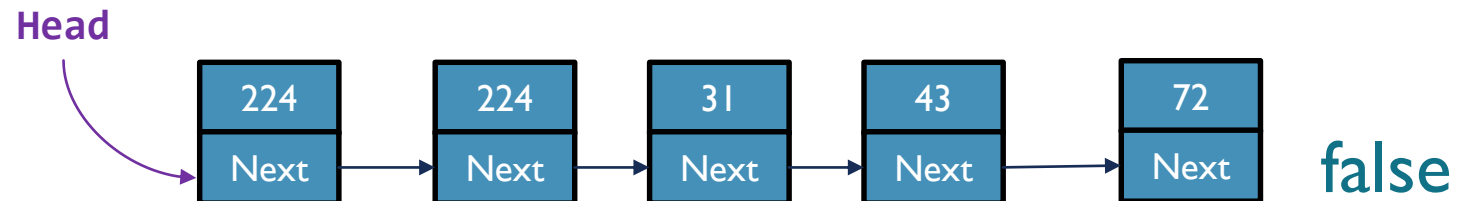
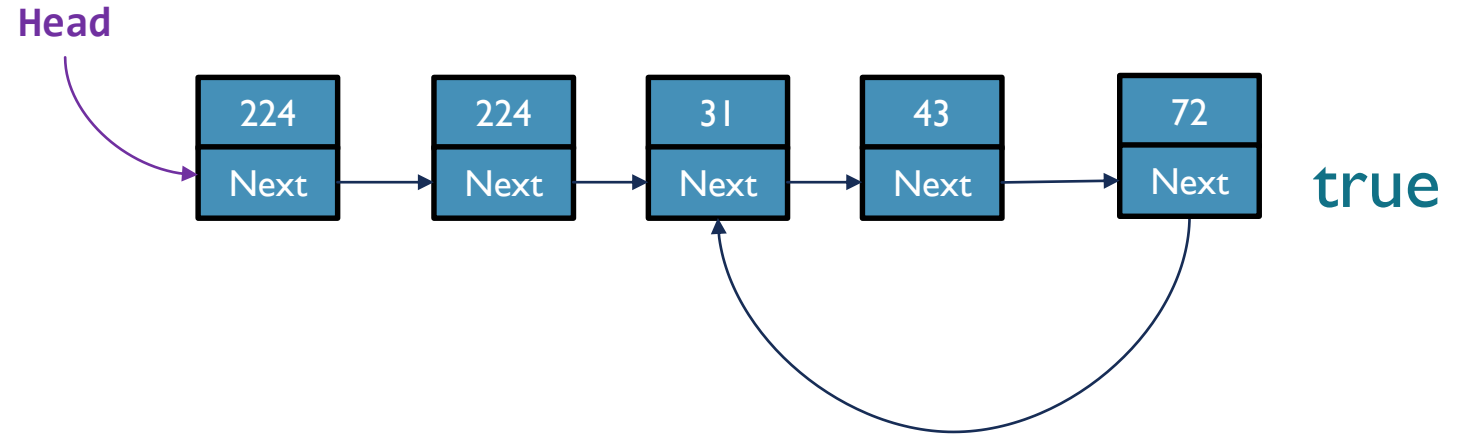
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LOOP DETECTION

Task

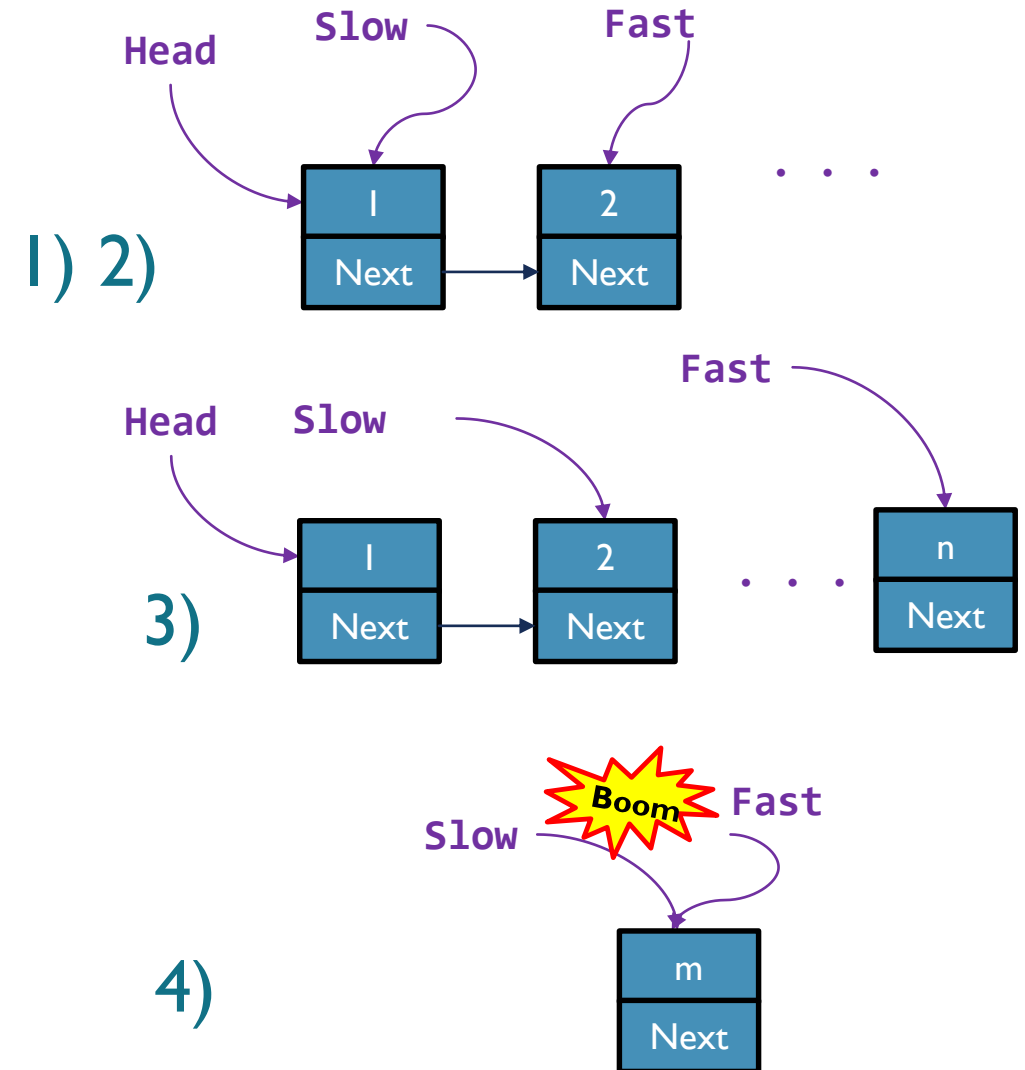
- Given linked List (head pointer)
- Detect the exiting of the loop



LOOP DETECTION

Algorithm

- Create 2 pointers. (1,2)
 - Slow Pointer,
 - Fast Pointer
- Start travers through the list (with different speed) (3)
 - $\text{Slow} = \text{Slow} \rightarrow \text{next}$
 - $\text{Fast} = \text{Fast} \rightarrow \text{next} \rightarrow \text{next}$
- If Loop exist: (4)
 - Fast and Slow pointers will eventually meet each other



LOOP DETECTION

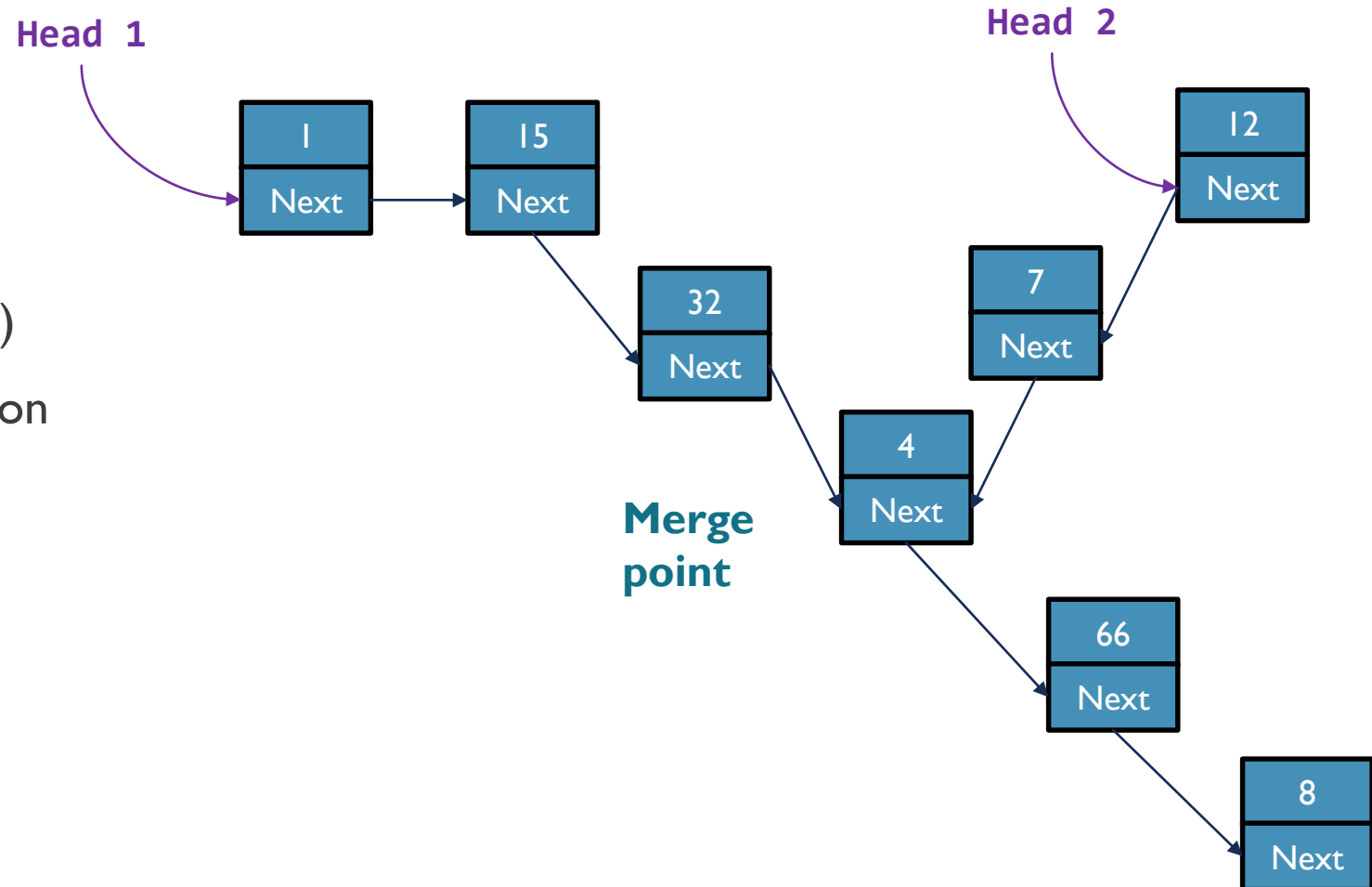
```
int find_loop(Node *list)
{
    Node *slow_p = list, *fast_p = list;

    while (slow_p && fast_p && fast_p->next )
    {
        slow_p = slow_p->next;
        fast_p  = fast_p->next->next;
        if (slow_p == fast_p)
        {
            cout<<"Loop Detected"<<endl;
            return true;
        }
    }
    return false;
}
```

MERGE POINT DETECTION

Task

- Given two Linked Lists (the head)
- Find the merge point (aka Insertion point) of two linked lists



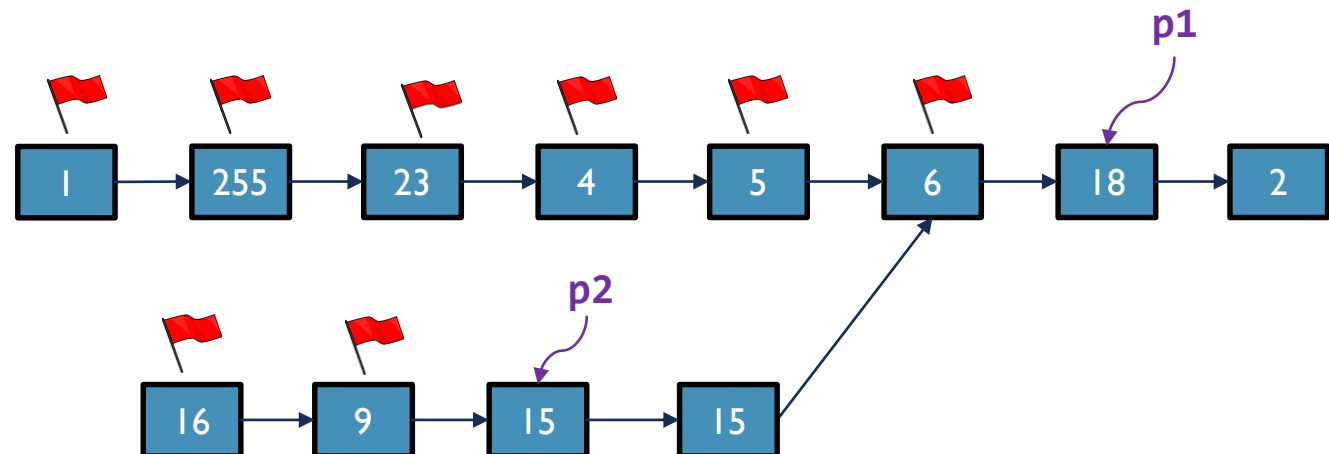
MERGE POINT DETECTION

Algorithm 1

- Brute Force Approach $O(n^2)$
 - Create two nested loops
 - Check if the node in the inner loop is the same as the node in the outer loop

Algorithm 2

- Additional information in the node $O(n + m)$
 - Modify the current Linked List structure by adding a flag.
 - Traverse both heads through the loop and change the state of the flag inside the nodes.
 - If one of heads detects that flag inside the traversed node has been changed – this node is an insertions node.



MERGE POINT DETECTION

Algorithm 3

- Counting the node $O(n + m)$
 - Create the first and the second pointer from head of both nodes
 - Count the number of nodes while traversing in both lists
 - Check the absolute difference between both list number **num = *abs(Count1 – Count2)***
 - traverse the bigger list from the first node till d nodes so that from here onwards both the lists have equal no of nodes
 - traverse both the lists in parallel till we come across a common node. (Note that getting a common node is done by comparing the address of the nodes)

MERGE POINT DETECTION

```
int count(struct Node* head)
{
    struct Node* current = head;
    int count = 0;

    while (current != NULL)
    {
        count++;
        current = current->next;
    }

    return count;
}
```

```
int merge_point_util(int d, Node* head1, Node* head2)
{
    int i;
    Node* current1 = head1;
    Node* current2 = head2;

    for(i = 0; i < d; i++)
    {
        if(current1 == NULL)
        { return -1; }
        current1 = current1->next;
    }

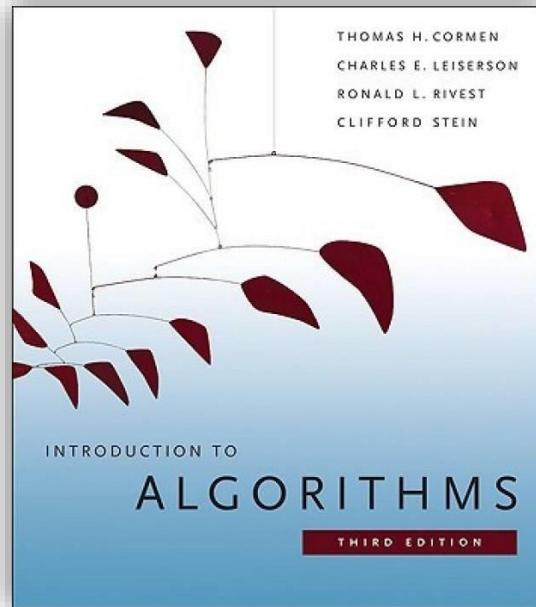
    while(current1 != NULL && current2 != NULL)
    {
        if(current1 == current2)
            return current1->data;
        current1 = current1->next;
        current2 = current2->next;
    }

    return -1;
}
```

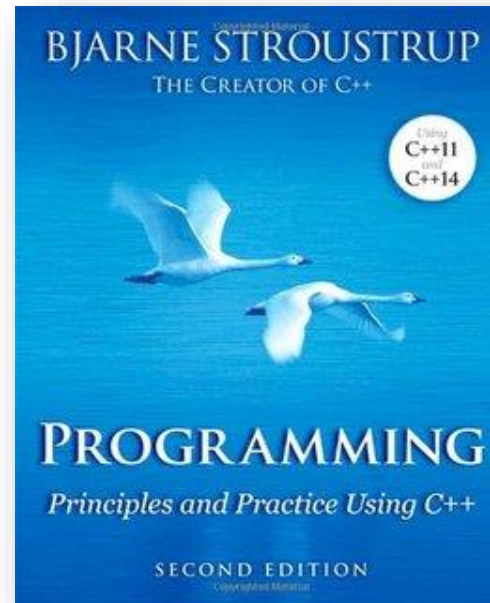
```
int Merge_point( Node* head1, Node* head2)
{
    int c1 = count(head1);
    int c2 = count(head2);
    int d;

    if(c1 > c2)
    {
        d = c1 - c2;
        return merge_point_util(d, head1, head2);
    }
    else
    {
        d = c2 - c1;
        return merge_point_util(d, head2, head1);
    }
}
```

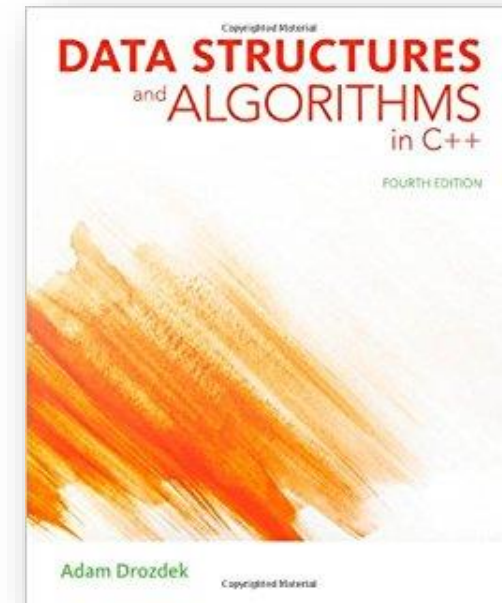
LITERATURE



Thomas H. Cormen
Introduction to Algorithms
Chapter III: Data structures
Page 236 (Linked Lists)



Bjarne Stroustrup
Principles and practice using C++
Chapter 17: vectors and free store
Page 569.



Adam Drozdek
Data structures and Algorithms in C++
Chapter 3 Linked List
Page 75