

Algorithm

Finite set of steps/instructions to solve a problem is called algorithm.

Analysis of Algorithms

Analysis of algorithms is the study of how efficient and effective an algorithm is in solving a problem. It involves evaluating the algorithm's performance in terms of:

- ❖ **Time complexity:** How long it takes to run.
- ❖ **Space complexity:** How much memory it uses.

This helps developers choose the best algorithm for a given task, especially when dealing with large data or limited resources.

Why Is It Important?

- ❖ **Efficiency:** Helps optimize programs for speed and memory usage.
- ❖ **Scalability:** Ensures algorithms perform well as input size grows.
- ❖ **Comparison:** Allows selection of the most suitable algorithm among alternatives.

Types of Algorithm Analysis

Algorithm analysis helps us understand how an algorithm performs under different conditions. The main types are:

1. Worst Case Analysis

What It Means:

This measures the **maximum time or resources** an algorithm might need — the slowest it can be.

Real Example: Searching for a Contact in Your Phone

Imagine you have 1,000 contacts and you're looking for someone named "Zara":

- ❖ If Zara is the **last contact** or **not in the list**, you'll check all 1,000 names.
- ❖ This is the **worst-case scenario**.
- ❖ **Time complexity: $O(n)$**

Real Example: Quick Sort

Quick Sort is fast most of the time, but if the pivot selection is poor (e.g., always choosing the smallest element), it can degrade to:

- ❖ **Worst-case time: $O(n^2)$**

2. Best Case Analysis

What It Means:

This measures the **minimum time or resources** needed — the fastest the algorithm can be.

Real Example: Searching for a Contact

If "Zara" is the **first contact**, you find her instantly.

- ❖ **Best-case time: $O(1)$**

Real Example: Insertion Sort

If the list is already sorted:

- ❖ Each item is compared once and placed correctly.
- ❖ **Best-case time: $O(n)$**

3. Average Case Analysis

What It Means:

This estimates the **typical performance** — assuming inputs are random or evenly distributed.

Real Example: Searching for a Contact

If Zara is somewhere in the middle:

- ❖ You might check around 500 contacts.
- ❖ **Average-case time: $O(n)$**

Real Example: Hash Table Lookup

If keys are evenly distributed:

- ❖ Most lookups take constant time.
- ❖ **Average-case time: $O(1)$**

5. Asymptotic Analysis

What It Means:

This focuses on how an algorithm behaves as the input size becomes **very large** — ignoring small details.

Real Example: Sorting a List of Names

- ❖ **Bubble Sort:** $O(n^2)$ — slow for large lists
- ❖ **Merge Sort:** $O(n \log n)$ — much faster as the list grows

Real Example: Web Search Engine

- ❖ Searching billions of pages:
 - Efficient algorithms like **Trie structures** or **Hashing** are used.
 - Asymptotic analysis helps engineers choose scalable solutions.

Summary Table with Real Examples

Type	Measures	Real Example	Time Complexity
Worst Case	Maximum effort	Searching last contact in phone	$O(n)$

Best Case	Minimum effort	Finding first contact	$O(1)$
Average Case	Typical effort	Random contact search	$O(n)$
Asymptotic	Growth with large inputs	Sorting millions of names with Merge Sort	$O(n \log n)$

Role of algorithms in computing

Algorithms play a crucial role in computing by providing a set of instructions for a computer to perform a specific task. They are used to **solve problems** and **carry out tasks** in computer systems, such as **sorting data**, **searching for information**, **image processing**, and much more. An algorithm defines the steps necessary **to produce the desired outcome**, and the computer follows the instructions to complete the task efficiently and accurately. The development of efficient algorithms is a central area of computer science and has significant impacts in various fields, from cryptography and finance to machine learning and robotics.

Key roles of algorithms in computing

❖ **Problem-solving:**

Algorithms break down complex problems into a series of manageable, logical steps, enabling computers to solve a vast range of issues.

❖ **Task automation:**

They are used to automate repetitive or complex tasks, saving time and effort for both users and developers.

❖ **Efficiency and optimization:**

Algorithms are designed to find the most efficient solutions, reducing the time and resources needed to complete a task.

❖ **Program blueprint:**

They serve as the blueprint for software, dictating the logic that a computer must follow, regardless of the specific programming language used.

❖ **Data processing and management:**

Algorithms are essential for sorting, searching, and processing large datasets. Examples include sorting numbers, recommending content on social media, or finding the shortest route in a navigation app.

❖ **Decision-making:**

Algorithms provide the logic for computers to make decisions based on specific conditions, which is the basis for everything from simple calculations to complex AI systems.

❖ **Security:**

They are crucial for security, with encryption and decryption algorithms protecting sensitive information like passwords and financial data.