

Algorithm

Finite set of steps/instructions to solve a problem is called algorithm.

Analysis of Algorithms

Analysis of algorithms is the study of how efficient and effective an algorithm is in solving a problem. It involves evaluating the algorithm's performance in terms of:

- ❖ **Time complexity:** How long it takes to run.
- ❖ **Space complexity:** How much memory it uses.

This helps developers choose the best algorithm for a given task, especially when dealing with large data or limited resources.

Why Is It Important?

- ❖ **Efficiency:** Helps optimize programs for speed and memory usage.
- ❖ **Scalability:** Ensures algorithms perform well as input size grows.
- ❖ **Comparison:** Allows selection of the most suitable algorithm among alternatives.

Types of Algorithm Analysis

Algorithm analysis helps us understand how an algorithm performs under different conditions.

The main types are:

1. Worst Case Analysis

What It Means:

This measures the **maximum time or resources** an algorithm might need — the slowest it can be.

Real Example: Searching for a Contact in Your Phone

Imagine you have 1,000 contacts and you're looking for someone named "Zara":

- ❖ If Zara is the **last contact** or **not in the list**, you'll check all 1,000 names.
- ❖ This is the **worst-case scenario**.
- ❖ **Time complexity:** $O(n)$

Real Example: Quick Sort

Quick Sort is fast most of the time, but if the pivot selection is poor (e.g., always choosing the smallest element), it can degrade to:

- ❖ **Worst-case time:** $O(n^2)$

★ 2. Best Case Analysis

🔍 What It Means:

This measures the **minimum time or resources** needed — the fastest the algorithm can be.

Real Example: Searching for a Contact

If "Zara" is the **first contact**, you find her instantly.

- ❖ **Best-case time:** $O(1)$

Real Example: Insertion Sort

If the list is already sorted:

- ❖ Each item is compared once and placed correctly.
- ❖ **Best-case time:** $O(n)$

||| 3. Average Case Analysis

🔍 What It Means:

This estimates the **typical performance** — assuming inputs are random or evenly distributed.

Real Example: Searching for a Contact

If Zara is somewhere in the middle:

- ❖ You might check around 500 contacts.
- ❖ **Average-case time: $O(n)$**

Real Example: Hash Table Lookup

If keys are evenly distributed:

- ❖ Most lookups take constant time.
- ❖ **Average-case time: $O(1)$**

5. Asymptotic Analysis

What It Means:

This focuses on how an algorithm behaves as the input size becomes **very large** — ignoring small details.

Real Example: Sorting a List of Names

- ❖ **Bubble Sort:** $O(n^2)$ — slow for large lists
- ❖ **Merge Sort:** $O(n \log n)$ — much faster as the list grows

Real Example: Web Search Engine

- ❖ Searching billions of pages:
 - Efficient algorithms like **Trie structures** or **Hashing** are used.
 - Asymptotic analysis helps engineers choose scalable solutions.

Summary Table with Real Examples

Type	Measures	Real Example	Time Complexity
Worst Case	Maximum effort	Searching last contact in phone	$O(n)$

Best Case	Minimum effort	Finding first contact	$O(1)$
Average Case	Typical effort	Random contact search	$O(n)$
Asymptotic	Growth with large inputs	Sorting millions of names with Merge Sort	$O(n \log n)$

Role of algorithms in computing

Algorithms play a crucial role in computing by providing a set of instructions for a computer to perform a specific task. They are used to solve problems and carry out tasks in computer systems, such as sorting data, searching for information, image processing, and much more. An algorithm defines the steps necessary to produce the desired outcome, and the computer follows the instructions to complete the task efficiently and accurately. The development of efficient algorithms is a central area of computer science and has significant impacts in various fields, from cryptography and finance to machine learning and robotics.

Key roles of algorithms in computing

- ❖ **Problem-solving:**

Algorithms break down complex problems into a series of manageable, logical steps, enabling computers to solve a vast range of issues.

- ❖ **Task automation:**

They are used to automate repetitive or complex tasks, saving time and effort for both users and developers.

- ❖ **Efficiency and optimization:**

Algorithms are designed to find the most efficient solutions, reducing the time and resources needed to complete a task.

- ❖ **Program blueprint:**

They serve as the blueprint for software, dictating the logic that a computer must follow, regardless of the specific programming language used.

- ❖ **Data processing and management:**

Algorithms are essential for sorting, searching, and processing large datasets. Examples include sorting numbers, recommending content on social media, or finding the shortest route in a navigation app.

❖ **Decision-making:**

Algorithms provide the logic for computers to make decisions based on specific conditions, which is the basis for everything from simple calculations to complex AI systems.

❖ **Security:**

They are crucial for security, with encryption and decryption algorithms protecting sensitive information like passwords and financial data.