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'clk' is the system clock, 'enable' activates the multiplication operation, 'A' is the 8-bit unsigned multiplicand input, 'B' is the 8-bit unsigned multiplier input, and 'C' is the 16-bit unsigned product output.

When designing multipliers there is always a compromise to be made between how fast the multiplication process is done and how much hardware we are using for its implementation.

A simple multiplication method that is slow, but efficient in use of hardware is the shift-and-add method. In this method, depending on bit i of operand A, either operand B is added to the collected partial result and then shifted to the right (when bit i is $\mathbf{1}$), or (when bit i is $\mathbf{0}$) the collected partial result is shifted one place to the right without being added to B.

This method is justified by considering how binary multiplication is done manually. Figure 11.2 shows manual multiplication of two 8-bit binary numbers.

We start considering bits of A from right to left. If a bit value is **0** we select 00000000 to be added with the next partial product, and if it is a **1**, the value of B is selected. This process repeats, but each time 00000000 or B is selected, it is written one place to the left with respect to the previous value. When all bits of A are considered, we add all calculated values to come up with the multiplication results.

Understanding hardware implementation of this procedure becomes easier if we make certain modifications to this procedure. First, instead of having to move our observation point from one bit of *A* to another, we put *A* in a shiftregister, always observe its right-most bit, and after every calculation, we move it one place to the right, making its next bit accessible.

Second, for the partial products, instead of writing one and the next one to its left, when writing a partial product, we move it to the right as we are writing it, and the next one will not have to be shifted.

Finally, instead of calculating all partial products and at the end adding them up, when a partial product is calculated, we add it to the previous partial result and write the newly calculated value as the new partial result. Therefore, if the bit of *A* that is being observed is **0**, 00000000 is to be added to the previously calculated partial result, and the new value should be shifted one place to the right. In this case, since the value being added to the partial result is 00000000, adding is not necessary, and only shifting the partial result is sufficient. This process is called *shift*. However, if bit of *A* being observed is **1**, *B* is to be added to the previously calculated partial result, and