

# Assignment 2: Joint-Space Trajectory Generation and Smoothness Analysis

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## Objective

The objective of this assignment is to move beyond static robot poses and understand how a robot transitions between configurations over time. Students will learn how to generate **joint-space trajectories** between two robot configurations and analyze the effect of different trajectory choices on motion smoothness.

This assignment introduces the concept of **trajectory as a function of time**, which is a critical foundation for trajectory optimization and learning-based methods explored later in the project.

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## Problem Description

Consider the same **2-link planar robotic arm** studied in Assignment 1, with link lengths  $l_1$ ,  $l_2$ . The robot starts at an initial joint configuration:

$(q_1^{\text{start}}, q_2^{\text{start}})$

and must move to a final joint configuration:

$(q_1^{\text{end}}, q_2^{\text{end}})$

Instead of directly visualizing only the start and end poses, you are now required to generate **continuous joint trajectories** that describe how the robot moves between these two configurations over a fixed time duration  $T$ .

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## Trajectory Representation

A joint-space trajectory is defined as:

$q_1(t), q_2(t), \quad t \in [0, T]$

You will generate and compare **two types of trajectories**:

1. **Linear joint-space trajectory**
  2. **Smooth polynomial joint-space trajectory**
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# Expected Work

## Linear Joint-Space Trajectory

In this approach, each joint angle varies linearly with time between its start and end values. This results in a simple trajectory but may introduce abrupt changes in velocity at the start and end of motion.

Students should:

- Define a time vector  $t \in [0, T]$
  - Linearly interpolate  $q_1(t)$  and  $q_2(t)$
  - Plot joint angles as functions of time
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## Smooth Polynomial Trajectory

To achieve smoother motion, students will generate a **polynomial trajectory** (cubic or quintic) that ensures smooth start and stop conditions.

The trajectory should:

- Start and end at the specified joint angles
- Have zero velocity at the start and end of motion
- Produce smoother joint angle profiles compared to linear interpolation

Students should:

- Compute polynomial coefficients for each joint
  - Plot the resulting joint trajectories over time
  - (Optional) Compute and plot joint velocities to observe smoothness
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## Analysis and Comparison

Students must compare the two trajectories by:

- Plotting joint angle vs. time for both methods
- Observing differences in smoothness near the start and end points
- Discussing which trajectory is more suitable for a real robotic system and why

No animation is required. The emphasis is on **trajectory plots and interpretation**.

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# Submission Requirements

Each submission must include:

1. A Python script or Jupyter notebook containing:
  - Linear trajectory generation
  - Polynomial trajectory generation
2. Clearly labeled plots showing:
  - Joint angles vs. time (for both trajectories)
3. A short written discussion (5–7 sentences) addressing:
  - Differences between linear and smooth trajectories
  - Why smoothness is important for real robots

Ps. Assignment is to be submitted on github, the instructions on how to submit is in the updated readme

**Deadline - 23rd December, EOD.**