Assignment#1

Group Members

Muhammad Hamza jamil 2572890 s8mujami@stud.uni-saarland.de

Hacane Hechehouche 2571617 S8hahech@stud.uni-Saarland.de

a)
i) is Symmetric

$$A = \begin{bmatrix} 4 & 2 & -1 \\ 2 & -1 & 9 \\ x & -2 & -8 \end{bmatrix}$$

$$A = A^{T}$$

$$A^{T} = \begin{pmatrix} 4 & 2 & x \\ 2 & -1 & -2 \\ -1 & y & -8 \end{pmatrix} = \begin{pmatrix} 4 & 2 & -1 \\ 2 & -1 & y \\ x & -2 & -8 \end{pmatrix}$$

$$\boxed{x = -1} \qquad \boxed{y = -2}$$

iil is Orthogonal:

if the Matrix is orthogonal the all the rectors in the Matrix are orthonormal to each other. So just take the product of vectors. a

Vectors.
$$\chi$$

$$\begin{pmatrix} 4 \\ 2 \\ -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} 2 \\ -1 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} 2 \\ -1 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} 2 \\ -1 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} 2 \\ -1 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ -2 \end{pmatrix} = 0$$

$$\begin{pmatrix} -2$$

$$A = \begin{bmatrix} 4 & 2 & -1 \\ 2 & -1 & 4 \\ x & -2 & -8 \end{bmatrix}$$

$$A = \begin{cases} 4 & 2 & -1 \\ 2 & -1 & 4 \\ x & -2 & -8 \end{cases} = 5$$

$$A = \begin{cases} 4 & 2 & -1 \\ 2 & -1 & y \\ x-4 & 0 & -2y-8 \end{cases} R_3^2 - 2R_2^2 + R_3$$

of matrix should be 0 so

$$\chi - 4 = 0$$

$$\chi = 4$$

$$-2y - 8 = 6$$

$$-2y = 8$$

$$y = -4$$

in) Singular

$$A = \begin{bmatrix} 4 & 2 & -1 \\ 2 & -1 & 4 \end{bmatrix}$$

$$|A| = \begin{bmatrix} 4 & 8 + 24 \\ -2 & -8 \end{bmatrix}$$

$$O = \begin{bmatrix} 16 + 8y + 32 + 2xy + 4 - x \\ -2 & -8 \end{bmatrix}$$

$$O = \begin{bmatrix} 52 + 8y - x + 2xy \\ -2 & -1 \end{bmatrix}$$

So we have 2 variables band having one equation so we cannot compute the value of x and y

$$A = \begin{pmatrix} 4 & 2 & -1 \\ 2 & -1 & 0 \\ 4 & -2 & 9 \end{pmatrix}$$

Elgen Decomposition

$$\begin{vmatrix} 4-x & 2 & -1 \\ 2 & -1-x & 0 \\ 4 & -2 & -8-x \end{vmatrix} = 0$$

$$4 = 2 \left(-8 - 2 \right) \left[(4 - 2) (-1 - 2) - 4 \right] - 42 = 0$$

$$(-8 - 2) \left[-4 - 42 + 2 + 2 - 4 \right] = 0$$

$$9^{2}-39-8=49$$

 $9^{2}-79-8=0$
 $(9-8)(9+1)=6$
 $(9-8)(9+1)=6$

Find Eigen vector

$$\begin{vmatrix}
5 & 2 & -1 \\
2 & 0 & 0
\end{vmatrix}
\begin{vmatrix}
7 & 2 & -1 \\
2 & -9 & 0 \\
4 & -2 & -16
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -9 & 0 \\
4 & -2 & -16
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -9 & 0 \\
4 & -2 & -16
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -9 & 0 \\
4 & -2 & -16
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -9 & 0 \\
4 & -2 & -16
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -9 & 0 \\
4 & -2 & -16
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -9 & 0 \\
4 & -2 & -16
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -9 & 0 \\
4 & -2 & -16
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -9 & 0 \\
4 & -2 & -16
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16 & 1
\end{vmatrix}$$

$$\begin{vmatrix}
7 & 2 & -1 \\
2 & -16$$

$$x = -8/5$$

$$(u + 8/5) 2 - 1$$

$$2 - 1 + 8/6 0$$

$$4 - 2 - 8 + 8/6$$

$$\sqrt{v_2} = 0$$

$$\sqrt{v_3} = 0$$

$$\frac{28}{5} v_1 + 2v_2 - v_3 = 0$$

$$2 v_1 + \frac{3}{5} v_2 = 0$$

$$4v_1 - 2v_2 - \frac{32}{5} v_3 = 0$$

$$V_1 = -\frac{3}{1p} V_2$$

$$\frac{28}{5} \left(\frac{-3}{10} \sqrt{2} \right) + 2 \sqrt{2} - \sqrt{3} = 0$$

$$\frac{-84 + 100V_2}{50} = V_3$$

$$\frac{16}{50}V_2 = V_3$$

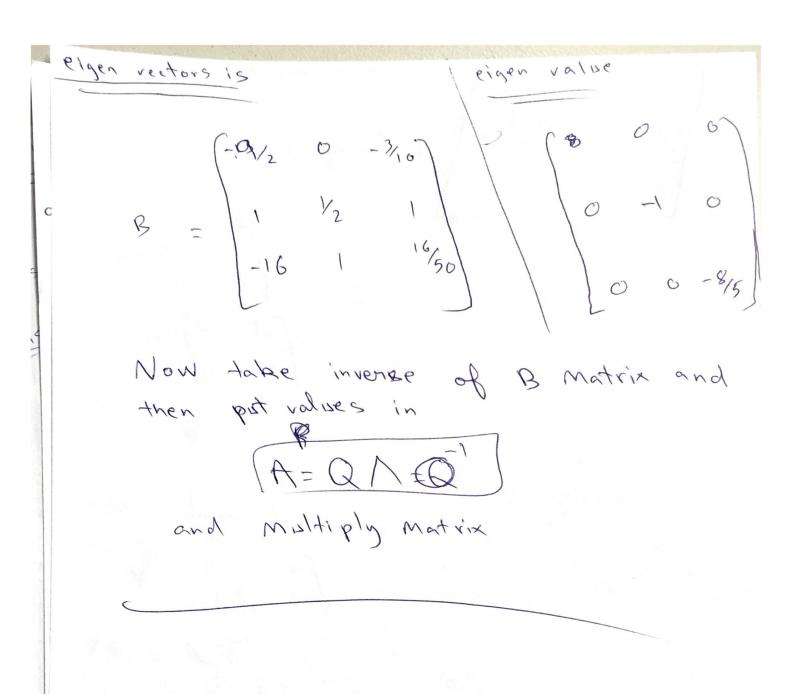
$$\frac{28}{84}$$
Let $\sqrt{2} = 1$

$$\sqrt{2} = \sqrt{3}$$

$$\sqrt{2} = \sqrt{3}$$

$$\sqrt{3} = \sqrt{16}$$

$$\sqrt{3} = \sqrt{50}$$



Eigen Values

$$\begin{array}{lll}
\lambda = \begin{pmatrix} 1 & 0 \\ 0 & 4 \end{pmatrix} \\
V = \begin{pmatrix} 3 & 2 \\ 1 & 1 \end{pmatrix} \\
A = V & X & V^{-1} \\
V = \begin{pmatrix} 1 & -2 \\ -1 & 3 \end{pmatrix} \\
V = \begin{pmatrix} 1 & -2 \\ -1 & 3 \end{pmatrix} \\
A = \begin{pmatrix} 3 & 2 \\ 1 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 \\ -4 & 12 \end{pmatrix} \\
A = \begin{pmatrix} 3 & 2 \\ 1 & 1 \end{pmatrix} \begin{pmatrix} 1 & -2 \\ -4 & 12 \end{pmatrix} \\
= \begin{pmatrix} 3 - 8 & -6 + 24 \\ 1 - 4 & -2 + 12 \end{pmatrix} = \begin{pmatrix} -5 & +18 \\ -3 & 10 \end{pmatrix}$$

Show that eigen values of AB
is equals to eigen values of BA

Ans We will show that AB and BA have the same characteristics polynomial

$$P_{AB} = det(AB - \lambda I)$$

$$= det(ABAA^{-1} - \lambda AA^{-1})$$

$$= det(A(BA - \lambda I)A^{-1})$$

$$= det(A) det(BA - \lambda I) det(A^{-1})$$

= det(A) det(BA-XI) 1
det(A*)

= det (BA- XI)

= PBA and se.

$$A.3.A)$$

$$B^{T}CO = U^{T}X^{T}X^{T}U^{T}$$

$$= (XU)^{T}X^{T}U^{T}$$

$$= ||X.U||^{2} > 0$$

$$A.3.B)$$

$$||U^{T}.x||_{2}^{2} = (U^{T}x)^{T}. U^{T}x$$

$$= x^{T}. U. U^{T}. x$$

$$= x^{T}. I. x$$

$$= x^{T}. x$$

$$= ||x||_{2}^{2} = 1$$

from the eigen decomposition property of a we can say that

Obviously these values lie in [], -- In] as we can see

by setting (10,0,--0) and w= (0,0,--,1) respectively then then minimum is obviously In which is the smellest