



Adder/Subtractor, BCD Adder, Multiplier

Instructor Name: Engr. Rimsha

- BCD Adder
- Binary Multiplier
- Magnitude Comparator

Decimal (BCD) Adder

- **Computers or calculators that perform arithmetic operation directly in the decimal number system represents decimal number in **binary coded form****
- **An adder for such a computer must employ arithmetic circuits that accepts coded decimal number and present results in the same code**
- **To add two BCD's, we require**
 - 9 inputs: eight inputs for two BCDs and one carry-in. Since four bits are required to code each decimal digit
 - 5 outputs: four outputs for one BCD and one carry-out

Decimal Adder

- **Design Strategy?**

Decimal Adder

- To design a BCD adder we require a truth table with 2^9 entries (since 9 inputs). This may become too difficult to work with so we devise some easy alternative to design a BCD adder. This is shown in table 4-5
- Each digit doesn't exceed 9 and so the output sum can't exceed, $9+9+1 = 19$ (two BCD digits and input carry)
- Suppose we apply two BCD digits to a 4-bit binary adder
- The adder will form the sum in binary and produces a result that ranges from 0 through 19
- These binary numbers are listed in table 4-5 and are labeled by symbols K , Z_8 , Z_4 , Z_2 and Z_1 . (K is the output carry). But the output sum must be represented in BCD (not binary) and should appear in the form listed in the columns C , S_8 , S_4 , S_2 and S_1 under BCD sum
- The problem is to find a **rule** by which **binary sum** is **converted** to corresponding **BCD sum**

The truth table

Derivation of a BCD Adder

K	Binary Sum				BCD Sum					Decimal
	Z _B	Z ₄	Z ₂	Z ₁	C	S _B	S ₄	S ₂	S ₁	
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	1	0	0	0	0	1	1
0	0	0	1	0	0	0	0	1	0	2
0	0	0	1	1	0	0	0	1	1	3
0	0	1	0	0	0	0	1	0	0	4
0	0	1	0	1	0	0	1	0	1	5
0	0	1	1	0	0	0	1	1	0	6
0	0	1	1	1	0	0	1	1	1	7
0	1	0	0	0	0	1	0	0	0	8
0	1	0	0	1	0	1	0	0	1	9
0	1	0	1	0	1	0	0	0	0	10
0	1	0	1	1	1	0	0	0	1	11
0	1	1	0	0	1	0	0	1	0	12
0	1	1	0	1	1	0	0	1	1	13
0	1	1	1	0	1	0	1	0	0	14
0	1	1	1	1	1	0	1	0	1	15
1	0	0	0	0	1	0	1	1	0	16
1	0	0	0	1	1	0	1	1	1	17
1	0	0	1	0	1	1	0	0	0	18
1	0	0	1	1	1	1	0	0	1	19

Correction for BCD Adder

- From the table it is apparent that when binary **sum** is equal to or less than **1001** (decimal 9), the corresponding BCD number is identical and therefore **no correction** is needed.
- **Modifications** are needed if the sum is greater than **1001** as we get non-valid BCD representation. The **addition** of **binary 6 (0110)** to binary sum converts it to the correct BCD representation and also produces an output carry as required (refer to section 1-7)
- The logic circuit that detects the necessary correction can be derived from the table entries. Correction (adding decimal 6 or binary 0110) is needed when the binary sum has an output
 - $K = 1$
 - $Z_8 Z_4 = 1$
 - $Z_8 Z_2 = 1$

Correction for BCD Adder

- This **condition for correction** and an **output carry** can be expressed as
 - $C = K + Z_8Z_4 + Z_8Z_2$
- In figure 4-14, the output carry generated from the bottom adder can be ignored since this is already available at the output carry terminal
- A decimal parallel adder that adds n decimal digits (in BCD form) needs n BCD adder stages with output carry from one stage connected to the input carry of next higher-order stage

Block Diagram

Numbers that need correction (add 6) are:

K	Z ₈	Z ₄	Z ₂	Z ₁	
0	1	0	1	0	(10)
0	1	0	1	1	(11)
0	1	1	0	0	(12)
0	1	1	0	1	(13)
0	1	1	1	0	(14)
0	1	1	1	1	(15)
1	0	0	0	0	(16)
1	0	0	0	1	(17)
1	0	0	1	0	(18)
1	0	0	1	1	(19)

$$C = K + Z_8Z_4 + Z_8Z_2$$

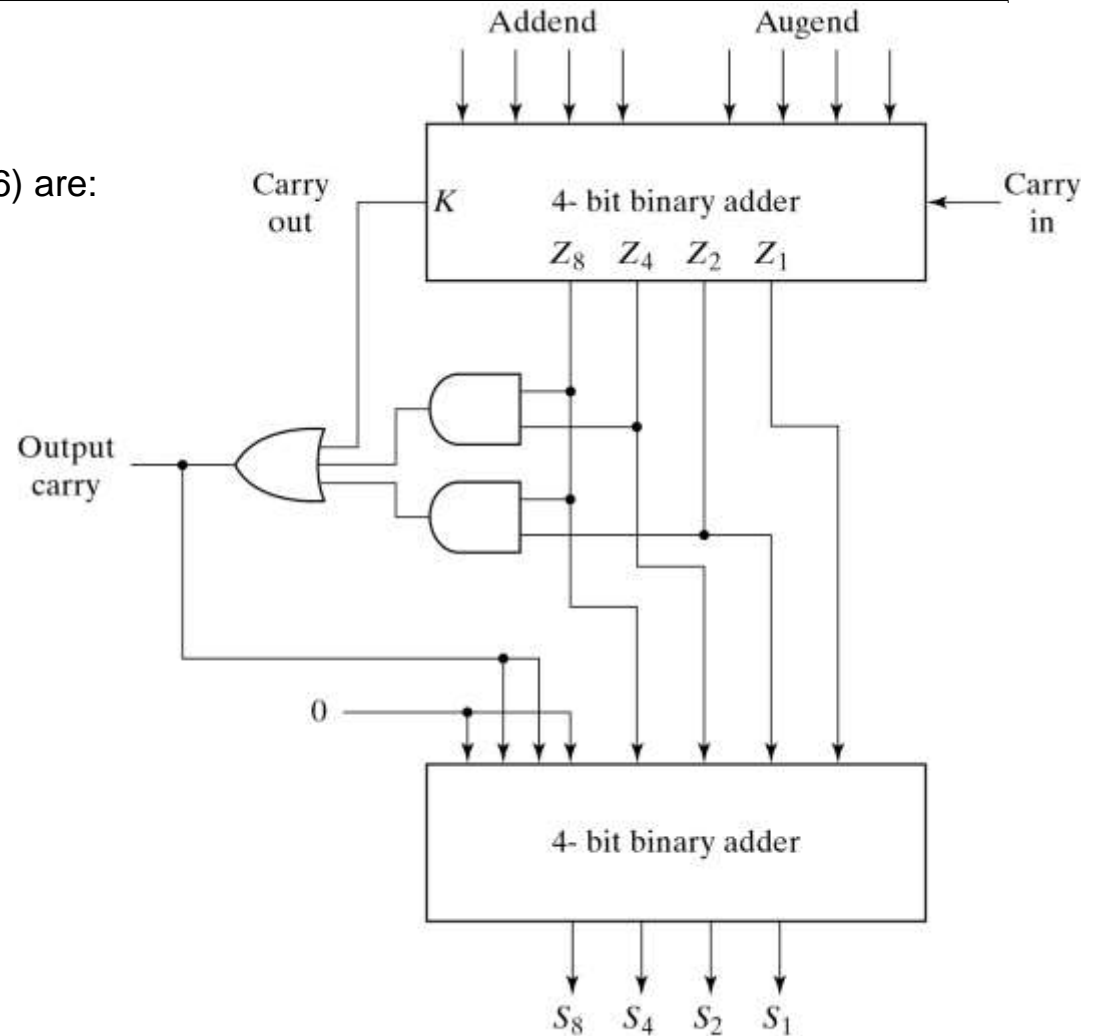


Fig. 4-14 Block Diagram of a BCD Adder

Binary Multiplier

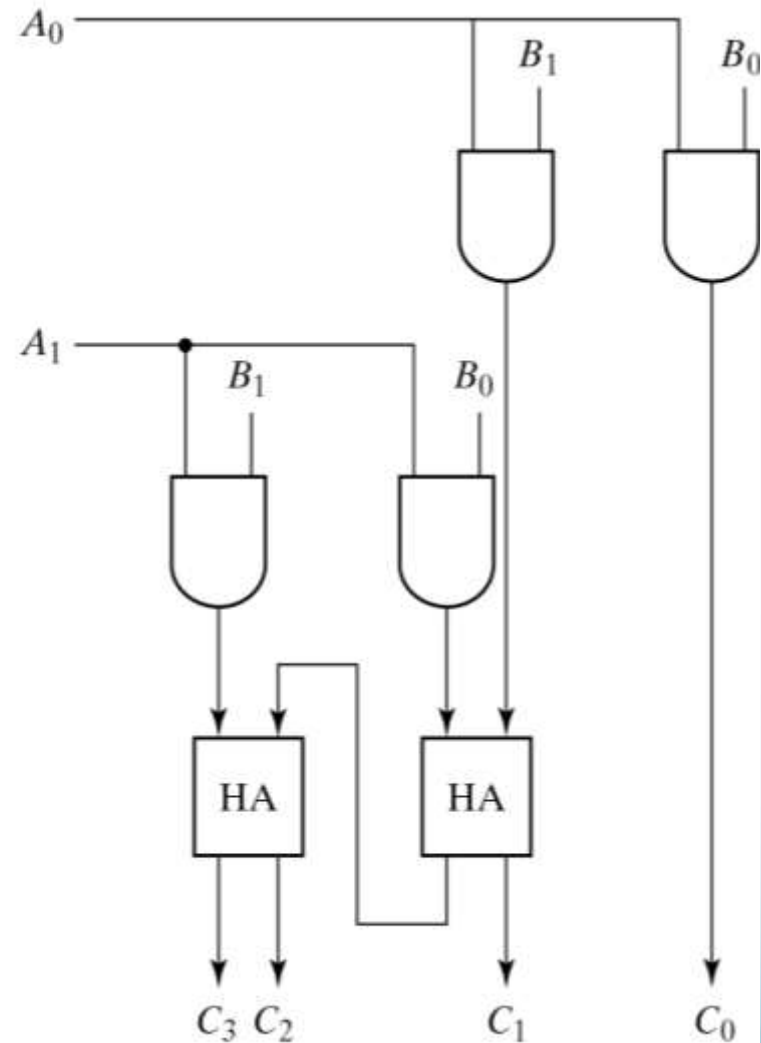
- Multiplication of the binary number is performed in the same way as in decimal numbers. The multiplicand is multiplied by each bit of the multiplier starting from the least significant bit
- Each such multiplication forms a **partial product**. Successive partial products are **shifted** one position to the left. The final product is obtained from the **sum** of the partial products
- Consider the binary multiplication of 2-bit numbers where B_1 and B_2 are multiplicand bits and A_1 and A_0 are multiplier bits. C_3 C_2 C_1 C_0 are the product bits

Binary Multiplier

- The first partial product is formed by multiplying A_0 by $B_1 B_0$. The multiplication of any two bits produces a 1 if both bits are 1, otherwise it produces a 0. This is identical to AND operation. Therefore partial product can be implemented with an AND gates as shown in figure 4 – 15
- The second partial product is formed by multiplying A_1 by $B_1 B_0$ and shifted one position to the left
- The two **partial products** are **added** with **two half adder** (HA) circuits. If there are more bits in the partial products then we use full adders to produce the sum of the partial products
- The least significant bit of the partial product doesn't have to go through an adder since it is formed by the output of the first AND gate

2-bit by 2-bit Binary Multiplier

		B_1	B_0
	A_1	$A_1 B_1$	$A_1 B_0$
	A_0	$A_0 B_1$	$A_0 B_0$
C_3	C_2	C_1	C_0



J-bit by K-bit Binary Multiplier

- A combinational circuit for binary multiplier with more bits can be constructed in a similar way. A bit of the multiplier is ANDed with each bit of the multiplicand in as many levels as there are bits in the multiplier
- The binary output in each level of AND gate is added with the partial product of the previous level to form a new partial product. The last level produces the product
- For J multiplier bits and K multiplicand bits we need $(J \times K)$ AND gates and $(J - 1)$ K bit adders to produce a product of $J + K$ bits

4-bit by 3-bit binary multiplier

- Consider a multiplier circuit that multiplies a binary number of four bits by a number of three bits.
- Let the multiplicand is represented by $B_3 B_2 B_1 B_0$ and the multiplier by $A_2 A_1 A_0$
- Since $K = 4$ and $J = 3$, we need 12 AND gates and two 4 – bit adders to produce a product of seven bits

$$\begin{array}{r}
 B_3 B_2 B_1 B_0 \\
 \times A_2 A_1 A_0 \\
 \hline
 A_0 B_3 A_0 B_2 A_0 B_1 A_0 B_0 \\
 A_1 B_3 A_1 B_2 A_1 B_1 A_1 B_0 \\
 A_2 B_3 A_2 B_2 A_2 B_1 A_2 B_0 \\
 \hline
 \end{array}$$

4-bit by 3-bit Binary Multiplier

$$\begin{array}{r}
 B_3 B_2 B_1 B_0 \\
 \times A_2 A_1 A_0 \\
 \hline
 A_0 B_3 A_0 B_2 A_0 B_1 A_0 B_0 \\
 A_1 B_3 A_1 B_2 A_1 B_1 A_1 B_0 \\
 A_2 B_3 A_2 B_2 A_2 B_1 A_2 B_0
 \end{array}$$

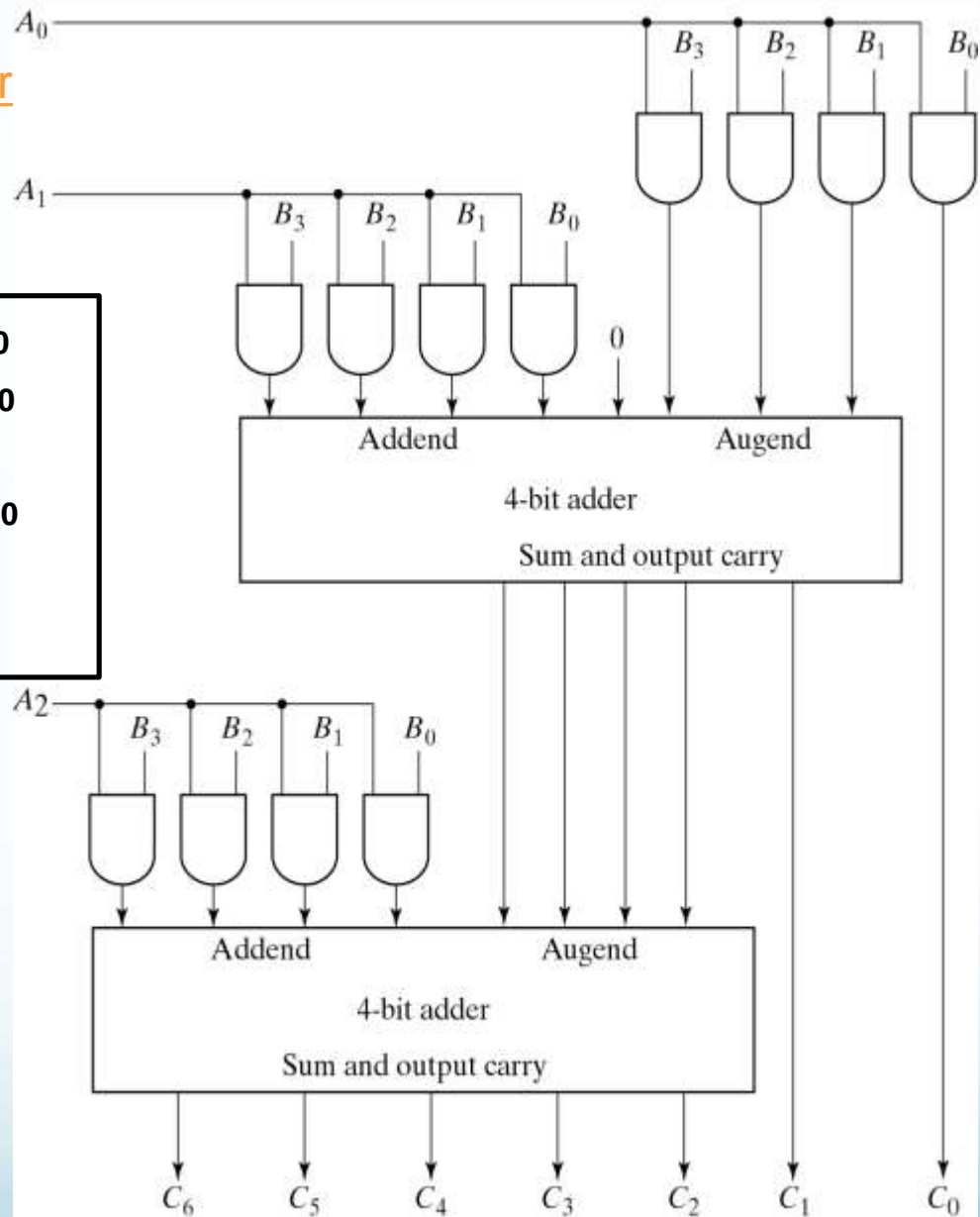


Fig. 4-16 4-Bit by 3-Bit Binary Multiplier



The End