

Question 2

Customer ID values:
(2, 3, 5, 7, 11, 17, 19, 23, 29, 31)

(a) hash function = $h(k) = k \bmod 6$

0		
1		
2		
3		
4		
5		

insert 2 $2 \bmod 6 = 2$.

0		
1		
2	2	
3		
4		
5		

insert 5, $5 \bmod 6 = 5$

0		
1		
2	2	
3	3	
4		
5	5	

insert 3, $3 \bmod 6 = 3$

0		
1		
2	2	
3	3	
4		
5		

insert 7, $7 \bmod 6 = 1$.

0		
1	7	
2	2	
3	3	
4		
5	5	

insert 11

0		
1	7	
2	2	
3	3	
4		
5	5, 11	

11 mod 6 = 5

insert 17, 17 mod 6 = 5

0		
1	7	
2	2	
3	3	
4		
5	5, 11, 17	

insert 19, 19 mod 6 = 1

0		
1	7, 19	
2	2	
3	3	
4		
5	5, 11, 17	

insert 23, 23 mod 6 = 5

0		
1	7, 19	
2	2	
3	3	
4		
5	5, 11, 17	

overflow bucket

insert 29

29 mod 6 = 5

0		
1	7, 19	
2	2	
3	3	
4		
5	5, 11, 17	→ [23, 29]

insert 31

31 mod 6 = 1

0		
1	7, 19, 31	
2	2	
3	3	
4		
5	5, 11, 17	→ [23, 29]

at the end table will be

0		
1	7, 19, 31	
2	2	
3	3	
4		
5	5, 11, 17	→ [23, 29]

(b)

as to access key from normal bucket we need 1 I/O and to access key(custom ID) from overflow bucket we need 2 I/O so

$$\text{average no. of block access} = \left(\text{no. of I/O} \times \frac{\text{IDs in normal bucket}}{\text{total ID's}} \right) + \left(\text{no. of I/O} \times \frac{\text{IDs in overflow bucket}}{\text{total ID's}} \right)$$

$$= \left(1 \times \frac{8}{10} \right) + \left(2 \times \frac{2}{10} \right)$$

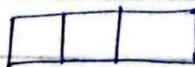
$$= \frac{8}{10} + \frac{4}{10}$$

$$= \frac{12}{10}$$

$$= 1.2$$

(c) Expandable Hashing $h(k) = k \bmod 7$

Initially, the first 3 records will be inserted as it because our bucket can hold max 3 records and we also do not need directory initially.



$$d = d' = 0$$

$$\text{insert } 2, 2 \bmod 7 = 2 = 010$$

2		
---	--	--

$$\text{insert } 3, 3 \bmod 7 = 3 = 011$$

2	3	
---	---	--

insert 5

$$5 \bmod 7 = 5 = 101$$

2	3	5
---	---	---

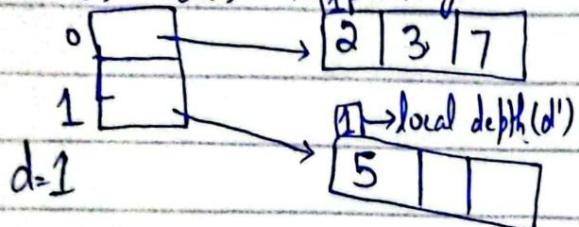
insert 7

$$7 \bmod 7 = 0 = 000$$

overflow, as $d=d$

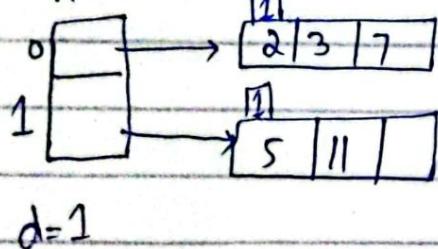
so split the bucket

also double the directory.



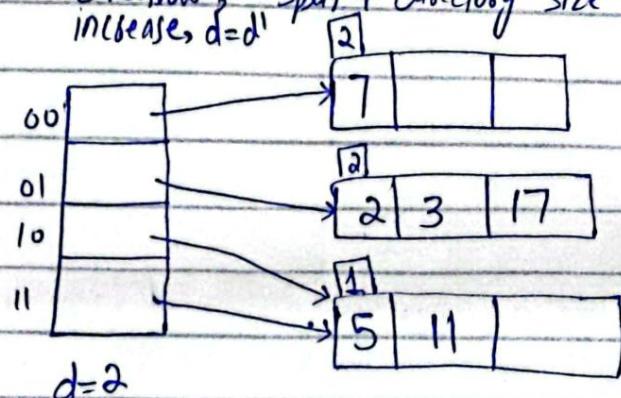
insert 11

$$11 \bmod 7 = 4 = 100$$

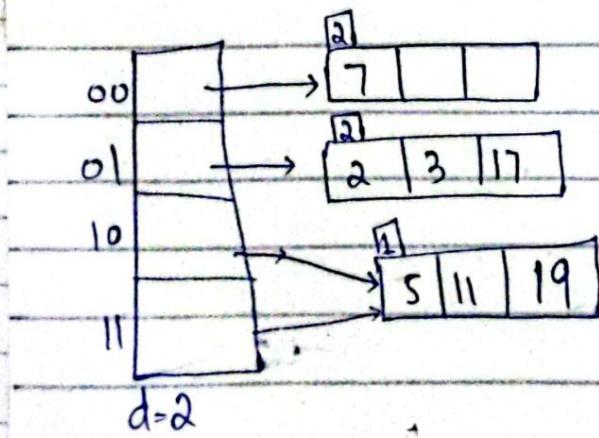


insert 17, $17 \bmod 7 = 3 = 011$

overflow, split + directory size increase, $d=d^1$

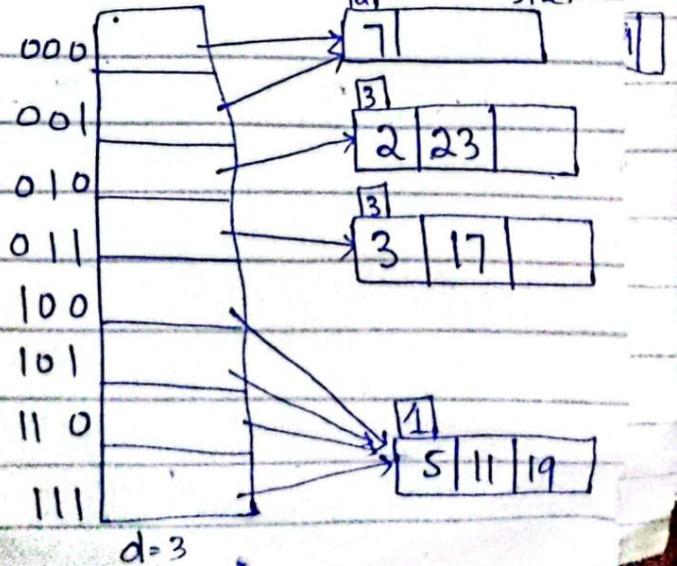


insert 19, $19 \bmod 7 = 5 = 101$



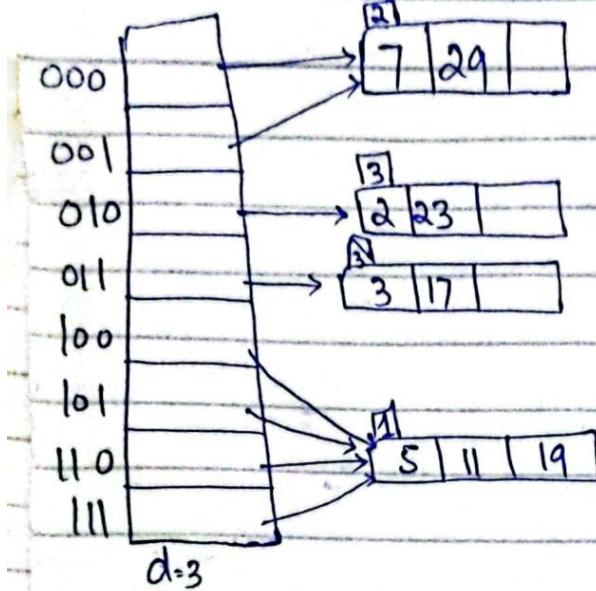
insert 23, $23 \bmod 7 = 2 = 010$

overflow, as $d=d^1$ so we will split the bucket and also increase directory size.

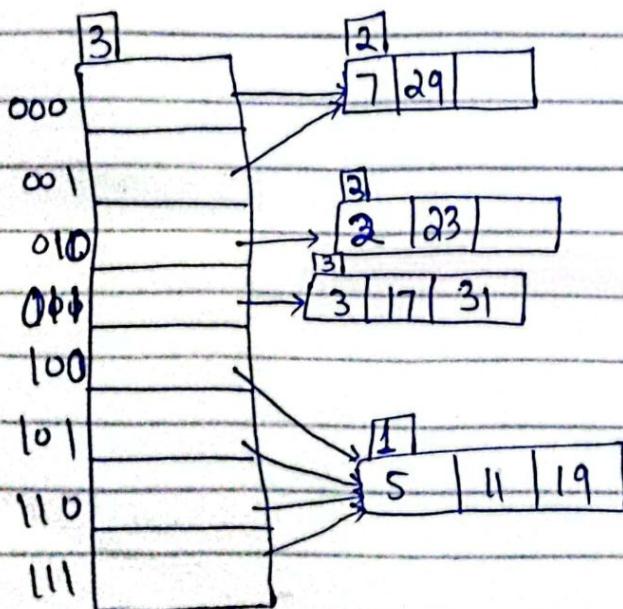


insert 29

$$29 \bmod 7 = 1 = 001$$

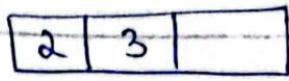
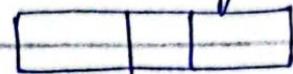


insert 31 , $31 \bmod 7 = 3 = 011$

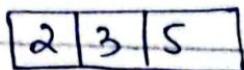


(d) As we have to show each step of dynamic hashing, so for that I will take help from part (c) as I have already done working there.

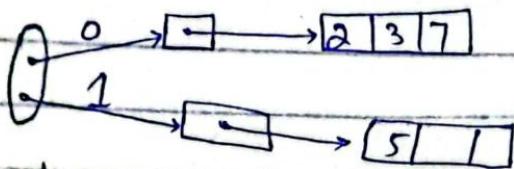
initially
insert 2 insert 3



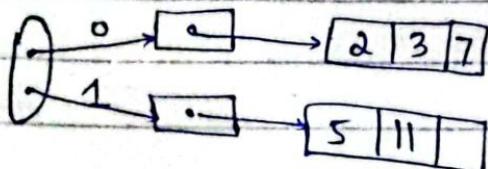
insert 5



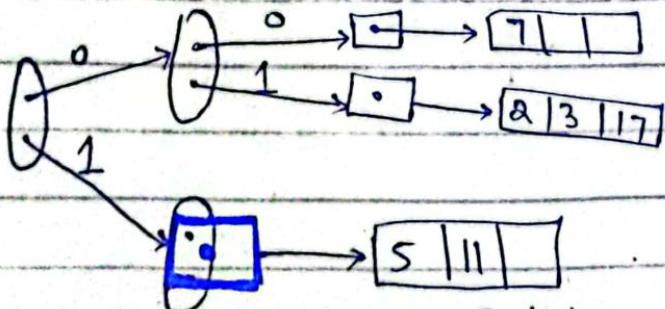
insert 7, $7 \bmod 7 = 0 = 000$
overflow



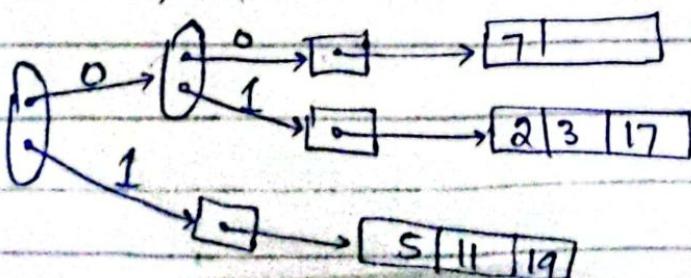
insert 11, $11 \bmod 7 = 4 = 100$



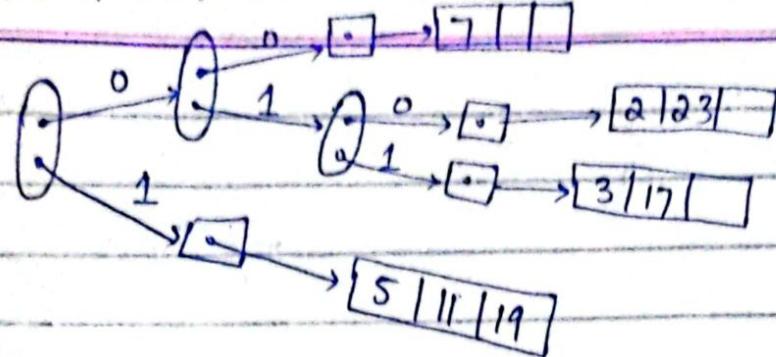
insert 17, $17 \bmod 7 = 3 = 011$



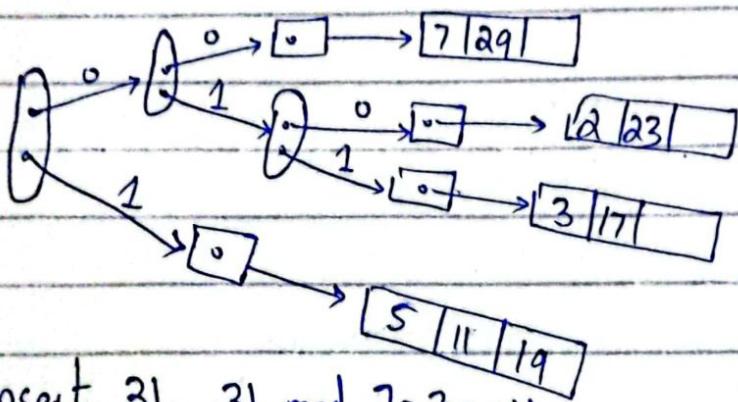
insert 19, $19 \bmod 7 = 5 = 101$



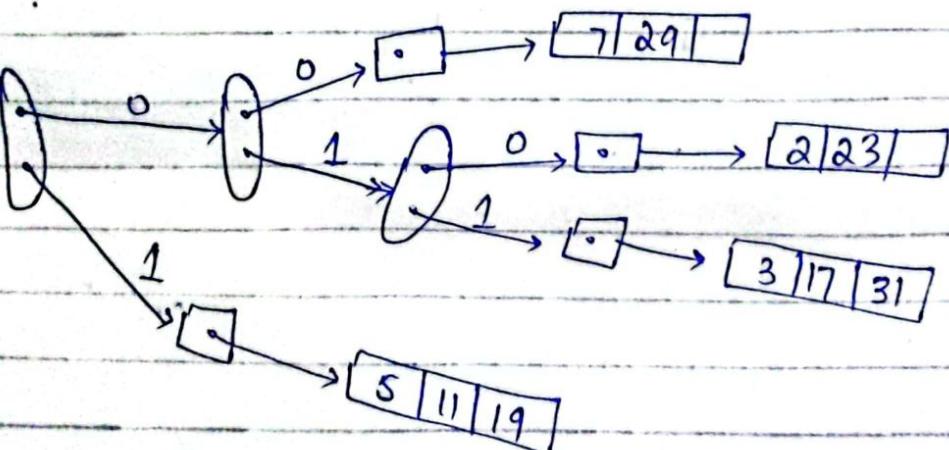
insert 23, $23 \bmod 7 = 2 = 010$



insert 29, $29 \bmod 7 = 1 = 001$



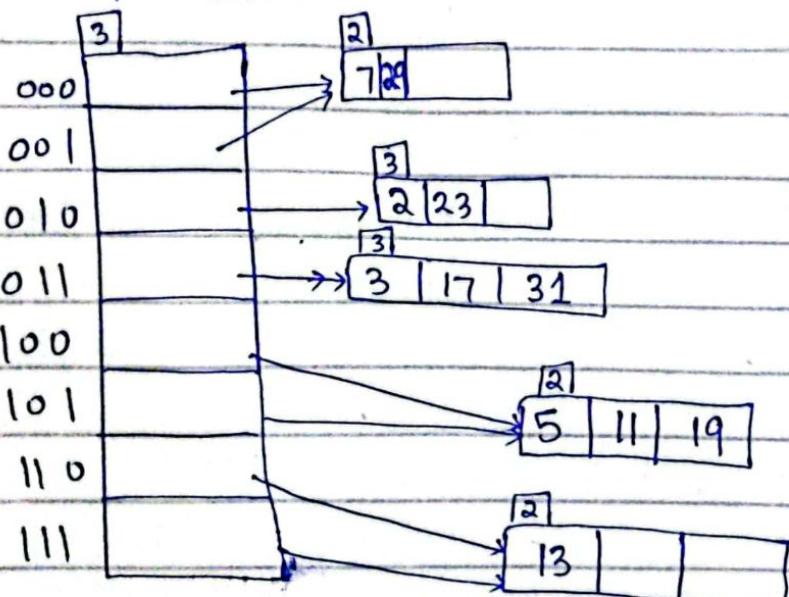
insert 31, $31 \bmod 7 = 3 = 011$



(7) insert 13 into final structure of part c.

$$13 \bmod 7 = 6 = 110$$

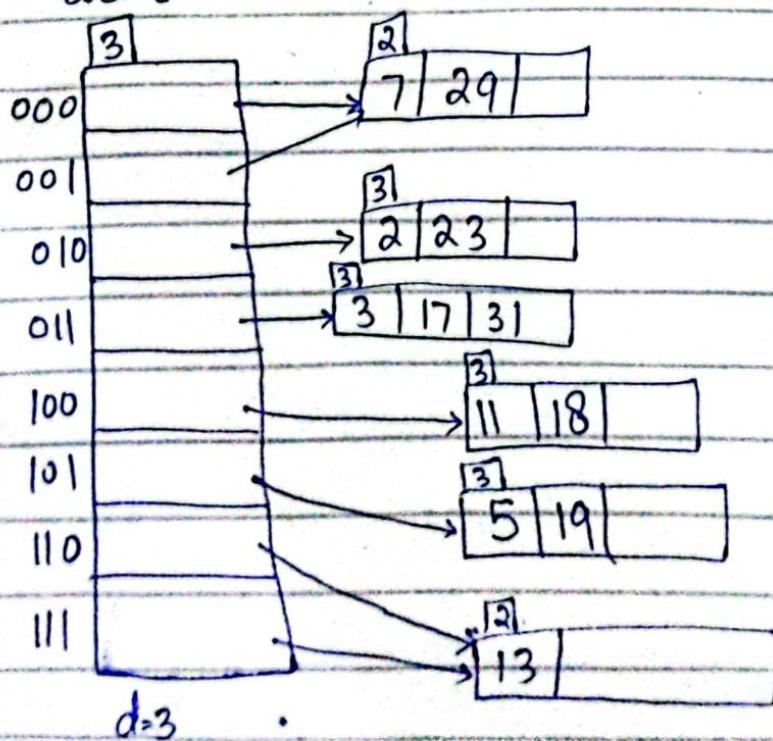
(overflow) as $d' < d$ so we will only split the bucket:



(8) insert 18 into final structure of part (7)

$$18 \bmod 7 = 4 = 100$$

(overflow) again $d' < d$ we will only split the bucket.



$d=3$

(e) Linear Hashing $h(k) = k \bmod 7$

initially. our table will be empty and we will have 7 buckets from 0 to 6.

new hash function = $k \bmod 2M$ $\frac{M+7}{2}$ (implying)

$n=0$

insert 2, $2 \bmod 7 = 2$

0		
1		
2	2	
3		
4		
5		
6		

insert 3, $3 \bmod 7 = 3$

0		
1		
2	2	
3	3	
4		
5		
6		

insert 5, $5 \bmod 7 = 5$

$n=0$

0		
1		
2	2	
3	3	
4		
5	5	
6		

insert 7, $7 \bmod 7 = 0$

$n=0$

0	7	
1		
2	2	
3	3	
4		
5	5	
6		

insert 11, $11 \bmod 7 = 4$

$n=0$

0	7	
1		
2	2	
3	3	
4	11	
5	5	
6		

insert 17, $17 \bmod 7 = 3$

$n=0$

0	7	
1		
2	2	
3	3	17
4	11	
5	5	
6		

insert 19

$$19 \bmod 7 = 5$$

$n=0$

0	7		
1			
2	2	.	.
3	3	17	
4	11		
5	5	19	
6			

insert 23

$$23 \bmod 7 = 2$$

$(n=0)$

0	7		
1			
2	2	23	
3	3	17	
4	11		
5	5	19	
6			

insert 29, $29 \bmod 7 = 1$

$n=0$

0	7		
1	29		
2	2	23	
3	3	17	
4	11		
5	5	19	
6			

insert 31, $31 \bmod 7 = 3$

$n=0$

0	7		
1	29		
2	2	23	
3	3	17	31
4	11		
5	5	19	
6			

so at the end our table will be

$n=0$

0	7		
1	29		
2	2	23	
3	3	17	31
4	11		
5	5	19	
6			

Question 3

first i will write ^{its} binary into decimal

$$a[010000] = 16$$

$$b[011010] = 26$$

$$c[111100] = 60$$

$$d[001110] = 14$$

$$e[010111] = 23$$

$$f[011010] = 26$$

$$g[101001] = 41$$

$$h[010111] = 23$$

$$i[000110] = 6$$

$$j[101001] = 41$$

hash function = $k \bmod M$

initially, we will take 4 buckets, so $M=4$

our original hash function will be $h(k) = k \bmod M$

and new hash function will be $h(k) = k \bmod 2M$

and $n=0$ initially.

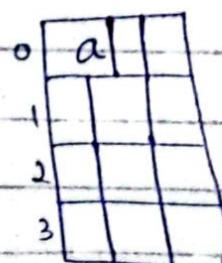
$n=0$



insert $a[010000] = 16$

$$16 \bmod 4 = 0$$

$n=0$



insert $b[011010] = 26 \bmod 4 = 2$



insert c [111100] = $60 \bmod 4 = 0$

$n=0$

0	a	c	
1			
2	b		
3			

insert d [001110]

$$= 14 \bmod 4 = 2$$

$n=0$

0	a	c	
1			
2	b	d	
3			

insert e [010111]

$$= 23 \bmod 4 = 3$$

$n=0$

0	a	c	
1			
2	b	d	
3	e		

insert f [011010]

$$= 26 \bmod 4 = 2$$

$n=0$

0	a	c	
1			
2	b	d	f
3	e		

as threshold was of 2 records
so as the third record comes into a
bucket we will add a new bucket
and redistribute the bucket with
n value of index.

adding an extra 'bucket' and redistributing ð bucket
using new hash function.

$n=1$

0	a		
1			
2	b	d	f
3	e		
4	c		

as 0th bucket contain a
and c so

$$a = 16, 16 \bmod 8 = 0$$

$$c = 60, 60 \bmod 8 = 4$$

insert $g[101001] = 41 \bmod 4 = 1$

$n=1$

0	a
1	g
2	b,d,f
3	e
4	c

insert $h[010111]$

$$= 23 \bmod 4 = 3$$

$n=1$

0	a
1	g
2	b,d,f
3	h,e
4	c

insert $i[000110]$

$$= 6 \bmod 4 = 2$$

we need to add an overflow bucket

$n=1$

0	a
1	g
2	b,d,f
3	h,e
4	c

i

now we need to add an extra bucket and redistribute the bucket 1 using new hash function.

bucket 1 contain:

$$g[101001] = 41 \bmod 8 = 1$$

$n=2$

0	a
1	g
2	b,d,f
3	h,e
4	c

l

insert $j[101001] = 41 \bmod 4 = 1$

$n=2$

0	a
1	g,j
2	b,d,f
3	h,e
4	c

i

overflow bucket

(3)

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Roll No: 20L-2074

Assignment H 03 (ADB-6A)

Q H 1

$$B = 4096 \quad \gamma = 10 \text{ million}$$

$$\gamma = 10,000,000 = 10^7$$

block pointers $P = 6$ bytes

record pointer $P_R = 7$ bytes

$$R = 30 + 9 + 9 + 40 + 9 + 8 + 1 + 4 + 4 + 1 = 115$$

$$bfr = \lceil \log_2 \left(\frac{B}{R} \right) \rceil = \lceil \log_2 \left(\frac{4096}{115} \right) \rceil = 35$$

$$b = \text{ceiling} \left(\frac{\delta}{bfr} \right) = \left(\frac{10^7}{35} \right) \text{ceiling} = \text{ceiling}(285714.3)$$

$$b = 285715$$

(a) Primary index on SSN

$R_i = \text{SSn Size} + \text{block pointer size}$

$$R_i = 9 + 6 = 15$$

$$bfr_i = \lceil \log_2 \left(\frac{B}{R_i} \right) \rceil = \left\lceil \frac{(4096)}{15} \right\rceil = \lceil \log_2 (273.06) \rceil = 8$$

first level records = $\gamma_1 = 285715$

$$b_1 = \text{ceiling} \left(\frac{\gamma_1}{b_{fri}} \right) = \left\lceil \frac{285715}{273} \right\rceil = 1047$$

$$\gamma_2 = 1047$$

$$b_2 = \text{ceiling} \left(\frac{\gamma_2}{b_{fri}} \right) = \text{ceiling} \left(\frac{1047}{273} \right) = 4$$

$$\gamma_3 = 4$$

$$b_3 = \text{ceiling} \left(\frac{\gamma_3}{b_{fri}} \right) = \text{ceiling} \left(\frac{4}{273} \right) = 1$$

so we will need 3 levels in case of multilevel indexing.

total no. of blocks required = $b_1 + b_2 + b_3$

$$= 1047 + 4 + 1 = 1052 \text{ blocks required}$$

no. of block access needed will be = $x + 1$

$$= 3 + 1 = 4$$

(b) Secondary Index on SSN

$R_i = 15$ already calculated in a part.

$$b_{fri} = 273$$

first level records = $\gamma_1 = 10^7$

$$b_1 = \text{ceiling} \left(\frac{\gamma_1}{b_{fri}} \right) = \left\lceil \frac{10^7}{273} \right\rceil = 36631$$

$$\gamma_2 = 36631, b_2 = \left\lceil \frac{36631}{273} \right\rceil = 135$$

we already solved the part (a) in detail so I
will not write general formulas again and again I will
solve the problem by putting values.

$$x_2 = 135$$

$$b_3 = \lceil \frac{135}{273} \rceil = 1$$

$$\text{so } x=3$$

we will need 3 levels.

$$\text{No. of blocks } b_i = b_1 + b_2 + b_3 = 36631 + 135 + 1 = 36767$$

no. of blocks in secondary indexing is
much more than primary indexing.

$$\text{No. of block access} = n+1 = 3+1 = 4$$

(C) Secondary Index on Department Code

$$R_i = \text{Dept. Code Size} + P_b = 9+6 = 15$$

$$b_{Tx_i} = \lceil \frac{B}{R_i} \rceil = \lceil \frac{4096}{15} \rceil = 273$$

total distinct values of dept. code = 20000

$$\text{no. of employee records against each dept. code} = \frac{10^7}{20000} = 500$$

$$\# \text{ of bytes needed for level of indirection block} = 7 \times 500 \\ = 3500 \text{ so all } 500$$

record pointers can fit in 1 block. So there
will be 20,000 blocks in level of indirection.

$$\text{no. of records at first level} = x_1 = 20,000$$

$$b_1 = \text{ceiling} \left(\frac{61}{b_{Tx_i}} \right) = \left\lceil \frac{20,000}{273} \right\rceil = 74$$

$$a_2 = 74$$

$$b_2 = \left\lceil \frac{74}{273} \right\rceil = 1$$

So in case of multilevel indexing there will be 2 levels.

$$x=2$$

$$\begin{aligned} \text{total no. of blocks} &= b_1 + b_2 + \text{no. of blocks} \\ &\quad \text{in level of indirection} \\ &= 74 + 1 + 20,000 = 20075 \end{aligned}$$

$$\begin{aligned} \text{block access} &= x + 1 + \text{average record for each value} \\ &= 2 + 1 + 500 = 503 \end{aligned}$$

(d) Clustering Index on Dept. Code

$$R_i = 9 + 6 = 15$$

$$b_{fri} = \text{Floor} \left(\frac{B}{R_i} \right) = \left\lfloor \frac{4096}{15} \right\rfloor = 273$$

$$\text{no. of first level records} = x_1 = 20000$$

$$b_1 = \left\lceil \frac{20000}{273} \right\rceil = 74$$

$$a_2 = 74$$

$$b_2 = \left\lceil \frac{74}{273} \right\rceil = 1$$

So we need $x=2$ levels in case of multilevel indexing.

$$\text{total no. of blocks required} = b_1 + b_2 = 74 + 1 = 75$$

$$\begin{aligned} \text{total no. of block access} &= x + \frac{S}{b_1} \\ &= 2 + \frac{500}{35} = 2 + 15 = 17 \text{ block access.} \end{aligned}$$

$$b_1 x = \left\lceil \frac{4096}{15} \right\rceil$$

$$b_1 x = 35$$

$$p \times P + (p-1)(V_{SSN}) < B$$

2

(e) B+ tree

for non-leaf nodes

$$(p \times P) + (p-1)(V_{SSN}) < B$$

$$(p \times 6) + (p-1)(9) < 4096$$

$$6p + 9p - 9 < 4096$$

$$15p < 4096 + 9$$

$$p < \frac{4105}{15}$$

$$p < 273.6$$

$$\boxed{p = 273}$$

$$P_{leaf} \times (V_{SSN} + P_s) + P < B$$

for leaf nodes

$$b_{leaf} \times (V_{SSN} + P_s) + P < B$$

$$b_{leaf} \times 16 + 6 < 4096$$

$$b_{leaf} < \frac{4096 - 6}{16}$$

$$b_{leaf} < 255.6$$

$$b_{leaf} = 255$$

as blocks are approximately 69% full so

$$0.69 \times 255 = 175.9 \quad 176 \text{ approximately}$$

$$b_1 = \text{ceiling}\left(\frac{10^7}{176}\right) = 56819$$

for non leaf nodes.

$$0.69 \times 273 = 188.3 \approx 189$$

$$b_2 = \text{ceiling} \left(\frac{b_1}{r_0} \right) = \left\lceil \frac{56819}{189} \right\rceil = 301$$

$$b_3 = \left\lceil \frac{301}{189} \right\rceil = 2$$

$$b_4 = \left\lceil \frac{2}{189} \right\rceil = 1$$

$$\text{total number of blocks} = b_1 + b_2 + b_3 + b_4 = 56819 + 301 + 2 + 1 = 57123$$

$$\text{block access} = n+1 = 4+1 = 5$$

(7) B-tree

$$(p \cdot P) + (p-1) \cdot (V_{SSN} + P_s) < B$$

$p \cdot 6 \quad (p-1) \cdot (16 \cancel{+ 1}) < 4096$

$$p < \frac{4096 + 16}{22}$$

$$p < 186.9$$

$$p = 186$$

as block is 69% full so $0.69 \times 186 = 128.3$

$$\approx 129$$

$$\text{so no. of blocks at } b_1 = \left\lceil \frac{10^7}{129} \right\rceil = 77520$$

$$b_2 = \left\lceil \frac{77520}{129} \right\rceil = 601$$

$$b_3 = \left\lceil \frac{601}{129} \right\rceil = 5$$

$$b_4 = \left\lceil \frac{5}{129} \right\rceil = 1$$

$$\text{total blocks} = b_1 + b_2 + b_3 + b_4 = 77520 + 601 + 5 + 1 = 78127$$

$$\text{total block access} = n+1 = 5$$

In case of B-tree no. of blocks (total) is much more than B+ tree total no. of blocks although block access cost remains same.

Q No: 2

$$B = 8192 \quad \delta = 10 \text{ billion}$$

$$\delta = 10 \text{ billion} = 10 \times 1000 \text{ million}$$

$$\delta = 10000 \text{ million} \quad \delta = 10000,00000$$

$$\delta = 10^{10}$$

$$R = 115$$

$$b_{fri} = \text{Floor}\left(\frac{B}{R}\right) = \left\lfloor \frac{8192}{115} \right\rfloor = 71$$

$$b = \text{ceiling}\left(\frac{\delta}{b_{fri}}\right) = \left\lceil \frac{10^{10}}{71} \right\rceil = 140845071$$

(a) Primary Index on SSN

$$R_i = \text{SSnSize} + P_b = 9 + 6 = 15$$

$$b_{fri} = \text{Floor}\left(\frac{B}{R_i}\right) = \left\lfloor \frac{8192}{15} \right\rfloor = 546$$

$$\gamma_1 = 140845071$$

$$b_1 = \text{ceiling}\left(\frac{\delta_1}{b_{fri}}\right) = \left\lceil \frac{140845071}{546} \right\rceil = 257958$$

$$\delta_2 = 257959$$

$$b_2 = \left\lceil \frac{257959}{546} \right\rceil = 473$$

$$\delta_3 = 473$$

$$b_3 = \left\lceil \frac{473}{546} \right\rceil = 1$$

So 3 levels will be needed in case of multilevel indexing.

$$\text{total no. of blocks required} = b_1 + b_2 + b_3 = 257959 + 473 + 1 \\ = 258433$$

$$\text{no. of blocks access needed} = x+1 = 3+1 = 4$$

(b) Secondary Index on SSN

$$R_i = 15$$

$$b_{fri} = 546$$

already computed in part a.

$$\text{First level records} = s_1 = 10^{10}$$

$$b_1 = \text{ceiling}\left(\frac{s_1}{b_{fri}}\right) = \left\lceil \frac{10^{10}}{546} \right\rceil = 18315019$$

$$s_2 = 18315019$$

$$b_2 = \left\lceil \frac{18315019}{546} \right\rceil = 33544$$

$$s_3 = 33544$$

$$b_3 = \left\lceil \frac{33544}{546} \right\rceil = 62$$

$$s_4 = 62$$

$$b_4 = \left\lceil \frac{62}{546} \right\rceil = 1$$

so we will need 4 levels in case of multilevel indexing.

$$\text{In this total no. of blocks} = b_1 + b_2 + b_3 + b_4 = 18315019 + 33544 + 62 + 1 \\ = 18348626$$

$$\text{no. of block access} = x+1 = 4+1 = 5$$

So in case of Secondary index on SSN

Total no. of blocks are much much more than primary indexing on SSN also block access cost is 5 in Secondary and 4 in primary.

(C) Secondary Index on Debt. Code

$$R_i = \text{DebtCodeSize} + P_B = 9 + 6 = 15$$

$$b7ic = 71000 \left(\frac{B}{R_i} \right) = \left\lfloor \frac{8192}{15} \right\rfloor = 546$$

Total distinct values of debt code = 20,000

Average no. of employee records against each debt code
 $= \frac{10^{10}}{20,000} = 500,000$

No. of bytes needed for level 1 indirection blocks

$$= 7 \times 500,000$$

= 3,500,000 bytes need against

1 debt code value in level of indirection.

as 1 block size = 8192

$$\text{so } \left\lceil \frac{3,500,000}{8192} \right\rceil = 427.2 = 428 \text{ blocks needed}$$

To hold record pointers against one distinct debt code

so there will be total $428 \times 20,000 = 8560000$ blocks in level of indirection.

No. of records at first level of indexing = $x_1 = 20000$

$$b_1 = \text{ceiling} \left(\frac{x_1}{b7ic} \right) = \left\lceil \frac{20,000}{8192} \right\rceil = 37$$

$$b_2 = 37$$

$$b_2 = \left\lceil \frac{37}{546} \right\rceil = 1$$

So in case of multilevel indexing there will be $n=2$ levels.

$$\begin{aligned} \text{total no. of blocks} &= b_1 + b_2 + \text{no. of blocks in level of induction} = 37 + 1 + 8560000 \\ &= 8560038 \end{aligned}$$

$$\begin{aligned} \text{block access} &= n + 428 + \text{average record for each value.} \\ &= 2 + 428 + 500,000 \\ &= 500430 \end{aligned}$$

(d) Cluster index on Debt. Code

$$R_i = 9 + 6 = 15$$

$$b_{fri} = \text{floor} \left(\frac{B}{R_i} \right) = \left\lfloor \frac{8192}{15} \right\rfloor = 546$$

$$\text{no. of first level records} = s_1 = 20,000$$

$$b_1 = \left\lceil \frac{20,000}{546} \right\rceil = 37$$

$$b_2 = 37,$$

$$b_2 = \left\lceil \frac{37}{546} \right\rceil = 1$$

So we need $n=2$ levels in case of multilevel indexing.

$$\text{total no. of blocks} = b_1 + b_2 = 37 + 1 = 38$$

$$\text{total no. of block access} = n + \frac{s}{bfr}$$

$$= 2 + \left\lceil \frac{500,000}{71} \right\rceil$$

$$= 2 + 7043 = \boxed{7045}$$

$$bfr = \left\lceil \frac{8192}{115} \right\rceil$$

$$bfr = 71$$

2) B^+ tree

for non-leaf nodes

$$(b+P) + (b-1)(V_{SSN}) < B$$

$$(b+6) + (b-1)(9) < 8192$$

$$15b < 8192 + 9$$

$$b < \frac{8192 + 9}{15}$$

$$b < 546.73$$

$$b = 546$$

for leaf node

$$b_{leaf} * (V_{SSN} + P_r) + P < B$$

$$16b_{leaf} + 6 < 8192$$

$$b_{leaf} < \frac{8192 - 6}{16}$$

$$b_{leaf} < 511.625$$

$$b_{leaf} = 511$$

as blocks are approximately 69% full so

$$0.69 \times 511 = 352.5 \approx 353$$

$$b_1 = \text{ceiling} \left(\frac{10^{10}}{353} \right) = \lceil 28328611.9 \rceil = 28328612 \quad (\text{no. of leaf blocks})$$

for non-leaf nodes

$$0.69 \times 546 = 376.7 \approx 377$$

$$b_2 = \text{ceiling} \left(\frac{28328612}{377} \right) = 75143$$

$$b_3 = \text{ceiling} \left(\frac{75143}{377} \right) = 200$$

$$b_4 = \text{ceiling} \left(\frac{200}{377} \right) = 1$$

$$\text{total no. of blocks} = b_1 + b_2 + b_3 + b_4 = 28328612 + 75143 + 200 + 1 \\ = 28403956$$

$$\text{block access} = x+1 = 4+1 = 5$$

(f) B-tree

$$(b \cdot P) + (b-1) \cdot (V_{SN} + P_R) < B$$

$$6b + 16b - 16 < 8192$$

$$b < \frac{8192 + 16}{22}$$

$$b < 373.09$$

$$b = 373$$

as block is 69% full so

$$0.69 \times 373 = 257.3 \approx 258$$

$$b_1 = \text{ceiling}\left(\frac{10^{10}}{258}\right) = 38759690$$

$$b_2 = \text{ceiling}\left(\frac{38759690}{258}\right) = 150232$$

$$b_3 = \text{ceiling}\left(\frac{150232}{258}\right) = 582$$

$$b_4 = \text{ceiling}\left(\frac{582}{258}\right) = 3$$

$$b_5 = \text{ceiling}\left(\frac{3}{258}\right) = 1$$

$$\text{total blocks} = b_1 + b_2 + b_3 + b_4 + b_5 = 38759690 + 150232 + 582 + 3 + 1 \\ = 38910509$$

$$\text{total block access} = n+1 = 5+1 = 6$$

In case of B-tree total no. of blocks

are way more than B+ tree. Also block access cost is increased by 1 and 1 level is also added.

Q No: 3 (a) B⁺-tree

For B⁺ tree we need to find order for both non-leaf and leaf nodes.

Non-leaf

$$b \cdot P + (b-1)(V_{SN} + P_R) < B$$

$$56b + (b-1)(8 + 12) < 1024$$

~~$$56b + 8b - 8 < 1024$$~~

$$b < 16.125$$

$$b = 16$$

Leaf

$$b_{leaf} \cdot (V_{SN} + P_R) + P < B$$

$$b_{leaf} \cdot (8 + 12) + 56 < 1024$$

$$20b_{leaf} + 56 < 1024$$

$$b_{leaf} < 48.4$$

$$b_{leaf} = 48$$

We have 3 levels in B⁺ tree including root.

Leaf-level having key-value pairs can have 48 index records (with data pointers)

Root can have 16 childs and the 2nd level nodes can also have 16 childs each.

so as in B⁺ tree index records are only present in leaf level hence

$$\begin{aligned} \text{maximum records that can be indexed} &= 16 \times 16 \times 48 \\ &= 12288. \end{aligned}$$

(b) B-tree

First we calculate order b .

$$b^*P + (b-1)^*(V_{SSN} + P_R) < B$$

$$b^*56 + (b-1)(8+12) < 1024$$

$$56b + 20b - 20 < 1024$$

$$76b < 1024 + 20$$

$$b < \frac{1024 + 20}{76}$$

$$b < 13.7$$

$$b = 13$$

First level can have 12 index records

Second level can have 13×12 index records
because first level can have maximum of 13 child
and each child can have 13 child further.

Hence each child, at second level can have
12 index records

Third level can have $13 \times 12 \times 12$ index records.

So

$$\begin{aligned} \text{total will be} &= 12 + (13 \times 12) + (13 \times 13 \times 12) \\ &= 12 + 156 + 2028 \\ &= 2196 \end{aligned}$$

^{Before marking this} Check the last sheet too. (Last page after Q. 4).

Q No: 4

$x = 4$

6/

(a)

$x + 1$

$$= 4 + 1$$

= 5 as index is on key field

(b)

: $x + 1$

$$= 4 + 1 = 5$$

by 5 block access we will
reach the block with A = 111
and then in that block we will
search for B = 3

(c)

$$2(x+1) = 2(4+1) = 2(5) = 10$$

index is on
key field and
we need two
A values.

(d)

as there are total 5000 blocks
and each block holds 1 value of A so

$$(5000 - 100) + (x+1)$$

$$= 4900 + 4 + 1 = 4905$$

(e)

$$(5000 - 100) + x \quad \text{here we only need count
not records so not}$$

$$= 4900 + 4 = 4904$$

I have done Q3 with Sir's method. There is also another method present at some sites([online](#)) so I will do so.
Q3 with that method too.

Q:3 (a) B⁺-tree

let each node of a B⁺tree contain at most n pointers and n-1 keys so $(n^{\times}12) + (n-1)^{\times}8 + 56 \leq 1024$

$$12n + 8n - 8 + 56 \leq 1024$$

$$n < \frac{1024 - 56 + 8}{20}$$

$$n < 48.8$$

$$n = 48$$

Therefore, the first level of a B⁺tree can hold at most ~~48x 48x 48~~ 48 record pointers. Therefore the maximum no. of records that can be indexed is ~~1024x1024x1024~~ 1024x1024

(b) B⁺-tree : let each inner node of a B⁺tree contain at most n index pointers, n-1 keys and n-1 record pointers.

$$(n-1)8 + ((n-1)^{\times}12) + 56 \leq 1024$$

$$8n - 8 + 24n - 12 + 56 \leq 1024$$

$$n < \frac{1024 - 56 + 12 + 8}{32}$$

$$n < 30.8$$

$$n = 30$$

The first level can hold at most 29 record pointers.

The second level can hold at most 29×30 record pointers. The first level can hold at most $29 \times 30 \times 30$ record pointers.

Therefore the maximum no. of records that can be indexed is $29 + (29 \times 30) + (29 \times 30 \times 30)$

$$= 29 + 870 + 26100$$

$$= \boxed{26999}$$

MIDTERM EXAM ANSWER SHEET



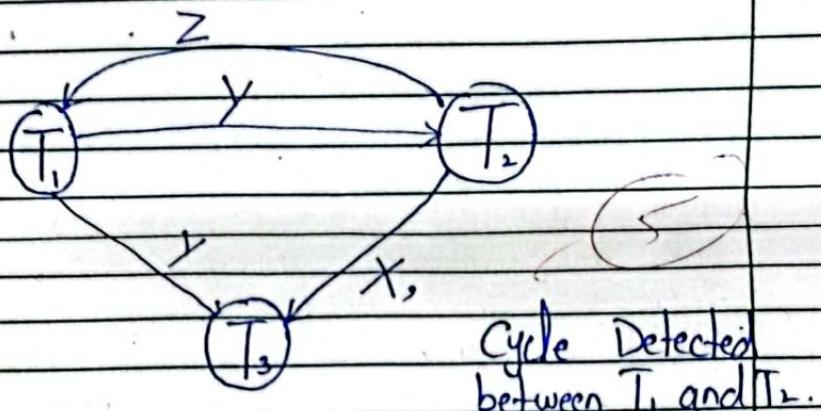
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LAHORE



Course	ADB	Answer Sheet No.	11238
Student's Name	Hanifa Majeed	Signature	<i>Hanifa</i> (2:0)
Roll No.	202-2074	Section	6A
		Date	28-Feb-2022

Q 1

Precedence Graph :-



The schedule is not conflict serializable as there exist a cycle in the precedence graph.

Q : 2

S1: $\delta_1(X)$; $w_3(X)$; $w_6(Y)$; $r_1(Y)$; $\delta_1(Z)$; $\delta_3(Y)$; c_1 ; c_4

Dirty read exist. (S1 is recoverable because of)

The transaction which write on item Y has committed first and the T who read item Y is committed later. So that's why S1 is "recoverable".

Dirty Read = 7 writes written over 2 different times.

Rough Work

Q / Part No.

S2: $\delta_1(X); W_2(X); \delta_1(Y); \delta_1(Z); \delta_3(Y); W_2(Y); C_1; C_2; C_3$

as I explained above what is dirty read. So we see S2 these is not dirty read in it so its neither recoverable nor non-recoverable. as of cascadelless and strict. There is not a single write or write operation on same data item by different Transactions, so its also not cascadelless or strict.)

(but there are some conflict operations $\delta_1(X), W_2(X)$ on that base $\delta_3(Y), W_2(Y)$ we can say)

Q No: 3

(a) Master log record

LSN	101
-----	-----

(b) During the analysis, the recovery manager checks whether did the last check point occur and then it will analyze all the transactions after that check point and make a transaction table in which all the T with their last operation and whether these are committed or active mentioned.

During analysis it will also make a dirty page table in which all the pages with their first update operation are written. The analysis will start from LSN 101 and end on LSN 112.

Dirty Page Table

Page-ID	LSN
X	103
Y	104
Z	106

Transactions

≡

During sedol

We will minimum page

Red-

d

D.
active
from
and
active

As

T4.

L

Transaction Table

Transaction	LSN	Status
T ₁	105	committed
T ₂	108	committed
T ₃	111	committed
T ₄	112	in progress

Redo

During the redo process we will redo all the operations.

We will start redo from the minimum LSN of page from dirty page table and redo till end.

Redo

Start LSN	End LSN
103	112

undo

During undo, we will undo only active transactions. We will start from last operation of active transaction and end at first operation of active transaction.

As there is only 1 active transaction T₄. So we will only undo T₄.

Undo (T₄)

Start LSN	End LSN
112	109

Q No: 4

Rigorous 2PL (wait for graph)

(a)

 T_1 S1-lock(w)
 $\delta_1(w)$ T_2 S2-lock(x)
 $\delta_2(x)$ T_3

(10)

X1-lock(y)
 $\delta_1(y)$ S2-lock(y)
Conflict T_2 will wait
for T_1 on y.S1-lock(z)
 $\delta_1(z)$ unlock(w)
unlock(y)
unlock(z) $\delta_2(y)$ wake
up call
S2-lock(z)
 $\delta_2(z)$
unlock(y)
unlock(x)
unlock(z)wake up $w_3(x)$
S3-lock(y)
 $\delta_3(y)$
unlock(y) unlock(x). T_1 T_1 T_2 T_1 T_2 T_3

x

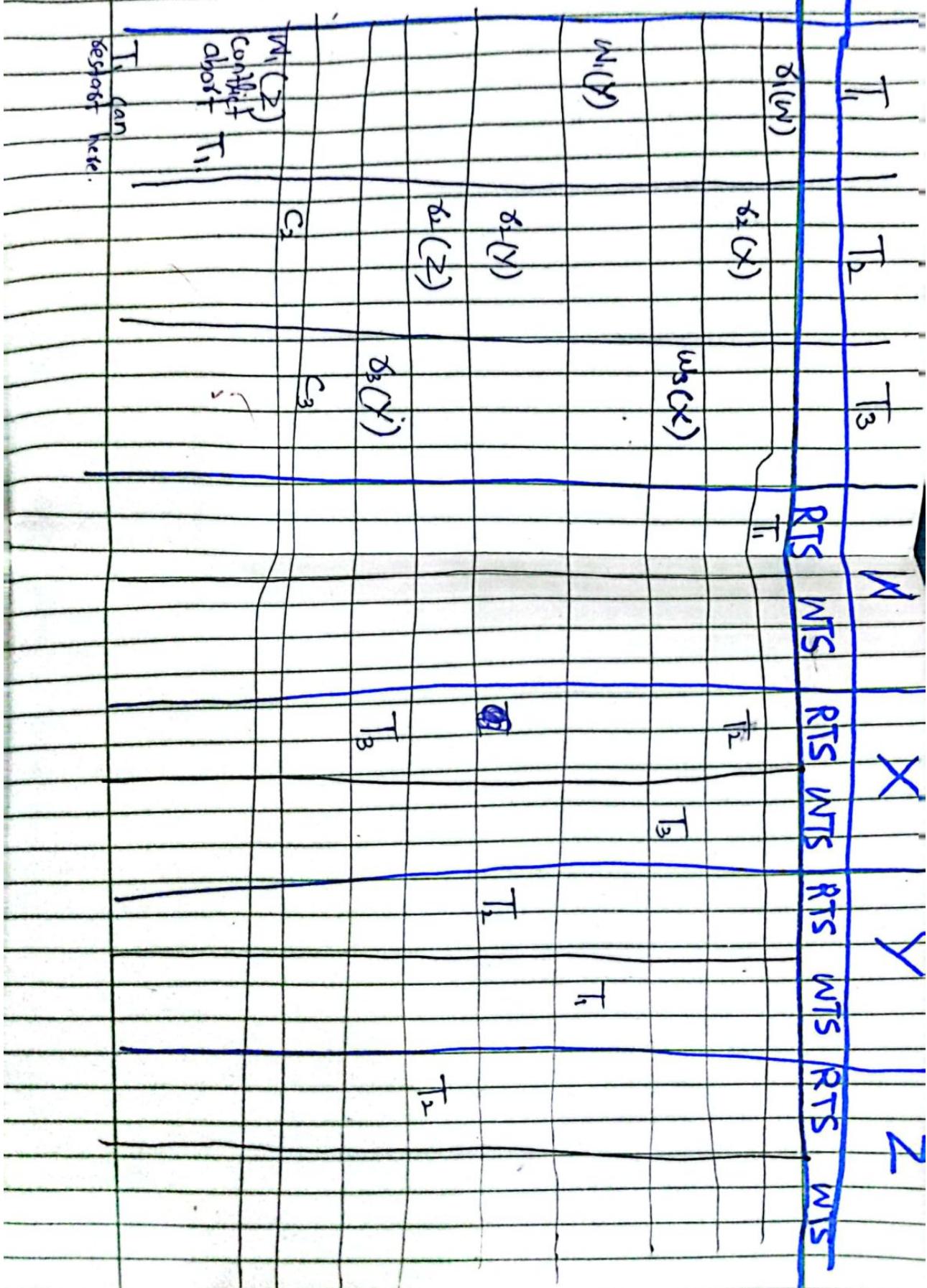
x

y

Q / Part No.

(b)

Basic TO



Name : Hamza Mojeed

93.5

Roll No: 20L-2074

ADB Assignment #1 (6A)

Schedule S1:

$\gamma_1(X), \gamma_2(Y), \gamma_1(Z), \gamma_2(X), w_2(X), \gamma_2(Z), \gamma_3(Y),$
 $w_2(Z), w_1(Y), w_3(Y), C_3, \gamma_1(Y), w_2(Y), C_2, C_1$

Q No: 1 Basic 2PL (wait-die Policy)

	T_1	T_2	T_3
1	$s_1\text{-lock}(X)$ $\gamma_1(X)$		
2		$s_1\text{-lock}(Y)$ $\gamma_1(Y)$	
3	$s_1\text{-lock}(Z)$ $\gamma_1(Z)$	$\gamma_2(X)$ $w_2\text{-lock}(X)$ abort due to T_1	
4			$s_3\text{-lock}(Y)$ $\gamma_3(Y)$
5	$\gamma_1\text{-lock}(Y)$ wait for T_3 on Y		$w_3(Y)$ lock upgraded to exclusive $unlock(Y)$ C_3
6	$w_1(Y)$ wake up		
7	$\gamma_1(Y)$		
8	$unlock(X)$		
9	$unlock(Y)$		
10	$unlock(Z)$		
11	C_1	T_2 can restart here.	

Q No:2 Strict 2PL (wound-wait Policy)

T_1	T_2	T_3
$S_1\text{-lock}(X)$ $\gamma_1(X)$		
$S_2\text{-lock}(Z)$ $\gamma_1(Z)$	$S_2\text{-lock}(Y)$ $\gamma_2(Y)$ $\gamma_2(X)$ read count++ $X_2\text{-lock}(X)$ conflict with T_1 it will wait...	
$\gamma_1(Y)$ $unlock(X)$ $unlock(Z)$ C_1 $unlock(Y)$	aborted	aborted due to T_1
	$unlock(X)$ $S_2\text{-lock}(Z)$ $\gamma_2(Z)$ $\gamma_2(Y)$ T_2 can restart here	$S_3\text{-lock}(Y)$ $\gamma_3(Y)$ read count++ T_3 can restart here.

Q No:3 Rigorous 2PL (Wait-die policy)

T_1	T_2	T_3
$S_1\text{-lock}(X)$ $\delta_1(X)$	$S_2\text{-lock}(Y)$ $\delta_2(Y)$	
$S_1\text{-lock}(Z)$ $\delta_1(Z)$	$\delta_2(X)$ read contention	
	$X_2\text{-lock}(X)$ conflict aborted due to T_1 .	$S_3\text{-lock}(Y)$ $\delta_3(Y)$
$X_1\text{-lock}(Y)$ conflict, it will wait for T_3 on Y		$w_3(Y)$ lock upgraded c_3 unlock(Y)
$w_1(Y)$ (wake up) $\delta_1(Y)$		
c_1 $unlock(X)$ $unlock(Y)$ $unlock(Z)$		T_2 can restart here.

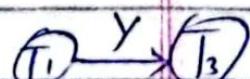
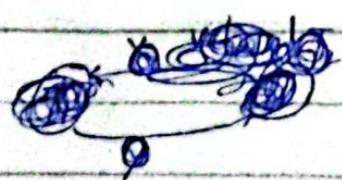
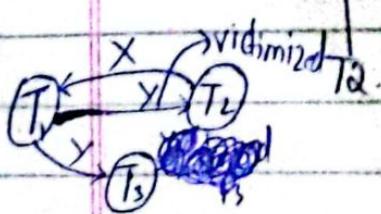
Q No:4 Rigorous 2PL (Wound-wait Policy)

T_1	T_2	T_3
$S1\text{-lock}(X)$ $s_1(X)$	$S2\text{-lock}(Y)$ $s_2(Y)$	
$S1\text{-lock}(Z)$ $s_1(Z)$	$s_2(X)$ $\chi_2\text{-lock}(X)$ conflict - if will wait due to T_1	
$\chi_1\text{-lock}(Y)$ conflict as it is older so it will abort T_3 and T_2 . and it will continue...	aborted due to T_1	$S3\text{-lock}(Y)$ $s_3(Y)$ read constraint
$s_1(Y)$ C_1 $unlock(X)$ $unlock(Y)$ $unlock(Z)$	T_2 can restart here	T_3 can restart there

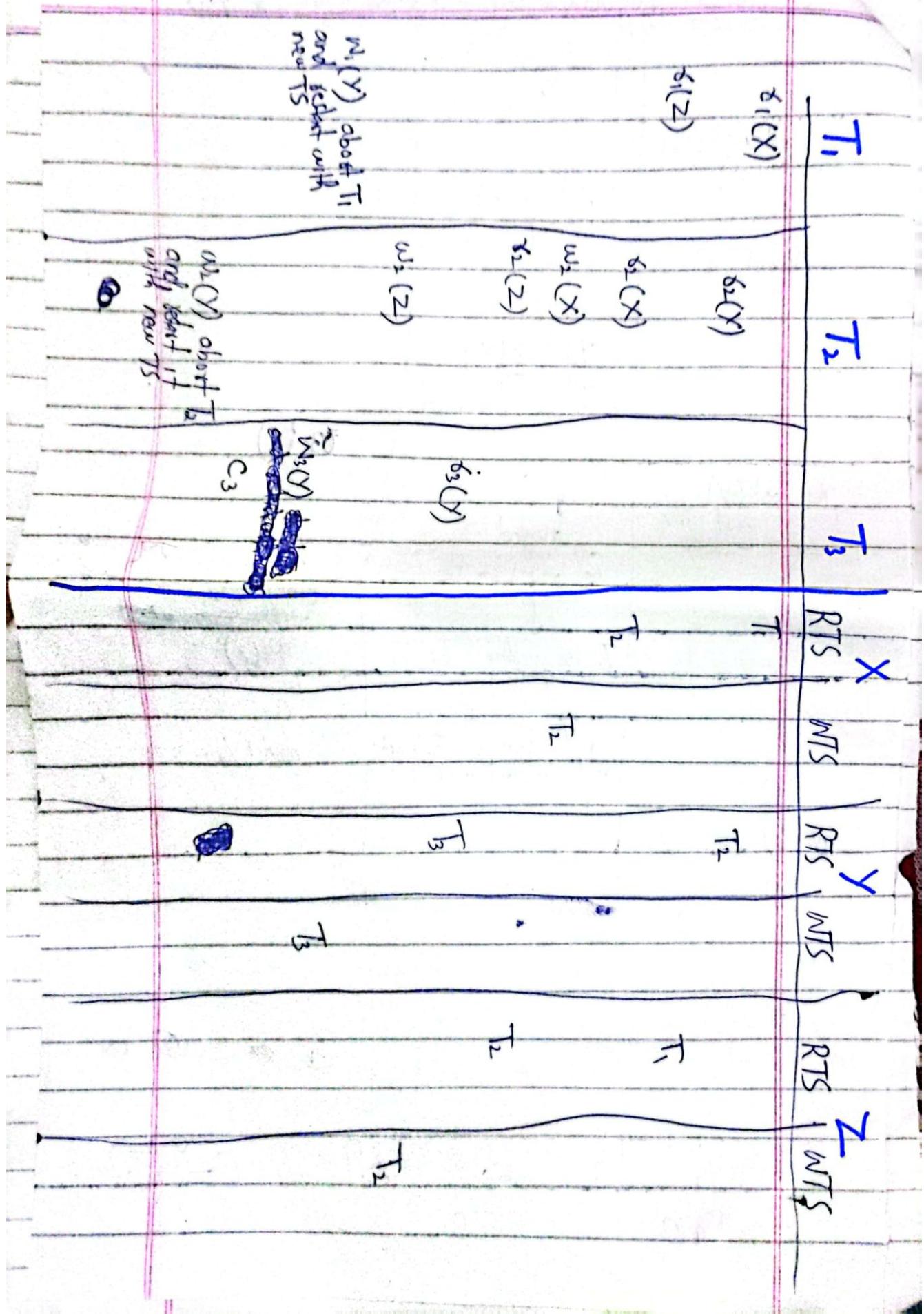
\therefore Younger T will be victimized and aborted in case of deadlock.

Q No: 5 Rigorous 2PL (wait-for graph)

T ₁	T ₂	T ₃
S ₁ -lock(X) S ₁ (X)	S ₂ -lock(Y) S ₂ (Y)	
S ₁ -lock(Z) S ₁ (Z)	S ₂ (X) X ₂ -lock(X) conflict -- T ₂ will wait for T ₁ on X	
X ₁ -lock(Y) T ₁ will wait for T ₂ and T ₃ on Y.		S ₃ -lock(Y)
	aborted T ₂ . and shared lock of Y will be transferred to T ₃ .	X ₃ -lock(Y) lock upgraded. (Victimized and restart with same TS)
	T ₁ is waiting for T ₂ on Y and T ₂ is waiting for T ₁ on X. Victimize T ₂ (abort) and restart with same TS	C ₃ unlock(Y).
W ₁ (Y) wake up S ₁ (Y)		
C ₁		
unlock(X) unlock(Y) unlock(Z)	T ₂ can restart here	B can restart here.



Q No: 6 Basic Timestamp Ordering



Q No: 7

Strict TO

	T_1	T_2	T_3	X	RTS	WTS	Y	RTS	WTS
$\delta_1(X)$				T_1					
$\delta_2(Y)$							T_2		
$\delta_1(Z)$								T_1	
$\delta_2(X)$			T_2						
$w_2(X)$						T_2			
$b_2(Z)$								T_2	
$w_3(Y)$							T_3		
$w_2(Z)$								T_2	
$w_1(Y)$ abort T_1 and restart with new TS.					$w_3(Y)$			T_3	
			C_3						
		$w_2(Y)$ abort T_2 and restart with new TS.							
				S					

Q No: 8 Thomas's Write Rule

T ₁	T ₂	T ₃	X	Y	Z
RTS	WTS	RTS	WTS	RTS	WTS
$\delta_1(X)$			T ₁		
	$\delta_2(Y)$			T ₂	
$\delta_1(Z)$					T ₁
	$\delta_2(X)$		T ₂		
	$\delta_2(X)$			T ₂	
	$\delta_2(Z)$				T ₂
	$\gamma_3(Y)$			T ₃	
	$\gamma_2(Z)$				T ₂
$w_1(y)$ ignore this operation		$\gamma_3(Y)$			T ₃
		C ₃			
$\delta_1(Y)$ ignore	$\gamma_2(Y)$ ignore				
		C ₂			
C ₁					

Q No:9

Multi-Version TO

			X		Y		Z
T_1	T_2	T_3	RTS	WTS	RTS	WTS	RTS
$\delta_1(X)$			T_1				
	$\delta_2(Y)$				T_2		
$\gamma_1(Z)$						T_1	
	$\delta_2(X)$		T_2				
	$w_2(X)$		T_2	T_2			
	$\delta_2(Z)$					T_2	
		$\delta_3(Y)$			T_3		
		$w_1(Z)$					
						T_2	T_2
	$w_1(Y)$				T_1	T_1	
		$w_3(Y)$			T_3	$\{T_1, T_3\}$	
		c_3					
	$\delta_1(Y)$				T_1		
	$w_2(Y)$ about T_2 .						
	c_1			y			

Schedule S2

$s_2(X), w_1(Y), w_L(Y), w_1(X), w_3(Z), c_1, w_2(X), c_2$
 $w_3(X), c_3$

Q No:1 Basic 2PL (wait-die policy)

T_1	T_2	T_3
	$s_2\text{-lock}(X)$ $s_2(X)$	
$x_1\text{-lock}(Y)$	$x_2\text{-lock}(Y)$ about due to T_1 and all locks released.	
$x_1\text{-lock}(X)$ $w_1(X)$		$x_3\text{-lock}(Z)$ $w_3(Z)$
$unlock(Y)$ $unlock(X)$		$x_3\text{-lock}(X)$ $w_3(X)$ $unlock(X)$ $unlock(Z)$ c_3
c_1	T_2 can restrict here.	

Q No:2 Strict 2PL (wound-wait policy)

T ₁	T ₂	T ₃
$x_1\text{-lock}(Y)$ $w_1(Y)$	$s_2\text{-lock}(X)$ $\sigma_2(X)$	
$x_1\text{-lock}(X)$ conflict so it will abort T ₂ and continue.	$\sigma_2\text{-lock}(Y)$ conflict so T ₂ will wait...	$x_3\text{-lock}(Z)$ $w_3(Z)$
c_1 unlock(X) unlock(Z)	aborted due to T ₁	$x_3\text{-lock}(X)$ $w_3(X)$

Q No: 3 Rigorous 2PL (Wait-Die Policy)

T_1	T_2	T_3
	$s_2\text{-lock}(X)$ $s_2(X)$	
$x_1\text{-lock}(Y)$ $w_1(Y)$	$x_2\text{-lock}(Y)$ conflict - aborted due to T_1 all locks released.	
$x_1\text{-lock}(X)$ $w_1(X)$		$x_3\text{-lock}(\Sigma)$ $w_3(\Sigma)$
c_1 $unlock(Y)$ $unlock(X)$		$x_3\text{-lock}(X)$ $l_3(X)$
		c_3 $unlock(X)$ $unlock(Z)$
	T_2 can restart here.	

Q No: 4 Rigorous 2PL (wound-wait Policy)

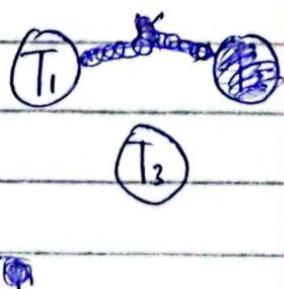
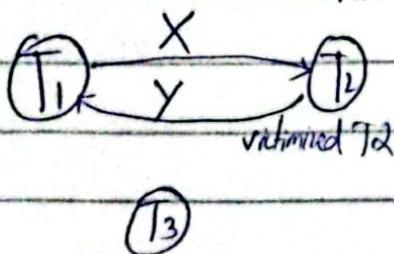
T_1	T_2	T_3
	$S_2\text{-lock}(X)$ $\delta_2(X)$	
$\chi_1\text{-lock}(Y)$ $w_1(Y)$	$\chi_2\text{-lock}(Y)$ conflict, it will wait due to T_1 .	
$\chi_1\text{-lock}(X)$ it will abort T_2	aborted due to T_1	$\chi_3\text{-lock}(Z)$ $w_3(Z)$
c_1 $unlock(X)$ $unlock(Y)$		$\chi_3\text{-lock}(X)$ $w_3(X)$ c_3 $unlock(X)$ $unlock(Z)$
	T_2 can restart here.	

S₂

PS:- Younger T's will be victimized and aborted in case of deadlock.

QNo:5 Rigorous 2PL (wait for graph)

T ₁	T ₂	T ₃
	S ₂ -lock(X) s ₂ (X)	
X ₁ -lock(Y) w ₁ (Y)	X ₂ -lock(Y) T ₂ will wait for T ₁ on Y.	
X ₁ -lock(X) conflict T ₁ will wait due to T ₂ on X	Victimize T ₂ and abort it all locks will be released.	
w ₁ (X) wake up		Z ₃ -lock(Z) w ₃ (Z)
C ₁		
unlock(X) unlock(Y)		Z ₃ -lock(X) w ₃ (X)
	C ₂	C ₃
	T ₂ can restart here.	unlock(Z) unlock(X)



Q No:6 Basic TD

			X		Y		Z
T ₁	T ₂	T ₃	RTS	WTS	RTS	WTS	RTS
W ₁ (X)	W ₂ (X)		T ₂				
W ₁ (Y)				W ₂ (Y)		T ₁	
W ₁ (X) about T ₁ and rest of array TS.						T ₂	
							T ₃
W ₂ (X)				T ₂			
C ₂	W ₃ (X)			T ₃			
		C ₃					

QNo: 7

Strict TO

T_1	T_2	T_3	X	'	Y	Z	
RTS	WTS	RTS	RTS	WTS	RTS	WTS	
$w_1(X)$			T_2			T_1	
$w_1(Y)$							
$w_2(X)$ abpt T_1 and reschedule with new TS.	$w_2(Y)$ delay until C_1 or C_2				T_2		
	$w_3(Y)$ wake up.					T_3	
		$w_3(Z)$					
			T_1				
	$w_2(X)$						
	C_2						
		$w_3(X)$					
		C_3					

Q No: 8

Thomas's Write Rule

T_1	T_2	T_3	X	Y	Z
RTS	WTS	RTS	WTS	RTS	WTS
$w_2(X)$			T_2		
$w_1(Y)$				T_1	
$w_2(Y)$				\bar{T}_2	
$w_1(X)$ ignore		$w_3(Z)$			T_3
c_1	$w_2(X)$		T_2		
	c_2	$w_3(X)$	T_3		
		c_3			
(P)		(Y)			

~~Q No: 9~~ Multi-Version

T_1	T_2	T_3	X	Y	
RTS	WTS	RTS	WTS	RTS	WTS
$b_2(X)$	T_2		T_1, T_1	T_2	$\{T_1, T_2\}$
$w_1(Y)$					
$w_2(Y)$					
$w_1(X)$	T_1, T_1			T_3	T_3
c_1	$w_3(Z)$				
	$T_2, \{T_1, T_2\}$				
	$w_2(X)$	$T_2, \{T_1, T_2\}$			
c_2	$w_3(X)$	$T_3, \{T_1, T_2, T_3\}$			
		$T_3, \{T_1, T_2, T_3\}$			
c_3					
(4)					

here.

Name : Hamza Majeed

Roll No: 20L-2074 ✓

Assignment No 2 (ADB - 6A)

Q.No: 1

$$B = 1024 \text{ bytes}$$

$$\delta = 10,000,000$$

$$R = 100 \text{ bytes}$$

$$\text{No. of students per department} = 50,000$$

$$\text{Blocking factor} = bfr = \left\lfloor \frac{B}{R} \right\rfloor = \left\lfloor \frac{1024}{100} \right\rfloor = \boxed{10.24}$$

$$\text{Total no. of data blocks} = b = \left\lceil \frac{\delta}{bfr} \right\rceil = \left\lceil \frac{10,000,000}{10} \right\rceil = \boxed{1,000,000}$$

$$b = 1000,000$$

(a) As file is unordered so it will take linear time.

$$\text{no. of block fetches needed} = O(b) = \boxed{1000,000}$$

(b) As file is ordered on roll no and we only need to read one record so it will take: $O(\log_b)$
no. of block fetches needed = $\log_a b = \log_a (1000,000) = \lceil \log_a (1000,000) \rceil = \lceil 9.93 \rceil = \boxed{10}$

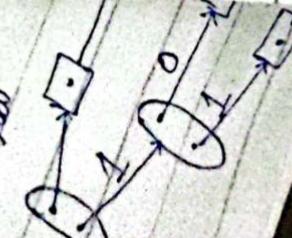
(c) As file is not ordered so it will take linear time. $O(b)$
No. of block fetches needed = $\lceil 1000,000 \rceil$

(d) As file is ordered on department no and we need to fetch 1 whole department as file size 50,000 students in one department
So selection cardinality = $50,000$

insert
over

$$\begin{aligned}\text{No. of block fetches needed} &= O(\log_2 b) + \left\lceil \frac{s}{b} \right\rceil - 1 \\ &= \left\lceil \log_2 (1000,000) \right\rceil + \left\lceil \frac{50,000}{10} \right\rceil - 1 \\ &= 20 + 5000 - 1 \\ &\approx 20 + 4999 \\ &= 5019\end{aligned}$$

insert 7,
overflow



Name : Hamza Majeed

roll No: 20L-2074
Quiz #2 (ADB-6A)

Q2

hash function = $k \bmod 8$

as a bucket can hold 3 records first
3 values will be inserted without any issue.

insert 2

1	1	1
---	---	---

$2 \bmod 8 = 2 = 010$

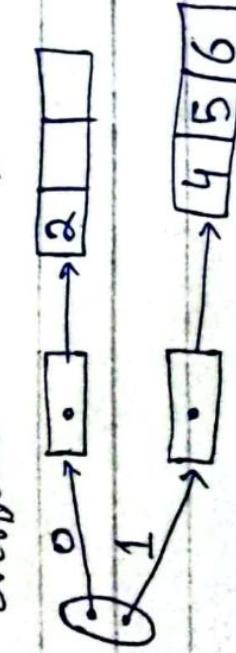
2	1	1
---	---	---

insert 4, $4 \bmod 8 = 4 = 100$, insert 5 $5 \bmod 8 = 5 = 101$

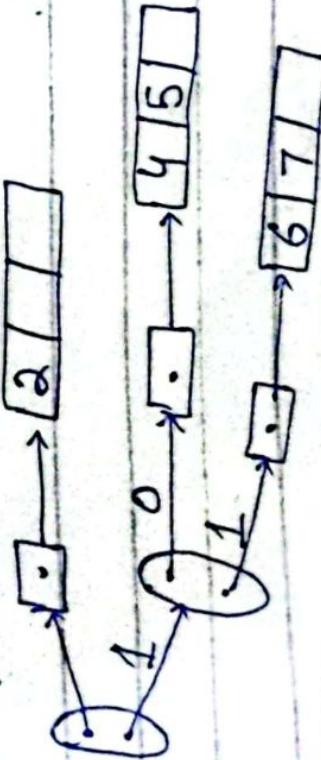
2	4	5
---	---	---

Binary Table. (for help).

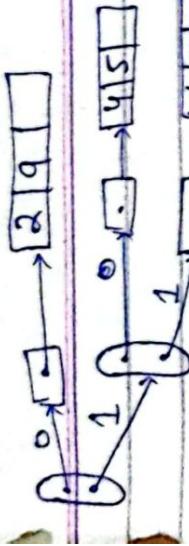
insert 6, $6 \bmod 8 = 6 = 110$
overflow (add extra bucket)



insert 7, $7 \bmod 8 = 7 = 111$
overflow



$$9 \bmod 8 = 1 = 001$$



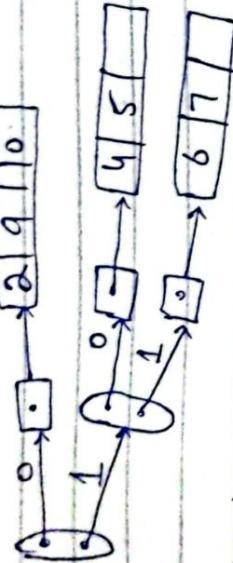
$$\text{No: } 201-2$$

Name :

$$\text{insert } 10, \quad 10 \bmod 8 = 2 = 010$$



$$\text{No: } 202 \text{ (AD)}$$



$$\text{insert } 14, \quad 14 \bmod 8 = 6 = 110$$



$$B = 1024 \text{ by}$$

$$b = 10,000,000$$

$$R = 100 \text{ bytes}$$

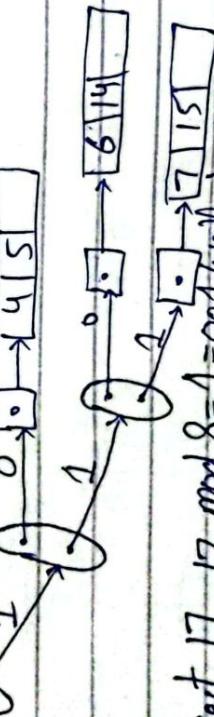
$$\text{No. of students per}$$

$$\text{blocking factor} = b/t =$$

$$\text{insert } 15, \quad 15 \bmod 8 = 7 = 111 \text{ (overflow)}$$



$$t = 10 \quad \text{No. of data blocks}$$



$$b = 1000,000$$

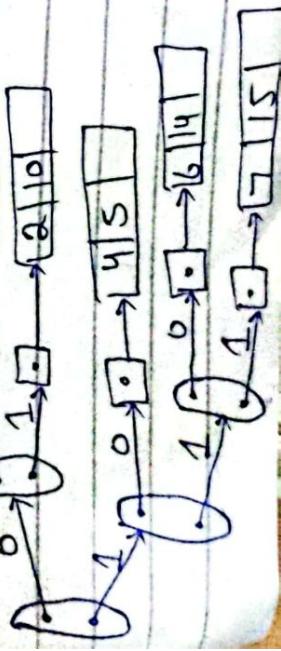
$$\text{file is unsorted}$$

$$\text{time:}$$

$$\text{block fetches needed}$$

$$\text{file is ordered on one record}$$

$$\text{block fetches needed}$$





(23)

Course	Advance Database Concepts	Answer Sheet No.	5608
Student's Name	Haniza Majeed	Signature	<i>[Signature]</i>
Roll No	20L-2074	Section	6A
Date	10-april-2013		

Question No: 1

$$S = 100,000$$

$$R = 10 + 10 = 30 \text{ bytes}$$

$$B = 1024$$

$$blk = \text{floor} \left(\frac{B}{R} \right) = \text{floor} \left(\frac{1024}{30} \right) = \text{floor}(34.13) = 34$$

$$\text{no. of blocks} = b = \text{ceiling} \left(\frac{S}{B} \right) = \left\lceil \frac{100,000}{34} \right\rceil = 2942$$

(a) as file is ordered on C so this query will take linear time.

So we will apply linear search:

$$\text{no. of block fetches needed} = O(b) = 2942$$

(b) as file is ordered on C so we will apply binary search. also we will consider selection cardinality of C in this part.

$$\text{selection Cardinality} = S = 5000$$

$$\begin{aligned}
 \text{no. of block fetches needed} &= \log_2(b) + \left\lceil \frac{S}{b} \right\rceil - 1 \\
 &= \log_2(2942) + \left\lceil \frac{5000}{34} \right\rceil - 1 \\
 &= 12 + 148 - 1 = 159 \text{ block fetches.}
 \end{aligned}$$

(c) we need 2 records in this part.

As file is ordered on C so

$$\text{no. of block fetches needed} = 2 \left(\log_2(b) + \left\lceil \frac{S}{b} \right\rceil - 1 \right)$$

we have already computed $\left(\log_2(b) + \left\lceil \frac{S}{b} \right\rceil - 1 \right)$ in previous part so

$$\text{no. of block fetches needed} = 2(159)$$

$$= 318$$

Question 2

key field size = 30 bytes

Record pointer = 10 bytes

Block pointer = P_B = 10 bytes

$$B = 1024$$

$$\delta = 1000,000$$

As it is a B⁺ tree so first we will calculate order p and order leaf.

Order p:

$$p * P + (p-1) * (\text{key field size}) < B$$

$$p * 10 + (p-1)(30) < 1024$$

$$10p + 30p - 30 < 1024$$

$$40p < 1024 + 30$$

$$p < \frac{1024 + 30}{40}$$

$$p < 26.35 \quad p = 26$$

Order

$$\frac{1}{P_{\text{rent}}} \times (\text{keyfield size} + P) + P < B$$

$$\frac{1}{P_{\text{rent}}} \times 30 + 10 + 10 < 1024$$

$$\frac{1}{P_{\text{rent}}} \times 40 < 1024 - 10$$

$$\frac{1}{P_{\text{rent}}} > \frac{1024 - 10}{40}$$

$$P_{\text{rent}} < 25.35$$

$P_{\text{rent}} \leq 25$ we will use ~~present~~ for level-1 nodes. no. of blocks/nodes at ~~leaf~~ level = $b_1 = \lceil \frac{1000000}{25} \rceil$

(a) no. of nodes at level-1 = b_1

$$b_1 = 40000$$

for internal levels we will use powers.

$$b_2 = \text{ceiling} \left(\frac{b_1}{2^6} \right) = \text{ceiling} \left(\frac{40000}{2^6} \right) = 1539$$

$$b_3 = \text{ceiling} \left(\frac{1539}{2^6} \right) = 60$$

$$b_4 = \text{ceiling} \left(\frac{60}{2^6} \right) = 3$$

$$b_5 = \text{ceiling} \left(\frac{3}{2^6} \right) = 1$$

so the rescaling tree will have 5 levels.

(b) no. of nodes at level b_1 (~~leaf level~~) will be = 40,000

at level b_2 no. of nodes will be = 1539

similarly at $b_3 = 60$

$$\text{at } b_4 = 3$$

$$\text{at } b_5 = 1$$

total nodes will be equal to $b_1 + b_2 + b_3 + b_4 + b_5 = 40,000 + 1539 + 1$

(c) As all the nodes (leaf + non-leaf).

Fill factor of 75%. So:

For b_{01}

$$0.75 \times b_{01} = 0.75 \times 25 = 18.75 \approx 19$$

So each leaf level node will have approximately 19 key records.

For b_1 :

$$0.75 \times b_1 = 0.75 \times 26 = 19.5 \approx 20$$

So each non-leaf level node will have approximately 20 key records.
So, now we will calculate no. of levels again.

No. of block nodes at first level = $b_1 = \lceil \frac{100,000}{19} \rceil$

$$b_1 = 52632$$

~~$b_2 = \text{ceiling} \left(\frac{52632}{20} \right) = 2632$~~

~~$b_3 = \text{ceiling} \left(\frac{2632}{20} \right) = 132$~~

~~$b_4 = \text{ceiling} \left(\frac{132}{20} \right) = 7$~~

~~$b_5 = \text{ceiling} \left(\frac{7}{20} \right) = 1$~~

So in this case we will again have 5 levels.

Question 3

as in both the queries we are joining the two tables on CID and OID.

So we will create primary index on CID for customer table and primary index on OID for orders table (as we are accessing data frequently on the base of these two key values).

Op gender, we will create Bit-map as its selection is low. (for customer table)

For date in orders table we can create clustering index if dates are in ordered form or secondary index if date is in unsorted.

For date ^(in order) we will use B+ tree as it is a range query so B+ tree works best in range queries.

Note: to make query more fast we can create hash index on CID and OID.

Question H4

Key values: 19, 14, 21, 8, 23, 15, 31, 25

hash function is $h(k) = k \bmod 4$

as each bucket can

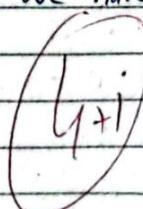
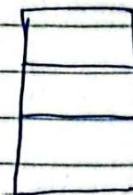
hold 3 records

so first 3 records
will be inserted as
it is without any
overflow.

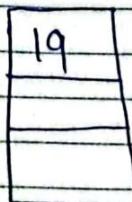
Binary table	
0	000
1	001
2	010
3	11

Step I: Initially global depth $d=0$

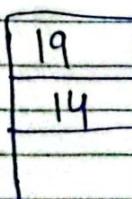
and local depth $d'=0$ and we have only
1 bucket



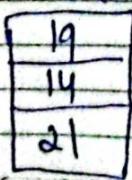
insert 19 $19 \bmod 4 = 3 \text{ (11)}$



insert 14 $14 \bmod 4 = 2 \text{ (10)}$



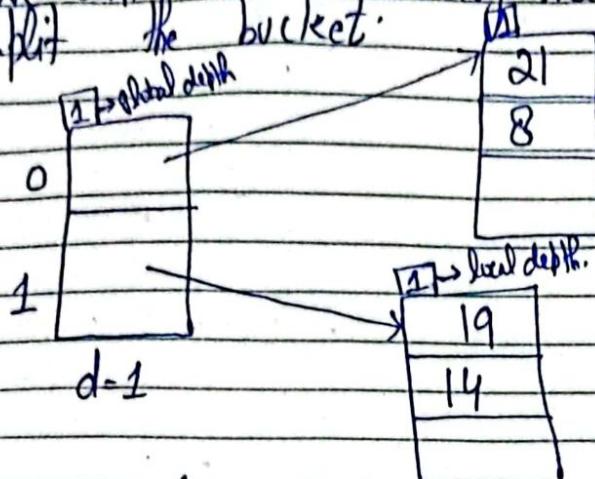
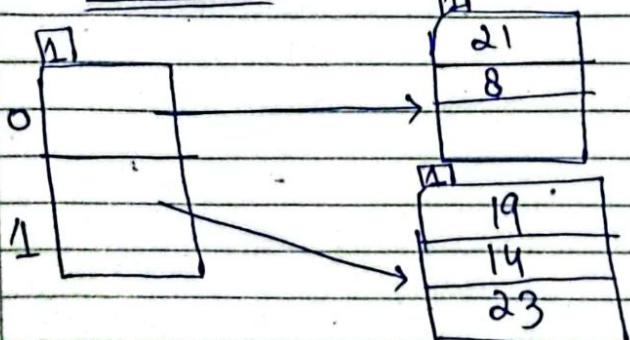
insert 21 $21 \bmod 4 = 1 \text{ (01)}$



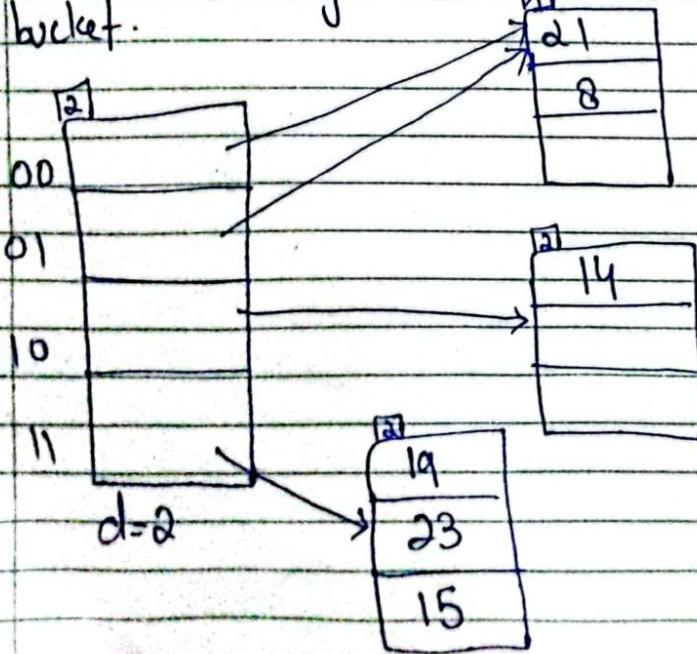
No.

insert 8 $8 \bmod 4 = 0$ (00)

as overflow occurred, since $d' = d$ so we will increase directory size and also split the bucket.

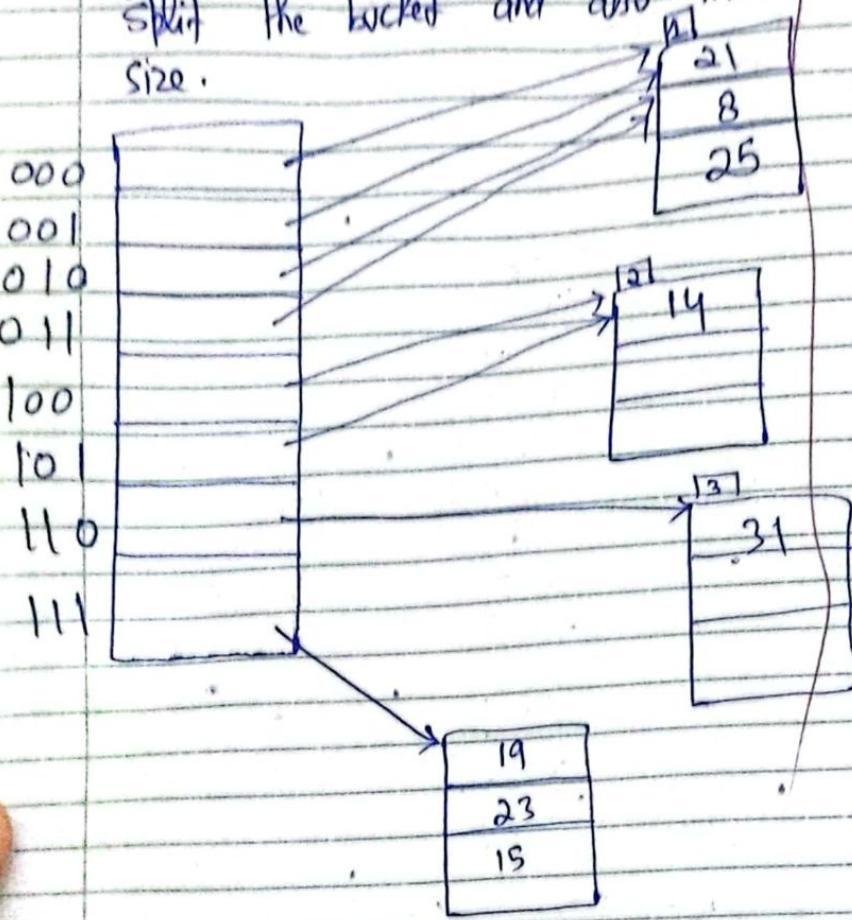
insert 23: $23 \bmod 4 = 3$ (11)insert 15 $15 \bmod 4 = 3$ (11)

overflow as $d' = d$ so we will increase directory size and also split the bucket.



insert 31 $31 \bmod 4 = 3(11)$

again overflow as $d' = d$ so we will split the bucket and also increase directory size.



insert 25 $25 \bmod 4 = 1(01)$