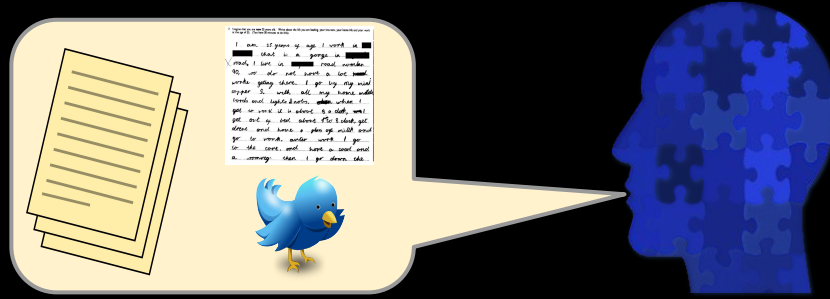


# Language Modeling

# Task



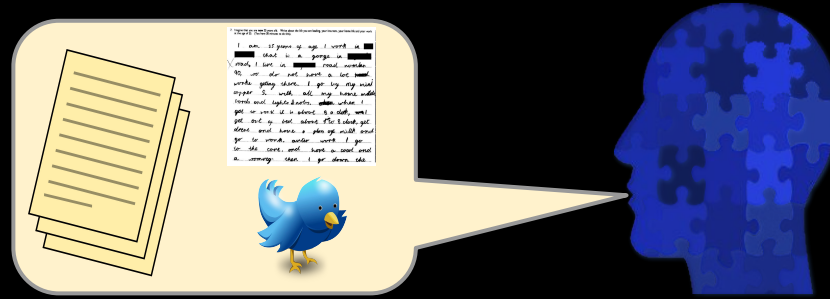
- Language Modeling (i.e. auto-complete)

# how?



- **Probabilistic Modeling**
  - **Probability Theory**
  - **Logistic Regression**
  - **Sequence Modeling**

# Task



- Language Modeling  
(i.e. auto-complete)

how?



- Probabilistic Modeling
  - Probability Theory
  - Logistic Regression
  - Sequence Modeling
- **Eventually: Deep Learning**
  - **Recurrent Neural Nets**
  - **Transformer Networks**

# Language Modeling

-- assigning a probability to sequences of words.

Version 1: Compute  $P(w_1, w_2, w_3, w_4, w_5) = P(W)$   
:probability of a sequence of words

# Language Modeling

-- assigning a probability to sequences of words.

Version 1: Compute  $P(w_1, w_2, w_3, w_4, w_5) = P(W)$   
:probability of a sequence of words

Version 2: Compute  $P(w_5 | w_1, w_2, w_3, w_4)$   
 $= P(w_n | w_1, w_2, \dots, w_{n-1})$   
:probability of a next word given history

# Language Modeling

Version 1: Compute  $P(w_1, w_2, w_3, w_4, w_5) = P(W)$

:probability of a sequence of words

$$P(\text{He ate the cake with the fork}) = ?$$

Version 2: Compute  $P(w_5 | w_1, w_2, w_3, w_4)$

$$= P(w_n | w_1, w_2, \dots, w_{n-1})$$

:probability of a next word given history

$$P(\text{fork} | \text{He ate the cake with the}) = ?$$

# Language Modeling

## Applications:

- Auto-complete: What word is next?
- Machine Translation: Which translation is most likely?
- Spell Correction: Which word is most likely given error?
- Speech Recognition: What did they just say?  
“eyes aw of an”

(example from Jurafsky, 2017; ..did you say "giraffe ski 2,017"? )

# Timeline: *Language Modeling* and *Vector Semantics*

1913 Markov: Probability that next letter would be vowel or consonant.

1948

1980

2003

2010

2018

*XLNet*

*RoBERTa*

*GPT3*

- Language Models
- Vector Semantics
- LMs + Vectors

~logarithmic scale



# Timeline: *Language Modeling* and *Vector Semantics*

1913 Markov: Probability that next letter would be vowel or consonant.

1948

1980

2003

2010

2018

These (or similar) are behind almost all state-of-the-art modern NLP systems

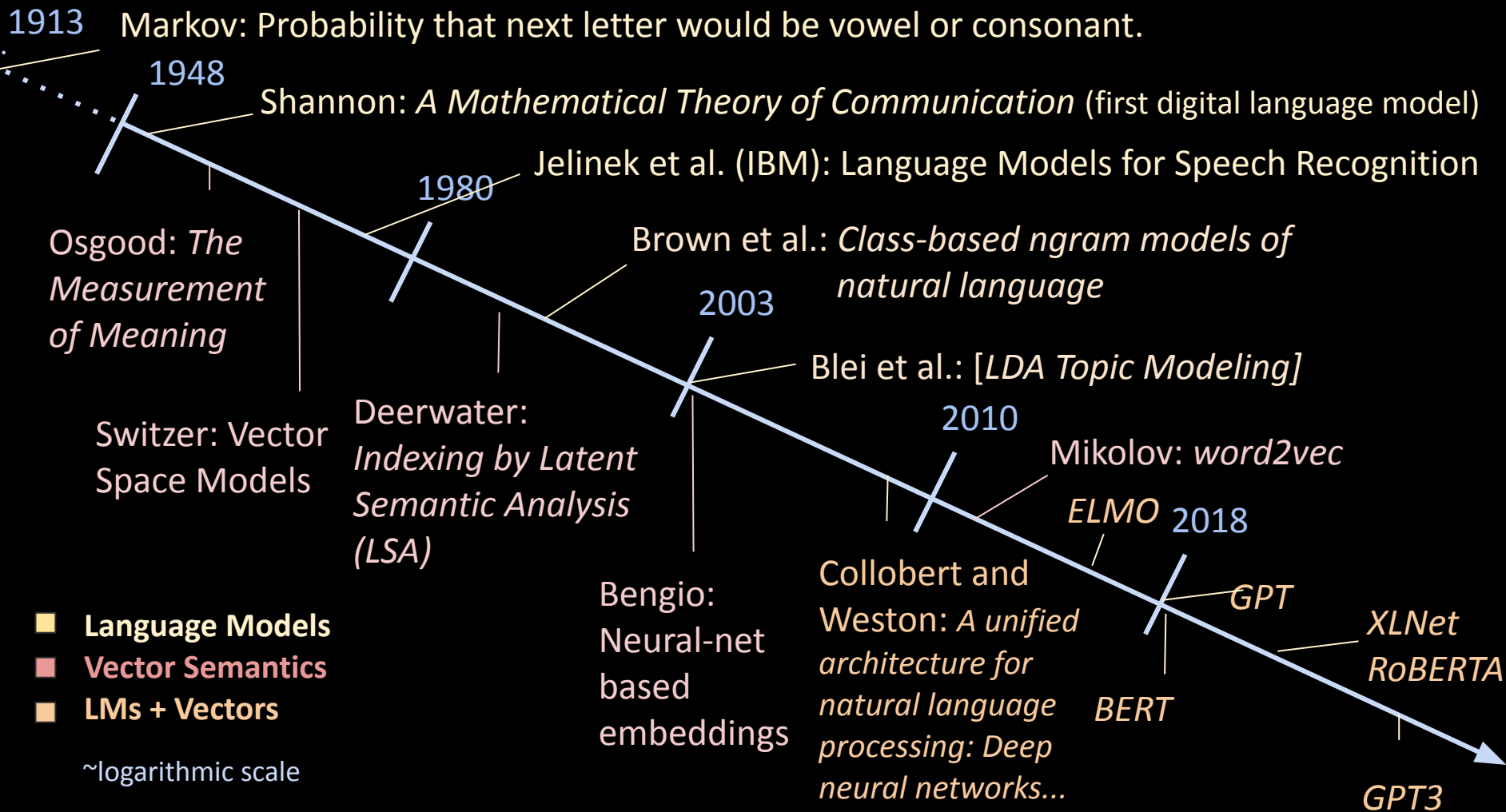
*XLNet*  
*RoBERTa*

*GPT3*

- Language Models
- Vector Semantics
- LMs + Vectors

~logarithmic scale

# Timeline: *Language Modeling* and *Vector Semantics*



# Language Modeling

Version 1: Compute  $P(w_1, w_2, w_3, w_4, w_5) = P(W)$

:probability of a sequence of words

$$P(\text{He ate the cake with the fork}) = ?$$

Version 2: Compute  $P(w_5 | w_1, w_2, w_3, w_4)$

$$= P(w_n | w_1, w_2, \dots, w_{n-1})$$

:probability of a next word given history

$$P(\text{fork} | \text{He ate the cake with the}) = ?$$

# Simple Solution

Version 1: Compute  $P(w_1, w_2, w_3, w_4, w_5) = P(W)$

:probability of a sequence of words

$P(\text{He ate the cake with the fork}) =$

$$\frac{\text{count}(\text{He ate the cake with the fork})}{\text{count}(* * * * * * *)}$$

# Simple Solution: The Maximum Likelihood Estimate

Version 1: Compute  $P(w_1, w_2, w_3, w_4, w_5) = P(W)$

:probability of a sequence of words

$P(\text{He ate the cake with the fork}) =$

total number of  
observed *7grams*

$$\frac{\text{count}(\text{He ate the cake with the fork})}{\text{count}(* * * * * *)}$$

# Simple Solution: The Maximum Likelihood Estimate

$$P(\text{He ate the cake with the fork}) =$$

$$\frac{\text{count}(\text{He ate the cake with the fork})}{\text{count}(* * * * *)}$$

$$P(\text{fork} \mid \text{He ate the cake with the}) =$$

$$\frac{\text{count}(\text{He ate the cake with the fork})}{\text{count}(\text{He ate the cake with the } *)}$$

# Simple Solution: The Maximum Likelihood Estimate

**Problem:** even the Web isn't large enough to enable good estimates of most phrases.

$$P(\textit{He ate the cake with the fork}) =$$

$$\frac{\textit{count(He ate the cake with the fork)}}{\textit{count(* * * * * *)}}$$

$$P(\textit{fork} \mid \textit{He ate the cake with the}) =$$

$$\frac{\textit{count(He ate the cake with the fork)}}{\textit{count(He ate the cake with the *)}}$$

**Problem:** even the Web isn't large enough to enable good estimates of most phrases.

**Solution:** Estimate from shorter sequences, use more sophisticated probability theory.



**Problem:** even the Web isn't large enough to enable good estimates of most phrases.

**Solution:** Estimate from shorter sequences, use more sophisticated probability theory.

$$P(B|A) = P(B, A) / P(A) \Leftrightarrow P(A)P(B|A) = P(B,A) = P(A,B)$$

**Problem:** even the Web isn't large enough to enable good estimates of most phrases.

**Solution:** Estimate from shorter sequences, use more sophisticated probability theory.

$$P(B|A) = P(B, A) / P(A) \Leftrightarrow P(A)P(B|A) = P(B, A) = P(A, B)$$

$$P(A, B, C) = P(A)P(B|A)P(C|A, B)$$

**Problem:** even the Web isn't large enough to enable good estimates of most phrases.

**Solution:** Estimate from shorter sequences, use more sophisticated probability theory.

$$P(B|A) = P(B, A) / P(A) \Leftrightarrow P(A)P(B|A) = P(B, A) = P(A, B)$$

$$P(A, B, C) = P(A)P(B|A)P(C|A, B)$$

**The Chain Rule:**

$$P(X_1, X_2, \dots, X_n) = P(X_1)P(X_2|X_1)P(X_3|X_1, X_2) \dots P(X_n|X_1, \dots, X_{n-1})$$

**Problem:** even the Web isn't large enough to enable good estimates of most phrases.

**Solution:** Estimate from shorter sequences, use more sophisticated probability theory.

$$P(B|A) = P(B, A) / P(A) \Leftrightarrow P(A)P(B|A) = P(B, A) = P(A, B)$$

$$P(A, B, C) = P(A)P(B|A)P(C|A, B)$$

**The Chain Rule:** 
$$P(X_1, X_2, \dots, X_n) = \prod_{i=1}^n P(X_i | X_1, X_2, \dots, X_{i-1})$$

$$P(X_1, X_2, \dots, X_n) = P(X_1)P(X_2|X_1)P(X_3|X_1, X_2) \dots P(X_n|X_1, \dots, X_{n-1})$$

**Markov Assumption:**

$$P(X_1, X_2, \dots, X_n) = \prod_{i=1}^n P(X_i | X_{i-k}, X_{i-(k-1)}, \dots, X_i)$$

**Solution:** Estimate from shorter sequences, use more sophisticated probability theory.

$$P(B|A) = P(B, A) / P(A) \Leftrightarrow P(A)P(B|A) = P(B, A) = P(A, B)$$

$$P(A, B, C) = P(A)P(B|A)P(C|A, B)$$

**The Chain Rule:** 
$$P(X_1, X_2, \dots, X_n) = \prod_{i=1}^n P(X_i | X_1, X_2, \dots, X_{i-1})$$

$$P(X_1, X_2, \dots, X_n) = P(X_1)P(X_2|X_1)P(X_3|X_1, X_2) \dots P(X_n|X_1, \dots, X_{n-1})$$

**Markov Assumption:**  $P(X_1, X_2, \dots, X_n) = \prod_{i=1}^n P(X_i | X_{i-k}, X_{i-(k-1)}, \dots, X_i)$   
 $P(X_n | X_1, \dots, X_{n-1}) \approx P(X_n | X_{n-k}, \dots, X_{n-1})$  where  $k < n$

**Solution:** Estimate from shorter sequences, use more sophisticated probability theory.

$$P(B|A) = P(B, A) / P(A) \Leftrightarrow P(A)P(B|A) = P(B, A) = P(A, B)$$

$$P(A, B, C) = P(A)P(B|A)P(C|A, B)$$

**The Chain Rule:**  $P(X_1, X_2, \dots, X_n) = \prod_{i=1}^n P(X_i | X_1, X_2, \dots, X_{i-1})$   
 $P(X_1, X_2, \dots, X_n) = P(X_1)P(X_2|X_1)P(X_3|X_1, X_2) \dots P(X_n|X_1, \dots, X_{n-1})$

## Markov Assumption:

$$P(X_n | X_1, \dots, X_{n-1})$$

$$P(X_n | X_{n-1})$$

What about Logistic Regression?  $Y$  = next word  
 $P(Y|X) = P(X_n | X_{n-1}, X_{n-2}, X_{n-3}, \dots)$

Not a terrible option, but  $X_{n-1}$  through  $X_{n-k}$   
would be modeled as independent dimensions.  
Let's revisit later.

## The Chain

$$P(X_1, X_2, \dots, X_n) = P(X_1) \prod_{i=2}^n P(X_i | X_1, X_2, \dots, X_{i-1})$$

**Markov Assumption:**  $P(X_1, X_2, \dots, X_n) = \prod_{i=1}^n P(X_i | X_{i-k}, X_{i-(k-1)}, \dots, X_i)$   
 $P(X_n | X_1, \dots, X_{n-1}) \approx P(X_n | X_{n-k}, \dots, X_{n-1})$  where  $k < n$

**Unigram Model:  $k = 0$ ;**  $P(X_1, X_2, \dots, X_n) = \prod_{i=1}^n P(X_i)$

$$P(B|A) = P(B, A) / P(A) \Leftrightarrow P(A)P(B|A) = P(B, A) = P(A, B)$$

$$P(A, B, C) = P(A)P(B|A)P(C|A, B)$$

**The Chain Rule:**  $P(X_1, X_2, \dots, X_n) = \prod_{i=1}^n P(X_i | X_1, X_2, \dots, X_{i-1})$   
 $P(X_1, X_2, \dots, X_n) = P(X_1)P(X_2|X_1)P(X_3|X_1, X_2) \dots P(X_n|X_1, \dots, X_{n-1})$



**Markov Assumption:**  $P(X_1, X_2, \dots, X_n) = \prod_{i=1}^n P(X_i | X_{i-k}, X_{i-(k-1)}, \dots, X_i)$   
 $P(X_n | X_1, \dots, X_{n-1}) \approx P(X_n | X_{n-k}, \dots, X_{n-1})$  where  $k < n$

**Bigram Model:  $k = 1$ ;**  $P(X_1, X_2, \dots, X_n) = \prod_{i=1}^n P(X_i | X_{i-1})$

Example generated sentence:

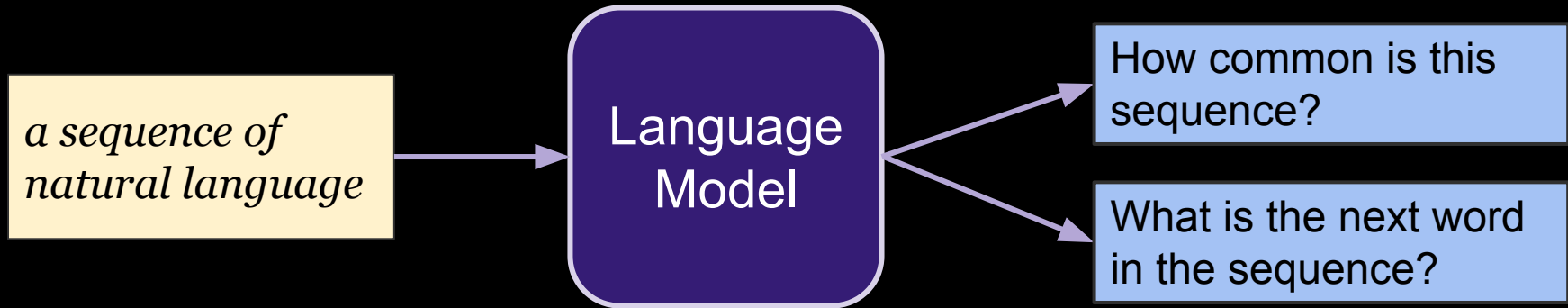
*outside, new, car, parking, lot, of, the, agreement, reached*

$P(X_1 = \text{"outside"}, X_2 = \text{"new"}, X_3 = \text{"car"}, \dots)$   
 $\approx P(X_1 = \text{"outside"}) * P(X_2 = \text{"new"} | X_1 = \text{"outside"}) * P(X_3 = \text{"car"} | X_2 = \text{"new"}) * \dots$

Example from (Jurafsky, 2017)

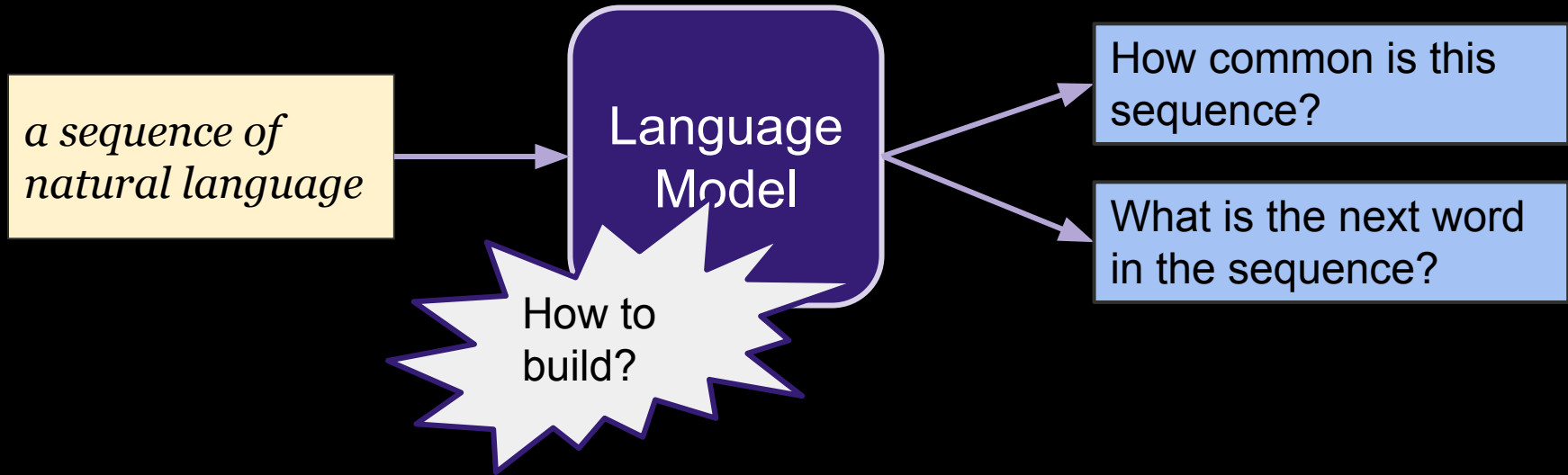
# Language Modeling

Building a model (or system / API) that can answer the following:



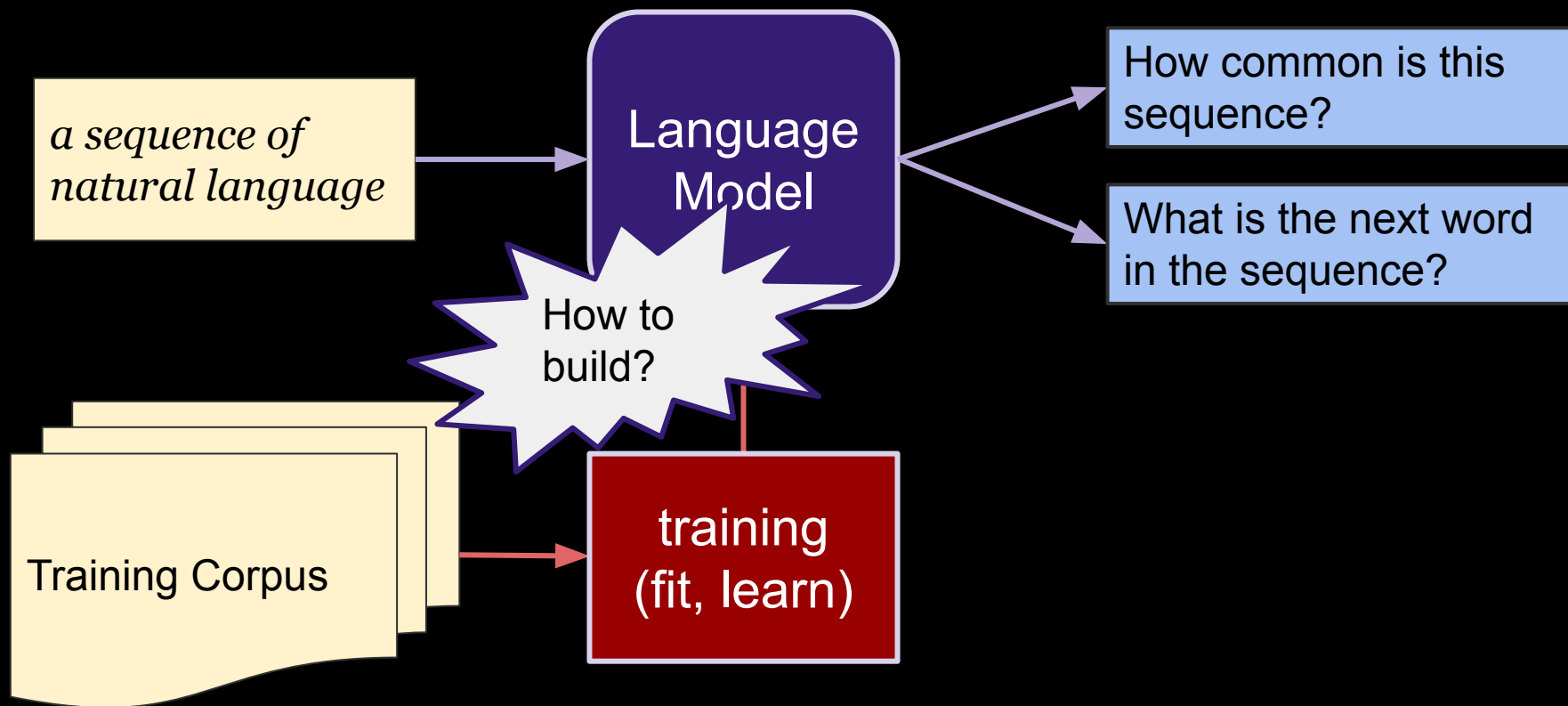
# Language Modeling

Building a model (or system / API) that can answer the following:



# Language Modeling

Building a model (or system / API) that can answer the following:



# Language Model

## Building a model (

*a sequence of  
natural language*

Food corpus from Jurafsky (2018). Samples:

*can you tell me about any good cantonese restaurants close by*

*mid priced thai food is what i'm looking for*

*tell me about chez panisse*

*can you give me a listing of the kinds of food that are available*

*i'm looking for a good place to eat breakfast*

*when is caffe venezia open during the day*

Training Corpus

training  
(fit, learn)

## Bigram Counts

first word \ second word

	i	want	to	eat	chinese	food	lunch	spend
i	5	827	0	9	0	0	0	2
want	2	0	608	1	6	6	5	1
to	2	0	4	686	2	0	6	211
eat	0	0	2	0	16	2	42	0
chinese	1	0	0	0	0	82	1	0
food	15	0	15	0	1	4	0	0
lunch	2	0	0	0	0	1	0	0
spend	1	0	1	0	0	0	0	0

Example from (Jurafsky, 2017)

Training Corpus

training  
(fit, learn)

# Bigram Counts

first word | second word

	i	want	to	eat	chinese	food	lunch	spend
i	5	827	0	9	0	0	0	2
want	2	0	608	1	6	6	5	1
to	2	0	4	686	2	0	6	211
eat	0	0	2	0	16	2	42	0
chinese	1	0	0	0	0	82	1	0
food	15	0	15	0	1	4	0	0
lunch	2	0	0	0	0	1	0	0
spend	1	0	1	0	0	0	0	0

i	want	to	eat	chinese	food	lunch	spend
2533	927	2417	746	158	1093	341	278

Training Corpus

training  
(fit, learn)

# Bigram Counts

first word | second word

	i	want	to	eat	chinese	food	lunch	spend
i	5	827	0	9	0	0	0	2
want	2	0	608	1	6	6	5	1
to	2	0	4	686	2	0	6	211
eat	0	0	2	0	16	2	42	0
chinese	1	0	0	0	0	82	1	0
food	15	0	15	0	1	4	0	0
lunch	2	0	0	0	0	1	0	0
spend	1	0	1	0	0	0	0	0

i	want	to	eat	chinese	food	lunch	spend
2533	927	2417	746	158	1093	341	278

Training corpus (fit, learn)

**Bigram model:**  $P(X_1, X_2, \dots, X_n) = \prod_{i=1}^n P(X_i | X_{i-1})$

Need to estimate:  $P(X_i | X_{i-1}) = \text{count}(X_{i-1} X_i) / \text{count}(X_{i-1})$



second word:  $x_i$

$$P(X_i | X_{i-1})$$

first word:  $x_{i-1}$

	i	want	to	eat	chinese	food	lunch	spend
i	0.002	0.33	0	0.0036	0	0	0	0.00079
want	0.0022	0	0.66	0.0011	0.0065	0.0065	0.0054	0.0011
to	0.00083	0	0.0017	0.28	0.00083	0	0.0025	0.087
eat	0	0	0.0027	0	0.021	0.0027	0.056	0
chinese	0.0063	0	0	0	0	0.52	0.0063	0
food	0.014	0	0.014	0	0.00092	0.0037	0	0
lunch	0.0059	0	0	0	0	0.0029	0	0
spend	0.0036	0	0.0036	0	0	0	0	0

i	want	to	eat	chinese	food	lunch	spend
2533	927	2417	746	158	1093	341	278

Training corpus

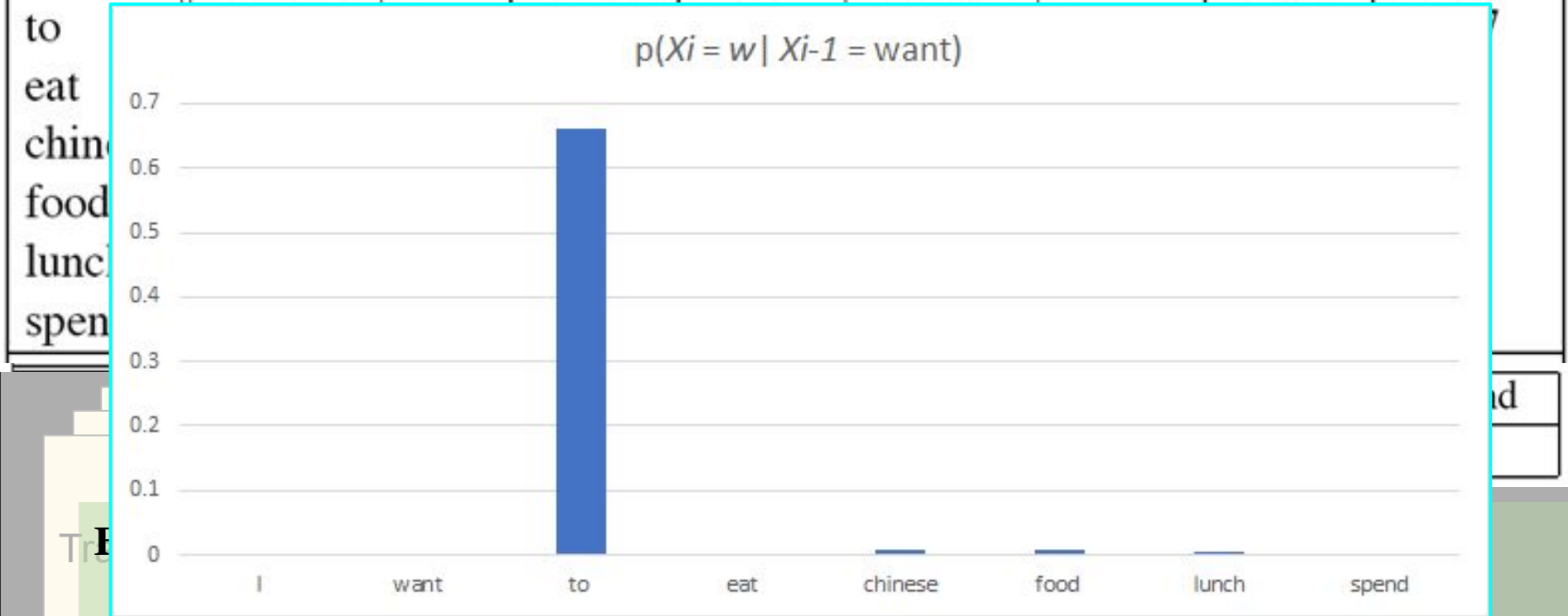
**Bigram model:**  $P(X_1, X_2, \dots, X_n) = \prod_{i=1}^n P(X_i | X_{i-1})$

Need to estimate:  $P(X_i | X_{i-1}) = \text{count}(X_{i-1} X_i) / \text{count}(X_{i-1})$

first word( $X_{i-1}$ ) \ second word ( $X_i$ )

$$P(X_i | X_{i-1})$$

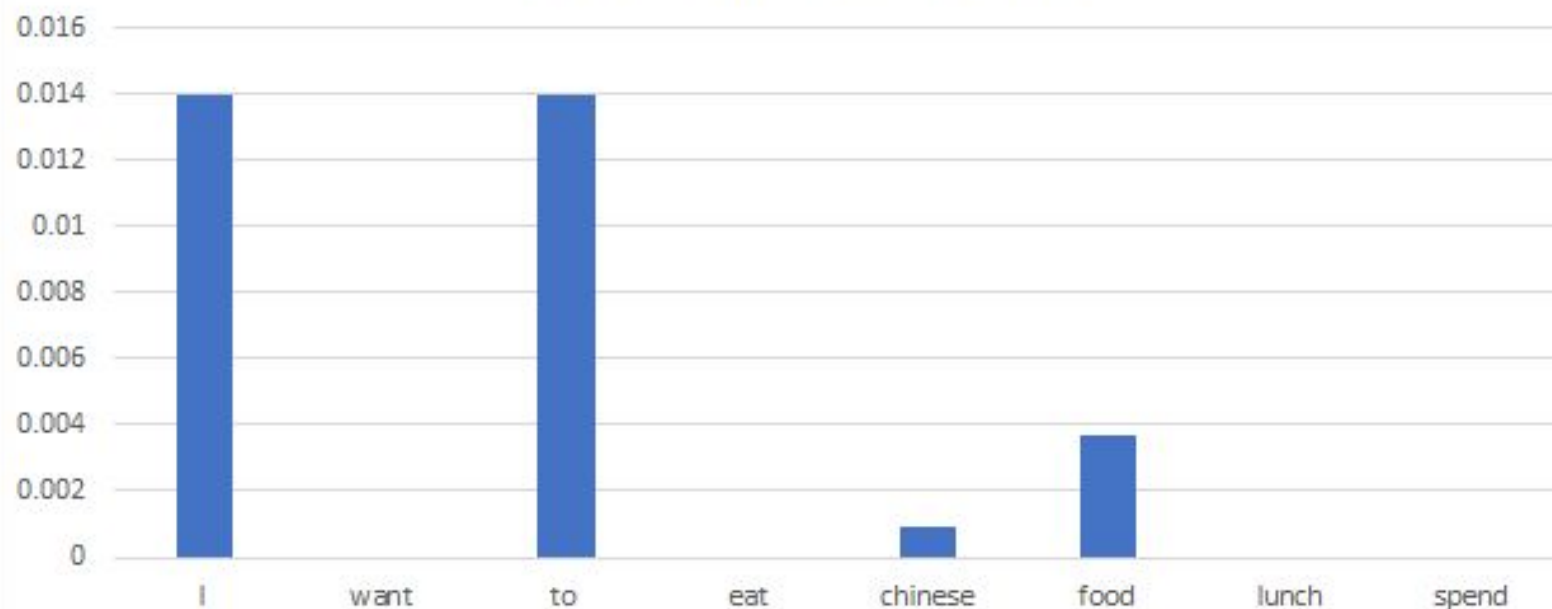
	i	want	to	eat	chinese	food	lunch	spend
i	0.002	0.33	0	0.0036	0	0	0	0.00079
want	0.0022	0	0.66	0.0011	0.0065	0.0065	0.0054	0.0011



Need to estimate:  $P(X_i | X_{i-1}) = \text{count}(X_{i-1} X_i) / \text{count}(X_{i-1})$

i	0.002	0.33	0	0.0036	0	0	0	0.00079
want	0.0022	0	0.66	0.0011	0.0065	0.0065	0.0054	0.0011
to	0.00083	0	0.0017	0.28	0.00083	0	0.0025	0.087
eat	0	0	0.0027	0	0.021	0.0027	0.056	0
chinese	0.0063	0	0	0	0	0.52	0.0063	0
food	0.014	0	0.014	0	0.00092	0.0037	0	0

$$p(X_i = w \mid X_{i-1} = \text{food})$$

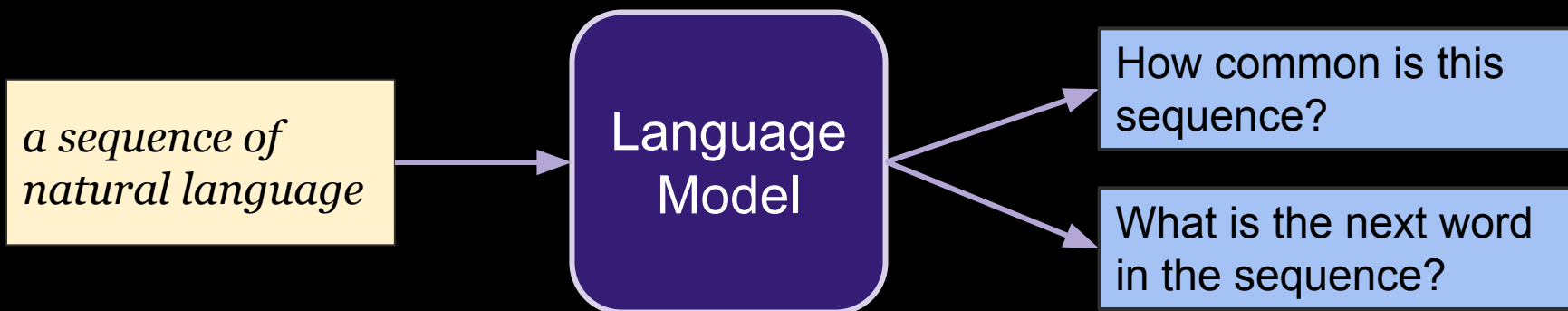


0
0
0
0
0
spend
278

count( $X_{i-1}$ )

# Language Modeling

Building a model (or system / API) that can answer the following:



Example from (Jurafsky, 2017)

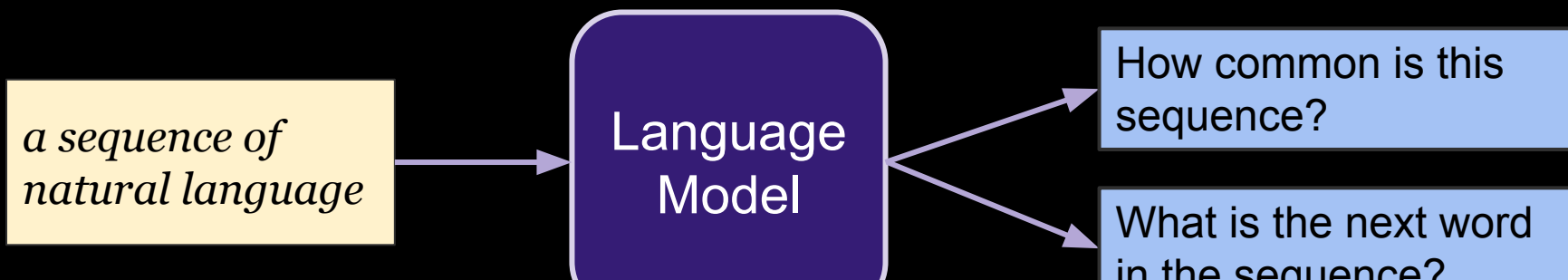
training

⌈ **Bigram model:**  $P(X_1, X_2, \dots, X_n) = \prod_{i=1}^n P(X_i | X_{i-1})$

Need to estimate:  $P(X_i | X_{i-1}) = \text{count}(X_{i-1} X_i) / \text{count}(X_{i-1})$

# Language Modeling

Building a model (or system / API) that can answer the following:



**Trigram model:** 
$$P(X_1, X_2, \dots, X_n) = \prod_{i=1}^n P(X_i | X_{i-2}, X_{i-1})$$

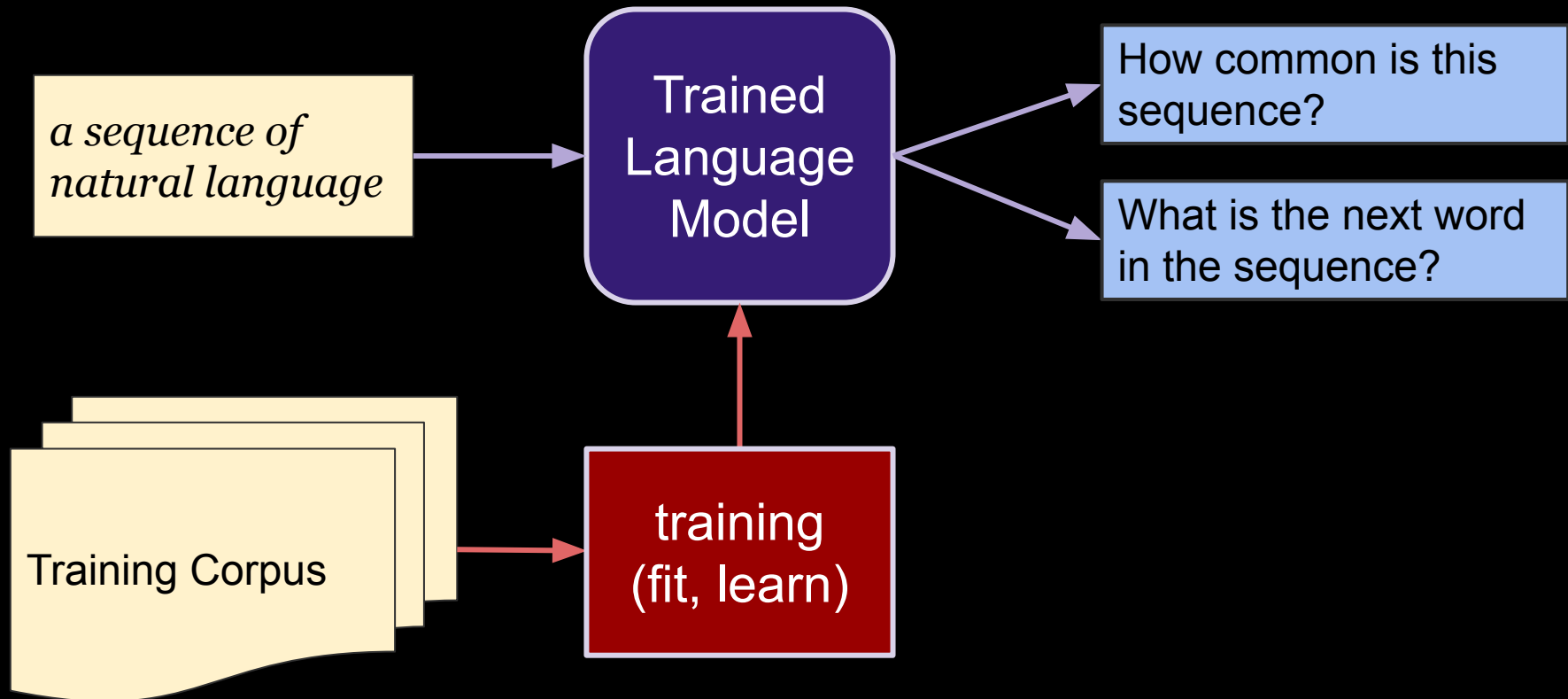
Need to estimate:  $P(X_i | X_{i-1}, X_{i-2}) = \text{count}(X_{i-2} X_{i-1} X_i) / \text{count}(X_{i-2} X_{i-1})$

**Bigram model:** 
$$P(X_1, X_2, \dots, X_n) = \prod_{i=1}^n P(X_i | X_{i-1})$$

Need to estimate:  $P(X_i | X_{i-1}) = \text{count}(X_{i-1} X_i) / \text{count}(X_{i-1})$

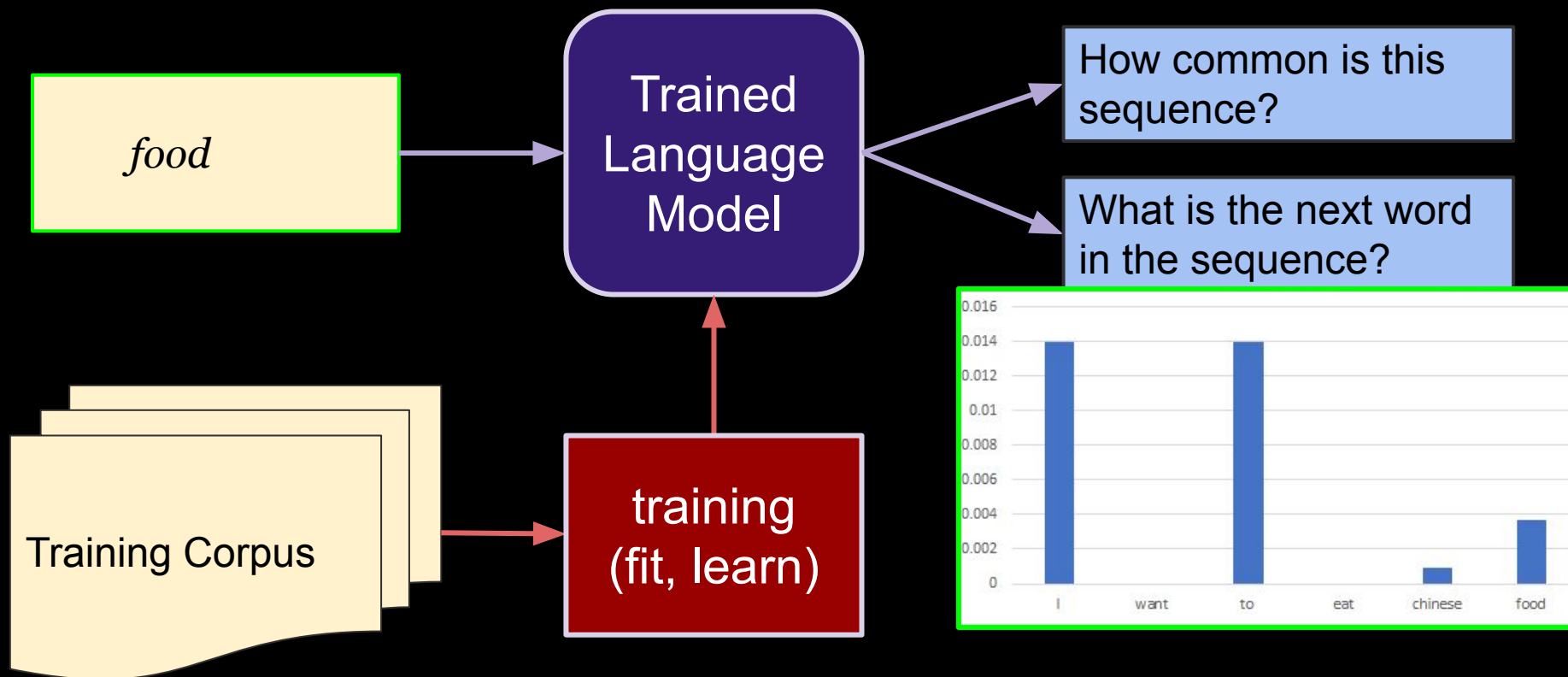
# Language Modeling

Building a model (or system / API) that can answer the following:



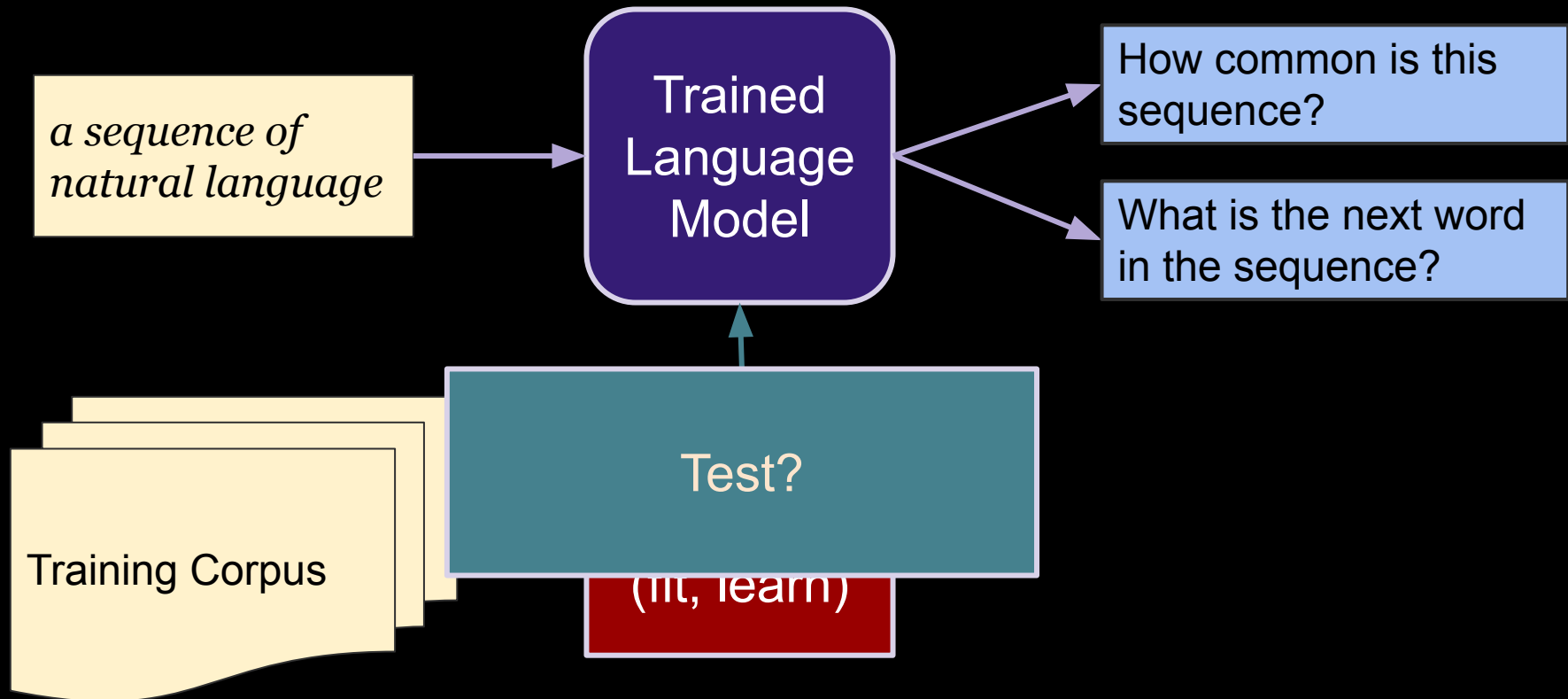
# Language Modeling

Building a model (or system / API) that can answer the following:



# Language Modeling

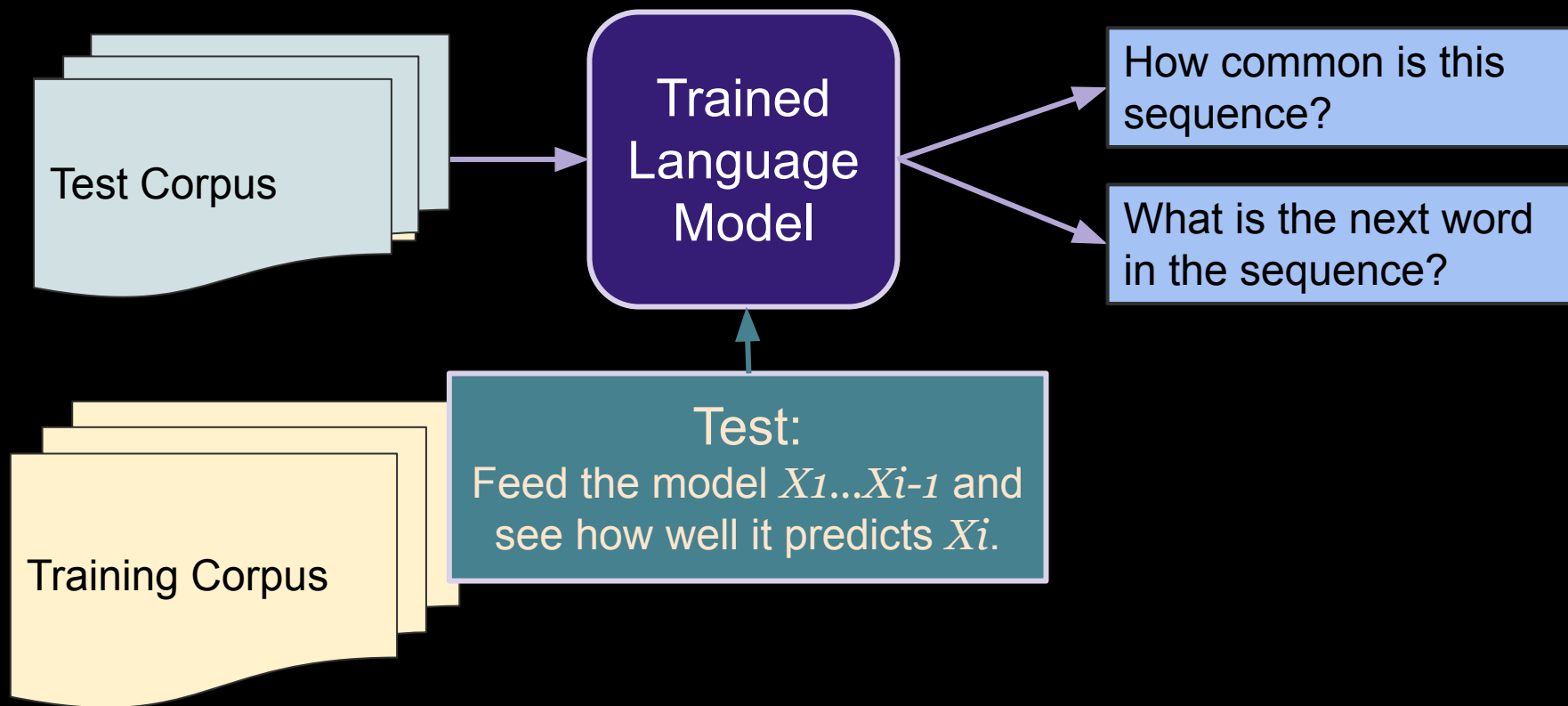
Building a model (or system / API) that can answer the following:





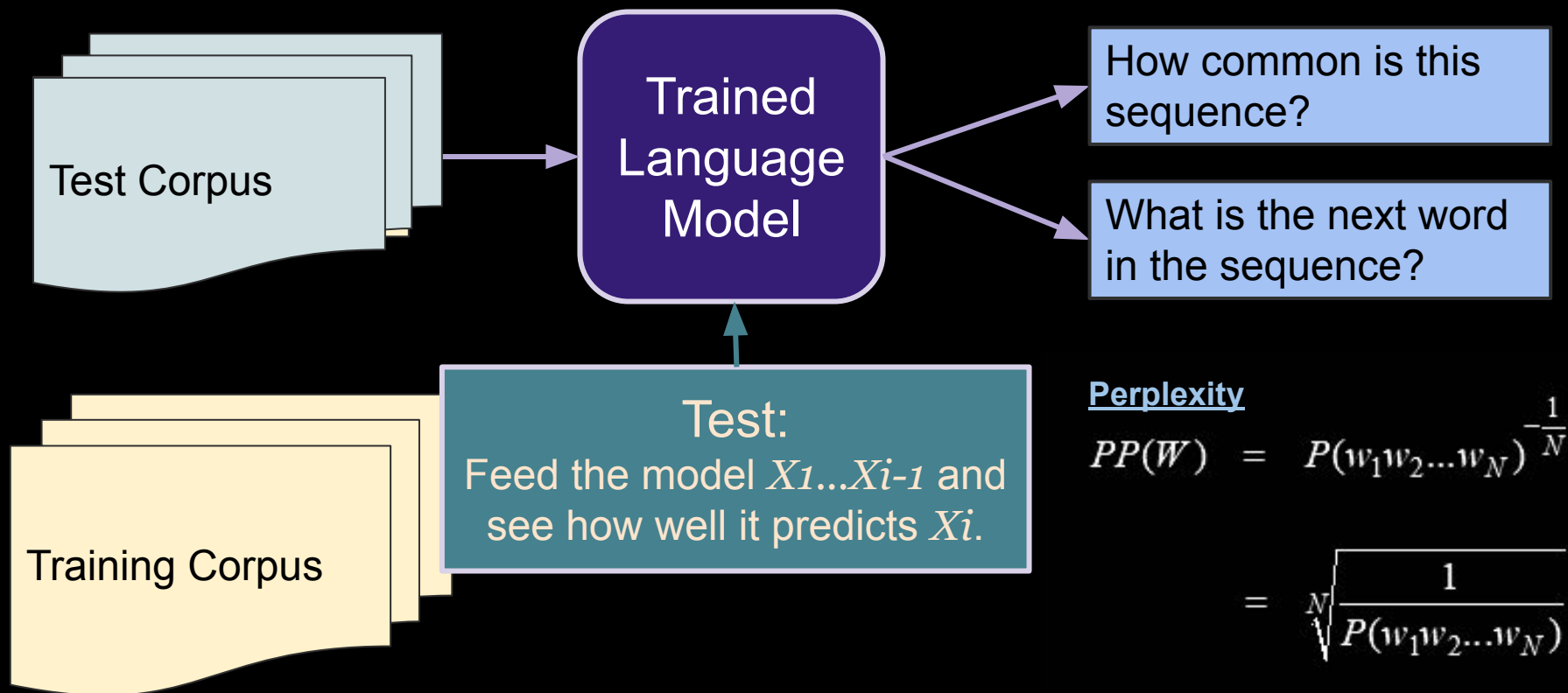
# Language Modeling

Building a model (or system / API) that can answer the following:

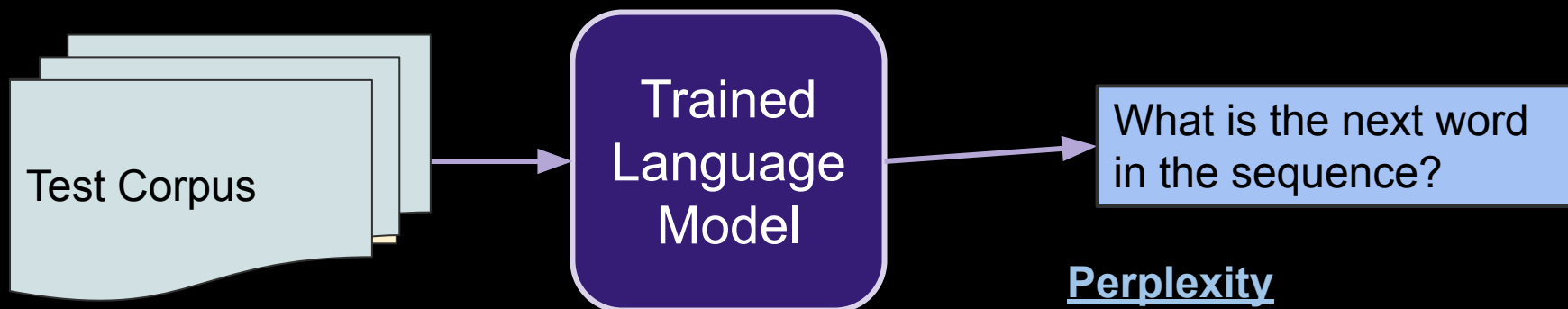


# Language Modeling

Building a model (or system / API) that can answer the following:



# Evaluation

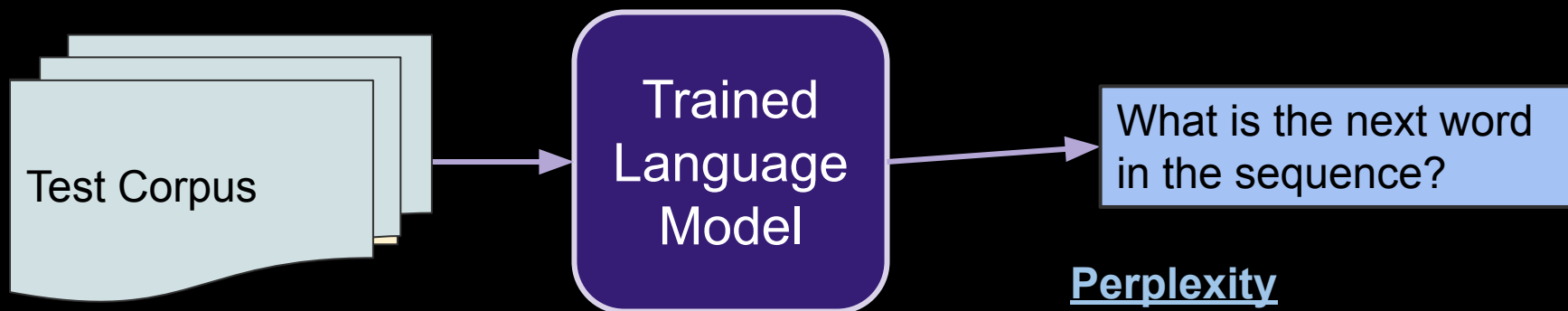


Perplexity

$$PP(W) = P(w_1 w_2 \dots w_N)^{-\frac{1}{N}}$$

$$= \sqrt[N]{\frac{1}{P(w_1 w_2 \dots w_N)}}$$

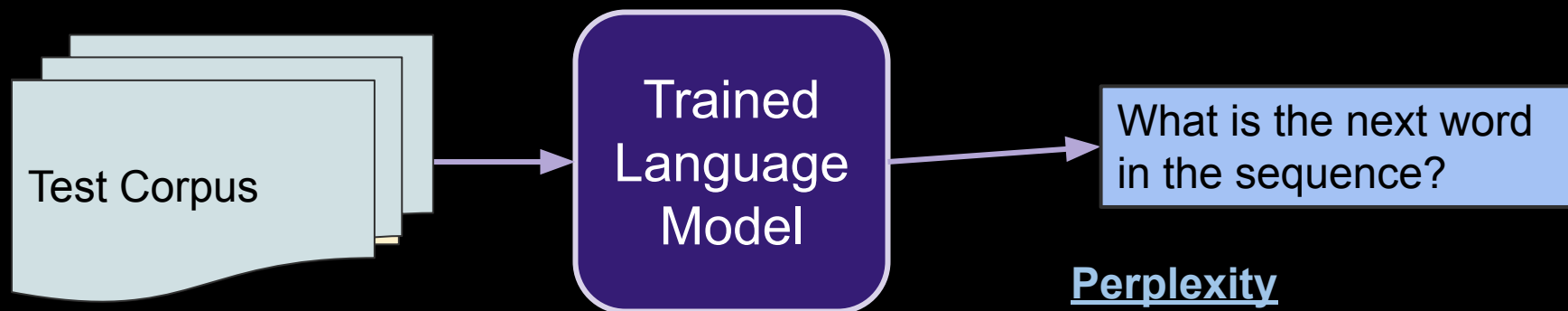
# Evaluation



Apply Chain Rule:  $PP(W) = \sqrt[N]{\prod_{i=1}^N \frac{1}{P(w_i | w_1 \dots w_{i-1})}}$

$$PP(W) = P(w_1 w_2 w_3 \dots w_N)^{1/N}$$
$$= \sqrt[N]{\frac{1}{P(w_1 w_2 w_3 \dots w_N)}}$$

# Evaluation



Apply Chain Rule:  $PP(W) = \sqrt[N]{\prod_{i=1}^N \frac{1}{P(w_i | w_1 \dots w_{i-1})}}$

Thus,  
PP for Bigrams:

$$PP(W) = \sqrt[N]{\prod_{i=1}^N \frac{1}{P(w_i | w_{i-1})}}$$

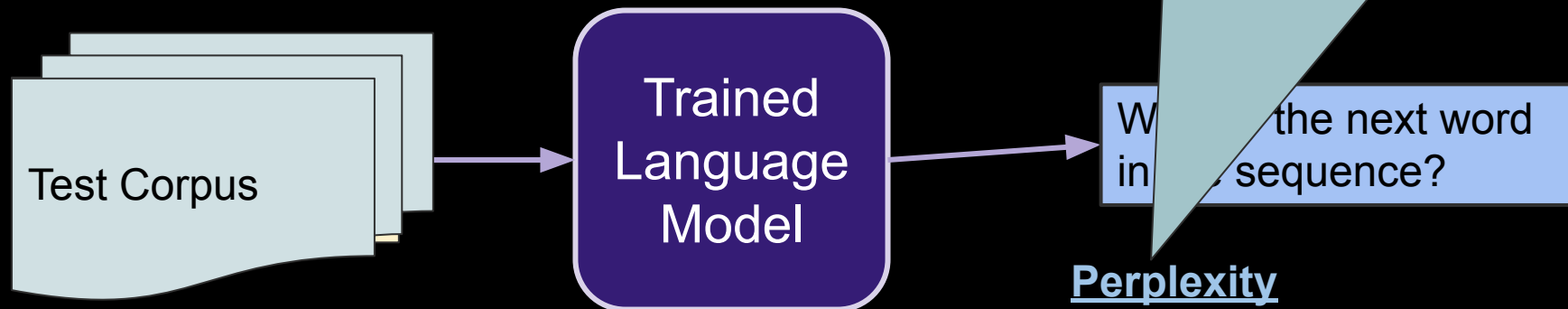
$$PP(W) = P(w_1 w_2 w_3 \dots w_N)^{1/N}$$

$$= \sqrt[N]{\frac{1}{P(w_1 w_2 w_3 \dots w_N)}}$$

# Evaluation

Reasoning:

- 1) Inverse of probability  
(i.e. minimize perplexity = maximize likelihood)
- 2) (weighted) average branching factor



Apply Chain Rule:  $PP(W) = \sqrt[N]{\prod_{i=1}^N \frac{1}{P(w_i | w_1 \dots w_{i-1})}}$

Thus,  
PP for Bigrams:

$$PP(W) = \sqrt[N]{\prod_{i=1}^N \frac{1}{P(w_i | w_{i-1})}}$$

$$PP(W) = P(w_1 w_2 w_3 \dots w_N)^{1/N}$$

$$= \sqrt[N]{\frac{1}{P(w_1 w_2 w_3 \dots w_N)}}$$

## Practical Considerations:

- Use log probability to keep numbers reasonable and save computation.  
(uses addition rather than multiplication)
- Out-of-vocabulary (OOV)  
Choose minimum frequency and mark as <OOV>
- Sentence start and end: <*s*> *this is a sentence* </*s*>  
Advantage: models word probability at beginning or end.

# Zeros and Smoothing

first word( $X_{i-1}$ ) \ second word ( $X_i$ )       $P(X_i | X_{i-1})$

	i	want	to	eat	chinese	food	lunch	spend
i	0.002	0.33	0	0.0036	0	0	0	0.00079
want	0.0022	0	0.66	0.0011	0.0065	0.0065	0.0054	0.0011
to	0.00083	0	0.0017	0.28	0.00083	0	0.0025	0.087
eat	0	0	0.0027	0	0.021	0.0027	0.056	0
chinese	0.0063	0	0	0	0	0.52	0.0063	0
food	0.014	0	0.014	0	0.00092	0.0037	0	0
lunch	0.0059	0	0	0	0	0.0029	0	0
spend	0.0036	0	0.0036	0	0	0	0	0

Example from (Jurafsky, 2017)



# Zeros and Smoothing

first word \ second word      Bigram Counts

	i	want	to	eat	chinese	food	lunch	spend
i	5	827	0	9	0	0	0	2
want	2	0	608	1	6	6	5	1
to	2	0	4	686	2	0	6	211
eat	0	0	2	0	16	2	42	0
chinese	1	0	0	0	0	82	1	0
food	15	0	15	0	1	4	0	0
lunch	2	0	0	0	0	1	0	0
spend	1	0	1	0	0	0	0	0

Laplace (“Add one”) smoothing: add 1 to all counts

# Zeros and Smoothing

first word \ second word      Bigram Counts

	i	want	to	eat	chinese	food	lunch	spend
i	6	828	1	10	1	1	1	3
want	3	1	609	2	7	7	6	2
to	3	1	5	687	3	1	7	212
eat	1	1	3	1	17	3	43	1
chinese	2	1	1	1	1	83	2	1
food	16	1	16	1	2	5	1	1
lunch	3	1	1	1	1	2	1	1
spend	2	1	2	1	1	1	1	1

Laplace (“Add one”) smoothing: add 1 to all counts

# Unsmoothed probs

first word( $X_{i-1}$ ) \ second word ( $X_i$ )

$$P(X_i | X_{i-1})$$

	i	want	to	eat	chinese	food	lunch	spend
i	0.002	0.33	0	0.0036	0	0	0	0.00079
want	0.0022	0	0.66	0.0011	0.0065	0.0065	0.0054	0.0011
to	0.00083	0	0.0017	0.28	0.00083	0	0.0025	0.087
eat	0	0	0.0027	0	0.021	0.0027	0.056	0
chinese	0.0063	0	0	0	0	0.52	0.0063	0
food	0.014	0	0.014	0	0.00092	0.0037	0	0
lunch	0.0059	0	0	0	0	0.0029	0	0
spend	0.0036	0	0.0036	0	0	0	0	0

Example from (Jurafsky, 2017)

# Smoothed

$$P_{Add-1}(w_i | w_{i-1}) = \frac{c(w_{i-1}, w_i) + 1}{c(w_{i-1}) + V}$$

(vocabulary size)

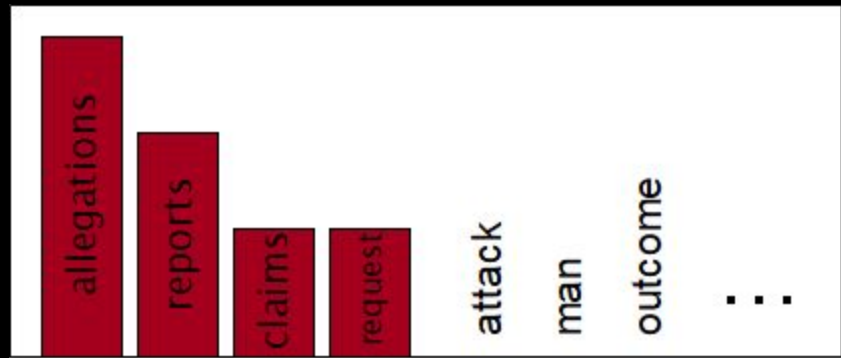
first word( $X_{i-1}$ ) \ second word ( $X_i$ )  
 $P(X_i | X_{i-1})$

	i	want	to	eat	chinese	food	lunch	spend
i	0.0015	0.21	0.00025	0.0025	0.00025	0.00025	0.00025	0.00075
want	0.0013	0.00042	0.26	0.00084	0.0029	0.0029	0.0025	0.00084
to	0.00078	0.00026	0.0013	0.18	0.00078	0.00026	0.0018	0.055
eat	0.00046	0.00046	0.0014	0.00046	0.0078	0.0014	0.02	0.00046
chinese	0.0012	0.00062	0.00062	0.00062	0.00062	0.052	0.0012	0.00062
food	0.0063	0.00039	0.0063	0.00039	0.00079	0.002	0.00039	0.00039
lunch	0.0017	0.00056	0.00056	0.00056	0.00056	0.0011	0.00056	0.00056
spend	0.0012	0.00058	0.0012	0.00058	0.00058	0.00058	0.00058	0.00058

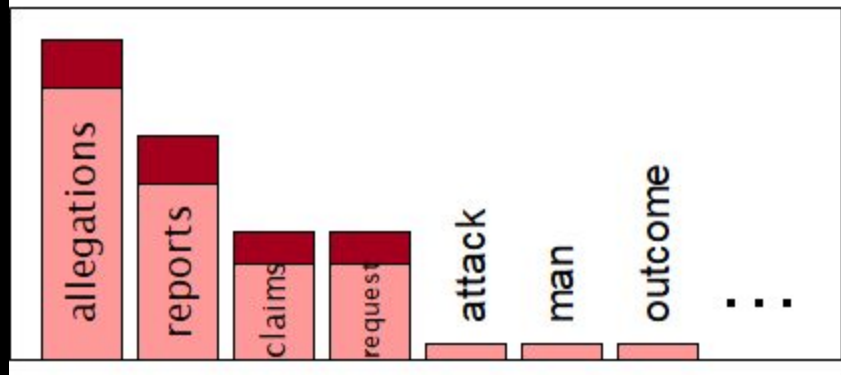
Example from (Jurafsky, 2017)

# Why Smoothing? Generalizes

Original



With Smoothing



(Example from Jurafsky / Originally Dan Klein)

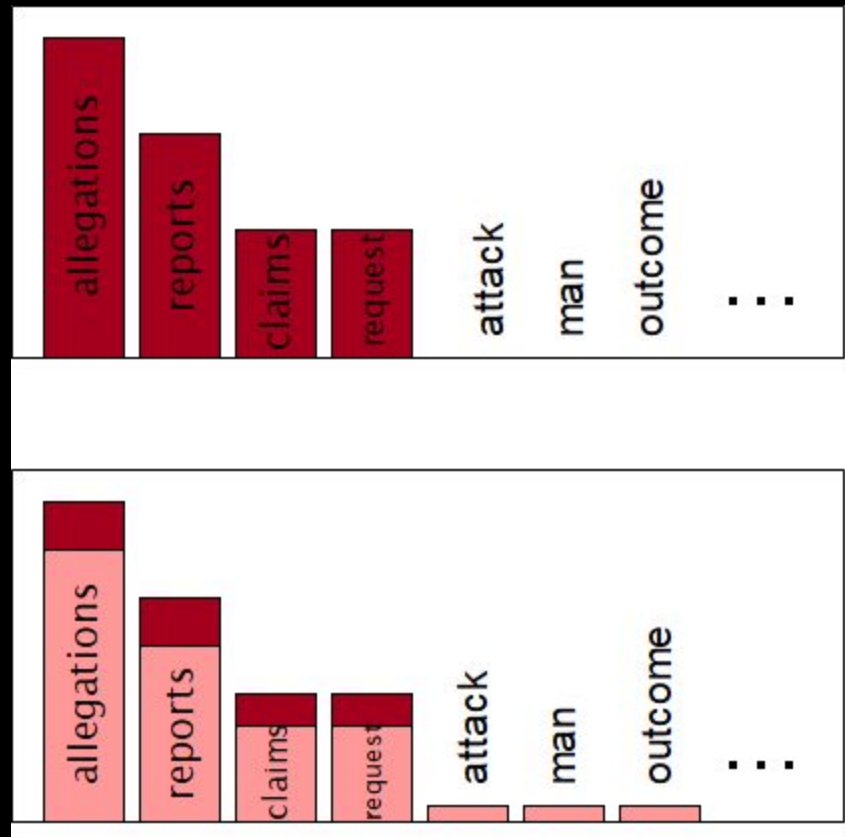
# Why Smoothing? Generalizes

Add-one is blunt:  
can lead to very large changes.

More Advanced:

Good-Turing Smoothing  
Kneser-Nay Smoothing

These are outside scope for now.  
We will eventually cover, even stronger,  
deep learning based models.



## Why Smoothing?

What about Logistic Regression?  $Y$  = next word  
 $P(Y|X) = P(X_n | X_{n-1}, X_{n-2}, X_{n-3}, \dots)$

Not a terrible option, but  $X_{n-1}$  through  $X_{n-k}$   
would be modeled as independent dimensions.  
Let's revisit later.

## Why Smoothing?

What about Logistic Regression?  $Y$  = next word  
 $P(Y|X) = P(X_n | X_{n-1}, X_{n-2}, X_{n-3}, \dots)$

Not a terrible option, but  $X_{n-1}$  through  $X_{n-k}$  would be modeled as independent dimensions.

Let's revisit later. Could use:

$P(X_n | X_{n-1}, [X_{n-1} X_{n-2}], [X_{n-1} X_{n-2} X_{n-3}], \dots)$



# Example how to produce language generator

1. Count unigrams, bigrams, and trigrams
2. Train probabilities for unigram, bigram, and trigram models (over training)
  - a. with smoothing
  - b. without smoothing
3. Generate language: Given previous word or previous 2 words, take a random draw from what words are most likely to be next.

Trigram model when good evidence (high counts)

Backing off to bigram or even unigram

Limitation: Long distance dependencies

*The horse which was raced past the barn tripped .*

# Language Modeling Summary

- Two versions of assigning probability to sequence of words
- Applications
- The Chain Rule, The Markov Assumption:  $P(X_1, X_2, \dots, X_n) = \prod_{i=1}^n P(X_i | X_{i-k}, X_{i-(k-1)}, \dots, X_i)$
- Training a unigram, bigram, trigram model based on counts
- Evaluation: Perplexity
- Zeros, Low Counts, and Generalizability
- Add-one smoothing