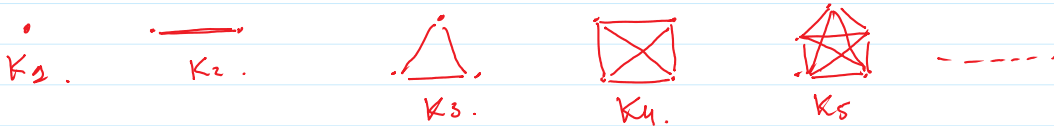


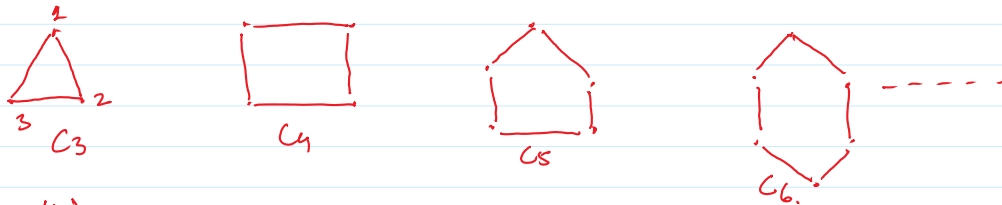
# Lecture 22:- Graphs.

## Special types of Simple Graphs.

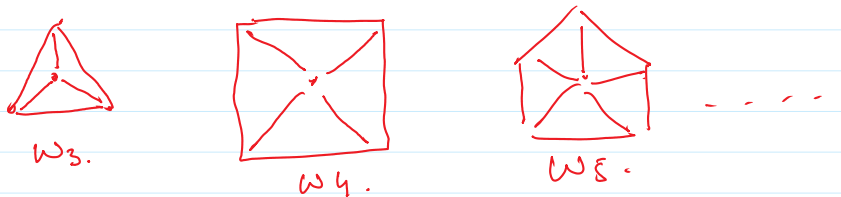
1- Complete Graphs:- Exactly one edge btw every pair of vertices.  $K_1, K_2, K_3, \dots, K_n$ .



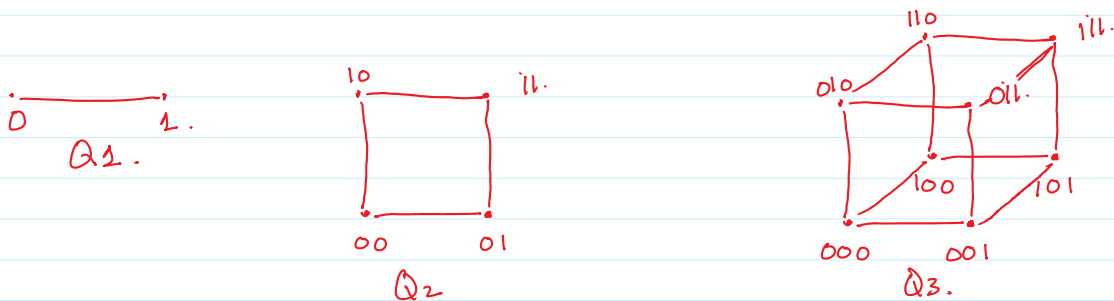
2- Cycles:-  $C_n$ .  $n \geq 3$ .  $1, 2, 3, \dots, n$ .  
Such that  $\{1, 2\}, \{2, 3\}, \{3, 4\}, \dots, \{n-1, n\}, \{n, 1\}$ .



3- Wheels:-  $W_n$ . A vertex in the center of a  $C_n$  which is connected to all.



4. Cuboid:-  $Q_1, Q_2, Q_3$ . Vertices.  
 $2^1 = 2$ .  
 $2^2 = 4$ .  
 $2^3 = 8$ .



$K_1, K_2, K_3, K_4, K_5, K_6, \dots, K_n$ .  
Vertices.  $\rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 5 \rightarrow 6 \rightarrow \dots \rightarrow n$ .

Edges . 0      1      3      6      10      15       $\frac{n(n-1)}{2}$

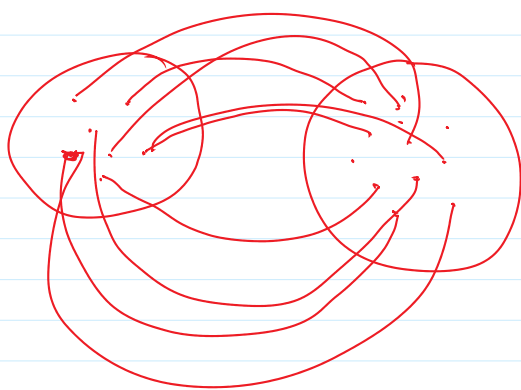
Vertices .  $C_3$        $C_4$        $C_5$        $C_6$       ----       $C_n$   
 3      4      5      6      ---      n  
 Edges . 3      4      5      6      ----      n .

Vertices .  $W_3$        $W_4$        $W_5$        $W_6$       ----       $W_n$   
 4      5      6      7      ----      n+1 .  
 Edges . 6      8      10      12      ----      2n

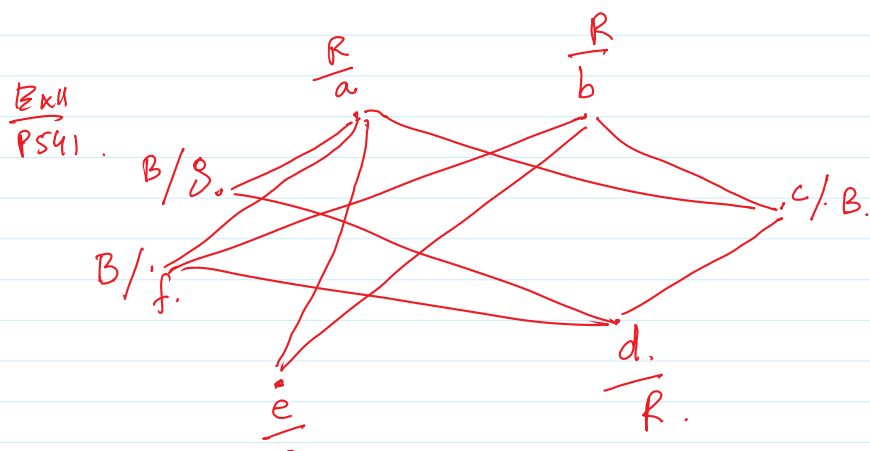
Vertices .  $Q_1$        $Q_2$        $Q_3$       - - -       $Q_n$   
 2      4      8            $2^n$   
 Edges . 1      4      12           #W?

Bipartite Graph:-

$V = \{V_1, \dots, V_n\}$   
 $E = \{e_1, e_2, \dots, e_m\}$



← No Internal Edge. within a Group.



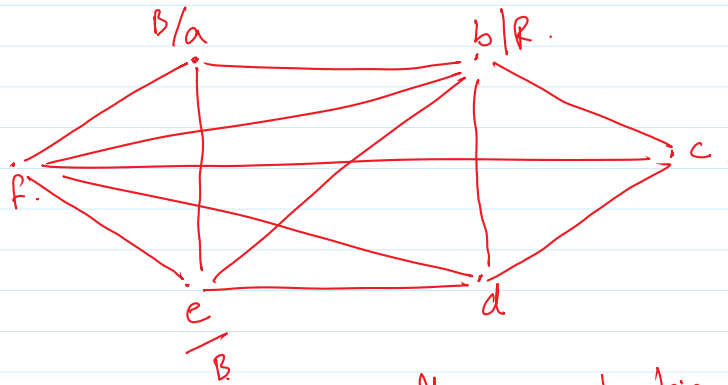
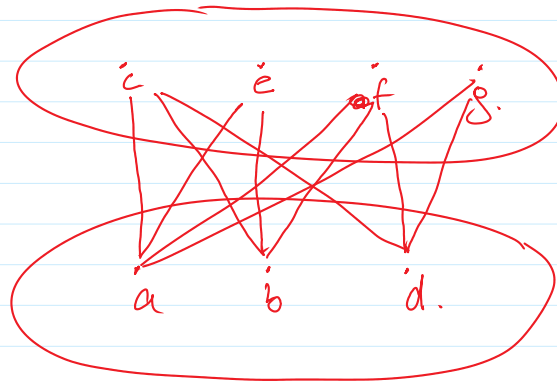
$R = \{a, b, d\}$

$B = \{c, e, f, g\}$

$$\frac{e}{B}$$

$$\frac{f}{R}$$

$$B = \{c, e, f, g\}$$



$$R = \{a\}$$

$$B = \{b, c, e\}$$

$$R = \{b\}$$

$$B = \{a, c, e\}$$

It is not bipartite.

Complete Bipartite Graph:-

$K_{m,n}$

from which we can find pictures.



