

HW7

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Problem 1

a)

```
if(!require("pacman")) install.packages("pacman")
```

```
## Loading required package: pacman
```

```
p_load(glmnet, penalized)

data <- ChickWeight
data$weight_group[ChickWeight$weight > 240] <- 1
data$weight_group[ChickWeight$weight <= 240] <- 0

day21 <- subset(data[which(data$Time == 21) ,])
day21 <- rbind(subset(day21[which(day21$Diet == 1),]), subset(day21[which(day21$Diet == 4),]))
day21$diet_group[day21$Diet == 1] <- 0
day21$diet_group[day21$Diet == 4] <- 1
fit <- glm(weight_group ~ diet_group, family = "binomial", data=day21)
summary(fit)
```

```
##
## Call:
## glm(formula = weight_group ~ diet_group, family = "binomial",
##      data = day21)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -0.9005  -0.5168  -0.5168  -0.5168   2.0393
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)  -1.9459     0.7559  -2.574   0.010 *
## diet_group    1.2528     1.0351   1.210   0.226
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 25.020  on 24  degrees of freedom
## Residual deviance: 23.514  on 23  degrees of freedom
## AIC: 27.514
##
## Number of Fisher Scoring iterations: 4
```

From the result, we could see that we have our logistic model as $\text{Logit} = -1.9459 + 1.2528 * \text{Diet_group}$. β_0 denotes the log odds ratio of $\text{Weight} > 240$ for Diet Group 1, the odds ratio of $\text{Weight} > 240$ for group 1 is $\exp(-1.9459)$. β_1 denotes the log odds ratio of $\text{weight} > 240$ for diet group 4 relative to the group 1. The odds ratio of $\text{weight} > 240$ for group 4 is $\exp(1.2528)$. The odds ratio of $\text{weight} > 240$ for group 1 is $\exp(-1.9459 + 1.2528)$.
 # Since p values are both larger than 0.05, we do not reject the null and we conclude there is no significance association between group 1 and group 4.

b)

```
BirthWeight<-subset(data,select=c(weight,Chick),Time==0)
names(BirthWeight)[names(BirthWeight)=="weight"]<-"BirthWeight"
dayadjust<-merge(day21,BirthWeight,by.y = "Chick")

fitadjust <- glm(weight_group ~ diet_group + BirthWeight, "binomial", dayadjust)
summary(dayadjust)
```

```
##      Chick      weight      Time      Diet      weight_group
## 13      : 1   Min.    : 96.0   Min.    :21   1:16   Min.    :0.0
## 9       : 1   1st Qu.:157.0  1st Qu.:21   2: 0   1st Qu.:0.0
## 20      : 1   Median :204.0  Median :21   3: 0   Median :0.0
## 10      : 1   Mean    :199.6  Mean    :21   4: 9   Mean    :0.2
## 17      : 1   3rd Qu.:237.0  3rd Qu.:21           3rd Qu.:0.0
## 19      : 1   Max.    :322.0  Max.    :21           Max.    :1.0
## (Other):19
##      diet_group      BirthWeight
## Min.    :0.00   Min.    :39.00
## 1st Qu.:0.00   1st Qu.:41.00
## Median :0.00   Median :41.00
## Mean    :0.36   Mean    :41.32
## 3rd Qu.:1.00   3rd Qu.:42.00
## Max.    :1.00   Max.    :43.00
##
```

From the result, we could see that we have our logistic model as $y = 21.836 + 0.9053 * \text{Diet_group} - 0.5743 * \text{BirthWeight}$. β_0 denotes the log odds ratio of $\text{Weight} > 240$ for Diet Group 1, the odds ratio of $\text{Weight} > 240$ for group 1 is $\exp(21.836 - 0.5743 * \text{BirthWeight})$. β_1 denotes the log odds ratio of $\text{weight} > 240$ for diet group 4 relative to the group 1. The odds ratio of $\text{weight} > 240$ for group 4 is $\exp(21.836 + 0.9053 - 0.5743 * \text{BirthWeight})$.
 # Since p values are both larger than 0.05, we do not reject the null and we conclude there is no significance association between group 1 and group 4 with adjusting for BirthWeight.

Problem 2

a)

```

dayall <- subset(data[which(data$Time == 21) ,])
dayall$Group1 <- rep(0,dim(dayall)[1])
dayall$Group1[dayall$Diet==1] <- 1
dayall$Group2 <- rep(0,dim(dayall)[1])
dayall$Group2[dayall$Diet==2] <- 1
dayall$Group3 <- rep(0,dim(dayall)[1])
dayall$Group3[dayall$Diet==3] <- 1
fitall <- glm(weight_group ~ Group1 + Group2 + Group3, "binomial", dayall)
summary(fitall)

```

```

##
## Call:
## glm(formula = weight_group ~ Group1 + Group2 + Group3, family = "binomial",
##      data = dayall)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -1.5518  -0.9005  -0.5168   0.8446   2.0393
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)  -0.6931     0.7071  -0.980   0.327
## Group1       -1.2528     1.0351  -1.210   0.226
## Group2        0.2877     0.9574   0.300   0.764
## Group3        1.5404     0.9880   1.559   0.119
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 58.574  on 44  degrees of freedom
## Residual deviance: 49.191  on 41  degrees of freedom
## AIC: 57.191
##
## Number of Fisher Scoring iterations: 4

```

From the result, we could see that we have our Logistic model as $y = -0.6931 - 1.2528 * \text{Group1} + 0.2877 * \text{Group2} + 1.5404 * \text{Group3}$. β_0 denotes the log odds ratio of Weight > 240 for Diet Group 4, the odds ratio of Weight > 240 for group 4 is $\exp(-0.6931)$. β_1 denotes the log odds ratio of weight > 240 for diet group 1 relative to the group 4. The odds ratio of weight > 240 for group 1 is $\exp(-0.6931-1.2528)$. β_2 denotes the log odds ratio of weight > 240 for diet group 2 relative to the group 4. The odds ratio of weight > 240 for group 2 is $\exp(-0.6931+0.2877)$. β_3 denotes the log odds ratio of weight > 240 for diet group 3 relative to the group 4. The odds ratio of weight > 240 for group 3 is $\exp(-0.6931+1.5404)$.

Since p values are both larger than 0.05, we do not reject the null and we conclude there is no significance association between group 1, group 2, group 3 and group 4 without adjusting for BirthWeight.

b)

```
dayalladj <- merge(dayall,BirthWeight,by.y = "Chick")
fitadjall <- glm(weight_group ~ Group1+Group2+Group3+BirthWeight,family="binomial",data=dayalladj)
summary(fitadjall)
```

```
##
## Call:
## glm(formula = weight_group ~ Group1 + Group2 + Group3 + BirthWeight,
##      family = "binomial", data = dayalladj)
##
## Deviance Residuals:
##      Min        1Q    Median        3Q        Max
## -1.5672   -0.8997   -0.5148    0.8459    2.0348
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)   0.08183   12.88220   0.006   0.995
## Group1       -1.24004    1.05632  -1.174   0.240
## Group2        0.28409    0.95936   0.296   0.767
## Group3        1.53889    0.98834   1.557   0.119
## BirthWeight  -0.01895    0.31463  -0.060   0.952
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 58.574  on 44  degrees of freedom
## Residual deviance: 49.188  on 40  degrees of freedom
## AIC: 59.188
##
## Number of Fisher Scoring iterations: 4
```

*# From the result, we could see that we have our Logistic model as $y = 0.08183 - 1.2404 * \text{Group1} + 0.28409 * \text{Group2} + 1.53889 * \text{Group3} - 0.01895 * \text{BirthWeight}$. β_0 denotes the log odds ratio of $\text{Weight} > 240$ for Diet Group 4, the odds ratio of $\text{Weight} > 240$ for group 4 is $\exp(0.08183 - 0.01895 * \text{BirthWeight})$. β_1 denotes the log odds ratio of $\text{weight} > 240$ for diet group 1 relative to the group 4. The odds ratio of $\text{weight} > 240$ for group 1 is $\exp(0.08183 - 1.2404 - 0.01895 * \text{BirthWeight})$. β_2 denotes the log odds ratio of $\text{weight} > 240$ for diet group 2 relative to the group 4. The odds ratio of $\text{weight} > 240$ for group 2 is $\exp(0.08183 + 0.28409 - 0.01895 * \text{BirthWeight})$. β_3 denotes the log odds ratio of $\text{weight} > 240$ for diet group 3 relative to the group 4. The odds ratio of $\text{weight} > 240$ for group 3 is $\exp(0.08183 + 1.53889 - 0.01895 * \text{BirthWeight})$.*

Since p values are both larger than 0.05, we do not reject the null and we conclude there is no significance association between group 1, group 2, group 3 and group 4 with adjusting for Birthweight.

Problem 3

```
fitl1 <- optl1(dayadjust$weight_group, penalized = -as.matrix(dayadjust$diet_group), fold = 5, model = "logistic")
```

```
## lambda= 0.6684405    1 2 3 4 5 cvl= -16.22268
## lambda= 1.081559     1 2 3 4 5 cvl= -15.72875
## lambda= 1.336881     1 2 3 4 5 cvl= -15.43013
## lambda= 1.494678     1 2 3 4 5 cvl= -15.25894
## lambda= 1.592203     1 2 3 4 5 cvl= -15.15735
## lambda= 1.652476     1 2 3 4 5 cvl= -15.09609
## lambda= 1.689727     1 2 3 4 5 cvl= -15.05879
## lambda= 1.712749     1 2 3 4 5 cvl= -15.03595
## lambda= 1.726978     1 2 3 4 5 cvl= -15.02191
## lambda= 1.735771     1 2 3 4 5 cvl= -15.01326
## lambda= 1.741206     1 2 3 4 5 cvl= -15.00793
## lambda= 1.744565     1 2 3 4 5 cvl= -15.00464
## lambda= 1.746641     1 2 3 4 5 cvl= -15.00261
## lambda= 1.747924     1 2 3 4 5 cvl= -15.00135
## lambda= 1.748717     1 2 3 4 5 cvl= -15.00058
## lambda= 1.749207     1 2 3 4 5 cvl= -15.0001
## lambda= 1.74951    1 2 3 4 5 cvl= -14.9998
## lambda= 1.749697    1 2 3 4 5 cvl= -14.99962
```

```
fitl1$fullfit
```

```
## Penalized logistic regression object
## 2 regression coefficients of which 1 are non-zero
##
## Loglikelihood =    -12.51006
## L1 penalty =  0   at lambda1 =  1.749697
```

```
fitl1_adj <- optL1(dayadjust$weight_group, penalized = -dayadjust$BirthWeight + as.matrix(dayadjust$diet_group), fold = 5, model = "logistic")
```

```
## lambda= 1.432373    1 2 3 4 5 cvl= -13.91647
## lambda= 2.317627    1 2 3 4 5 cvl= -13.81029
## lambda= 2.864745    1 2 3 4 5 cvl= -13.85336
## lambda= 2.30739    1 2 3 4 5 cvl= -13.81029
## lambda= 2.309537    1 2 3 4 5 cvl= -13.81029
## lambda= 2.309484    1 2 3 4 5 cvl= -13.81029
## lambda= 2.308463    1 2 3 4 5 cvl= -13.81029
## lambda= 2.309094    1 2 3 4 5 cvl= -13.81029
```

```
fitl1_adj$fullfit
```

```
## Penalized logistic regression object
## 2 regression coefficients
##
## Loglikelihood =    -11.74999
## L1 penalty =  0.5743996   at lambda1 =  2.309484
```