An RBC model with asset price

A represntative firm solves the following problem:

$$J(k;S) = \max_{k'} Ak^{\alpha} - k' + (1 - \delta)k + \mathbb{E}M(S, S')J(k'; S')$$

The household-side problem is as follows:

$$V(a;S) = \max_{c,a'} log(c) + \beta \mathbb{E}V(a';S')$$

s.t. $c + \int M(S,S')a'(S')d\Gamma_{S'} = a$

The stochastic discount factor M(S, S') is determined at the competitive market:

$$[M]: \quad a(S) = J(k(S); S)$$