An RBC model with asset price, irreversibility, and endogenous labor supply

A represntative firm solves the following problem:

$$J(k;S) = \max_{k',n} Ak^{\alpha} n^{1-\alpha} - w(S)n - k' + (1-\delta)k + \beta \mathbb{E}M(S,S')J(k';S')$$

s.t. $k' - (1-\delta)k \ge \phi I_{ss}$

where I_{ss} is the steady-state investment level.

The household-side problem is as follows:

$$V(a;S) = \max_{c,N,a'} log(c) - \frac{\eta}{1 + \frac{1}{\chi}} N^{1 + \frac{1}{\chi}} + \beta \mathbb{E}V(a';S')$$

s.t. $c + \int a'(S') d\Gamma_{S'} = a + w(S)N$

The stochastic discount factor $M(S,S^\prime)$ and wage w(S) are determined at the competitive market:

$$[M]: a(S) = J(k(S);S)$$

$$[w]: N(S) = n(S)$$