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- (a) We plan on using Zoom in order to use the share screen settings for use of the whiteboard and sharing notes/sources.
- (b) We will work on Friday and Sunday afternoons.
- (c) We will take turns drawing on the whiteboard and talk through the problems together.
- (d) When one person explains something, they will ask the other person if things made sense / if they have any questions. We will make sure that we are on the same page before moving forward with each problem or each step of a problem.
- (e) We will use Latex.

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Find a general solution to  $u_x + u = e^{2x+y}$ 

- 1. We will use the method of undetermined coefficients to find our general solution to this PDE. First, we need to find one particular solution to the inhomogenous PDE.
  - Our guess is  $U(x,y) = Ae^{2x+y}$ , and we need to discover A.
  - Then, we have  $2Ae^{2x+y} + Ae^{2x+y} = e^{2x+y}$  by differentiating our guess with respect to x and plugging our guess into  $u_x + u = e^{2x+y}$
  - $\bullet \implies 3Ae^{2x+y} = e^{2x+y}$
  - $\bullet \implies A = 1/3$
  - Therefore, one particular solution is  $U(x,y) = 1/3e^{2x+y}$
- 2. Now, we need to find a general solution in the form:  $u(x,y) = c_1u_1(x,y) + c_2u_2(x,y) + U(x,y)$ , where  $c_1$  and  $c_2$  are constants with respect to x,  $u_1$  and  $u_2$  are solutions to the associated homogenous PDE  $u_x + u = 0$ , and U(x,y) is a particular solution to the inhomogenous PDE. We used this source: Nonhomogenous Equations: Method of Undertermined Coefficients
  - First, we need to find the solutions  $u_1$  and  $u_2$  such that  $u_x + u = 0$ :

$$u_1(x, y) = f(y)e^{-x}$$
  
 $u_2(x, y) = e^{-x+g(y)}$ ,

where f(y) and g(y) are arbitrary functions.

3. Now, we can begin to write our general solution. We know that  $u(x,y) = c_1 f(y) e^{-x} + c_2 e^{-x+g(y)} + 1/3 e^{2x+y}$ 

- 4. However, we also know that  $c_1$  and  $c_2$  are constants with respect to x. So, we can represent them as arbitrary functions of y.
- 5. So, our general solution to this PDE is:  $u(x,y) = f(y)e^{-x} + h(y)e^{-x+g(y)} + 1/3e^{2x+y}$ , where f(y), g(y), and h(y) are arbitrary functions.