

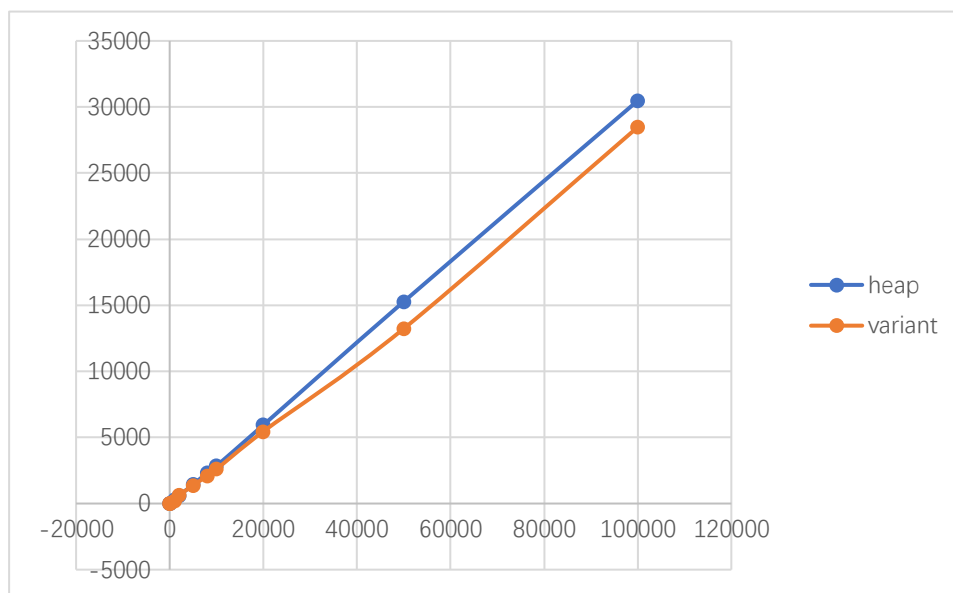
Below is the comparison of time execution between the original Heap Sort and its variant in different n sizes: 10, 100, 1000, 2000, 5000, 8000, 10000, 20000, 50000, 100000, 500000.

id	10		100		1000		2000		5000		8000		10000		20000		50000		100000		500000					
	heap	variant	heap	variant	heap	variant	heap	variant	heap	variant	heap	variant	heap	variant	heap	variant	heap	variant	heap	variant	heap	variant				
1	0	0	0	0	0	1001	0	0	999	1000	998	2000	2001	2996	1999	5999	6001	15001	13001	30002	26001	175013	148011			
2	0	0	0	0	0	998	0	1000	1000	1001	1001	4001	2000	3001	3000	4001	7001	16002	14999	30003	30003	185016	162554			
3	0	0	0	0	0	1008	0	1000	2999	2000	2999	2000	2000	2000	2000	5000	6003	13003	13003	29002	27001	27001	167403			
4	0	0	0	0	0	1000	0	1000	1001	992	2000	2000	2001	2000	2000	5002	4999	14001	12001	29001	36001	173019	153477			
5	0	0	0	0	0	0	1000	0	0	999	1001	2000	2001	2001	2999	3000	5001	17000	13001	29003	27002	180028	178400			
6	0	0	0	0	0	0	0	1000	1001	999	2001	1999	2001	2001	2001	5001	7001	13001	12000	29002	27002	168017	162012			
7	0	0	0	0	0	0	1000	1001	1001	1000	2002	1999	2000	2000	2000	5000	5000	13000	12000	29003	27003	170002	170002			
8	0	0	0	0	0	0	1001	0	1000	999	2000	3000	1999	2999	2001	5001	5003	18003	12000	29004	27001	168083	181012			
9	0	0	0	0	0	998	0	1000	0	1001	1001	2000	2000	3000	2003	5002	7000	14001	13001	32004	27002	179824	163811			
10	0	0	0	0	0	0	0	1000	999	999	2001	2000	3001	1999	8000	6001	16001	16999	31002	27001	180068	151183				
11	0	0	0	0	0	0	1000	1001	0	1002	1002	2002	2001	2002	2000	6001	6998	14001	12003	29002	27002	228529	178452			
12	0	0	0	0	0	1000	0	1000	2999	999	1000	2000	2000	2000	2000	5000	5000	12000	12000	29003	27003	178802	178802			
13	0	0	0	0	0	0	1002	0	0	998	2000	2998	3001	3000	2001	5000	5000	17001	19000	30000	27002	171566	150114			
14	0	0	0	0	0	999	0	1003	999	1999	3000	3000	2002	2000	8001	8002	14002	13001	30003	26002	170264	152306				
15	0	0	0	0	0	0	999	0	999	0	2002	2000	2000	2000	2998	2000	7000	6001	13001	29000	27002	172719	152284			
16	0	0	0	0	0	999	0	1001	0	1000	1001	2000	2000	1001	2001	6001	5001	17001	12001	29003	27003	185030	160535			
17	0	0	0	0	0	1001	0	998	2000	1000	1999	2000	3000	4002	5000	5000	14001	12002	29002	30483	171677	165956				
18	0	0	0	0	0	0	1000	0	1000	0	2001	1001	2001	2000	2000	2998	4999	5000	14003	13002	29006	31004	171345	151089		
19	0	0	0	0	0	1002	0	1000	1000	999	2000	2000	2000	3999	3001	8000	500	16002	16002	12001	46002	32000	175309	150976		
20	0	0	0	0	0	0	1000	1000	1000	1000	1001	2000	2000	3999	2000	5001	5001	21001	13002	29003	27003	27003	170190	150976		
21	0	0	0	0	0	0	1001	1001	1000	1001	1999	2001	2001	2001	5001	5996	14000	12509	30004	28004	169015	156504				
22	0	0	0	0	0	998	0	0	0	1000	1000	2000	2001	3001	2000	5001	7000	13000	13001	31519	27002	206192	151038			
23	0	0	0	0	0	0	0	0	1000	1001	1000	4001	2000	3001	2000	5227	5000	14001	12001	30003	32002	176429	168027			
24	0	0	0	0	0	0	1000	1000	1000	1000	4002	2000	1999	2000	5001	4001	14000	13002	30002	32000	177743	159584				
25	0	0	0	0	0	0	1000	1000	1001	1001	3001	2001	2000	2000	4002	5000	5000	14002	13000	30002	32000	177743	159584			
26	0	0	0	0	0	0	0	0	2003	1000	4002	1000	2000	2000	5000	9001	13998	12001	29004	27001	182016	159478				
27	0	0	0	0	0	0	0	1000	1000	1997	1000	1996	2000	2001	2000	8001	6001	13999	13000	29005	26999	192022	155737			
28	0	0	0	0	0	0	999	0	2000	1000	2000	2000	2004	3001	1999	6000	6999	14001	12510	29003	27001	173017	154525			
29	0	0	0	0	0	0	0	1000	1999	1000	1000	1000	1000	1000	5003	6003	14001	12000	29003	27003	178802	178802				
30	0	0	0	0	0	999	0	1001	0	1000	1000	1002	3001	3000	2998	2002	5001	15001	12000	30001	27002	181275	152195			
31	0	0	0	0	0	0	1001	0	1001	2001	2001	2986	2000	2999	2000	8503	5001	14001	11997	36001	27001	177805	152668			
32	0	0	0	0	0	0	0	0	0	1001	1999	1997	2004	2000	5004	2001	5001	7999	14002	13002	30000	47004	188111	158790		
33	0	0	0	0	0	1000	0	1000	999	1999	1999	1002	4999	1000	5000	5000	5000	15001	12003	29008	32770	185012	159581			
34	0	0	0	0	0	1000	1001	1000	1999	2000	1999	2000	1000	1000	3000	8001	8001	18003	13000	29003	30003	169661	158790			
35	0	0	0	0	0	0	0	0	0	1001	1002	2000	3001	3002	2997	3000	5999	8000	14001	13002	29998	27001	168578	170806		
36	0	0	0	0	0	0	0	1000	999	1001	2001	2002	3000	3001	3000	3001	5000	19002	12001	30002	27003	167459	154053			
37	0	0	0	0	0	0	1000	999	1000	1998	2000	1998	3001	2001	2000	5000	5002	14002	11999	30005	26002	166227	158885			
38	0	0	0	0	0	0	1000	999	2000	2000	1999	2001	2000	2001	4001	4001	4001	14000	12000	29001	29402	178802	178802			
39	0	0	0	0	0	0	1001	1000	0	1002	2000	2001	2000	3003	3999	3000	5001	15002	13001	32001	27002	195319	163016			
40	0	0	0	0	0	0	0	0	0	1001	2000	1002	1998	3000	3000	5001	8001	14002	13001	29002	26974	178308	189990			
41	0	0	0	0	0	0	1002	1001	0	999	999	2000	2001	2003	2001	5000	6000	14002	17001	30436	30004	172096	178317			
42	0	0	0	0	0	0	0	1000	1001	1000	1000	1000	1000	1000	1000	5000	4999	13000	11999	30002	263119	158790				
43	0	0	0	0	0	0	1001	0	999	1000	1000	999	2000	1999	2000	8002	4999	16001	16001	30002	33001	192063	154047			
44	0	0	0	0	0	999	0	1000	1001	1001	1001	2000	2003	2994	2003	5001	8001	14002	16001	29007	27003	169117	153430			
45	0	0	0	0	0	0	0	0	999	1999	1000	3001	1000	1002	1999	4999	4000	13002	21005	29002	27002	172109	156021			
46	0	0	0	0	0	0	0	1000	1000	2001	1000	1999	1000	1999	2002	9000	4001	14005	19999	29002	29002	197015	151544			
47	0	0	0	0	0	0	0	1000	2997	1000	1001	2000	2001	2001	2001	5002	5002	13000	11000	29002	27003	168482	158020			
48	0	0	0	0	0	0	1000	1000	0	3001	2000	2001	2000	2001	2001	7999	4001	14000	14999	33004	25998	196372	162950			
49	0	0	0	0	0	0	1000	1001	1999	2001	2000	998	2999	2000	6001	4999	15997	16001	45004	29001	170361	159016				
50	0	0	0	0	0	0	0	0	1001	1999	2000	1001	2001	2000	5001	5001	16004	12000	39000	28000	172017	156026				
51	0	0	0	0	0	0	1000	999	2000	2002	2000	2000	2000	2000	2000	5000	5000	17001	12000	30003	32003	174035	154035			
52	0	0	0	0	0	0	0	1000	2001	1000	2000	2000	2000	1999	5000	5001	17001	12003	29002	30847	174684	158099				
53	0	0	0	0	0	1000	0	1002	1000	998	999	2000	1000	4000	4000	5002	5000	14002	13000	30003	31003	171913	171952			
54	0	0	0	0	0	1001	0	0	1000	1000	2000	998	4000	4000	5001	7000	14001	13002	30001	33002	202519	156662				
55	0	0	0	0	0	0	0	1000	2005	2998	2000	2005	2999	2000	5000	5000	15001	12000	29003	32003	172281	158790				
56	0	0	0	0	0	1000	1000	1000	1000	1993	2000	1000	3000	1999	4000	7997	5000	14000	16001	29001	26002	174235	153037			
57	0	0	0	0	0	0	0	1001	2001	2001	1000	2000	2001	4005	5001	4000	16001	13001	30000	27001	176298	155545				
58	0	0	999	0	1004	0	0	998	2000	1001	3000	1997	2000	4997	5000	4002	15003	13001	30003	26004	172028	160203				
59	0</																									

In order to get a fair comparison, I recorded 100 times of each size of n and calculated the average.

n	heap	variant
10	0	0
100	20	9.77
1000	269.97	200.05
2000	590.06	610.08
5000	1439.98	1369.94
8000	2310.18	2090.22
10000	2841.7	2600.24
20000	5938.33	5450.52
50000	15271.03	13228.17
100000	30477.25	28478.1

Below is the graph showing relationship of these two algorithms.



As expected, since the variant algorithm is actually optimized based on the original Heap Sort by reducing some comparison tests in Max-Heapify, the time complexity of the original Heap Sort is higher than its variant. Although there is not much difference for small sizes of n, according to the graph even 20000, after the n gets bigger, the difference of two algorithm is shown. Also, the original Heap Sort is a upper bound time complexity of its variant.