

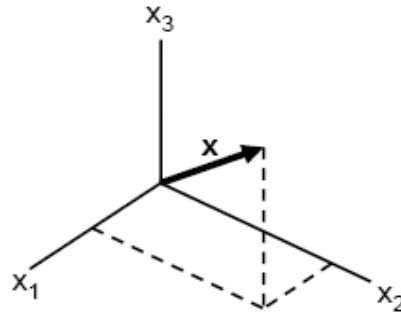
Feature Engineering

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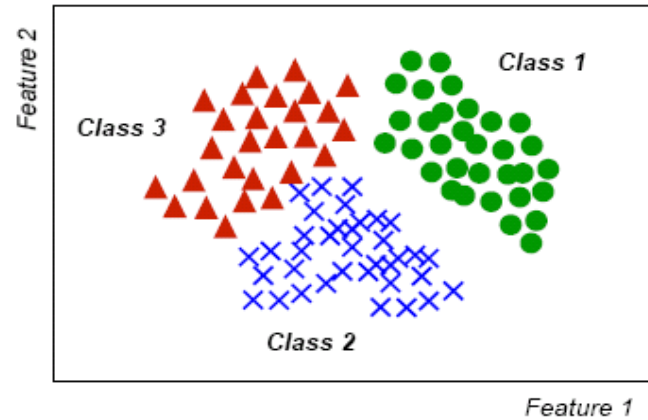
What is Feature ?

$$X = \begin{bmatrix} X_1 \\ X_2 \\ \vdots \\ X_d \end{bmatrix}$$

Feature vector

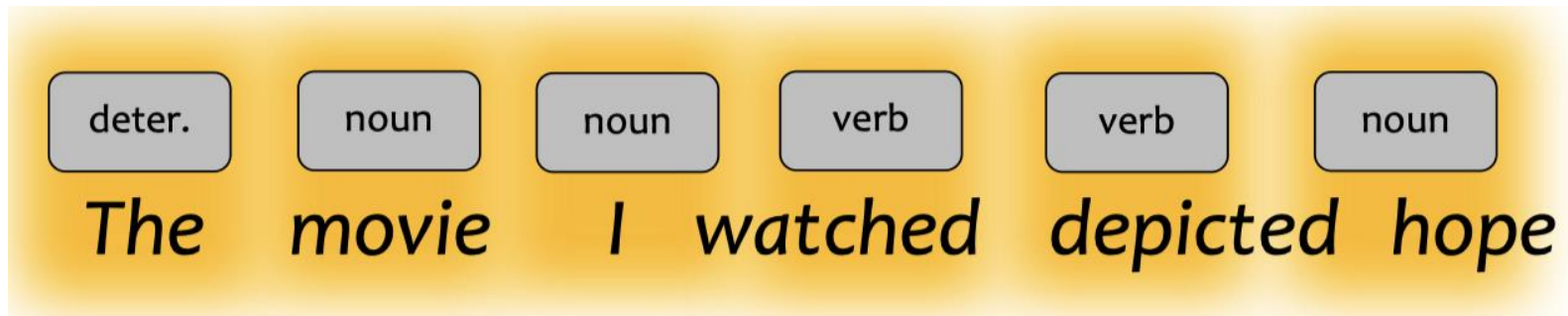


Feature space (3D)

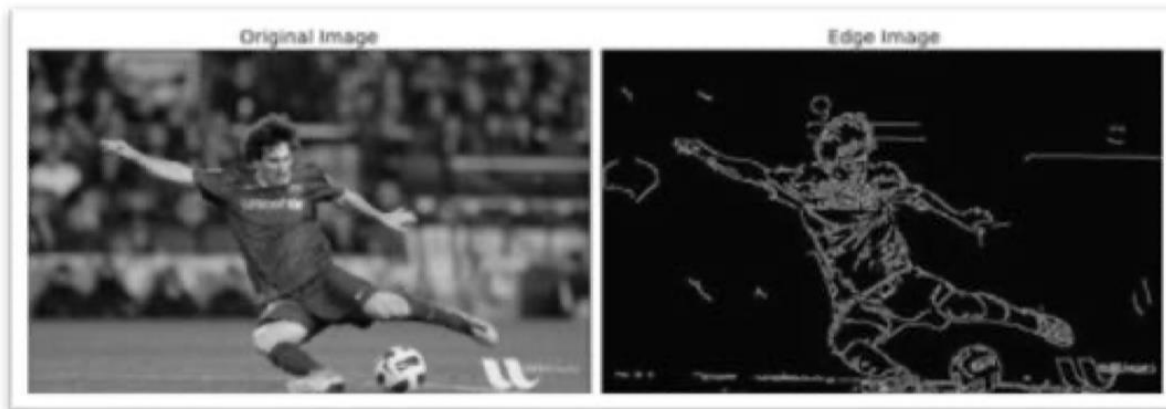


Scatter plot (2D)

Hand Crafted Features

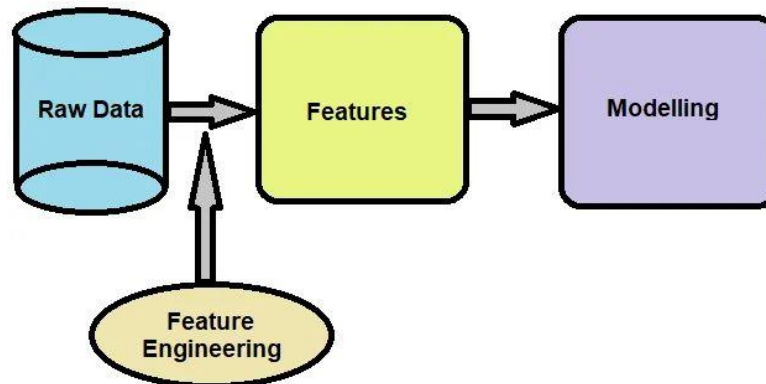


Edge detection (Canny)



What is Feature Engineering?

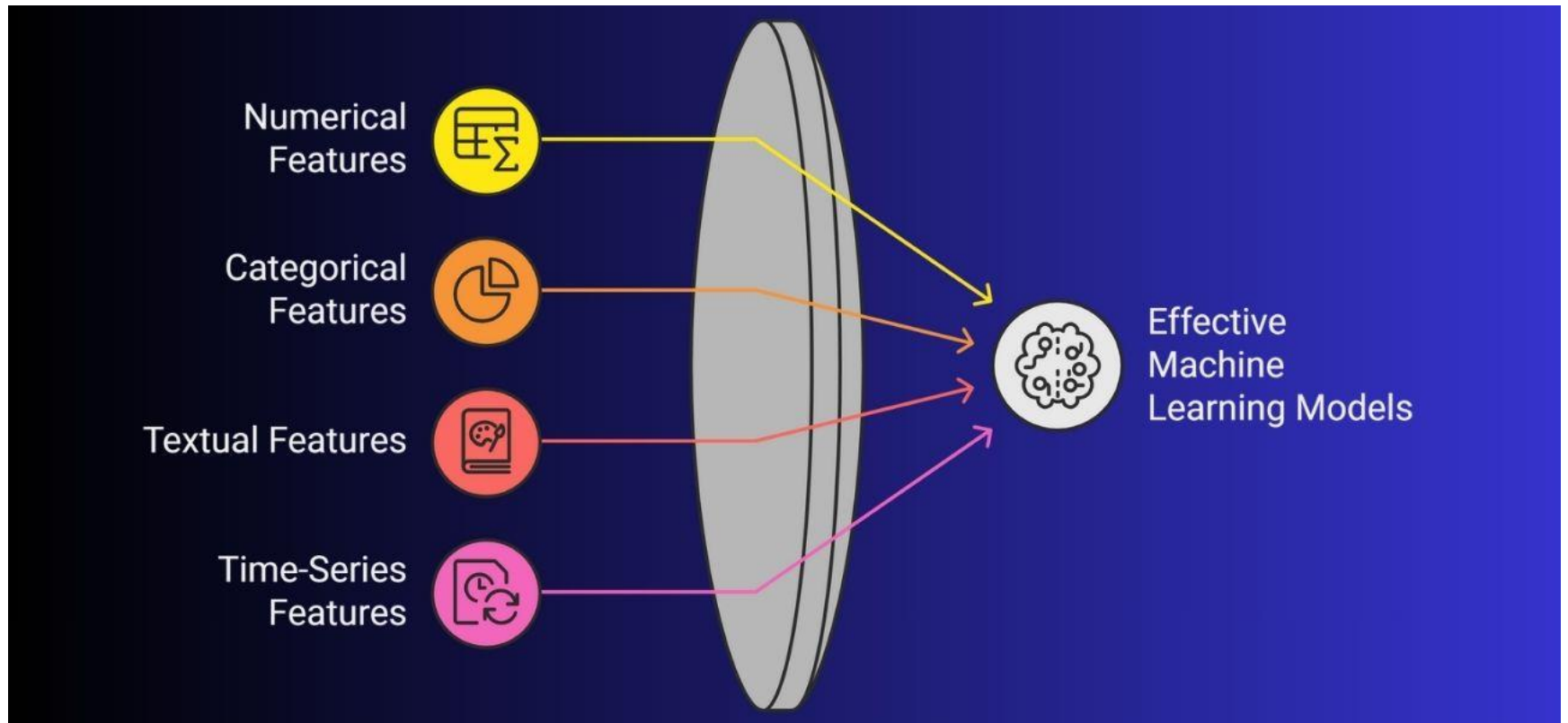
- Feature engineering is transforming **raw data** into **informative variables** (features)
- It is the process of creating, transforming, or selecting input variables (features) so that a machine learning model can learn patterns more easily and effectively



Why Feature Engineering ?

1. **Improves Accuracy:** It helps the model capture complex relationships that raw data might hide
2. **Enhances Interpretability:** Clear, meaningful features make it easier to understand how a model makes decisions.
3. **Reduces Overfitting:** Focusing on important features helps models generalize better to new, unseen data.
4. **Boosts Efficiency:** Using fewer but high-impact features speeds up model training and reduces computational cost.

Types of Features



Categorical Features

Categorical feature engineering converts text-based categories into meaningful numerical values using encoding methods like **one-hot**, **label**, and **target encoding**.

Label Encoding

| Food Name | Categorical # | Calories |
|-----------|---------------|----------|
| Apple | 1 | 95 |
| Chicken | 2 | 231 |
| Broccoli | 3 | 50 |



One Hot Encoding

| Apple | Chicken | Broccoli | Calories |
|-------|---------|----------|----------|
| 1 | 0 | 0 | 95 |
| 0 | 1 | 0 | 231 |
| 0 | 0 | 1 | 50 |

The problem with one-hot encoding is that it increases the dimensionality of the training data

Categorical Features

- Target Encoding:

- Each category is encoded by how the target behaves for that cate
 - X = categorical feature
 - y = target variable

For category c :

$$\text{TargetEncode}(c) = \mathbb{E}[y \mid X = c]$$

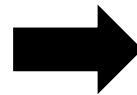
For binary classification:

$$\text{TargetEncode}(c) = P(y = 1 \mid X = c)$$

Categorical Features

- Target Encoding Example

| | Animal | Target | Encoded Animal |
|---|---------|--------|----------------|
| 0 | cat | 1 | 0.40 |
| 1 | hamster | 0 | 0.50 |
| 2 | cat | 0 | 0.40 |
| 3 | cat | 1 | 0.40 |
| 4 | dog | 1 | 0.67 |
| 5 | hamster | 1 | 0.50 |
| 6 | cat | 0 | 0.40 |
| 7 | dog | 1 | 0.67 |
| 8 | cat | 0 | 0.40 |
| 9 | dog | 0 | 0.67 |



| | Animal Group | Target 0 | Target 1 | Probability of 1 |
|---|--------------|----------|----------|------------------|
| 0 | cat | 3 | 2 | 0.40 |
| 1 | dog | 1 | 2 | 0.67 |
| 2 | hamster | 1 | 1 | 0.50 |

Textual Features

1. Bag of Words (BoW) Example :

- **Review 1:** This movie is very scary and long
- **Review 2:** This movie is not scary and is slow
- **Review 3:** This movie is spooky and good

| | 1 This | 2 movie | 3 is | 4 very | 5 scary | 6 and | 7 long | 8 not | 9 slow | 10 spooky | 11 good | Length of the review(in words) |
|-------------|-----------|------------|---------|-----------|------------|----------|-----------|----------|-----------|--------------|------------|--------------------------------------|
| Review 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 7 |
| Review 2 | 1 | 1 | 2 | 0 | 0 | 1 | 1 | 0 | 1 | 0 | 0 | 8 |
| Review 3 | 1 | 1 | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 1 | 6 |

Vector-of-Review1: [1 1 1 1 1 1 1 0 0 0 0]

Vector-of-Review2: [1 1 2 0 0 1 1 0 1 0 0]

Vector-of-Review3: [1 1 1 0 0 0 1 0 0 1 1]

Textual Features

1. Drawbacks of Bag of Words (BoW):

- If the new sentences contain new words, then our vocabulary size would increase and thereby, the length of the vectors would increase too.
- Additionally, the vectors would also contain many 0s, thereby resulting in a sparse matrix (which is what we would like to avoid)
- We are retaining no information on the grammar of the sentences nor on the ordering of the words in the text.

Textual Features

2. TF-IDF (Term Frequency — Inverse Document Frequency:

- Weights words by:
 - how frequent they are in the document
 - how rare they are across documents

$$TF = \frac{\text{Number of times a word "X" appears in a Document}}{\text{Number of words present in a Document}}$$

$$IDF = \log \left(\frac{\text{Number of Documents present in a Corpus}}{\text{Number of Documents where word "X" has appeared}} \right)$$

$$TF\ IDF = TF * IDF$$

Term Frequency : how often a term appears in a document

Inverse Document Frequency: how rare or unique the item is across the entire collection of document.

Textual Features

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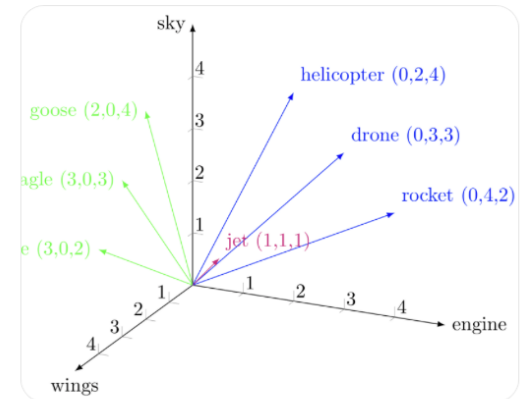
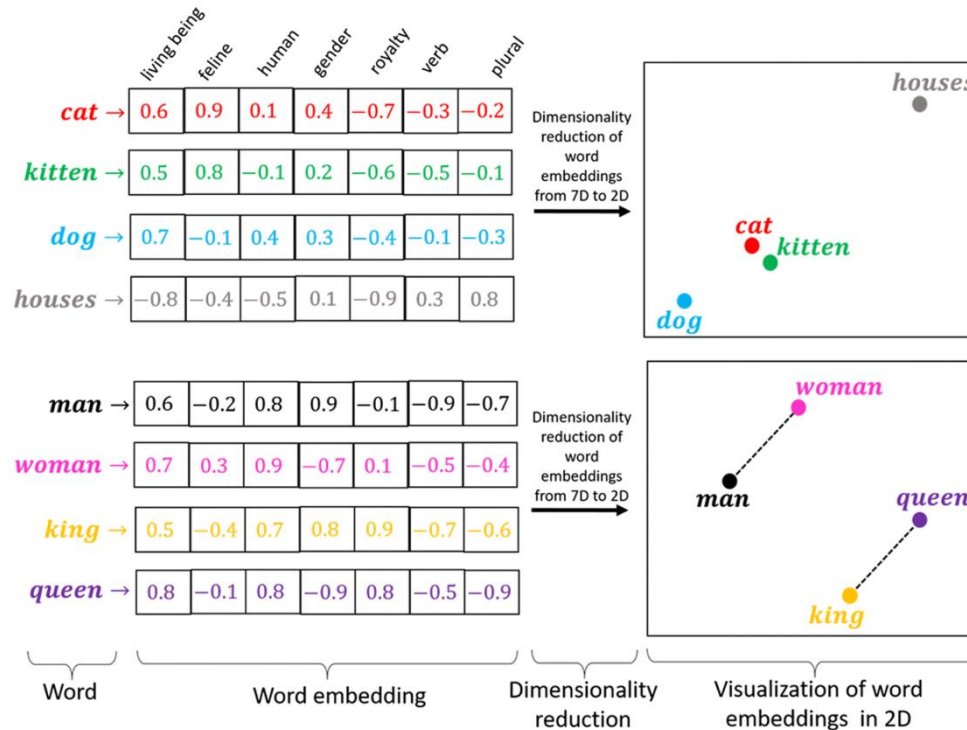
Textual Features

3. Word Embeddings (Dense semantic features)

- A word embedding is a learned representation for text where **words that have the same meaning have a similar representation**
- Words become points in a semantic space
- An embedding is a dense vector of floating point values (the length of the vector is a parameter you specify).
- Map each word to a **dense vector** where:
 - similar words → close vectors
 - meaning is encoded geometricall
- Instead of specifying the values for the embedding manually, they are trainable parameters (weights learned by the model during training, in the same way a model learns weights for a dense layer)

Textual Features

3. Word Embeddings (Dense semantic features)

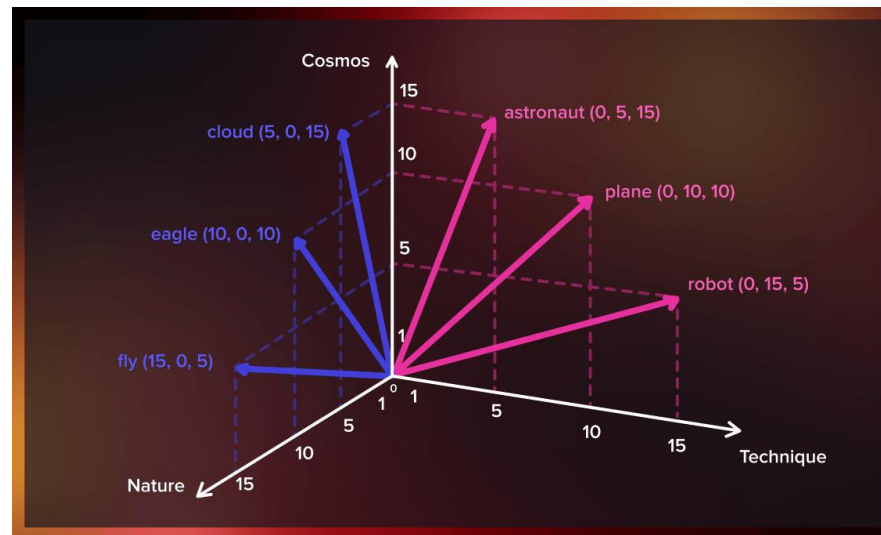


Textual Features

3. Word Embeddings (Dense semantic features)

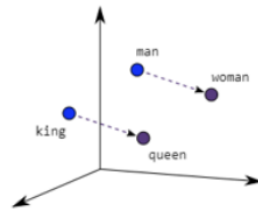
Word2Vec:

- Words that appear in similar contexts get similar vectors
- It is trained using a neural network that learns the relationships between words in large databases of texts
- It learns word embeddings by predicting surrounding words, turning context similarity into geometric similarity.
- Similar words have similar vectors



Textual Features

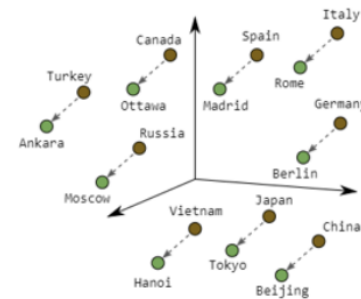
Word2Vec



Male-Female

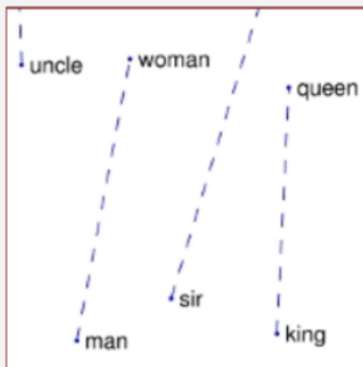


Verb Tense

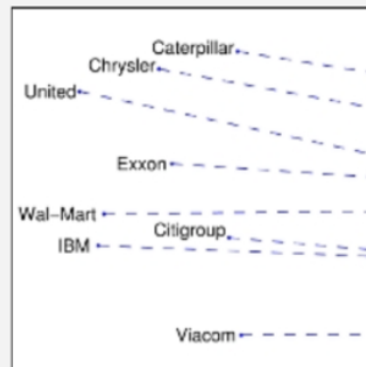


Country-Capital

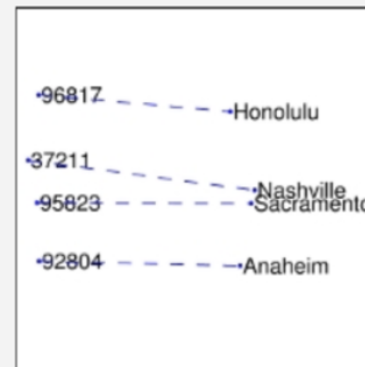
GloVe



man - woman



company - ceo



city - zip code



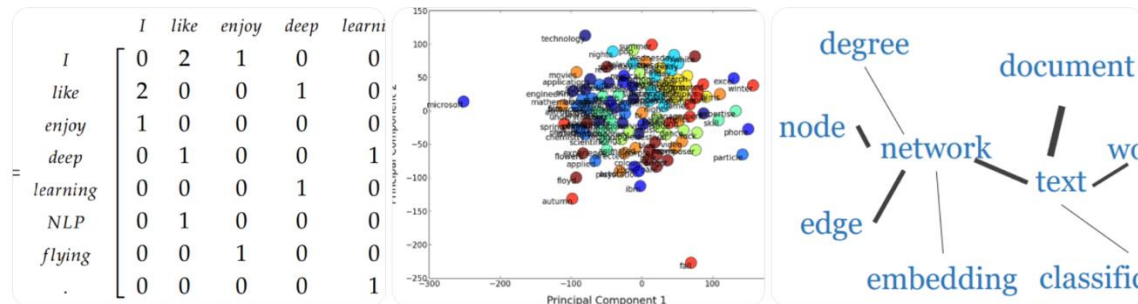
comparative - superlative

Textual Features

3. Word Embeddings (Dense semantic features)

GloVe (Global Vector for word Representation)

- learns word embeddings by using global word co-occurrence statistics from a corpus.
- Word meaning is encoded in ratios of co-occurrence probabilities (ice co-occurs more with snow).
- GloVe learns vectors with **self supervised regression**



X_{ij} number of times word j appears in the context of word i

Context is defined using sliding window and distance weighting

Applications of Word2Vec and GloVe

- text classification, similarity search,
- recommendation systems,
- Information retrieval
- Document clustering

Choose Word2Vec if:

- you train on your own corpus
- data is domain-specific
- memory is limited
- you want fast iteration

Choose GloVe if:

- you use pretrained embeddings
- you want strong semantic regularities
- corpus is static and large

Time Series Features

Time series features are numerical descriptors extracted from sequential temporal data

1. Statistical Features:

- **Ignores time order**, summarize **value distribution**.
- Useful when magnitude matters more than shape
- Applications: medicine(heart rate variability), finance(high variance shows unstable system behavior)
- Features: **mean, median, variance, standard deviation, kurtosis etc.**
- Not enough for: long term dependencies, forecasting future values, phase and ordering is critical
- Can't use for: speech recognition, language modelling, gesture recognition

Time Series Features

2. Frequency Domain Features:

- when the periodic, oscillatory, or rhythmic structure of a time series is more informative than its raw time evolution
 - **Example:** EEG/ECG rhythms, machinery vibrations
- Frequencies have direct physical meaning
 - **Example:** motor speed, brain rhythms(alfa-beta bands
- A long time series signal may be described by few dominant frequencies
- Classes that overlap in time domain may be well separated in frequency domain
 - **Example:** healthy vs faulty motor: same mean, different vibration freq.
- Features: **dominant frequency, spectral centroid, frequency variance etc.**
- Not good for: exact timing, non-periodic events, short signals without cycles

Time Series Features

3. Autocorrelation Based Features:

- quantify how much a time series is related to its own past values
- Measures temporal dependencies
 - **Example:** EEG/ECG rhythms, machinery vibrations
- Frequencies have direct physical meaning
 - **Example:** motor speed, brain rhythms(alfa-beta bands
- A long time series signal may be described by few dominant frequencies
- Classes that overlap in time domain may be well separated in frequency domain
 - **Example:** healthy vs faulty motor: same mean, different vibration freq.
- Features: **dominant frequency, spectral centroid, frequency variance etc.**
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Traditional Feature Engineering



Traditional Feature Engineering

- **Data Cleaning:** Fix missing values, remove duplicates, and correct errors to ensure clean, reliable data for machine learning.
- **Data Transformation:** Scale, normalize, and encode raw data so models can easily understand and process different feature types.
- **Feature Extraction:** Create new, meaningful features by deriving or combining information from existing data to boost model learning.
- **Feature Selection:** Choose the most important features using correlation, mutual information, or model-based methods to reduce noise and overfitting.
- **Feature Iteration:** Continuously test and refine features by adding, removing, or adjusting them based on model performance improvements.

Traditional Feature Engineering Examples

Customer Churn Prediction (Telecom)

Feature engineering helps predict which customers may leave a telecom service. Useful features include monthly usage trends, call drops, complaint history, payment delays, contract type, and recent plan changes.

Fraud Detection (Banking & Payments)

Banks use feature engineering to identify suspicious transactions. Key features include transaction frequency, amount spikes, device location mismatches, login patterns, merchant risk scores, and spending behavior anomalies.

Healthcare Risk Prediction (Claims/Hospitalization)

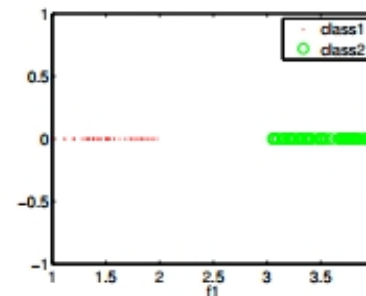
In healthcare ML models, engineered features include patient history, claim patterns, medication usage, diagnosis codes, recurring visits, vitals trends, and time since last consultation to predict hospitalization risks.

Retail & E-commerce Personalization

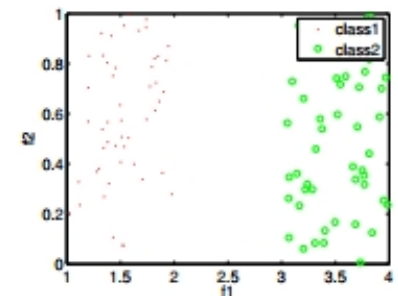
E-commerce platforms engineer features like browsing behavior, purchase frequency, cart activity, discount usage, product categories viewed, session duration, and seasonal trends to power personalized recommendations.

Why are not all features used?

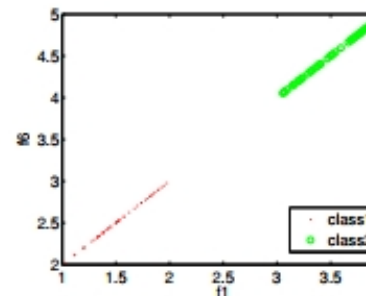
- f1: separate two classes
- f2: can't separate
- f4: noisy feature
- f6: f1 correlated feature



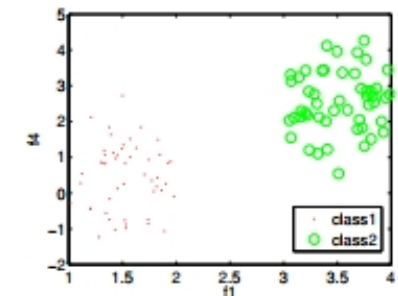
(a) relevant feature



(b) irrelevant feature



(c) redundant feature

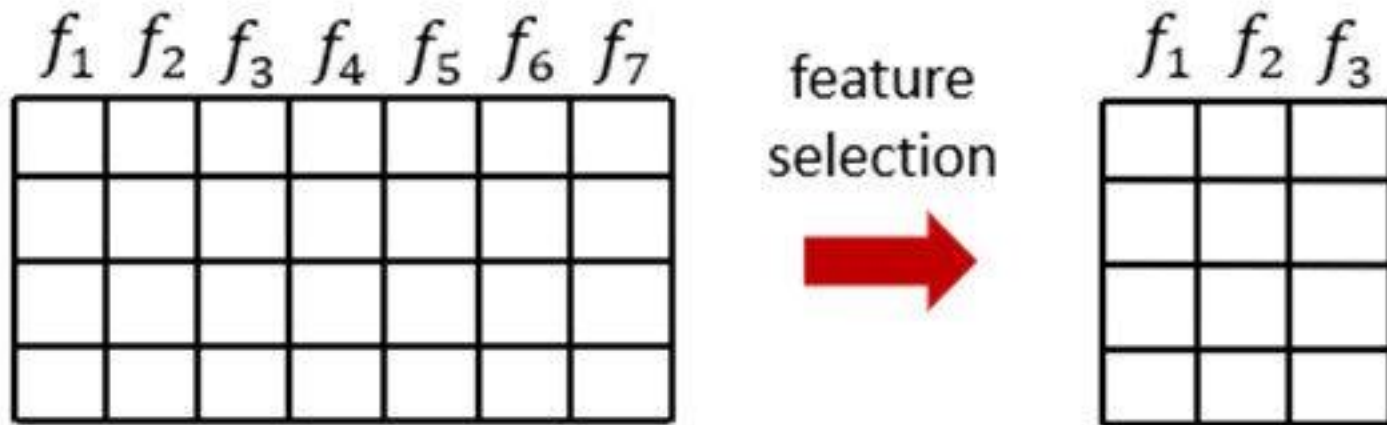


(d) noisy feature

Dimensionality Reduction

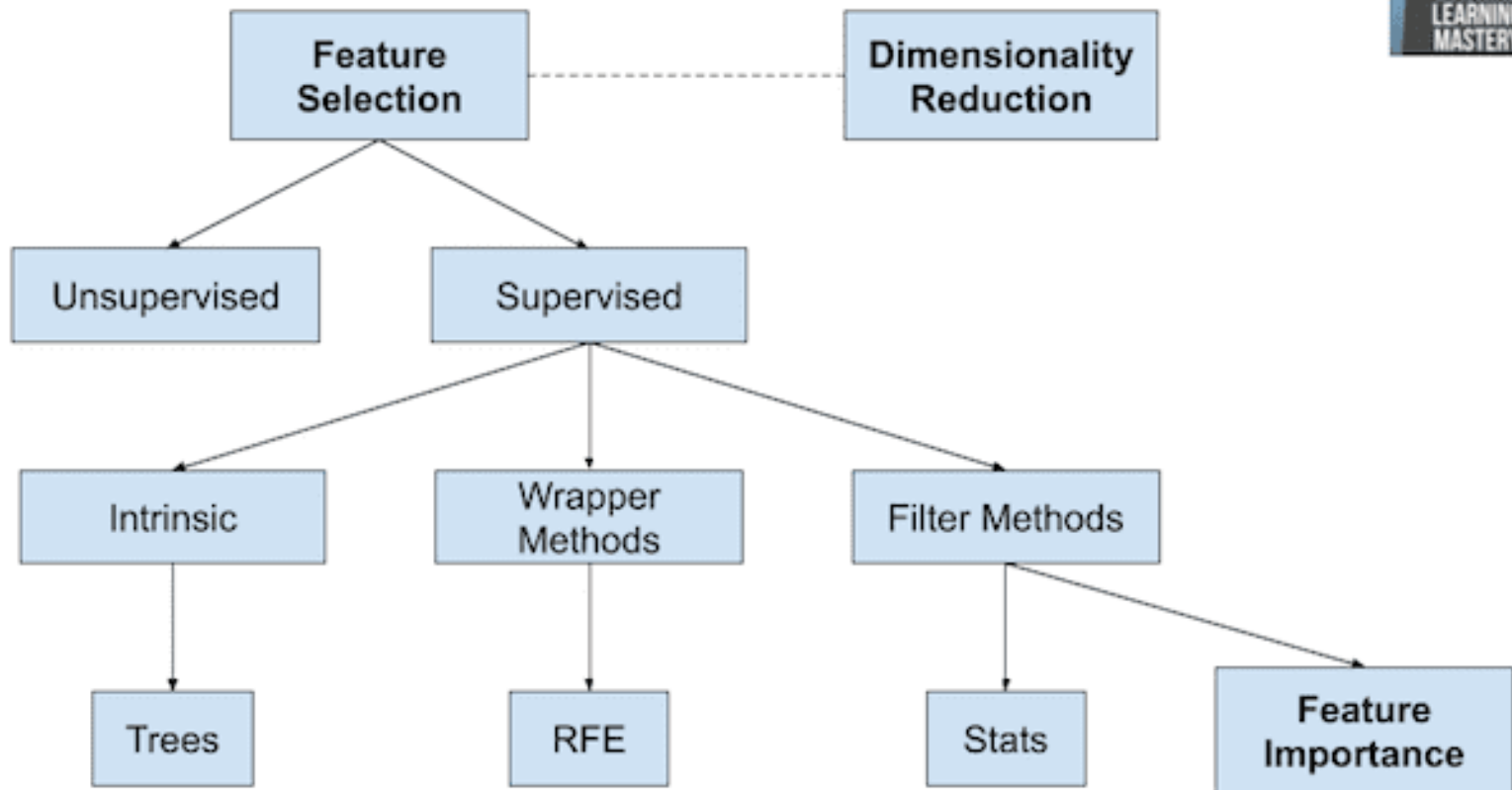
- **Feature Selection:** Selects characteristic features from all features
- **Feature Extraction:** Produce new features from all features

Feature Selection



Feature Selection

Overview of Feature Selection Techniques



Traditional Feature Selection Methods

- **Supervised Feature Selection**

- **Filter Based:** select features **before** model training by using **statistical properties of the data**, *independent of any specific learning algorithm*.
- **Wrapper Based:** evaluate subsets of features by training a machine learning model and measure its performance
- **Embedded:** Özellik çıkarma öğrenme modeli tarafından yapılır.

Filter Based Feature Selection

Each feature x_j is scored using a criterion:

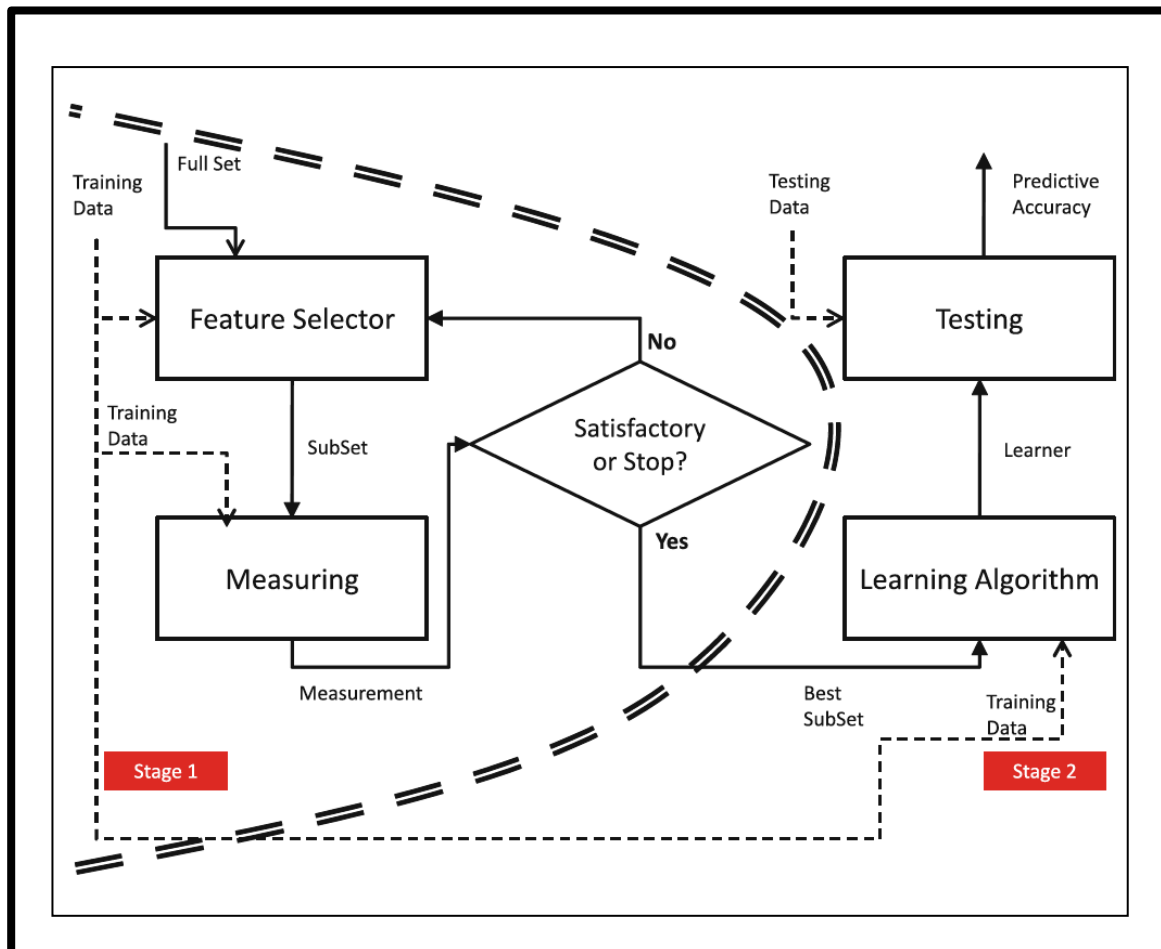
$$\text{Score}(x_j, y)$$

Then:

- Rank features
- Select top- k or those above a threshold

Filter Based Feature Selection

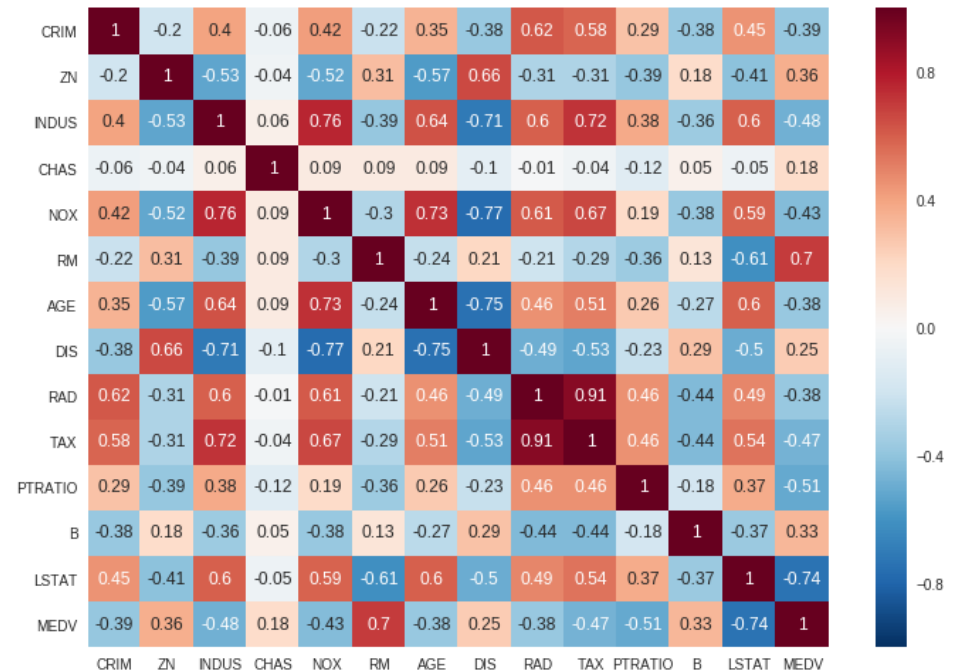
Set of all Features → **Selecting the Best Subset** → **Learning Algorithm** → **Performance**



Filter Based Feature Selection

- Correlation based:

$$\rho(x, y) = \frac{\text{cov}(x, y)}{\sigma_x \sigma_y}$$



Variance

- **Population Variance:** Bir veri kümesindeki her örneğin **ortalamadan ne kadar uzak olduğunu gösterir.**
- **Sample Variance:** Veri kümesinin tamamı için hesap yapmak mümkün olmadığında seçilen bir grup üzerinde varyans hesaplandığı için (değer çok küçük olmasın diye $(n-1)$ 'e bölünür.

$$\text{Population Variance: } \text{Var}(x) = \frac{\sum_{i=1}^N (X_i - \mu)^2}{N}$$

$$\text{Sample Variance: } \text{Var}(x) = \frac{\sum_{i=1}^n (X_i - \bar{x})^2}{n-1}$$

- **Standart Sapma:** Çoğunluğun durumunu gösterir. Örneğin bir gruptaki kişilerin ağırlık ortalaması 75 ve standart sapma 20 kg ise, insanların çoğunluğu 55 kg ile 95kg arasındadır.

Varyans ve Kovaryans

- **Varyans büyükse** örnekler birbirlerinden ve ortalamadan uzak demektir.

$$\sigma^2 = \frac{\sum (x - \mu)^2}{N}$$

- Kovaryans : İki değişkenin birbirleri ile ilişkisini gösterir. Negatif ve pozitif değer alabilir. Pozitif kovaryans iki değişkenin aynı yönde birlikte değiştiğini gösterir.

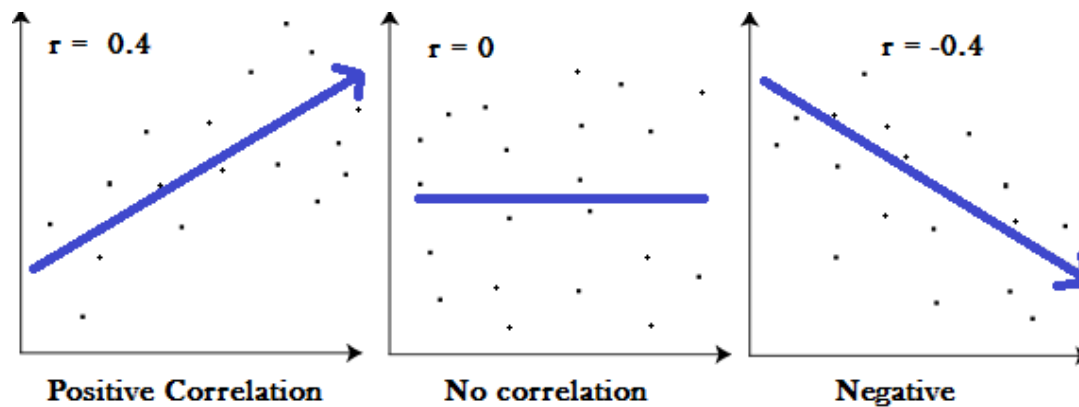
$$\text{Population Covariance: Cov}(x, y) = \frac{\sum_{i=1}^N (X_i - \mu_x)(Y_i - \mu_Y)}{N}$$

$$\text{Sample Covariance: Cov}(x, y) = \frac{\sum_{i=1}^N (X_i - \bar{x})(Y_i - \bar{y})}{n - 1}$$

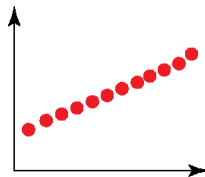
Korelasyon Nedir?

- Korelasyon iki değişken arasındaki ilişkinin kuvveti ve yönüdür. Korelasyon katsayısı bu ilişkinin $[-1,+1]$ arasındaki ölçüm sonucudur.

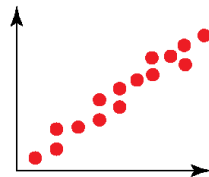
$$\text{Correlation} = \frac{\text{Cov}(x, y)}{\sigma_x * \sigma_y}$$



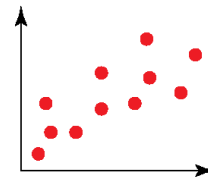
Korelasyon Nedir?



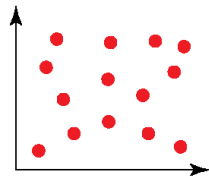
Perfect
Positive
Correlation



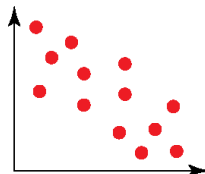
Strong
Positive
Correlation



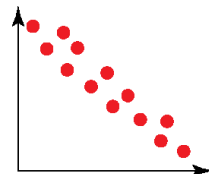
Weak
Positive
Correlation



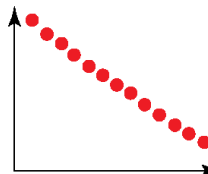
No
Correlation



Weak
Negative
Correlation



Strong
Negative
Correlation



Perfect
Negative
Correlation

Filter Based Feature Selection

- **Chi-square test:** Are two categorical variables independent?
- If a feature is useful, its values should appear unevenly across classes

$$\chi^2 = \frac{(\text{Observed frequency} - \text{Expected frequency})^2}{\text{Expected frequency}}$$

- Observed frequency: Number of observations of class
- Expected frequency: Number of expected observations of class

Filter Based Feature Selection

- **Chi-square test:** Are two categorical variables independent?
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$$\chi^2 = \frac{(\text{Observed frequency} - \text{Expected frequency})^2}{\text{Expected frequency}}$$

- Observed frequency: Number of observations of class
- Expected frequency: Number of expected observations of class

Chi-square test:

Step 1 Build a contingency table

Suppose:

- Binary classification: Positive / Negative
- Feature: word = "excellent"

| | Positive | Negative | Total |
|--------------|----------|----------|-------|
| word present | 40 | 5 | 45 |
| word absent | 10 | 45 | 55 |
| Total | 50 | 50 | 100 |

Step 2 Compute expected counts (independence assumption)

Expected value formula:

$$E_{ij} = \frac{(\text{row total}) \times (\text{column total})}{\text{grand total}}$$

Expected counts should be reasonably large

Rule of thumb: $E_{ij} \geq 5$

Example:

$$E(\text{present, positive}) = \frac{45 \times 50}{100} = 22.5$$

If feature and label were independent, we'd expect **22.5**, but we observed **40**.

Chi-square test:

Step 3 Compute Chi-square statistic

$$\chi^2 = \sum \frac{(O - E)^2}{E}$$

Where:

- O = observed count
- E = expected count

📌 Large deviation \rightarrow large $\chi^2 \rightarrow$ **strong dependence**

Step 4 Interpretation

- $\chi^2 \approx 0 \rightarrow$ independent \rightarrow feature is useless
- χ^2 large \rightarrow dependent \rightarrow feature is informative

For feature selection:

- We **rank features by χ^2**
- Select **top-k** features

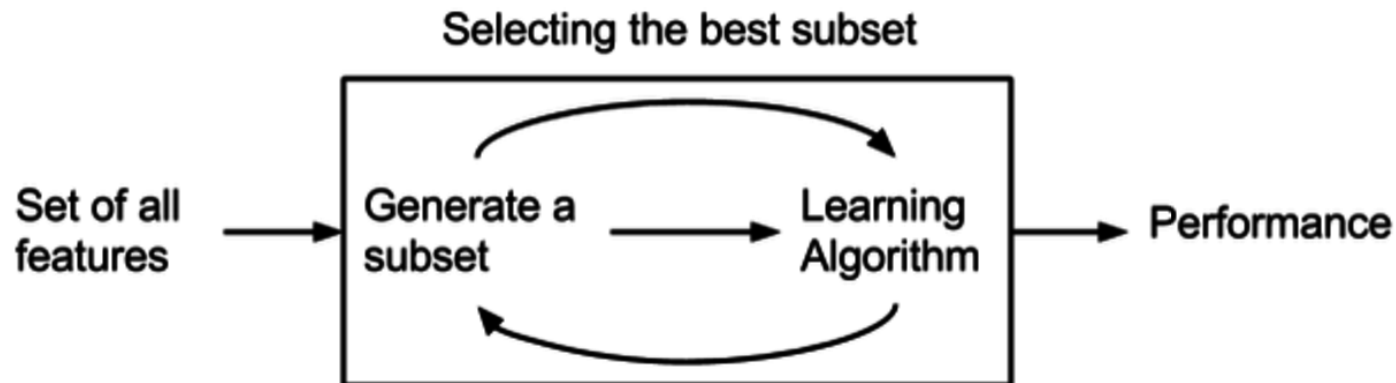
Chi-Square Olasılık Tablosu

The areas given across the top are the areas to the right of the critical value. To look up an area on the left, subtract it from one, and then look it up (ie: 0.05 on the left is 0.95 on the right)

| df | 0.995 | 0.99 | 0.975 | 0.95 | 0.90 | 0.10 | 0.05 | 0.025 | 0.01 | 0.005 |
|-----|--------|--------|--------|--------|--------|---------|---------|---------|---------|---------|
| 1 | --- | --- | 0.001 | 0.004 | 0.016 | 2.706 | 3.841 | 5.024 | 6.635 | 7.879 |
| 2 | 0.010 | 0.020 | 0.051 | 0.103 | 0.211 | 4.605 | 5.991 | 7.378 | 9.210 | 10.597 |
| 3 | 0.072 | 0.115 | 0.216 | 0.352 | 0.584 | 6.251 | 7.815 | 9.348 | 11.345 | 12.838 |
| 4 | 0.207 | 0.297 | 0.484 | 0.711 | 1.064 | 7.779 | 9.488 | 11.143 | 13.277 | 14.860 |
| 5 | 0.412 | 0.554 | 0.831 | 1.145 | 1.610 | 9.236 | 11.070 | 12.833 | 15.086 | 16.750 |
| 6 | 0.676 | 0.872 | 1.237 | 1.635 | 2.204 | 10.645 | 12.592 | 14.449 | 16.812 | 18.548 |
| 7 | 0.989 | 1.239 | 1.690 | 2.167 | 2.833 | 12.017 | 14.067 | 16.013 | 18.475 | 20.278 |
| 8 | 1.344 | 1.646 | 2.180 | 2.733 | 3.490 | 13.362 | 15.507 | 17.535 | 20.090 | 21.955 |
| 9 | 1.735 | 2.088 | 2.700 | 3.325 | 4.168 | 14.684 | 16.919 | 19.023 | 21.666 | 23.589 |
| 10 | 2.156 | 2.558 | 3.247 | 3.940 | 4.865 | 15.987 | 18.307 | 20.483 | 23.209 | 25.188 |
| 11 | 2.603 | 3.053 | 3.816 | 4.575 | 5.578 | 17.275 | 19.675 | 21.920 | 24.725 | 26.757 |
| 12 | 3.074 | 3.571 | 4.404 | 5.226 | 6.304 | 18.549 | 21.026 | 23.337 | 26.217 | 28.300 |
| 13 | 3.565 | 4.107 | 5.009 | 5.892 | 7.042 | 19.812 | 22.362 | 24.736 | 27.688 | 29.819 |
| 14 | 4.075 | 4.660 | 5.629 | 6.571 | 7.790 | 21.064 | 23.685 | 26.119 | 29.141 | 31.319 |
| 15 | 4.601 | 5.229 | 6.262 | 7.261 | 8.547 | 22.307 | 24.996 | 27.488 | 30.578 | 32.801 |
| 16 | 5.142 | 5.812 | 6.908 | 7.962 | 9.312 | 23.542 | 26.296 | 28.845 | 32.000 | 34.267 |
| 17 | 5.697 | 6.408 | 7.564 | 8.672 | 10.085 | 24.769 | 27.587 | 30.191 | 33.409 | 35.718 |
| 18 | 6.265 | 7.015 | 8.231 | 9.390 | 10.865 | 25.989 | 28.869 | 31.526 | 34.805 | 37.156 |
| 19 | 6.844 | 7.633 | 8.907 | 10.117 | 11.651 | 27.204 | 30.144 | 32.852 | 36.191 | 38.582 |
| 20 | 7.434 | 8.260 | 9.591 | 10.851 | 12.443 | 28.412 | 31.410 | 34.170 | 37.566 | 39.997 |
| 21 | 8.034 | 8.897 | 10.283 | 11.591 | 13.240 | 29.615 | 32.671 | 35.479 | 38.932 | 41.401 |
| 22 | 8.643 | 9.542 | 10.982 | 12.338 | 14.041 | 30.813 | 33.924 | 36.781 | 40.289 | 42.796 |
| 23 | 9.260 | 10.196 | 11.689 | 13.091 | 14.848 | 32.007 | 35.172 | 38.076 | 41.638 | 44.181 |
| 24 | 9.886 | 10.856 | 12.401 | 13.848 | 15.659 | 33.196 | 36.415 | 39.364 | 42.980 | 45.559 |
| 25 | 10.520 | 11.524 | 13.120 | 14.611 | 16.473 | 34.382 | 37.652 | 40.646 | 44.314 | 46.928 |
| 26 | 11.160 | 12.198 | 13.844 | 15.379 | 17.292 | 35.563 | 38.885 | 41.923 | 45.642 | 48.290 |
| 27 | 11.808 | 12.879 | 14.573 | 16.151 | 18.114 | 36.741 | 40.113 | 43.195 | 46.963 | 49.645 |
| 28 | 12.461 | 13.565 | 15.308 | 16.928 | 18.939 | 37.916 | 41.337 | 44.461 | 48.278 | 50.993 |
| 29 | 13.121 | 14.256 | 16.047 | 17.708 | 19.768 | 39.087 | 42.557 | 45.722 | 49.588 | 52.336 |
| 30 | 13.787 | 14.953 | 16.791 | 18.493 | 20.599 | 40.256 | 43.773 | 46.979 | 50.892 | 53.672 |
| 40 | 20.707 | 22.164 | 24.433 | 26.509 | 29.051 | 51.805 | 55.758 | 59.342 | 63.691 | 66.766 |
| 50 | 27.991 | 29.707 | 32.357 | 34.764 | 37.689 | 63.167 | 67.505 | 71.420 | 76.154 | 79.490 |
| 60 | 35.534 | 37.485 | 40.482 | 43.188 | 46.459 | 74.397 | 79.082 | 83.298 | 88.379 | 91.952 |
| 70 | 43.275 | 45.442 | 48.758 | 51.739 | 55.329 | 85.527 | 90.531 | 95.023 | 100.425 | 104.215 |
| 80 | 51.172 | 53.540 | 57.153 | 60.391 | 64.278 | 96.578 | 101.879 | 106.629 | 112.329 | 116.321 |
| 90 | 59.196 | 61.754 | 65.647 | 69.126 | 73.291 | 107.565 | 113.145 | 118.136 | 124.116 | 128.299 |
| 100 | 67.328 | 70.065 | 74.222 | 77.929 | 82.358 | 118.498 | 124.342 | 129.561 | 135.807 | 140.169 |

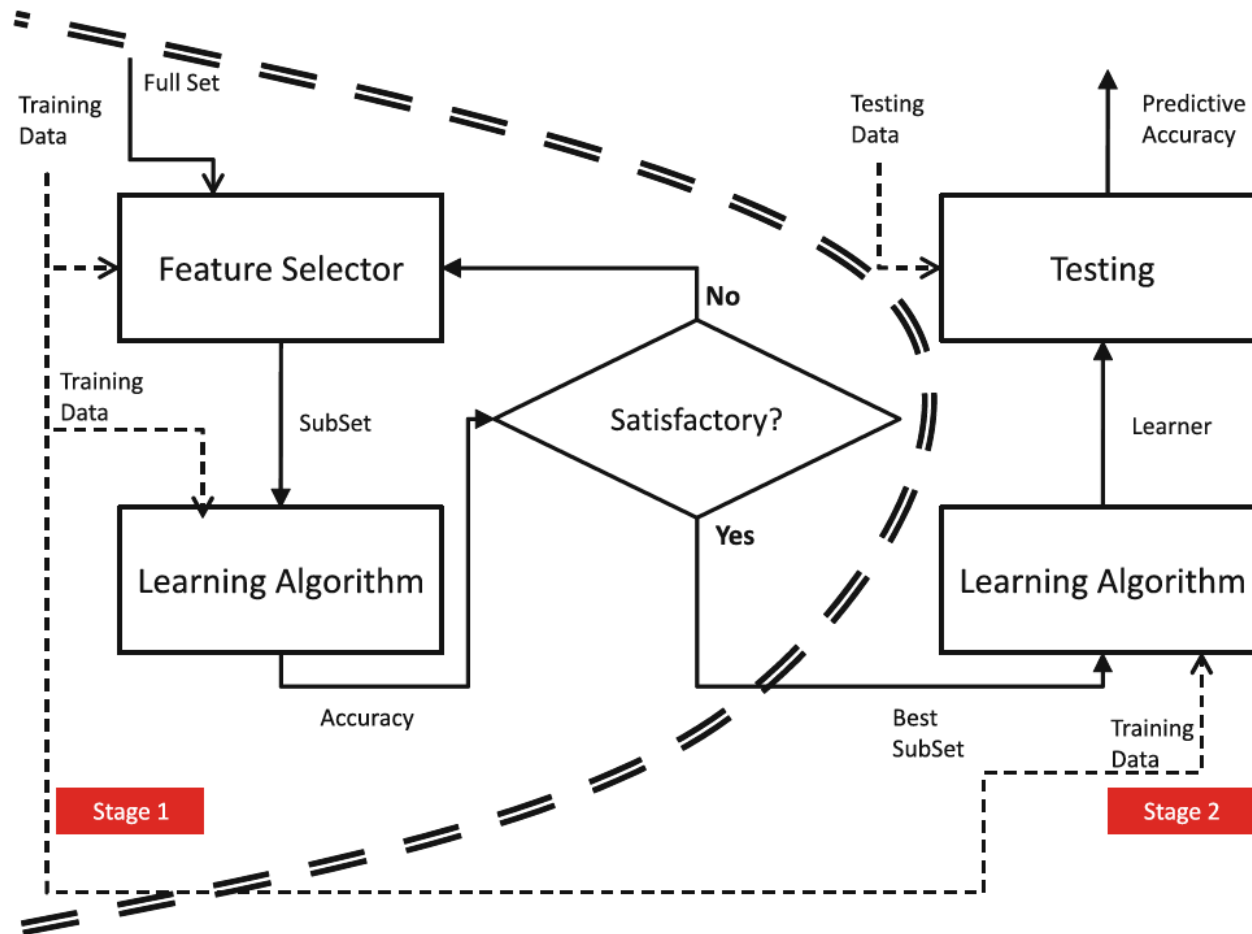
Wrapper Based Methods

- Trains a model repeatedly on different feature subsets and evaluating perform
- Feature usefulness is defined by **model performance**



- ✓ Small-medium feature sets
- ✓ Expensive features
- ✓ Accuracy more important than speed
- ✓ Strong interactions expected

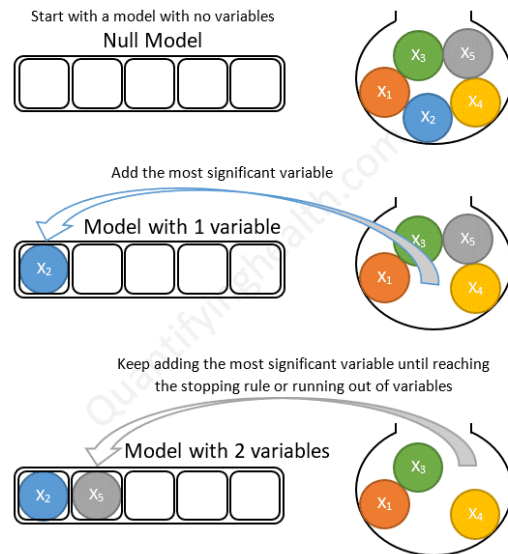
Wrapper Based Methods



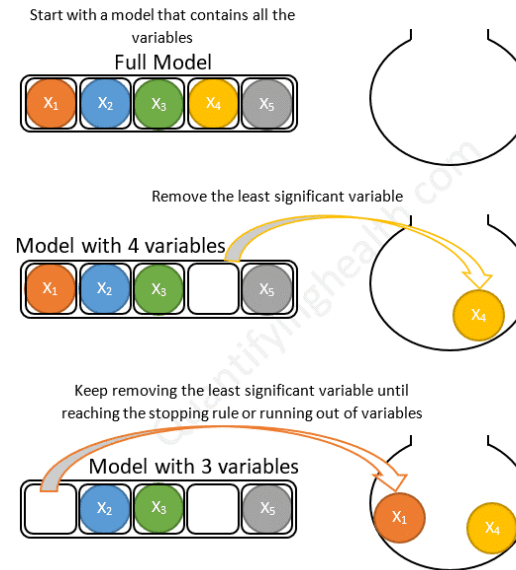
Wrapper Based Methods

- Forward Selection ve backward elimination yöntemleri

Forward stepwise selection example with 5 variables:



Backward stepwise selection example with 5 variables:



Wrapper Based Methods

Steps to perform Forward Feature Selection

1. Train n model using each feature (n) individually and check the performance
2. Choose the variable which gives the best performance
3. Repeat the process and add one variable at a time
4. Variable producing the highest improvement is retained
5. Repeat the entire process until there is no significant improvement in the model's performance

Embedded Feature Selection

- Embedded methods perform feature selection during model training itself.
 - ✓ Model-aware
 - ✓ More efficient than wrappers
 - ✓ Less prone to overfitting than wrappers
 - ✓ Capture interactions (trees)

Embedded Feature Selection

- Regularization
 - LASSO (Least Absolute Shrinkage and Selection Operator (LASSO), L1
 - Ridge (L2)
 - Elastic Net (L1+L2)
- Tree Based Methods
 - Decision Tree
 - Random Forest
- Linear Models
 - SVM
 - Sparse Logistic Regression

Traditional Feature Selection Methods

| Aspect | Filter | Wrapper | Embedded |
|----------------------|--------|---------|----------|
| Model-aware | ✗ | ✓ | ✓ |
| Speed | Fast | Slow | Medium |
| Feature interactions | ✗ | ✓ | ✓ |
| Generality | High | Low | Medium |

Feature Extraction

- Features are transformed into a new space that captures the underlying structure of the data

Feature selection

Choose subset of original features

Keeps original meaning

Example: remove low-variance features

Feature extraction

Create new features

Meaning is abstract

Example: PCA components

Feature Extraction

Unsupervised Feature Selection Techniques



Principal Component Analysis (PCA)

PCA is a linear dimensionality reduction method that converts the original feature space into a new orthogonal space defined by principal components.



Independent Component Analysis (ICA)

ICA can be used to convert the original feature space into a new space characterized by statistically independent components.



Non-Negative Matrix Factorization (NMF)

The non-negative matrix factor (NMF) approximates a non-negative data matrix as the product of two lower-dimensional non-negative matrices.



t-distributed Stochastic Neighbor Embedding (t-SNE)

t-SNE is a nonlinear dimensionality reduction method that tries to preserve the dataset's structure by reducing the difference between pairwise probability distributions in high and low-dimensional locations.



Autoencoder

An autoencoder, which is a kind of artificial neural network, learns to encode input data into a lower-dimensional representation and then decode it back to the original version.

Feature (Representation) Learning

- Representation learning is the idea of automatically **learning useful features from raw data**, instead of hand-crafting those features manually

Raw input : X

Representation: $Z = f(x)$

- Classical Pipeline:** Raw Data \rightarrow **Hand-crafted Features** \rightarrow Classifier \rightarrow Output.
- Representation Learning Pipeline:** Raw Data \rightarrow **Learnable Transformation** \rightarrow Latent Representation \rightarrow Output.

| Feature Engineering | Representation Learning |
|---------------------|-------------------------|
| Manual | Automatic |
| Domain expertise | Data-driven |
| Interpretable | Often abstract |
| Limited scalability | Scales well |
| Task-specific | Often reusable |

Feature (Representation) Learning

- Representation learning is the idea of automatically **learning useful features from raw data**, instead of hand-crafting those features manually

Raw input : X

Representation: $Z = f(x)$

- Examples:

Text

- Word2Vec, GloVe → word representations
- BERT, GPT → contextual representations

Vision

- CNN feature maps
- Vision Transformers

Time series

- Autoencoder embeddings
- Learned temporal representations

Audio

- Spectrogram embeddings
- Learned speech representations

Supervised Representation Learning

- Representations are learned from labeled data
- In supervised representation learning, representations are optimized directly for a labeled task through the loss function
- **Examples:**
 - CNN features for image classification
 - BERT learns contextual representations dynamically using self attention

Self-Supervised Representation Learning

- In Self Supervised Learning labels are automatically generated from the data itself, not manually annotated

The model creates **its own supervision signal**.

Examples:

- Word2Vec (predict context words)
- GloVe (predict co-occurrence statistics)
- BERT (masked language modeling)
- Contrastive learning

Pros:

- no labels needed
- scalable

Cons:

- representations may be generic

Unsupervised Representation Learning

Unsupervised learning focuses on data density estimation, dimensionality reduction, or clustering to extract meaningful features

Why do we need unsupervised representation learning?

- ✓ Labels are expensive
- ✓ Large unlabeled datasets exist
- ✓ Improves downstream tasks
- ✓ Enables transfer learning
- ✓ Reduces dimensionality

Unsupervised Representation Learning

Unsupervised learning focuses on data density estimation, dimensionality reduction, or clustering to extract meaningful features

Examples: Autoencoder, PCA, k-Means, contrastive learning, variational AE

| Domain | Example |
|-------------|-------------------------------|
| NLP | Word2Vec, GloVe |
| Vision | Autoencoders |
| Time series | Contrastive encoders |
| Audio | Self-supervised speech models |