

# Adaptive Voltage Droop Method of Multiterminal VSC-HVDC Systems for DC Voltage Deviation and Power Sharing

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**Abstract**—Voltage source converter based multiterminal HVDC (VSC-MTDC) technology has shown many advantages. However, following a large disturbance, the dc voltage and the output power of the VSC station with fixed droop control may hit their limits, thereby reducing the dc voltage control ability of the whole MTDC system. Here an adaptive droop control scheme is proposed on the basis of both the dc voltage deviation factor and the power sharing factor. It contributes to ensure the dc voltage and the power loading rate of each converter within their limits during large disturbances, and the power sharing capability of the whole MTDC system remain high. The working principle of the proposed adaptive droop control is discussed in details. Case study and simulations are performed based on the PSCAD/EMTDC model of a  $\pm 320$  kV four-terminal VSC-HVDC system to validate the effectiveness of the proposed adaptive droop method.

**Index Terms**—VSC-MTDC, adaptive voltage droop method, power sharing, DC voltage deviation.

## I. INTRODUCTION

THE RAPID development of offshore wind farm projects far away from the coast, as well as the ring demand to connect the remote renewable energy sources to the major load centers, led to an increasing interest in high voltage direct current (HVDC) technology in the last decade. Compared with line-commutated converters, voltage source converters (VSCs) presents clear advantages due to the fully controlled semiconductors, such as gate turn-off thyristors and insulated gate bipolar transistors (IGBTs). VSCs enable better transmission efficiency, reactive power compensation, independent and flexible power control, and unlimited terminal configurations. With these advantages, VSC-HVDC provides a feasible choice for

city centers in-feed, power supply to islands, grid connection, offshore wind energy integration, and multi-terminal HVDC (MTDC) systems [1]–[4]. Compared with the point-to-point HVDC system, MTDC systems have more advantages on enhanced reliability of the DC system, flexibility of power dispatch control, reduction in curtailment of renewable energy, and efficient utilization of converters and cables [5]–[7]. These distinguishing features make the VSC-MTDC system promising to transmit wind energy from offshore islands or to connect different grids in the future. Two VSC-MTDC demonstration projects have already been commissioned in China, namely, “Nan’ao  $\pm 160$  kV three-terminal VSC-HVDC project” and “Zhoushan  $\pm 200$  kV five-terminal VSC-HVDC project” [8], [9].

The VSC-MTDC system poses several challenges as the technology of different elements connected to the system is still evolving in terms of power and voltage levels. Given that DC voltage serves as an indicator of power balance and operation stability in an MTDC system, the DC voltage control of the VSC-MTDC system has become a priority to ensure overall system stability.

Theoretically, mainly three basic methods that control the DC voltage of the VSC-MTDC system, namely, (1) master-slave method, (2) the voltage margin method (VMM), (3) the voltage droop method (VDM), have been proposed. The first method can achieve high operation accuracy because the master converter can keep the DC voltage at the reference value and other slave converters can regulate power according to the power references [10], [11]. However, master-slave control method is tightly dependent on fast communication and the remote information is required. Since the DC voltage control is totally lost if the master converter fails, the master-slave control method suffers from poor reliability. To reduce dependency on fast communication and increase system reliability, decentralized control strategies such as VMM and VDM have been proposed. Reference [12] reviews VMM and different types of VDM methods. In VMM, one converter (master converter) is responsible for maintaining its DC voltage in the desired level, whereas other terminals operate at the constant power mode. Given some technical constraints, when the master converter is no longer able to supply or extract the active power necessary for controlling its DC voltage, another converter will operate as the master converter. However, a margin must be considered between the reference DC voltages of terminals. The transition between these two reference

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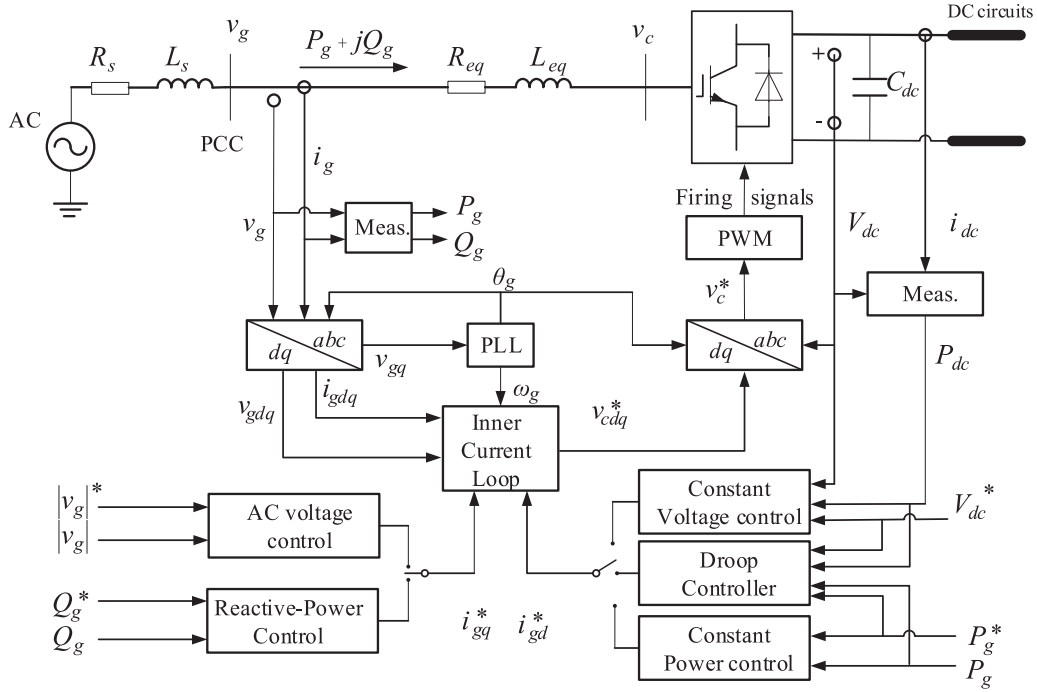


Fig. 1. The main diagram and control system of a VSC-HVDC station.

voltages places great stress on the converter. Moreover, the voltage margin must be large enough to avoid interactions between controllers [13], [14]. VDM is independent of communication. In VDM, which originates from power-frequency droop control in AC systems, all or some converters participate in regulating the DC voltage and sharing the power imbalance simultaneously in an appropriate way [15]. VDM exhibits higher reliability than the master-slave control and does not lead to voltage oscillation associated with VMM [12]. This feature is why VDM has attracted considerable research interest.

However, despite the popularity of VDM, problems caused by disturbance under fixed droop control cannot be neglected, including DC voltage deviating from its rated value [6], [16], [17], frequency deviation in the neighboring AC system [18], [19], and power flow calculation methods incorporating AC and DC systems [20]–[22]. One particular issue is how an MTDC system reacts to power disturbances such as loss/outage of one or more converters, DC line disconnection, and normal changes in power settings.

When a power disturbance occurs, the powers of the converters with fixed droop control may hit their limits; hence, such converters no longer contribute to power sharing, and the DC voltage deviation may be large. Reference [23] proposes a DC voltage droop design methodology that considers the different dynamics involving a VSC-MTDC system, but the calculation is complicated and the droop coefficients must be revised based on different operation conditions. Reference [24], [25] provide power-sharing control strategies that utilizes an adaptive VDM scheme based on optimal -power flow, but the computing time is slightly long. Reference [26] proposes a droop controller structure that maintains the DC voltage close

to the nominal value and simultaneously attempts to preserve the power flow in the DC grid. Reference [27] introduces DC voltage regulation and frequency support in pilot voltage droop control by changing the reference operating point of voltage droop control, thereby maintaining adequate power sharing and efficient voltage regulation among the converter stations. However, the pilot voltage droop control needs a fast communication to transfer the measurements of DC voltages of different converter stations [28]. Reference [29] proposes a critical loading characterization method to identify the maximum exchange active powers for MTDC converters; this method is useful when connected to weak AC systems. Reference [30] introduces an efficient algorithm to adaptively determine the droop coefficients of MTDC converters to improve the stability margin of integrated AC/DC power networks. However, the transient performance of the whole system and the influence of DC voltage deviation are not considered. Reference [31] proposes a control scheme for adapting droop coefficients to share the burden in accordance with the available headroom of each converter station, but the DC voltage deviation of each converter is not considered during the transient process. Reference [32] points out that DC voltage deviation and power sharing capability are the two most important aspects of droop control, based on which a fuzzy logic based adaptive droop controller is proposed. However, only a basic fuzzy inference rule is formulated, which does not include a concrete equation or quantitative analysis.

On the basis of [31] and [32], this paper aims to propose an adaptive VDM scheme that ensures DC voltage deviations of the converters with droop control does not hit their limits during large events, and the power sharing capability of the whole

MTDC system remain high. The rest of this paper is organized as follows. In Section II, VSC structure and basic ideas of droop control are addressed. The adaptive VDM based on DC voltage deviation and power sharing is proposed in Section III. In Section IV, simulations of a four-terminal VSC-HVDC system under different disturbances have been done in PSCAD/EMTDC to validate the effectiveness of the proposed adaptive VDM. Finally, conclusions and future work are provided in Section V.

## II. VSC STRUCTURE AND CONTROL MODES

### A. Typical Structure and Control of a VSC-HVDC Station

The basic structure and control of a VSC-HVDC station is presented in Fig. 1 [26]. The adjacent AC system is equivalent to a Thevenin circuit of a fixed AC voltage source and serial impedance ( $R_s$  and  $L_s$ ) at the point of common coupling (PCC). The converter transformer is not shown in this structure, but the inductances and resistances of the converter transformer and the bridges of VSC are modeled as an equivalent inductance  $L_{eq}$  with a small resistance  $R_{eq}$  in series. Modular multilevel converter (MMC) is one topology of VSC. The capacitors located at the DC terminals of the two-level VSC station or the paralleled DC capacitors of the sub-modules of MMC are symbolized as the capacitor  $C_{dc}$ . The VSC station is connected to other stations via DC circuits.

Typically, the control system of a VSC-HVDC station has two cascaded control loops, namely, the outer control loop and inner current control loop. The inner current control loop is implemented in the synchronously rotating  $dq$ -frame (voltage oriented), which makes the  $dq$ -frame current ( $i_{gd}$ ,  $i_{gq}$ ) track the current reference ( $i_{gd}^*$ ,  $i_{gq}^*$ ) rapidly by regulating the output voltage of the VSC. The current and the power in the VSC are directly governed by the inner current loop control in accordance with the reference generated by the outer loop.

The dynamics of the VSC station in Fig. 1 can be expressed in the rotating  $dq$ -frame as

$$\begin{cases} L_{eq} \frac{di_{gd}}{dt} = -R_{eq}i_{gd} + \omega_g L_{eq}i_{gq} - v_{cd} + v_{gd} \\ L_{eq} \frac{di_{gq}}{dt} = -R_{eq}i_{gq} - \omega_g L_{eq}i_{gd} - v_{cq} + v_{gq} \end{cases} \quad (1)$$

where ( $i_{gd}$ ,  $i_{gq}$ ), ( $v_{gd}$ ,  $v_{gq}$ ), and ( $v_{cd}$ ,  $v_{cq}$ ) denote the grid current, the voltage at PCC node, and output voltage of VSC in  $dq$ -frame, respectively.  $R_{eq}$ ,  $L_{eq}$  denote the equivalent resistance and inductance between the PCC and VSC, respectively.  $\omega_g$  is the electrical angular frequency.

The inner current control loop receives current references ( $i_{gd}^*$ ,  $i_{gq}^*$ ) and acts on the output voltage of the converter. The current in  $dq$ -frame can realize decoupling control by adpating the voltage coupling compensations ( $\omega_g L_{eq}i_{gd}$ ,  $\omega_g L_{eq}i_{gq}$ ) and feedforward compensations of AC system voltage ( $v_{gd}$ ,  $v_{gq}$ ) in the inner current control loop. The detailed diagram of the inner current loop controller is shown in Fig. 2.

The outer controller is responsible for controlling the DC voltage and power of the VSC, which provides reference values to the inner current control loop. Depending on the DC voltage and power modes, which will be introduced in the following

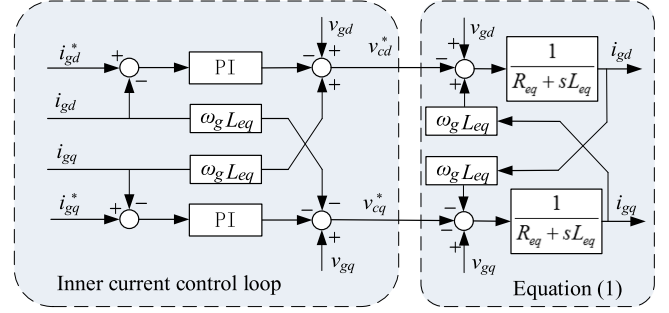


Fig. 2. The diagram of inner current loop controller.

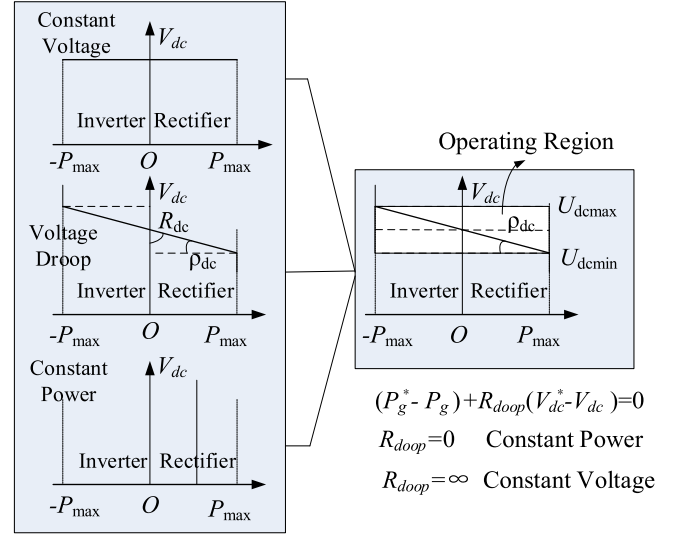


Fig. 3. The DC Voltage versus power characteristic curves of three control modes.

section, the reference values for the active current  $i_{gd}^*$  is provided by the constant voltage controller, constant power controller or droop controller, whereas the active current  $i_{gq}^*$  is provided by a reactive-power or AC voltage controller.

### B. DC Voltage and Power Control Modes

A VSC-HVDC terminal may have one of three control modes, namely, constant power control mode, constant voltage control mode, and VDC mode. The DC voltage versus power characteristic curves of the three control modes are shown in Fig. 3. The constant voltage control mode maintains a constant DC voltage at the terminal regardless of the power flow change. The voltage  $V_{dc}$  will gradually become equal to the reference  $V_{dc}^*$ . The constant power control mode maintains a constant power flow of the converter regardless of the voltage level at that terminal.  $P_g$  will eventually be equal to the reference power  $P_g^*$ . The DC voltage control mode can be considered a combination of the two first types of VSC control modes. It attempts to control power to its reference level depending on the DC voltage deviation. Given that these two actions are somewhat contradicting, one action occurs at the cost of steady state deviation for the other.  $R_{droop}$  refers to the DC voltage response and is expressed by the unit MW/kV. The slope is given in terms of the DC droop coefficient  $\rho_{dc}$ , which is defined as the change in DC voltage per unit that

results in 100% change in converter power flow.  $R_{droop}$  is selected based on the maximum allowable DC voltage deviation to the rated value.

$$R_{droop} = \frac{P_{rated}}{V_{rated}\rho_{dc}} \quad (2)$$

where  $P_{rated}$  and  $V_{rated}$  refer to the rated power and rated DC voltage of the VSC, respectively.

At steady state, the relationship between DC voltage and the converter power is

$$(P_g^* - P_g) + R_{droop}(V_{dc}^* - V_{dc}) = 0 \quad (3)$$

Notable, the steady state characteristics in constant power control mode and constant DC voltage control mode are represented by DC voltage control controllers. In Fig. 3, if  $R_{droop} = 0$ , then droop control is regarded as constant power control; if  $R_{droop} = \infty$ , then droop control is regarded as constant DC voltage control. Thus, we can change the droop coefficient depending on the operating state of the VSC station to realize reasonable power sharing and voltage deviation.

### III. ADAPTIVE DROOP CONTROL FOR DC VOLTAGE DEVIATION AND POWER SHARING

#### A. Fixed Droop

For an MTDC system with more than two converter stations, all the VSC stations with droop control should share the resulting power imbalance in a certain appropriate proportion following a large disturbance.

To simplify VDM, we assume that the MTDC system is an ideal lossless DC grid, and all DC bus voltages will be equal. These conditions imply

$$\Delta V_{dci} = \Delta V_{dc} \quad i = 1, 2, \dots, n \quad (4)$$

where  $\Delta V_{dci}$  refers to the DC voltage deviation of the  $i$ th converter.

From (3), if the droop coefficient is fixed, then the power deviation  $\Delta P_{gi}$  is expressed by

$$\Delta P_{gi} = -R_{droopi}\Delta V_{dci} \quad (5)$$

where  $\Delta P_{gi}$  refers to the power deviation of the  $i$ th converter.

When a large imbalance power  $\Delta P$  occurs in the MTDC system, the  $n$  VSC station with droop control will share the imbalance power by

$$\Delta P = \sum_{i=1}^n \Delta P_{gi} = \left( - \sum_{i=1}^n R_{droopi} \right) \Delta V_{dc} = -R\Delta V_{dc} \quad (6)$$

where  $R$  is the DC voltage response of the DC grid (analogous to frequency response of AC grids), i.e.,  $R$  shows the total amount of change in grid power flow in MW as a result of 1 kV change in DC bus voltage.

The imbalance power sharing of the  $i$ th converter is

$$\Delta P_{gi} = \frac{R_{droopi}}{\sum_{i=1}^n R_{droopi}} \Delta P = \frac{R_{droopi}}{R} \Delta P \quad (7)$$

From (7), the imbalance power sharing of the  $i$ th converter will exclusively be dependent on the DC voltage response

$R_{droopi}$  of the individual DC terminal and the total DC voltage response  $R$  of the MTDC system. When  $R_{droopi}$  rises, the imbalance power sharing will increase, and vice versa.

In general, the DC voltage response  $R_{droopi}$  of the  $i$ th VSC converter is designed in proportion to its capacity. However, powers and DC voltage deviations of converters with fixed droop control may reach their limits in case of unexpected events such as faults or disconnection of a station. This problem with fixed droop control can be avoided using an adaptive droop scheme described in the next subsection.

#### B. Adaptive Droop Control

For fixed droop control, the droop coefficients are usually dependent on the respective converter ratings. However, under a particular operating condition, all the converter stations with droop control may not be equally loaded and hit their limits. From (7), a relatively small  $R_{droop}$  (large  $\rho_{dc}$ ) means the controller is restrictive toward power, allowing a small deviation of power in case of large deviation of  $V_{dc}$ . By contrast, a relatively large  $R_{droop}$  (small  $\rho_{dc}$ ) indicates that the controller is restrictive toward voltage and will not allow a large deviation  $V_{dc}$  for a large deviation of power. The voltage deviation and power sharing are a trade-off.

The power headroom (difference between the rated capacity and present loading) is proposed to participate in power sharing [31]. However, the DC voltage deviation in transient and steady state is not considered. Reference [32] proposes a basic fuzzy inference rule: under the condition that the voltage deviation is large and power headroom is sufficient, the droop coefficient  $R_{droop}$  should be increased to ensure that the DC voltage is within a safe region. Otherwise, the droop coefficient should be reduced to ensure desirable power sharing. On the basis of the results proposed in [31] and [32], this paper proposes an adaptive droop control that consists of both the power sharing factor and DC voltage deviation factor.

$$R_{droopi}^{PV} = \alpha_i R_{droopi} \frac{H_{Pi}}{H_{Vi}} = \alpha_i R_{droopi} \frac{P_{maxi} - |P_{gi}|}{\xi - |\Delta V_{dci}|} \quad (8)$$

where  $R_{droopi}^{PV}$  refers to the adaptive DC voltage response coefficient.  $H_{Pi} = P_{maxi} - |P_{gi}|$  refers to the power sharing factor of the  $i$ th converter.  $H_{Vi} = \xi - |\Delta V_{dci}|$  refers to the DC voltage deviation factor.  $\xi$  refers to the limit of the DC voltage deviation, usually,  $\xi = 5\% \sim 10\%$ .  $\Delta V_{dci} = V_{dci} - 1$  refers to the DC voltage deviation from the rating voltage in per-unit.  $\alpha_i$  is a user-defined positive constant, ensuring that the adaptive DC voltage response coefficient  $R_{droopi}^{PV}$  is equal to the given  $R_{droopi}$  in steady state. Thus,  $\alpha_i$  is tuned by the operating state of the converter station (DC voltage and active power) and droop coefficient order ( $R_{droopi}$ ) from the scheduling system or the energy management system.

As shown in Fig. 4, the DC voltage response coefficient will adaptively change based on the operating state of the converter station. This strategy ensures that the converters, which are already operating very close to the power limits, will not try to share the imbalance power, and the converters already operating very close to the DC voltage limits will not attempt to sacrifice



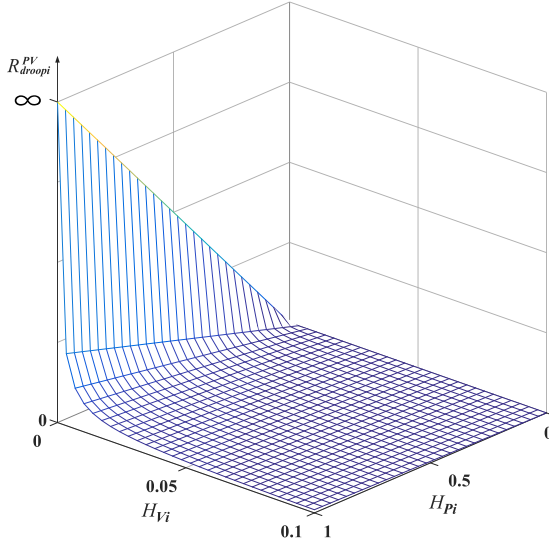


Fig. 4. The adaptive DC voltage response coefficient based on both the power sharing factor and the DC voltage deviation factor.

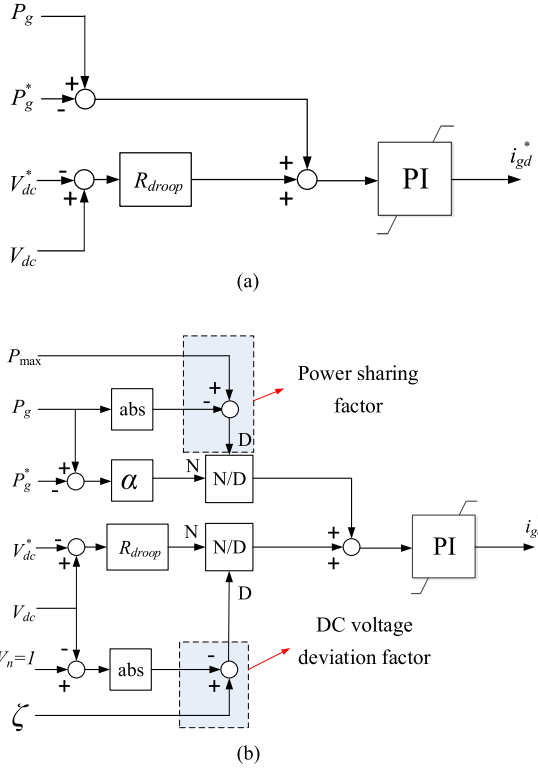


Fig. 5. The block diagram of voltage droop method. (a) The fixed droop control. (b) The proposed adaptive droop control.

DC voltage control ability for power sharing. The diagram of the proposed adaptive droop controller is shown in Fig. 5.

### C. Discussion and Improvement

This section mainly discusses the control effect of the proposed adaptive droop scheme of a lossless MTDC system.

We assume that the loading ratio of VSC1 is the highest. VSC1 adopts the proposed adaptive droop control, whereas the

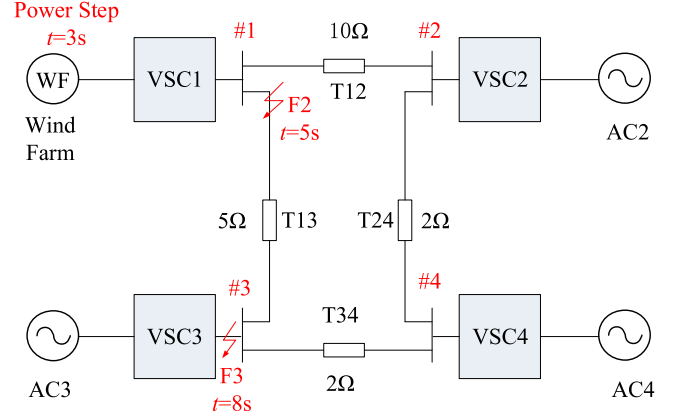


Fig. 6. The diagram of the four-terminal VSC-HVDC system.

other  $n-1$  converters adopt fixed droop control. Once a large imbalance power  $\Delta P$  occurs in the MTDC system, after substituting (8) into (7), the power sharing of VSC1 can be expressed by

$$\Delta P_{g1} = \frac{R_{droop1}^{PV}}{R_{droop1}^{PV} + \sum_{i=2}^n R_{droopi}^{PV}} \Delta P \quad (9)$$

At the highest loading ratio of VSC1, the power sharing factor  $H_{Pi}$  adopts the predominant position than the DC voltage deviation factor  $H_{Vi}$ , resulting in the decrease in  $R_{droop1}^{PV}$ .

From (9), the power sharing of VSC1  $\Delta P_{g1}$  decreases with  $R_{droop1}^{PV}$ , thereby ensuring that the power of VSC1 does not hit its limit. In particular, when there is no room for the power sharing,  $R_{droop1}^{PV}$  decreases to zero, and the control mode of VSC1 switches to constant power control.

Assuming all the VSCs with droop control modes adopt the proposed droop control, (7) can be rewritten as

$$\Delta P_{gi} = \frac{R_{droopi}^{PV}}{\sum_{i=1}^n R_{droopi}^{PV}} \Delta P = \frac{R_{droopi}^{PV}}{R^{PV}} \Delta P \quad (10)$$

In a lossless MTDC system, all DC bus voltages are equal, so the DC voltage deviation factors  $H_{Vi}$  are also equal. Thus, (10) can be transformed into

$$\Delta P_{gi} = \frac{\alpha_i H_{Pi} R_{droopi}}{\sum_{i=1}^n \alpha_i H_{Pi} R_{droopi}} \Delta P \quad (11)$$

From (11), in a lossless MTDC system, the power sharing of the converters with the proposed droop control scheme is not related to the DC voltage deviation factor  $H_{Vi}$ . The function of the DC voltage deviation factor  $H_{Vi}$  is to ensure that the DC voltage of the VSCs, which participate in voltage control, does not hit the voltage limits in transient and steady state.

## IV. SIMULATION

This section adopts a four-terminal  $\pm 320$  kV VSC-HVDC system under different disturbances in PSCAD/EMTDC to validate the effectiveness of the adaptive VDM discussed in Section III.

As shown in Fig. 6, the function of the MTDC system is to transfer power from a wind farm to three load centers. VSC1 is

TABLE I  
THE PARAMETERS OF THE FOUR-TERMINAL VSC-HVDC SYSTEM

Symbol	Parameters	Value
$v_l$	line voltage of valve side ac system (rms)	370kV
$L$	The equivalent inductance of ac system	0.025H
$R$	The equivalent resistance of ac system	0.08Ω
$C_0$	Capacitance of each sub-module	1.4mF
$N$	Number of sub-modules of each bridge arm	200
$L_s$	Inductance of each arm bridge	0.25H
$V_{dcn}$	Rated dc-link voltage	±320kV
$S_{n1}$	Rated capacity of VSC1 station	2000MVA
$S_{n2}$	Rated capacity of VSC2 Station	400MVA
$S_{n3}$	Rated capacity of VSC3 Station	600MVA
$S_{n4}$	Rated capacity of VSC4 Station	1000MVA
$f$	Fundamental frequency	50Hz
$f_s$	Carrier frequency as multiple of fundamental	5
$R_l$	The unit resistance of the dc line	0.4Ω/km
$L_l$	The unit inductance of the dc line	0.45mH/km
$l_{12}$	The line length between VSC1 and VSC2	25km
$l_{23}$	The line length between VSC2 and VSC3	5km
$l_{34}$	The line length between VSC3 and VSC4	5km
$l_{41}$	The line length between VSC4 and VSC1	12.5km
$\rho_{dc2}$	The fixed droop coefficient of VSC2 in p.u.	0.025
$\rho_{dc3}$	The fixed droop coefficient of VSC3 in p.u.	0.0167
$\rho_{dc4}$	The fixed droop coefficient of VSC4 in p.u.	0.01
$\zeta$	The limit of the DC voltage deviation in p.u.	0.05
$K_d$	Proportional gain of outer control loop	6
$\tau_d$	Time constant of outer control loop	0.05
$K_d$	Proportional gain of inner control loop	0.6
$\tau_d$	Time constant of inner control loop	0.01

a wind farm connected station, and it operates at the AC voltage control and constant frequency control mode (VF control mode). VSC2, VSC3 and VSC4 are the three AC grid-connected stations that operates at the VDM mode. The parameters of the four-terminal ±320 kV VSC-HVDC system are listed in Table I.

In this case, VSCs adopt MMC topology to avoid series of hundreds of IGBTs. Besides, carrier phase shift modulation method (CPSM) is adopted, and the carrier frequency is set to be 5 times fundamental frequency. The PI controller of the outer control loop in Fig. 5 is designed to achieve a closed loop bandwidth of 300 rad/s since the tracking parameters are DC in nature.

In the steady state, the output power of VSC1 station P1 is 1000 MW, VSC2, VSC3 and VSC4 station receives 110 MW, 258 MW and 580 MW, respectively. The DC voltages of VSC2, VSC3, and VSC4 station are 655.6 kV, 656.5 kV, and 654.3 kV, respectively.

The disturbances are set as follows:

- 1)  $t = 3$  s, the output power of wind farm steps to 1400 MW.
- 2)  $t = 5$  s, the DC line T13 between VSC1 and VSC3 station disconnects without faults (F2 in Fig. 6).
- 3)  $t = 8$  s, VSC3 station disconnects from the MTDC system without faults (F3 in Fig. 6).

After adopting fixed droop control and the proposed adaptive droop control, the active power and DC voltage responses of the grid-connected VSC stations (VSC2, VSC3 and VSC4) under the above disturbances are shown in Figs. 7 and 8, respectively.

In the steady state before the first disturbance, the DC voltages and output power of the grid-connected VSC stations with the two control methods (fixed droop and proposed adaptive droop) are the same.

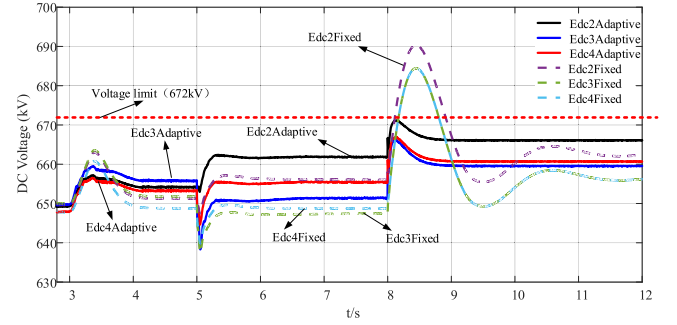


Fig. 7. The DC voltage simulation results of the grid-connected VSC stations under large disturbances. Where Edc2Adaptive, Edc3Adaptive and Edc4Adaptive denote the DC voltages of VSC2, VSC3 and VSC4 station with the proposed adaptive droop control scheme respectively. Edc2Fixed, Edc3Fixed and Edc4Fixed denote the DC voltages of VSC2, VSC3 and VSC4 station with fixed droop control scheme respectively.

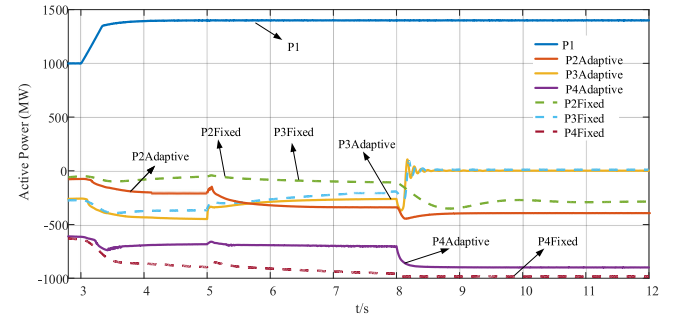


Fig. 8. The output active power simulation results of the grid-connected VSC stations under large disturbances. Where P2Adaptive, P3Adaptive and P4Adaptive denote the output active power of VSC2, VSC3 and VSC4 station with the proposed adaptive droop control scheme respectively. P2Fixed, P3Fixed and P4Fixed denote the output active power of VSC2, VSC3 and VSC4 station with fixed droop control scheme respectively.

When the output power of the wind farm steps to 1400 MW at  $t = 3$  s, the DC voltages rise up to reduce the pressure of power sharing between the grid-connected VSC stations. Compared with fixed droop control, the DC voltages with the proposed adaptive droop control rise to a higher steady level more quickly, and the power loading rate of each grid-connected VSC is more balanced, thereby indicating the power sharing is more reasonable.

When the DC line T13 between VSC1 and VSC3 station disconnects at  $t = 5$  s, the DC voltage and output active power reach a new steady state after some fluctuations. Compared with fixed droop control, the fluctuation is smaller and power sharing is more reasonable by adopting the proposed adaptive droop control scheme.

When VSC3 station disconnects from the MTDC system at  $t = 8$  s, the output active power of VSC3 decreases to zero quickly, and the imbalanced power of VSC3 is shared by VSC2 and VSC4. Under the fixed droop control scheme, the output active power of VSC4 reaches its limit. Moreover, the fluctuation of DC voltage is large, thereby exceeding the DC voltage limit. Compared with fixed droop control, the proposed adaptive droop control ensures that the DC voltages of the grid-connected VSC stations (VSC2 and VSC4) are within their voltage limits, and

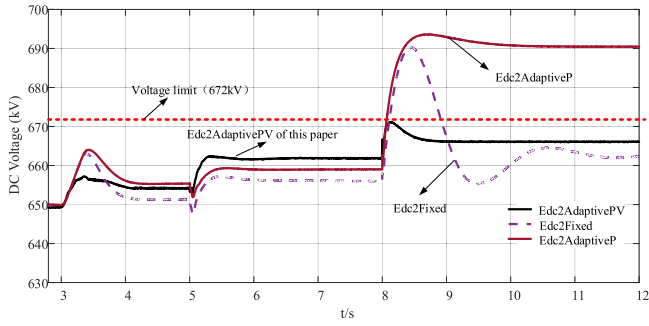


Fig. 9. The DC voltage simulation results of VSC2 with different droop control schemes under large disturbances. Where Edc2Fixed, Edc2AdaptivePV and Edc2AdaptiveP denote the DC voltages of VSC2 with fixed droop control scheme, adaptive droop control scheme of this paper and headroom-based power-sharing adaptive droop control scheme, respectively.

the power loading rates of the grid-connected VSC stations are almost equal and do not hit their power limits.

To validate the effectiveness of the proposed adaptive droop control further, the simulation of the four-terminal VSC-HVDC system with headroom-based power-sharing adaptive droop control is also conducted. A detailed comparison simulation results with the three droop methods (fixed droop control, the proposed adaptive droop control of this paper, and headroom-based power-sharing adaptive droop control) is shown in Fig. 9. The maximum DC voltage deviation of VSC2 with the proposed adaptive droop method is within the voltage limit, whereas those with fixed droop control and headroom-based power-sharing adaptive control exceeds the voltage limit. This result validates the effectiveness of the proposed adaptive droop control. Moreover, the response rate of the proposed adaptive droop control is fast, thereby shortening the transient process under large disturbances.

In sum, the simulations of the four-terminal VSC-HVDC system under large disturbances in PSCAD/EMTDC validate the effectiveness of the proposed adaptive droop control.

## V. CONCLUSION AND FUTURE WORK

The typical structure and control of a VSC station is introduced. The constant power control and the constant DC voltage control can be unified as special forms of VDM. Therefore, this paper proposes an adaptive VDM scheme for the grid-connected VSC stations.

Considering both the power sharing factor and the DC voltage deviation factor, an adaptive droop control is proposed to ensure DC voltage deviations within their limits during large disturbances, and the power sharing capability of the whole MTDC system remain high. A four-terminal VSC-HVDC system is established in PSCAD/EMTDC to validate the effectiveness of the proposed adaptive droop control.

Impacts of varying droop coefficients on the stability of the MTDC system, the adaptive droop control scheme considering frequency support, and impacts of line resistances on steady performance of the VSC-MTDC system with the proposed adaptive droop control [33] should be studied in the future.

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