<pre>import sys sys.path.append('/content/drive/MyDrive/DSBA M2/2 Reinf Mounted at /content/drive %capture %matplotlib inline import numpy as np import pickle import tools</pre>	
the city's preference for the situation, and time is discretized by hour. A	cating how many parking spaces are occupied, actions are nonnegative integers designating the price of street parking, the reward is a real value of the street parking and price is likely to decrease occupancy over the hour, while charging a low price is likely to increase it. Three price points. Note that an environment with three parking spaces actually has four states — zero, one, two, or three spaces could be occupancy over the hour, while charging a low price is likely to increase it.
pi array([[0.33333333, 0.33333333, 0.33333333],	es the value of i spaces being occupied.
<pre>array([0., 0., 0., 0.]) state = 0 V[state] 0.0 state = 0</pre>	
<pre>value = 10 V[state] = value v array([10., 0., 0., 0.]) for s, v in enumerate(V): print(f'State {s} has value {v}') State 0 has value 10.0</pre>	
State 1 has value 0.0 State 2 has value 0.0 State 3 has value 0.0 The policy is a two-dimensional array where the (i,j) -th entry gives the pi array([[0.33333333, 0.33333333, 0.3333333], [0.33333333, 0.33333333], [0.33333333, 0.33333333], [0.33333333, 0.33333333], [0.333333333, 0.33333333], [0.333333333, 0.33333333]])	ne probability of taking action j in state i .
<pre>state = 0 pi[state] array([0.33333333, 0.33333333, 0.3333333]) state = 0 action = 1 pi[state, action]</pre>	
<pre>0.333333333333333333333333333333333333</pre>	
<pre>for s, pi_s in enumerate(pi): print(f''.join(f'pi(A={a} S={s})) = {p.round(2)}' + pi(A=0 S=0) = 0.75 pi(A=1 S=0) = 0.21 pi(A=2 S=0) pi(A=0 S=1) = 0.33 pi(A=1 S=1) = 0.33 pi(A=2 S=1) pi(A=0 S=2) = 0.33 pi(A=1 S=2) = 0.33 pi(A=2 S=2) pi(A=0 S=3) = 0.33 pi(A=1 S=3) = 0.33 pi(A=2 S=3)</pre> tools.plot(V, pi) Value Function	= 0.04 = 0.33 = 0.33
8	Action 1 Probability
expected return of zero. On the right, the policy is displayed on a two-d	o 1 2 3 State In the tools module. On the left, the value function is displayed as a barplot. State zero has an expected return of ten, while the other states dimensional grid. Each vertical strip gives the policy at the labeled state. In state zero, action zero is the darkest because the agent's policy many contents and the states are the states a
choice with the highest probability. In the other states the agent has the You can access the state space and the action set as attributes of the env.S [0, 1, 2, 3] env.A	
You will need to use the environment's transitions method to compare the formal state i from the current state and the entry at $(i,1)$ is the conditional probability of the state i action i	mplete this assignment. The method takes a state and an action and returns a 2-dimensional array, where the entry at $(i,0)$ is the reward for trorobability of transitioning to state i given the current state and action.
array([[1.	= {p.round(2)}')
Section 1: Policy Evaluation	I like you to evaluate the quality of the existing pricing scheme. Policy evaluation works by iteratively applying the Bellman equation for v_π to a $v(s) \leftarrow \sum_a \pi(a s) \sum_{s',r} p(s',r s,a) [r+\gamma v(s')]$
version usually converges faster. In this assignment, we will be imple	ially applied to each state) or with "two-arrays" (i.e. the update rule is simultaneously applied to each state). Both versions converge to v_{π} but the lementing all update rules in-place, as is done in the pseudocode of chapter 4 of the textbook. The textbook in chapter 4.1 of the textbook. It is left to you to fill in the bellman_update function to complete the algorithm.
<pre>delta = max(delta, abs(v - V[s])) if delta < theta: break return V # [Graded] def bellman_update(env, V, pi, s, gamma): """ Mutate ``V`` according to the Bellman update equati """</pre>	ion.
<pre>### START CODE HERE ### sum1 = np.zeros(len(env.A)) # number of actions in for action in env.A:</pre>	en a state, apply transitions for all of the actions ate the sum for each action s): [s1])
<pre>The cell below uses the policy evaluation algorithm to evaluate the city' %reset_selective -f "^num_spaces\$ ^num_prices\$ ^env\$ ^v num_spaces = 10 num_prices = 4 env = tools.ParkingWorld(num_spaces, num_prices) V = np.zeros(num_spaces + 1) city_policy = np.zeros((num_spaces + 1, num_prices)) city_policy[:, 1] = 1 gamma = 0.9 theta = 0.1 V = evaluate_policy(env, V, city_policy, gamma, theta)</pre>	
V = evaluate_policy(env, V, city_policy, gamma, theta) You can use the plot function to visualize the final value function and tools.plot(V, city_policy) Value Function 95	Policy 3
	Action 1- O.8 O.6 Probability O.2
0 2 4 6 8 10 State for s, v in enumerate(V): print("{}: {:1f}".format(s, v)) 0: 80.041734 1: 81.655323	State O 2 4 6 8 10 O 2 5 4 6 8 10
2: 83.373940 3: 85.129756 4: 86.871749 5: 88.555891 6: 90.140204 7: 91.581806 8: 92.819298 9: 93.789159 10: 87.777930 You can check the output (rounded to one decimal place) against the a	answer below:
0 80.0 1 81.7 2 83.4 3 85.1 4 86.9 5 88.6 6 90.1 7 91.6 8 92.8	
simple reward function (more reward is accrued when many but not all positive probability of being reached each time step) the value functions words, better policies will increase the expected return at every state rate less desirable state. Similarly, the value of a more desirable state can	I's preferences — it monotonically increases as more parking is used, until there is no parking left, in which case the value is lower. Because of parking spots are taken and less reward is accrued when few or all parking spots are taken) and the highly stochastic dynamics function (each is of most policies will qualitatively resemble this graph. However, depending on the intelligence of the policy, the scale of the graph will differ. It ather than changing the relative desirability of the states. Intuitively, the value of a less desirable state can be increased by making it less likely in be increased by making it more likely to remain in a more desirable state. That is to say, good policies are policies that spend more time in dement, such a steady state distribution is achieved by setting the price to be low in low occupancy states (so that the occupancy will increase) a
the price high when occupancy is high (so that full occupancy will be average to the cell below will check that your code passes the test case above. (You can now move to the next Assertion correct. You can now move to the next Section.	Your code passed if the cell runs without error.) 2.8,93.8,87.8] section.")
value function. We have written an outline of the policy iteration algorith	using policy iteration. Policy iteration works by alternating between evaluating the existing policy and making the policy greedy with respect to the described in chapter 4.3 of the textbook. We will make use of the policy evaluation algorithm you completed in section 1. It is left to you to to be greedy with respect to the q-values at s , to complete the policy improvement algorithm.
<pre>q_greedify_policy(env, V, pi, s, gamma) if not np.array_equal(pi[s], old): policy_stable = False return pi, policy_stable def policy_iteration(env, gamma, theta): V = np.zeros(len(env.S)) pi = np.ones((len(env.S), len(env.A))) / len(env.A) policy_stable = False while not policy_stable: V = evaluate_policy(env, V, pi, gamma, theta) pi, policy_stable = improve_policy(env, V, pi,</pre>	
	the environment initiated at zero en a state, apply transitions for all of the actions
<pre># for each transition and its probabilities, up for s1, (reward, prob) in enumerate(transitions</pre>	s): [s1]) s hest sum gets subset and assigned probability of 1 pelow.
<pre>%reset_selective -f "^num_spaces\$ ^num_prices\$ ^env\$ ^vous env = tools.ParkingWorld(num_spaces=10, num_prices=4) gamma = 0.9 theta = 0.1 V, pi = policy_iteration(env, gamma, theta) You can use the plot function to visualize the final value function and tools.plot(V, pi)</pre> Value Function	nd policy.
95	Policy 3
You can check the value function (rounded to one decimal place) and p	0 2 4 6 8 10 0.0 State
State Value Action 0 81.6 0 1 83.3 0 2 85.0 0 3 86.8 0 4 88.5 0 5 90.2 0 6 91.7 0 7 93.1 0	
8 94.3 0 9 95.3 3 10 89.5 3 print(pi) [[1. 0. 0. 0.] [1. 0. 0. 0.] [1. 0. 0. 0.] [1. 0. 0. 0.]	
[1. 0. 0. 0.] [1. 0. 0. 0.] [1. 0. 0. 0.] [1. 0. 0. 0.] [1. 0. 0. 0.] [0. 0. 0. 1.] [0. 0. 0. 1.]] The cell below will check that your code passes the test case above. (Y ## Test Code ## V_correct = [81.6,83.3,85.0,86.8,88.5,90.2,91.7,93.1,94 pi_correct = [[1., 0., 0., 0.],	
[1., 0., 0., 0.],	
np.testing.assert_array_almost_equal(pi, pi_correct) print("Assertion correct. You can now move to the next correct value function Assertion correct. You can now move to the next section. Section 3: Value Iteration The city has also heard about value iteration and would like you to imple	olement it. Value iteration works by iteratively applying the Bellman optimality equation for v_st to a working value function, as an update rule, as
<pre>def value_iteration(env, gamma, theta): V = np.zeros(len(env.S)) while True: delta = 0 for s in env.S: v = V[s]</pre>	$v(s) \leftarrow \max_a \sum_{s',r} p(s',r s,a)[r+\gamma v(s')]$ in chapter 4.4 of the textbook. It is left to you to fill in the bellman_optimality_update function to complete the value iteration algorithm.
<pre>bellman_optimality_update(env, V, s, gamma)</pre>	
<pre>Mutate ``V`` according to the Bellman optimality up """ ### START CODE HERE ### sum1 = np.zeros(len(env.A)) # number of actions in for action in env.A: transitions = env.transitions(s, action) # given # for each transition and its probabilities, upda for s1, (reward, prob) in enumerate(transitions): sum1[action] += prob * (reward + gamma * V[V[s] = sum1[np.argmax(sum1)] # update V with the hi</pre>	the environment initiated at zero a state, apply transitions for all of the actions ate the sum for each action : [s1])
<pre>### END CODE HERE ### When you are ready to test the value iteration algorithm, run the cell be %reset_selective -f "^num_spaces\$ ^num_prices\$ ^env\$ ^v env = tools.ParkingWorld(num_spaces=10, num_prices=4) gamma = 0.9 theta = 0.1 V, pi = value_iteration(env, gamma, theta)</pre>	V\$ ^pi\$ ^gamma\$ ^theta\$"
You can use the plot function to visualize the final value function and tools.plot(V, pi) Value Function 95	Policy 3 - 1.0 -0.8
Value 90 85	Action Action Probability 0.2 0.0 0.2 0.0 0.0 0.0 0.0 0.
0 2 4 6 8 10 State You can check your value function (rounded to one decimal place) and State Value Action 0 81.6 0 1 83.3 0 2 85.0 0 3 86.8 0	0 2 4 6 8 10 State
86.8 0 4 88.5 0 5 90.2 0 6 91.7 0 7 93.1 0 8 94.3 0 9 95.3 3 10 89.5 3 The cell below will check that your code passes the test case above. (Y	Your code passed if the cell runs without error)
<pre>## Test Code ## V_correct = [81.6,83.3,85.0,86.8,88.5,90.2,91.7,93.1,94 pi_correct = [[1., 0., 0., 0.],</pre>	
[1., 0., 0., 0.], [0., 0., 0., 1.], [0., 0., 0., 1.]] np.testing.assert_array_almost_equal(V, V_correct, 1) print("correct value function") np.testing.assert_array_almost_equal(pi, pi_correct) print("Assertion correct. You can now move to the next correct value function Assertion correct. You can now move to the next section. In the value iteration algorithm above, a policy is not explicitly maintained.	
<pre>value iteration in this form makes its relationship to policy iteration more between doing local greedifications and local evaluations. def value_iteration2(env, gamma, theta): V = np.zeros(len(env.S)) pi = np.ones((len(env.S), len(env.A))) / len(env.A) while True: delta = 0 for s in env.S: v = V[s] q_greedify_policy(env, V, pi, s, gamma)</pre>	re evident. Policy iteration alternates between doing complete greedifications and complete evaluations. On the other hand, value iteration alte
<pre>bellman_update(env, V, pi, s, gamma)</pre>	
gamma = 0.9 theta = 0.1 V, pi = value_iteration2(env, gamma, theta) tools.plot(V, pi) Value Function 95	Policy 3 - 1.0 -0.8
Value 90 85	Action Action Probability 0.2 0.0 0.2 0.0 0.0 0.0 0.0 0.
State Wrapping Up Congratulations, you've completed assignment 2! In this assignment, waservice!	State we investigated policy evaluation and policy improvement, policy iteration and value iteration, and Bellman updates. Gridworld City thanks you