

BROWN

Haneesh Kesari School of Engineering  
Assistant Professor Brown University  
of Engineering 184 Hope Street, B&H 612  
Providence, RI 02912  
Phone: 401-863-1418  
Email: Haneesh\_Kesari@brown.edu

---

Regarding: Point-by-point response to issues raised by referees (manuscript JMBBM-D-21-00364).

Dear Editors and Reviewers,

We thank you for your very valuable feedback. In response to your feedback, we have made the revisions listed in the section *List Of Changes (LoC)*, which can be found on page 2 of this response letter. We provide a point-by-point response to the Reviewers' comments in the following pages. Our responses to Reviewer #1's and Reviewer #2's comments can be found on pages 4 and 9, respectively, of this response letter. Through these changes and our responses to your comments, we hope that we have addressed all of your concerns.

We thank you for your consideration of our revised manuscript.

Sincerely,

Wenqiang Fang, Sayaka Kochiyama, and Haneesh Kesari

## List of Changes

The following changes appear in red in the revised version of the manuscript.

*Mc.1* In response to Reviewer #1's comment (listed as comment [1.3](#) of this letter) regarding the need of clarification for the details of the loading being considered, we have added the following sentence to the eighth paragraph of §1: "Each point on that curve corresponds to a static equilibrium configuration."

*Mc.2* In response to Reviewer #1's comment (listed as comment [1.3](#) of this letter) regarding the experimental details of the loading, we have added several sentences to the third paragraph of §3 to discuss the stage's motion and the time scales involved.

*Mc.3* In response to Reviewer #2's comment (listed as comment [2.2](#) of this letter) regarding the labeling of figures, we have made the following changes.

*Mc.3.i* Reference to Figure 3 was incorrectly displayed as Figure 1 and were corrected in the following locations:

- §1, first sentence of fourth paragraph
- §1, fourth, fifth, and sixth sentences of fifth paragraph
- §1, first sentence of sixth paragraph
- §1, seventh sentence of eighth paragraph
- §4.1.1, third sentence of first paragraph

*Mc.3.ii* Reference to Figure 8 was incorrectly displayed as Figure 4.2.2 and were corrected in the following locations:

- §4.2.4, second sentence of second paragraph
- §4.2.4, second sentence of Remark 1

*Mc.4* In response to Reviewer #2's comment (listed as comment [2.2](#) of this letter) regarding the language being spoken and not quite polished, we have made the following changes to the text.

*Mc.4.i* Several sentences were replaced in the manuscript for better flow and readability. These changes appear in red in the revised manuscript and are found in:

- §1, fifth sentence of third paragraph
- §1, fourth to sixth sentences of sixth paragraph
- §1, second sentence of eighth paragraph

*Mc.4.ii* Minor changes were made in the following locations to enhance readability. This included eliminating spoken languages in the text such as "that is," "of course," and other informal phrases and rectifying the overuse of first-person narrative. The changes appear in red in the revised manuscript and can be found in:

- §1, first, third, and sixth sentences of fifth paragraph
- §1, first, seventh, eighth, and tenth sentences of sixth paragraph
- §1, first, fifth, seventh, and eighth sentences of eighth paragraph
- §1, second and fourth sentences of ninth paragraph

- §2, second sentence of fourth paragraph
- §3, third sentence of second paragraph
- §4.2.4, first and fourth sentences of first paragraph
- §4.2.4, first sentence of second paragraph
- §4.2.4, first and second sentences of fourth paragraph
- §4.3, third sentence of second paragraph
- §4.3.1, third sentence of third paragraph
- §5, second sentence of third paragraph
- §5, first and second sentences of fourth paragraph
- §5, tenth sentence of sixth paragraph
- §6, first sentence of first paragraph
- §6, second, fourth, and last sentences of third paragraph
- §6, fourth sentence of fifth paragraph

## **Response to Reviewer #1's comments**

**1.1 “The authors have presented a good piece of work, through which they are able to explain the sawtooth patterns observed in the force-displacement curves. This is done by allowing for slippage at the test supports and paying attention to the coefficient of friction.”**

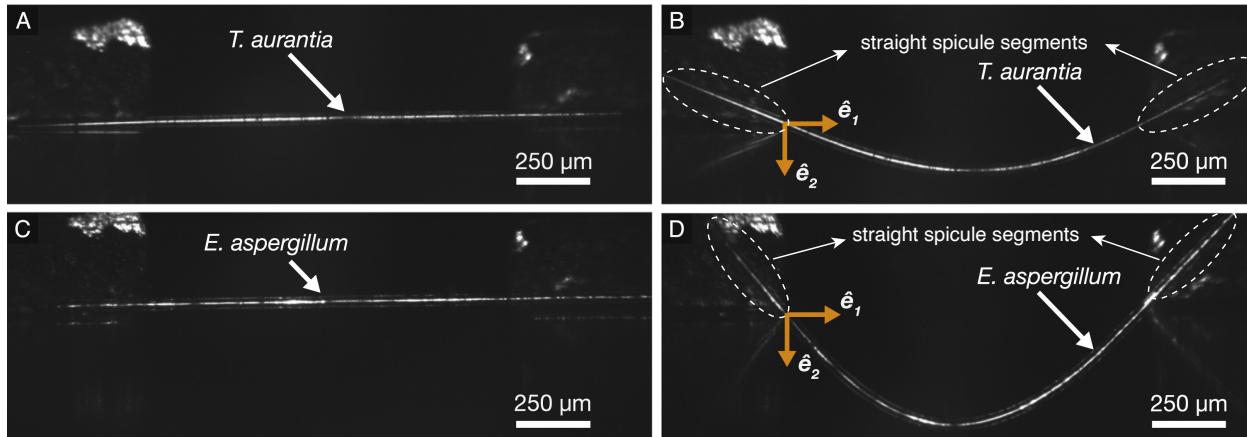
We thank the Reviewer for their very generous comments regarding our manuscript.

**1.2 “A few minor comments to help clarify and strengthen the work: a) In the SS experiments, how it is ascertained that the boundary conditions correspond to the simply supported conditions.”**

We thank the reviewer for their feedback on how to clarify and strengthen our arguments.

We use the phrase “simply supported” to connote that there were no bending moments acting at the spicule’s supports. We assume that there are no bending moments acting at the spicule’s supports due to the following three reasons.

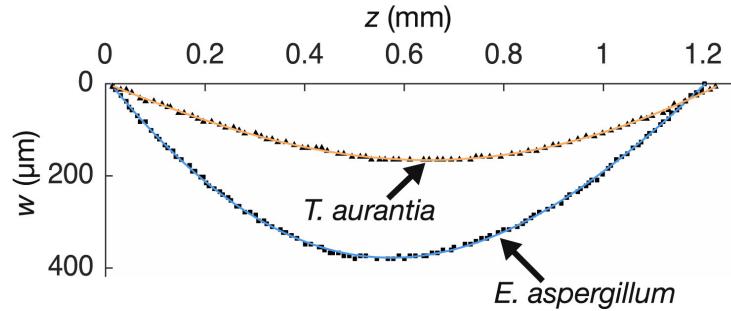
1. The experiments that we refer to as simply supported were set-up by simply placing the spicules on the mechanical testing stage, across the trench; and not using glue or any other means to render the spicules immobile on the stage (e.g., see Fig. 1 (A) and (C)). Partly due to this reason, the spicules experienced no adhesive interaction with the stage. This was quite evident to us from the tremendous difficulty we faced in getting the spicules to their proper positions across the trench. (A proper position was one in which the spicules lay symmetrically across the trench, and their entire length lay in the focal plane of the experiment’s optical microscope.) Since the spicules had no adhesive interaction with the stage, no bending moments could act on them at their supports (trench edges).
2. We collected optical microscopy images of the spicule’s deformed configurations during the experiments. The experiments that we modeled were originally reported in Monn and Kesari (2017). Additional experiments to support the hypothesis that we presented in the current manuscript were presented in Kochiyama et al. (2021). The optical images of the spicule’s deformed configurations can be found in Fig. 3 of Monn and Kesari (2017) and Fig. 5 of Kochiyama et al. (2021). For the Reviewer’s convenience, we also present some of those images in Fig. 1. In all those images it can be observed that the sections of the spicule that lie outside the trench (i.e., towards the left and right of the trench) always have a straight shape. (In Fig. 1 (B) and (D), the spicule sections lying outside the trench are marked using white dashed ellipses.) As per elementary beam theories, these straight shapes are only possible if there are no bending moments acting at the supports.



**Figure 1.** (A) and (B) (resp. (C) and (D)) show the undeformed configuration and deformed configuration just before failure of a representative *Tethya aurantia* (resp. *Euplectella aspergillum*) spicule (adapted from Fig. 3 of Monn and Kesari (2017)). In (B) and (D) the spicule segments lying outside the trench are marked using white ellipses.

3. On assuming simply-supported boundary conditions, the predictions from the elastica theory for the deformed shapes of the spicules match remarkably well with the shapes’ measurements from the optical microscopy images (see Fig. 2). We employed no fitting parameters when comparing the predictions for the deformed shapes with their optical microscopy measurements. The lengths and diameters

were measured independently from optical and scanning electron microscopy imaging, and the Young's modulus was measured independently from the force-deflection measurements.



**Figure 2.** Comparison of the predictions from the elastica theory for the deformed shapes of the spicules with the shapes' measurements from optical microscopy images. The black triangles (resp. squares) mark the measured positions of the material points from the mid-axis of the *Tethya aurantia* (resp. *Euplectella aspergillum*) spicule shown in Fig. 1 (B) (resp. (D)). The orange (resp. blue) curves correspond to the deformed shapes predicted by the elastica theory. (adapted from Fig. 4(D) of Monn and Kesari (2017)).

1.3 “b) The experiments all appear to be conducted for a static loading and this needs to be pointed out explicitly, in particular, when using friction in the model. The time scales over which the loading could be critical if dynamic friction is involved. Can any relevant details be provided in the paper?”

We thank the reviewer for pointing out this lapse on our part. In order to rectify this lapse we have made the following changes.

(i) In §1 of the revised manuscript, we now explicitly state that, in our model, each of the configurations for which we derive quantitative predictions are taken to be in static equilibrium. This change can be found as *Mc.1* in the *LoC*.

(ii) Through change *Mc.2* in the *LoC*, we now provide details about the stage’s motion and the time scales involved in the experiment in the revised version of the manuscript. These newly added details appear in red in the third paragraph of §3 of the revised manuscript. We repeat those details below for the Reviewer’s convenience.

Note that in the below quote MTS stands for Mechanical Testing Stage.

*The loading phase of the tests were conducted by moving the MTS in the  $-\hat{e}_2$  direction at an average velocity of  $\approx 1 \mu\text{m/sec}$ . The MTS was driven by a DC servo motor, whose motion was controlled through a PID algorithm. The stage was moved in  $2 \mu\text{m}$  increments. During the increment, the stage’s velocity was maintained between  $50$  and  $200 \mu\text{m/sec}$ . Thus, each stage increment took anywhere between  $10$  and  $40 \text{ ms}$ . After each increment, the stage was held motionless so that there was a  $2100 \text{ ms}$  time interval between the starting points of any two consecutive increments. Each data point that we report was calculated using the average value of the sensor readings collected over the last  $100 \text{ ms}$  of each of those time intervals.*

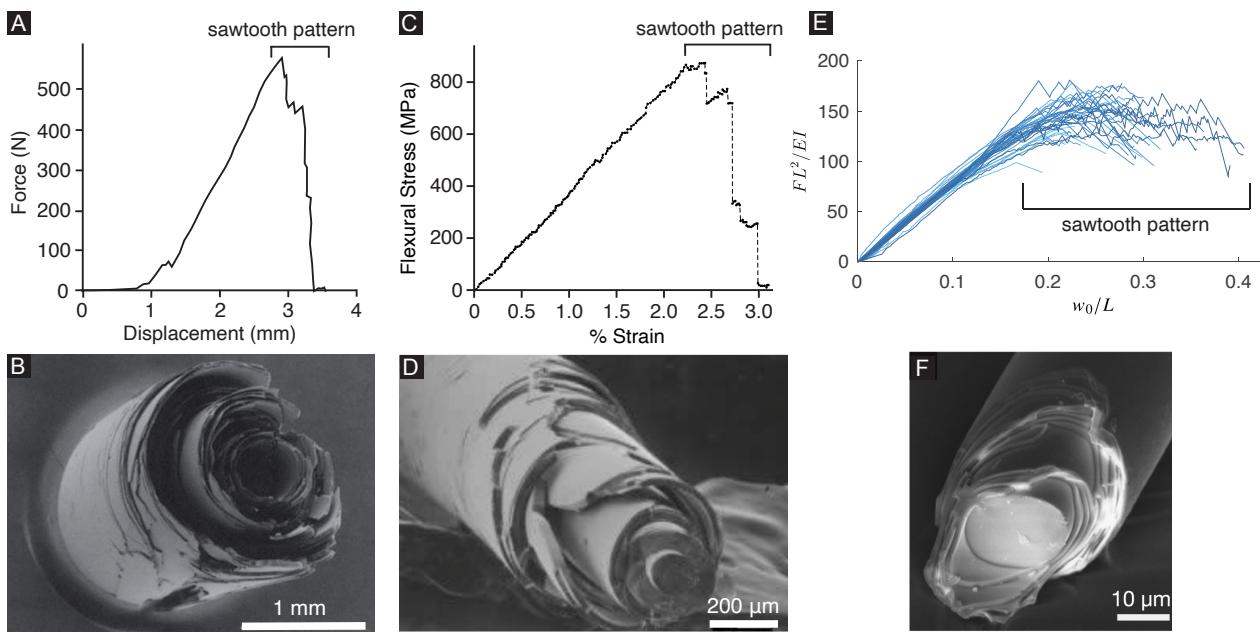
**1.4 “c) With regard to the elastica theory, an extension would be the rod theory, which would be needed for a three-dimensional setting; see Antman, S. S., Problems in Nonlinear Elasticity, Springer.”**

We thank the Reviewer for bringing up the rod theory and encouraging us to expand our model to the 3D context. We are very interested in that type of a generalization, and thank the Reviewer for their encouragement and guidance.

## Response to Reviewer #2's comments

2.1 "The authors report on the three-point bending tests of marine sponge fibers and the possible mechanism for the sawtooth-pattern during the bending tests. They argued that the sawtooth-pattern is originated from the stick-slip motion on the supporting substance and eliminated the Cook-Gordon mechanism. While Cook-Gordon mechanism is valid during the fracture of the materials, I am curious whether the experiment here caused the fracture of the spicule? If not, then the bending of spicule may remain in the "elastic deformation" and the stick-slip should be caused by the friction on the supporting layer, as stated by the authors. Then the initial argument is meaningless. If yes, how is the fractured surface looks like? Will the propagation of cracks have any correlation to the sawtooth-pattern?"

All sawtooth patterns that we attempt to explain in our manuscript are from experiments in which the spicules were loaded until failure. Some of the spicule fractured surfaces are shown in Fig. 3.



**Figure 3.** Force-displacement curves and optical images of the fractured surfaces for (A) and (B) *Monorhaphis chuni* anchor spicules, (C) and (D) *Rosella racovitzae* spicules (adapted from Fig. 4 of Kochiyama et al. (2021)), and (E) and (F) *Euplectella aspergillum* (*Ea.*) anchor spicules (adapted from Fig. 3 of Monn and Kesari (2017)).

In Fig. 3, the experiments on *Ea.* spicules were performed by us, while the experiments on *M. chuni* and *R. racovitzae* are taken from literature.

Regarding the Reviewer's question of "Will the propagation of cracks have any correlation to the sawtooth-pattern?" we have not measured the evolution of the crack(s) with loading in our experiments. (Only the final fracture surfaces, as those shown in Fig. 3, are available.) Neither is such information available for the experiments on *M. chuni* and *R. racovitzae*. Measurement of the crack(s) evolution in spicules during loading is quite a challenging task due to the length scales involved (the *Ea.* spicules are typically 50 micrometer in diameter), and the fact that the crack(s) surface(s) can be 3D and/or multiply connected in nature. Since no data is available on how the crack(s) evolve during the loading process, we cannot answer whether or not the "propagation of cracks have any correlation to the sawtooth-pattern." We can only comment that if such a correlation is indeed observed then

that would be evidence against our hypothesis, and if no such correlation is found then that would further strengthen our hypothesis.

In the work of Clegg et al. (1990), a correlation was found between the evolution of the crack(s) and the drops in the force-deflection curve. The correlation of the evolution of the crack(s) with the force-deflection curve in the work of Clegg et al. is a reflection of the operation of the Cook-Gordon mechanism, whereby the interfaces repeatedly arrest crack growth, leading to a toughening effect. However, recent experiments and large scale fracture simulations (Monn et al., 2020) have revealed that the spicules are not significantly tougher compared to the biogenic silica that composes them, and that the Cook-Gordon mechanism is suppressed in them due to the curved nature of the interfaces.

**2.2 “The labelling of figures is chaos! The language should be polished, it is quite spoken language.”**

In response to the reviewer’s above comments, we have made the following two changes.

(i) Regarding the comment that the labeling is unclear, we believe that what led to this comment was the wrong figures being referred to at some locations in the text. For example, in the fifth and sixth paragraphs of §1 in the original submission, Figure 1 was incorrectly referred to instead of Figure 3. We have corrected these incorrect references in the revised version of the manuscript. The changes are listed under *Mc.3* in the *LoC*.

(ii) Regarding the Reviewer’s concern about the language appearing “spoken” and not polished, we have tried our utmost to address this comment by changing the text at several locations in the revised version of the manuscript. These changes are listed under *Mc.4* in the *LoC*.

# Bibliography

- W. Clegg, K. Kendall, N. M. Alford, T. Button, and J. Birchall. A simple way to make tough ceramics. *Nature*, 347:455–457, 1990.
- S. Kochiyama, W. Fang, M. A. Monn, and H. Kesari. Sawtooth patterns in flexural force curves of structural biological materials are not signatures of toughness enhancement: Part i. *Journal of the Mechanical Behavior of Biomedical Materials*, 119:104362, 2021.
- M. A. Monn and H. Kesari. Enhanced bending failure strain in biological glass fibers due to internal lamellar architecture. *Journal of the mechanical behavior of biomedical materials*, 76:69–75, 2017.
- M. A. Monn, K. Vijaykumar, S. Kochiyama, and H. Kesari. Lamellar architectures in stiff biomaterials may not always be templates for enhancing toughness in composites. *Nature communications*, 11 (1):1–12, 2020.