

# FAKULTÄT FÜR INFORMATIK

DER TECHNISCHEN UNIVERSITÄT MÜNCHEN

Bachelor's Thesis in Informatik

# Perceptual Losses for Deep Learning on Fluid Simulations

Hanfeng Wu





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Perceptual Losses for Deep Learning on Fluid Simulations

Perceptual Losses für Deep Learning von Flüssigkeitssimulationen

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I confirm that this bachelor's thesis is my own work and all sources and material used.	I have documented
Munich, 15.09.2021	Hanfeng Wu

# Acknowledgements

#### Abstract

This thesis studies the integration of perceptual loss into several models that are related to fluid simulation. Perceptual losses are used to compare high level differences, while traditional loss functions like MSE and MAE only compare the pixel level differences which is more brute force.

Now some famous perceptual loss functions like comparing the intermediate layers of pretrained vgg network already improve its performance in some image related tasks. [JAFF16] We want to show that in the context of fluid simulation, the integration of some pretrained perceptual losses should also outperform the traditional loss functions.

We tested some fluid simulation tasks in SOL [UBF<sup>+</sup>20] to improve the performance of the percetual loss functions. Meanwhile we also integrate such loss functions into models like autoencoder and superresolution to compare their results with those from the same models but trained by MSE loss functions

Finally we combined the result of SOL and superresolution model to conduct some fluid simulations at a lower cost to show the advantage of integrating perceptual losses in such tasks.

#### Zusammenfassung

Diese Dissertation untersucht die Integration von Wahrnehmungsverlusten in verschiedene Modelle, die sich auf die Fluidsimulation beziehen. Wahrnehmungsverluste werden verwendet, um Unterschiede auf hohem Niveau zu vergleichen, während herkömmliche Verlustfunktionen wie MSE und MAE nur die Pixelniveauunterschiede vergleichen, was roher ist.

Einige berühmte Wahrnehmungsverlustfunktionen wie der Vergleich der Zwischenschichten eines vortrainierten VGG-Netzwerks verbessern bereits seine Leistung bei einigen bildbezogenen Aufgaben. [JAFF16] Wir wollen zeigen, dass die Integration einiger vortrainierter Wahrnehmungsverluste im Kontext der Fluidsimulation übertreffen auch die traditionellen Verlustfunktionen.

Wir haben einige Fluidsimulationsaufgaben in SOL [UBF<sup>+</sup>20] getestet, um die Leistung der Percetual Loss Functions zu verbessern. Inzwischen integrieren wir solche Verlustfunktionen auch in Modelle wie Autoencoder und Superresolution, um deren Ergebnisse mit denen aus den gleichen Modellen zu vergleichen, die jedoch mit MSE-Verlustfunktionen trainiert wurden

Schließlich haben wir die Ergebnisse von SOL und Superauflösungsmodell kombiniert, um einige Fluidsimulationen zu geringeren Kosten durchzuführen, um den Vorteil der Integration von Wahrnehmungsverlusten in solchen Aufgaben zu zeigen. Note: Insert the German translation of the English abstract here.

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 ${f SOL}$  Solver in the Loop

 ${\bf LSIM}\;$  Learning Similarity Metrics for Numerical Simulations

## Introductions

Our main purpose of this paper is to demonstrate the advantage of adopting the perceptual loss functions in various deep learning tasks on fluid simulation. We try to show statistically and perceptually that by integrating suitable perceptual loss functions in such tasks can outperform the original model trained on traditional loss functions such as MSE and MAE. In the end we will also compare the performance and outputs of running solely the simulation and the simulation combined with some deep learning models.

#### 1.1 Fluid simulation

## 1.1.1 Navier Stokes Equation

The state of art Fluid simulation is based on the famous incompressible equation Navier-Stokes equation

$$\frac{\partial \vec{u}}{\partial t} + \vec{u} \cdot \nabla \vec{u} + \frac{1}{\rho} \nabla p = \vec{g} + \nu \nabla \cdot \nabla \vec{u}$$
 (1.1)

$$\nabla \cdot \vec{u} = 0 \tag{1.2}$$

where  $\nabla$  denotes the gradient,  $\nabla \cdot$  denotes the Divergence,  $\vec{u}$  denotes the velocity of the fluid, t denotes the time step,  $\rho$  denotes the density of the fluid, p denotes the pressure,  $\vec{g}$  denotes the gravity and  $\nu$  denotes the viscosity of the fluid.

The equation (1.1) is actually a transformation of the  $\vec{F} = m\vec{a}$  and the equation (1.2) describes the incompressibility of the fluid.

#### 1.1.2 Grid Stucture

The way of storing the velocity and the density is based on two different grid structure. We store the dencity in the center of each cell, we call it centeredgrid or scalar grid. However for storing the velocity, we sample them at the face centers of each cell [HW65]. In such way we can more easily compute the inflow and outflow of each grid for each direction, however as a trade off, the data format would be more complex than normal centeredgrid, and we usually have to stack each verlocity array of each dimension together and also adopt them individually in some computations(e.g. computing loss function in deep learning)

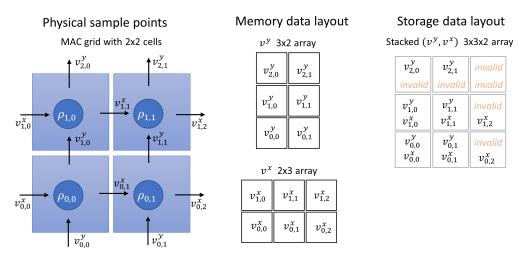


Figure 1.1: Staggered grid format

#### 1.1.3 Advection

With the knowledge base of the NS-equation and grid structures we now need the advection algorithm to run the simulation. We adopt the semi-lagrangian advection algorithm. In the lagrangian point of view, if we want to compute the grid value of the n+1 time step of grid position  $\vec{x_G}$ , we should figure out which particle actually flows to the grid  $\vec{x_G}$  from time step n+1. If we name the grid position of the particle as  $\vec{x_P}$ , then the new particle at time step n+1 in  $\vec{x_G}$  should have the same physical property as the particle at time step n in  $\vec{x_P}$ 

we first use the euler equation to calculate the  $\vec{x_P}$  as a step before of  $\vec{x_G}$ 

$$\vec{x}_P = \vec{x}_G - \Delta t \frac{d\vec{x}_G}{dt} \tag{1.3}$$

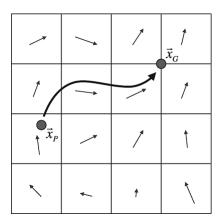


Figure 1.2: advection

because  $\frac{d\vec{x}}{dt} = \vec{u}(\vec{x})$  we have

$$\vec{x}_P = \vec{x}_G - \Delta t \vec{u}(\vec{x}_G) \tag{1.4}$$

where  $\vec{u}(\vec{x}_G)$  denotes the velocity sampled at the position  $x_G$ , with the advection we can update the velocity, pressure and density of the whole vector field.

with all the knowledge above, we can formulate a sequence to conduct the basic fluid simulation.

- start with an initial velocity field  $\vec{u}^0$  with the property  $\nabla \cdot \vec{u} = 0$
- choose a time step  $\Delta t$
- For time step n = 0, 1, 2, ...
  - $\vec{u}^A = advect(\vec{u}^n, \vec{u}^n, \Delta t)$
  - add the extra force  $\vec{u}^B = \vec{u}^A + \Delta t \vec{g}$
  - $\vec{u}^{n+1} = make\_incompressible(\Delta t, \vec{u}^B)$

## 1.2 Deep learning tasks

There are also various ways of integrating deep learning models into the fluid simulation.

#### 1.2.1 Autoencoder

The Autoencoder model has a bottle neck shape, which aims to produce the same output as the input. Once trained, the Autoencoder model can be saparated into two parts, namely the encoder and the decoder, which can

compress the image with the encoder and later decompress the image with the decoder to its forer shape.

## 1.2.2 Superresolution

With the superresolution model, we can upscale the low-resolution images to high-resolution images, which based on that we have fed lots of similar data to the model. In this paper, we apply the Superresolution model at the end of the Solver in the Loop model in order to boost the fluid simulation while still obtain a fairly similar output.

## 1.2.3 Solver in the Loop

When we want to perform our fluid simulation on a lower-resolution domain to decrease the time cost, we always suffer from the numerical error comparing to the simulation running on the higher-resolution domain. It is reasonable because with the same initial state, the vector field on the higher domain has richer information than the one sampled in the lower domain. Dr. Kiwon Um [UBF<sup>+</sup>20] developed a mechanisim to learn the difference between the 2 different domains to reduce the numerical error.

## 1.3 Perceptual loss functions

Perceptual loss functions are used when comparing two images, they are not like traditional loss functions like MSE or MAE which only computes the low level pixel differences. Perceptual losses on the other hand, are normally forward networks trained for specific tasks. For example, VGG-16 network was trained for massive image classification, and LSIM was trained on smoke and fluid simulations. When adopting those networks, we can either compute the mse loss between the intermediate layers of the trained network, or directly passing it through depending on the goal of the chosen perceptual loss network. These perceptual loss networks tries to retrieve the high level differences between the images, hence will usually have a better performance than the traditional loss functions. In a word, traditional loss functions have more general use cases, while perceptual loss functions will achieve better performance on specific tasks. In this paper we mainly focus on comparing the performance between traditional loss function MSE and perceptual loss functions LSIM, VGG-16 and lpips.

# Chapter 2 Related Work

similar goal area methods

## Metrics and Perceptual Losses

In this chapter we will cover several loss functions that we adopted in this paper and briefly explain their characteristics and their drawbacks. More percise integrations and results will be convered in the chapter 5.

## 3.1 Mean Squre Error

MSE is one of the most widely used loss functions.

$$MSE = \frac{1}{n} \sum_{i=1}^{n} (Y_i - \hat{Y}_i)^2$$
 (3.1)

Where Y is the reference tensor and  $\hat{Y}$  is the predicted tensor based on the trainable parameters. With this loss function being adopted, the network will try to do the gradient decent on the weights in a way that can achieve minimum square error. The optimal case is that the predicted tensor  $\hat{Y}$  is exactly the same is the reference tensor Y. We can see that the core idea for the MSE is very general so that this loss function can be applied almost for any models, however the MSE loss function is not suitable for some image related tasks. If the two inputs of the MSE loss function is merely a image with its core content shifted by some pixels, the MSE will produce a very high value, which is not representitive, in another word, the MSE does not have shift or rotate invariance.

Besides, MSE computes the squre error of the two tensors, which means that MSE is also prone to the outliers, beacause when it has a very large outlier in the tensor, the result of MSE loss function will be strongly influenced, so in most image construction cases, in order to achieve a lower square error, the output will be a relative blur one compared with the original.

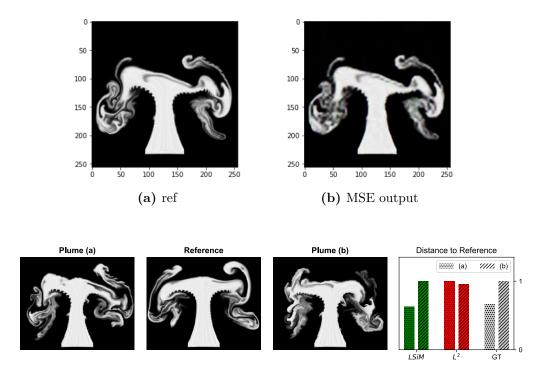


Figure 3.2: The loss computed between two different plume images and the reference with LSiM and  $L^2$  metrics. While the GT is the ground truth distance determined by the data generation.

## 3.2 Learning Similarity Metrics for Numerical Simulations

LSiM [KUT20] is a neural network-based approach that computes a stable and generalizing metric. Due to the unreliability of the MSE loss in numerical simulation tasks, LSiM has been established. It aims to demonstrate the performance of CNN-based evaluations on numerical simulation tasks. The data used to train LSiM are generated with known partial differential equations (PDEs).

With figure 3.2, we can tell that the  $L^2$  loss function consider plume be a closer image to the reference, while the fact is that plume a has a smaller distance to the reference image, which is exactly predicted by the LSiM.

The LSiM itself is also a CNN-based metric, see figure 3.3. The input of the network must be two batches of images with 3 channels

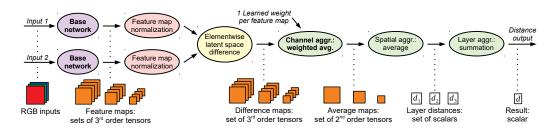


Figure 3.3: The Network structure of LSiM

As a metric, it also holds the metric properties  $\forall x, y, z \in \mathbb{I}$ :

$$m(\boldsymbol{x}, \boldsymbol{y}) \ge 0$$
 non-negativity (3.2)

$$m(\boldsymbol{x}, \boldsymbol{y}) = m(\boldsymbol{y}, \boldsymbol{x})$$
 symmetry (3.3)

$$m(\boldsymbol{x}, \boldsymbol{y}) \leq m(\boldsymbol{x}, \boldsymbol{z}) + m(\boldsymbol{z}, \boldsymbol{y})$$
 triangle ineq. (3.4)

$$m(\mathbf{x}, \mathbf{y}) = 0 \iff \mathbf{x} = \mathbf{y}$$
 identity of indisc. (3.5)

#### 3.3 VGG-16 loss network

VGG-16 [SZ14] is originally a CNN-based network trained for image classification problems. The author proposed 6 versions of vgg networks with different numbers of CNN layers but applied 3 fully connected layers for all of them at the end to realize the classification functionality. We adopted in the paper only the pretrained vgg-16 network(see figure 3.4) and apply it as a perceptual loss function. This pretrained model achieves 92.7% top-5 test accuracy in ILSVRC-2014, which is challenge based on a dataset of over 14 million images belonging to 1000 classes. Although the networks was not originally trained for computing the distance, we can still use transfer learning to use it as a perceptual loss. In the paper [JAFF16], they chose to extract the third intermediate layer outputs and compute the MSE loss between them to realize the perceptual loss functionality(shown in figure 3.5)

Apartfrom that we have also tested extracting the first, second or the fourth intermediate layers to calculate the mse loss in order to compare the performance with the current method. We found out that computing mse between the third one has the best performance in our training task.

## 3.4 Lpips

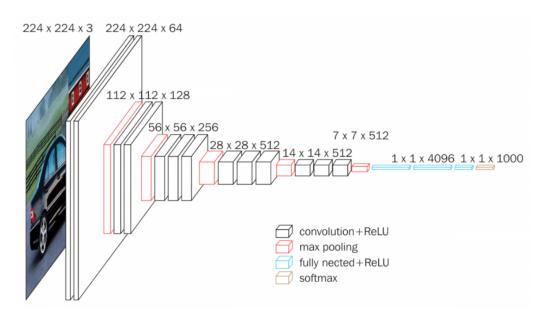
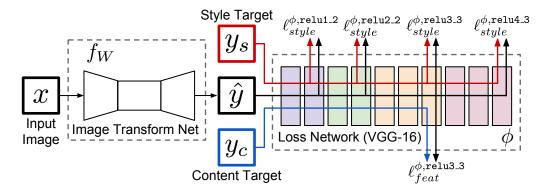


Figure 3.4: The network structure of vgg-16



**Figure 3.5:** The system figure of their style transfer learning, we only focus on how they compute the loss function based on the vgg-16 network

## **Datasets**

In this chapter we will cover the various dataset that we have adopted for training validation and testing in the following three tasks.

## 4.1 Autoencoder

## 4.2 Superresolution

The data we used in the superresolution task came from various sources. We first used the training data of LSiM model, because these are all numerical simulation data including the verlocity, density and pressure images, so we recon that LSiM can outperform the other metrics.

As we also want to test the performance of combining Solver in the loop and superresolution together to compete against the time cost with performing the simulation purely on the higher domain, we therefore also feed the

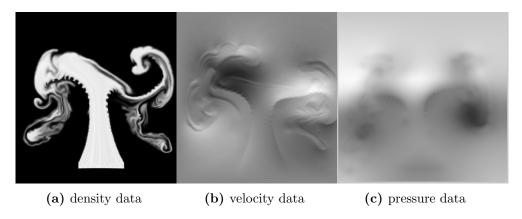


Figure 4.1: Training set of LSiM model

training data of the Solver in the Loop to the superresolution model, so that our model can learn to super sampling the plume density images when we feed the corrected simulation images on the lower domain, and we are able to abtain the plume images with the same resolution as the higher domain.

Apart from that, we also test the our model performance on some random videos data which are not related to numerical simulations but still can be of some assistance to our model.

## 4.3 Solver in the Loop

#### 4.3.1 Simulation tasks

In the solver in the loop tasks, we have trained and tested out our model with 2 different fluid simulations, which are the 2-D karman flow and 2-D buoyancy driven flow. The author of the solver in the loop has mainly trained their model on the karmanflow, based on which we extend the model to a more complex simulation i.e. the buoyancy driven flow.

For both simulation tasks, we have prepared two dataset with different resolutions in order to compare the performance of different loss functions on different resolutions. The two resolutions we chose for the Karmanflow are 128\*64 and 64\*32, and for buoyancy driven flow tasks we picked 64\*64 and 128\*128. As we want to reduce the numerical error for the model trained on a lower domain, for each resolution ratio we have to firstly generate a higher resolution dataset as the reference dataset, but we can not compare two datasets with different resolution therefore we have to downsample the higher resolution training set to a lower one that matches our training domain, and the downsampled dataset with rich simulation details from higher domain is our actual reference set.

## 4.3.2 Phiflow set up

The tool we used to perform the fluid simulation is Phiflow [HKT20].

For the karmanflow generation, we define an open domain with the size of 200(height) \* 100(width). (notice that domain size is not the same concept as the domain resolution. The domain size helps to locate the position of the inflow and obstacles of the simulation, while the resolution is used to define how percise we should sample our domain. Hence we could perform different resolution formats on the same domain size.) we set the inflow as a 5 \* 50 rectangle at the top center, and the obstacle as a circle with radius 10 positioned in the very

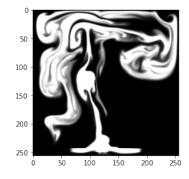


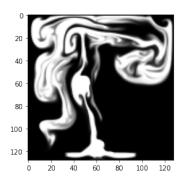


(a) Karmanflow example

(b) Buoyancy driven flow example

Figure 4.2: Two simulation examples for Solver in the Loop





with 256\*256

(a) Buoyancy driven flow image (b) Downsampled buoyancy driven flow image with 128\*128

Figure 4.3: Reference images generation and downsampling

center of the upper half of the domain. The step size  $\Delta t$  we chose here is 1.0. For each simulation we chose to generate 1500 frames for the karman flow.

For the buoyancy driven flow generation, we define a 200 \* 200 closed domain and set the inflow as a 5 \* 100 rectangle at the bottom center. We generate 250 frames for each simulation. Why we only chose 250 steps for the buoyancy driven flow is because we defined a closed boundary for the buoyancy flow so the simulation after 250 steps are extremely complex, and we also set the timestep to 0.1 to slow down the simulation so we will not have a chaotic frame of plumes. Which helps to make our training easier.

For both tasks, we have a total of 8 simulations with their renolds numbers ranging from  $1*10^5$  to  $8*10^5$  as the training set. As for the test set we can alter the renolds number and the seed of the simulation to generate a sets of simulation frames that are overall similar but in details deviated from the used training set.

# Tasks and Experiments Setup

## 5.1 Autoencoder

## 5.2 Superresolution

#### 5.2.1 Network

We adopt the same ImageTranformNetwork as in the paper [JAFF16], which is a fully convolutional network that has the same output tensor as the input. The network consists of three Convlayers, three UpsampleConvlayers and five residual blocks. (Notice that we do not use the deconvolutinal layer in the UpsampleConvlayers as suggested in the paper [ODO16], that deconvolutional layers will likely result into checkerboards artifacts due to the overlapping when doing the reverse convolution operations.)

## 5.3 Solver in the Loop

After we have generated the training set and its downsampled version, we can start the training. We will first cover the basics of the network and its training goal, then we will go into details of how to apply the loss function.

#### 5.3.1 Network

The training network we used is called MarsMoon, which is the same network that Prof. Um adopted in the his project (see figure 5.1) we can see that the number of channels for both input and output is 2. This is because the input is the staggered tensor of the verlocity which has two directions one represents the y direction and the other represents the x direction. The output of the

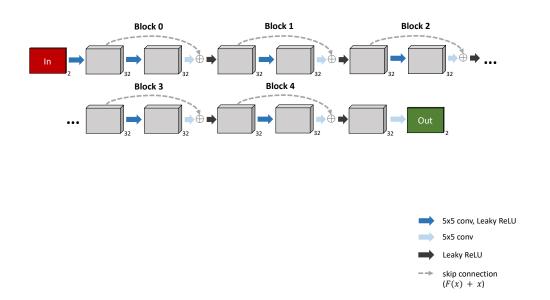


Figure 5.1: The network architecture [UBF<sup>+</sup>20]

network is also a staggered tensor however it can not be directly addressed as the verlocity but a correction of the verlocity, which can be added to the verlocity calculated on the lower domain, then the corrected verlocity can be applied for the next simulation step. The reason why we do not train the output towards the verlocity for the next simulation step is because we want to take advantage of the physical information stored in those tensors, if we should simply get the next verlocity from passing the former verlocity through the nerwork, then we would not need to perform the physical simulation, which is very unstable. Thus, adding the trained correction to the physical simulation output of the former verlocity would at least make sure that our simulation is performing on the right track. That means our consective steps of the simulation are based on valid physical simulation, which can not be ensured by purely passing through the neural network.

## 5.3.2 Training Set

In karman flow simulation, we choose not to use the whole training set to train our model, as in the first several steps of karman flow do not have much difference between high and low domains. So we only try to train the last 1000 steps of the total 1500 steps. When we train the lower domain 64\*32 karmanflow, we also find out that the 64\*32 image for LSiM model is too small, so we decide to alter the domain to the resolution of 64\*64, correspondingly the training set also need to be retrained on the domain of

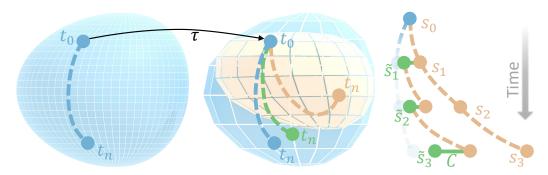


Figure 5.2: The training goal is to obtain the suitable correction, with which the simulation on the lower domain can reduce the numerical error. The brown one represents the source simulation of the lower domain without any corrections, the blue one represents the simulation on the higher domain which is our target, the green one is the brown one plus the trained correction, which aims to apporach the blue one [UBF<sup>+</sup>20]

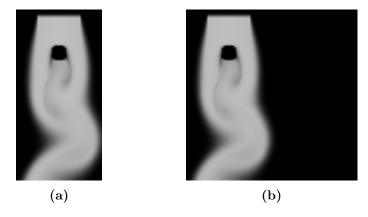


Figure 5.3: Padding plume image to match the input size of LSiM model

128\*128. However the size of the plume remains unchanged, we only pad the domain such that they can be applied to LSiM loss function. (see figure 5.3) For the buoyancy driven flow simulation, it only consists of 250 steps and each step has rich numerical information, so we regard the whole simulation as the training set. Besides, since the buoyancy simulation on the lower domain already has the shape of 64\*64 we don't need to add extra padding to suit the LSiM model.

## 5.3.3 Applying loss functions

In order to compute the loss we have to define the reference and the model output. We know our model output is the correction, however it is unreasonable to directly compare the correction with the reference simulation. So the two inputs of the loss functions should be

- 1. V: The sum between the verlocity tensor on the lower-domain simulation and our trained correction .
- 2.  $\dot{V}$ : The downsampled verlocity tensor from the higher-domain simulation.

For the MSE loss, which is exactly used by Prof. Um in his project, we can simply calculate their pixel wise square difference and compute their mean. This traditional loss function does not rely on the structure of the tensor as long as they share the same shape. So the MSE loss between two staggered tensors can be esaily computed. However the perceptual loss function has some demands on our tensor shape due to its CNN structure. For example, LSiM requires that the input tensor should consist of 3 channels to represent the RBG channels, while the size of the input tensor should be large enough to pass through several conv-layers. In our case, the output of the model is a staggered tensor with 2 channels which respectively represent x and y directions. Our solution is, that we compute the loss over each direction separately and sum them up. We firstly both extract the x direction tensor X and y direction tensor X and y direction tensor X from our model output X, then we also extract the x direction tensor X and y direction tensor X and y direction tensor X from the reference verlocity tensor X. Our final loss function representation looks like:

$$Loss(V, \hat{V}) = F(X, \hat{X}) + F(Y, \hat{Y})$$

$$(5.1)$$

where F is the respective perceptual loss function. In this way, we are able to treat the verlocity tensor on each direction as an image(or triplicate the channel to RBG image) and compare them with their ground truth.

# Results and Analysis

- 6.1 Comparison
- 6.1.1 Numerical evaluation
- 6.1.2 Time cost evaluation
- 6.2 Limitaions

# Conclusion

- 7.1 Future work
- 7.2 Summary

# Appendix A

# e.g. Questionnaire

Note: If you have large models, additional evaluation data like questionnaires or non summarized results, put them into the appendix.

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